

$$1) \quad p = 107$$

$$g = 2 \pmod{107}$$

$$a = 66$$

$$b = 33$$

$$A = g^a \pmod{p} = 2^{66} \pmod{107} = 47$$

$$B = g^b \pmod{p} = 2^{33} \pmod{107} = 58$$

$$S_{\text{Alice}} = B^a \pmod{p} = 58^{66} \pmod{107} =$$

75

} shared
secret

$$S_{\text{Bob}} = A^b \pmod{p} = 47^{33} \pmod{107} =$$

75

$$2) \quad \begin{array}{lll} m = 9 & p = 31 & A = 17 \\ b = 12 & g = 3 & a = 7 \end{array}$$

$$B = g^b = 3^{12} = 531441$$

Verschlüsselung:

$$c = A^b \cdot m = 17^{12} \cdot 9 = 5'243'600'135'067'849$$

Entschlüsselung:

$$m = c \cdot B^{(p-1-a)} \pmod{p} = c \cdot B^{31-1-7} \pmod{p} = c \cdot B^{23} \pmod{31} = 9$$

$$3) \quad n = 59'153 \quad x_0 = 24'72 = y_0$$

$$a = 1$$

$$i = 1$$

while no collision found:

$$x_i = (x_{i-1})^2 + a \pmod{n}$$

$$y_i = ((y_{i-1})^2 + a) \pmod{n}$$

$$d = \gcd(x_i - y_i, n)$$

if $(1 < d < n)$

return d

i++

calculated using python

$$d = 149$$