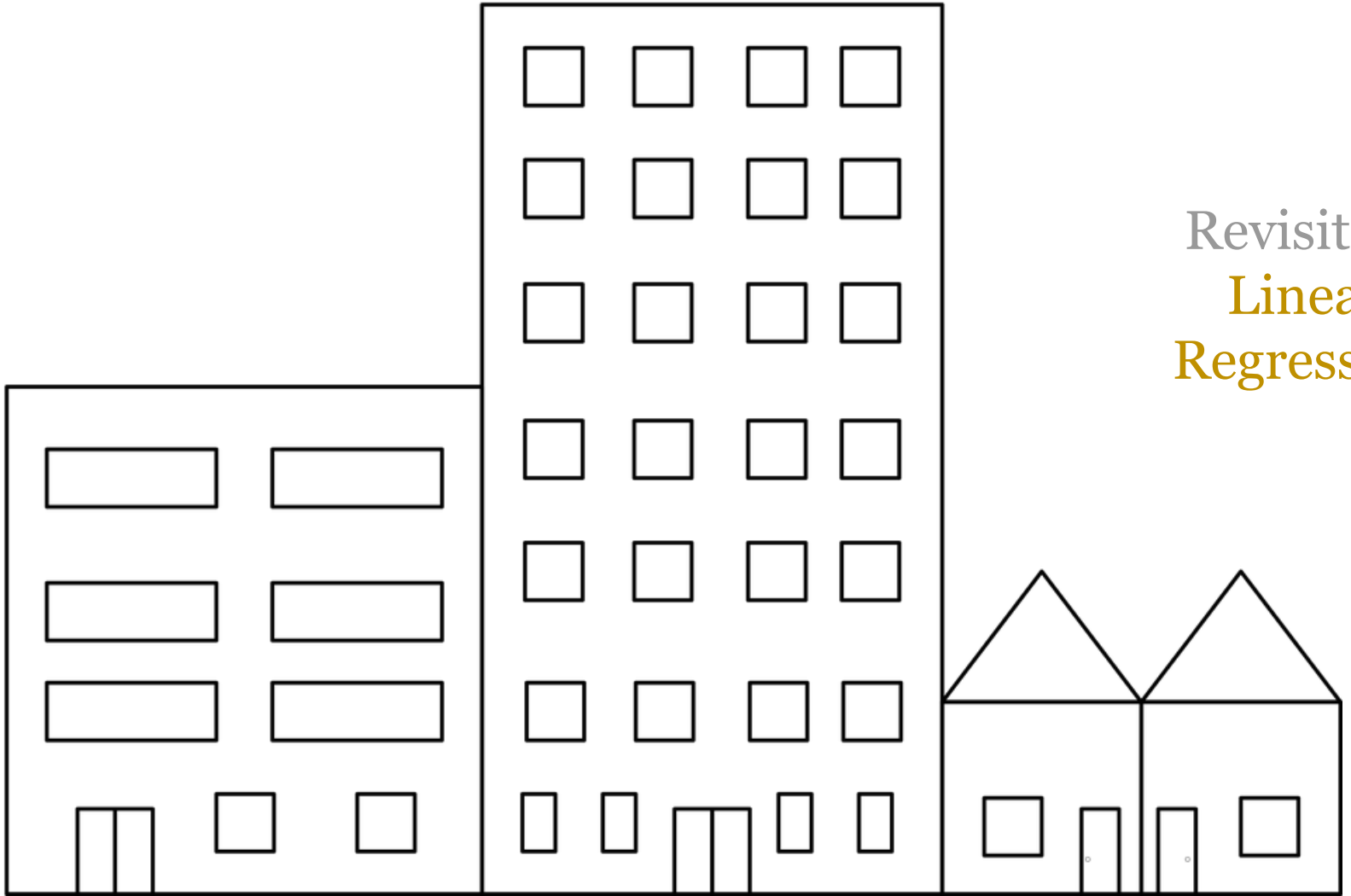
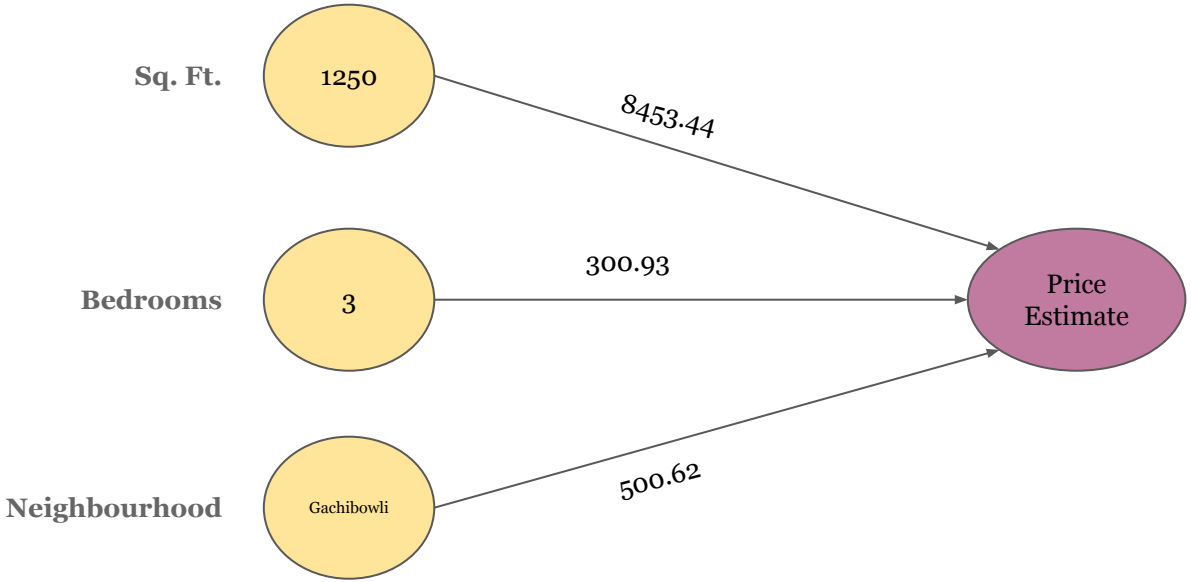


Revisiting Linear Regression

Sq. Ft	Neighbourhood	Bedrooms	Price (‘000)
2000	Gachibowli	3	180
1750	Jubilee Hills	3	210
1100	Kukatpally	2	55
900	Gachibowli	2	72
1245	KPHB	3	60
…	…	…	…
…	…	…	…

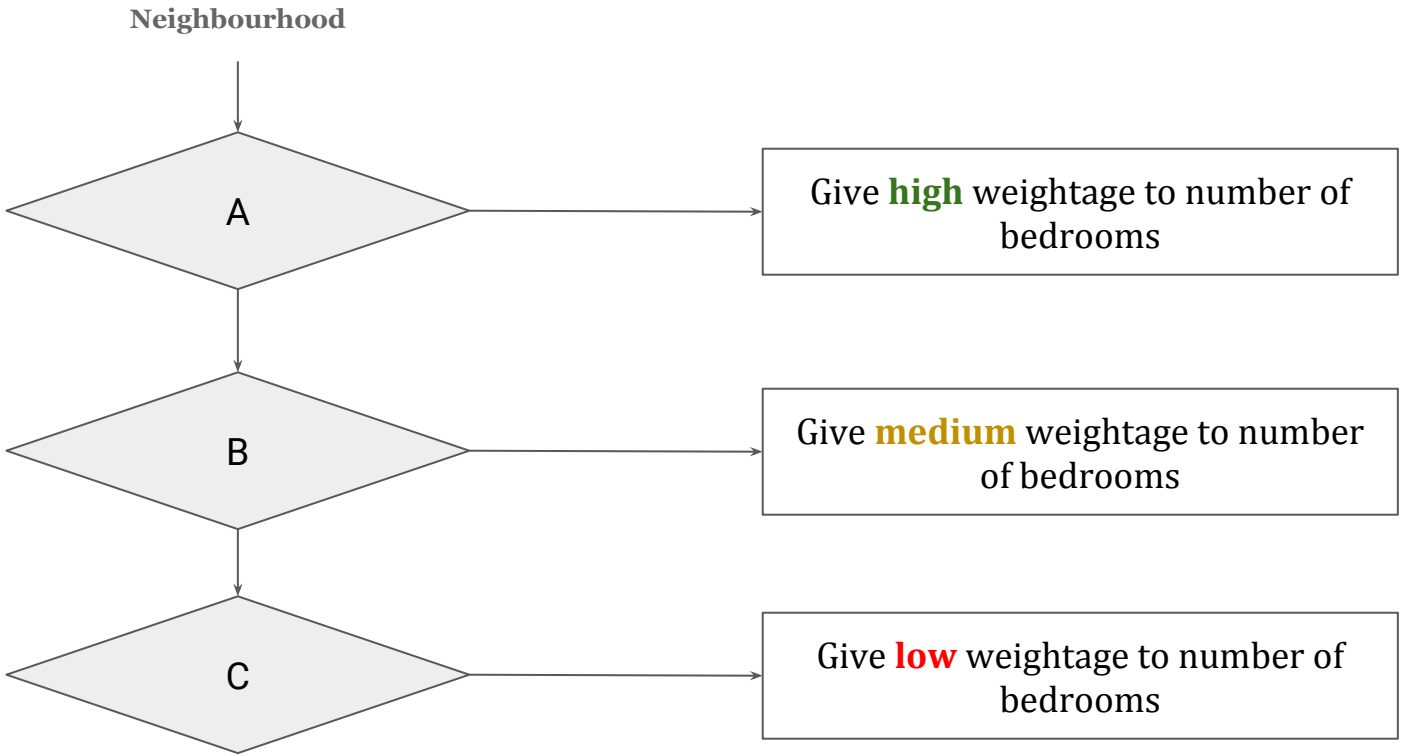
Sq. Ft	Neighbourhood	Bedrooms	Price (‘000)
1250	Gachibowli	3	???

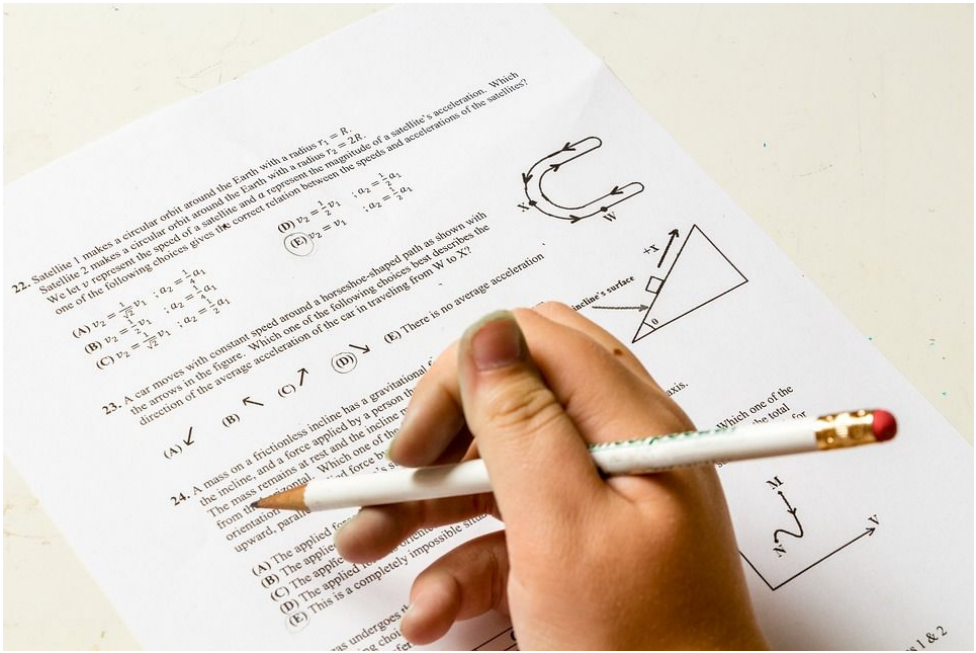


$$y = w_1 x_1 + w_2 x_2 + w_3 x_3 + b$$

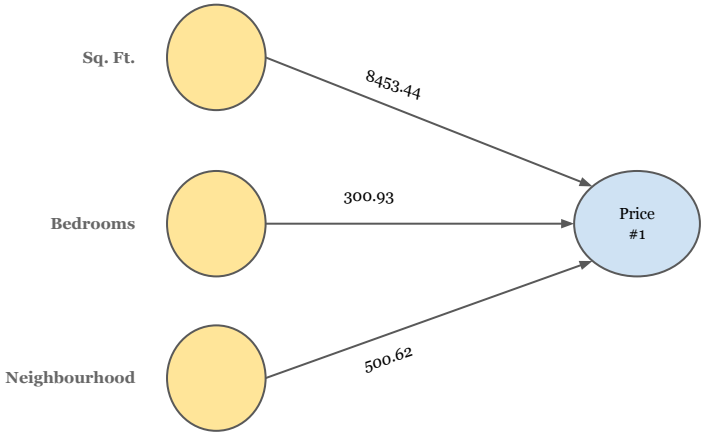
Not this simple!!!

There are usually lots of ifs and buts...


Neighbourhood
A
B
C
Give high weightage to number of bedrooms
Give medium weightage to number of bedrooms
Give low weightage to number of bedrooms

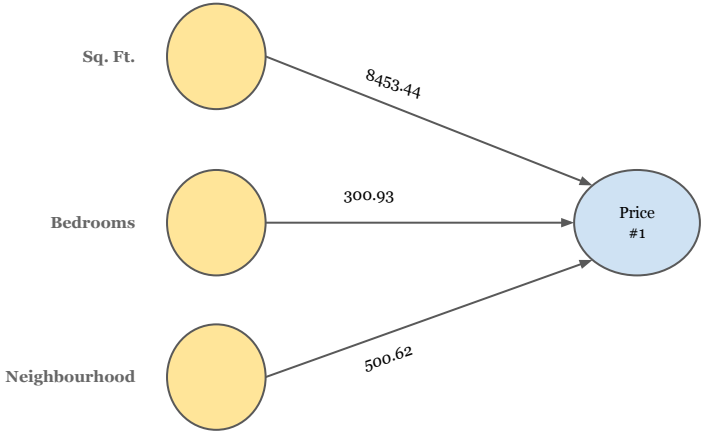


How do we capture complex logic?

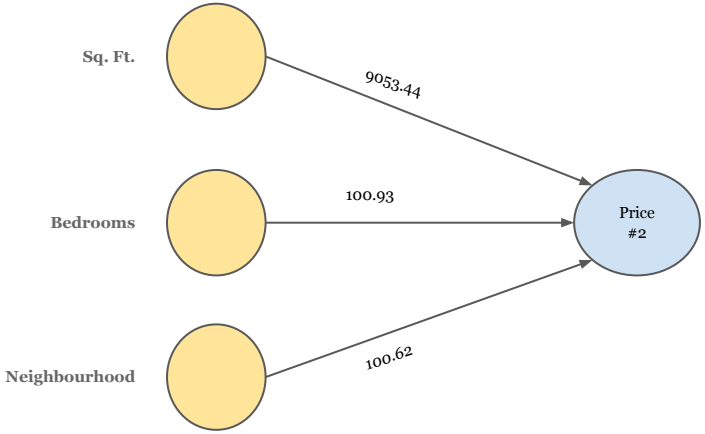


First Set of Weights

Learn some logic in data

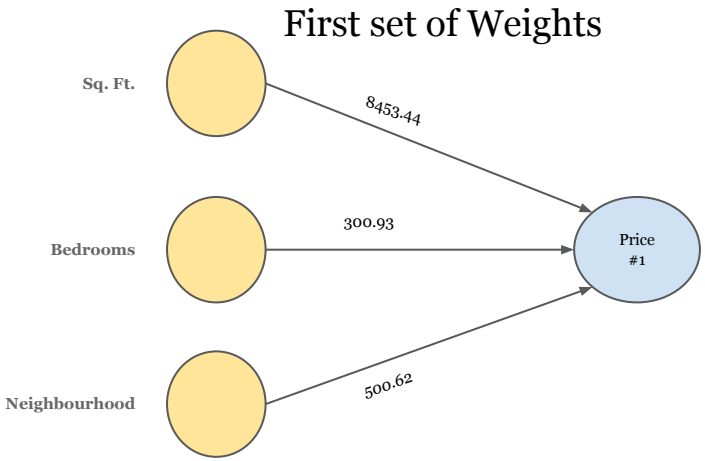


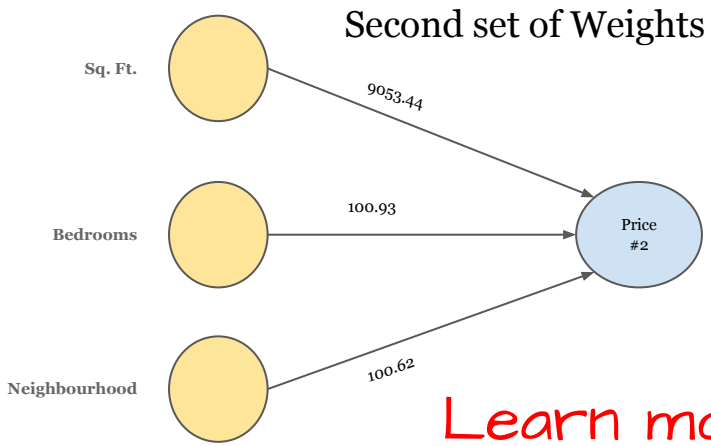
First Set of Weights



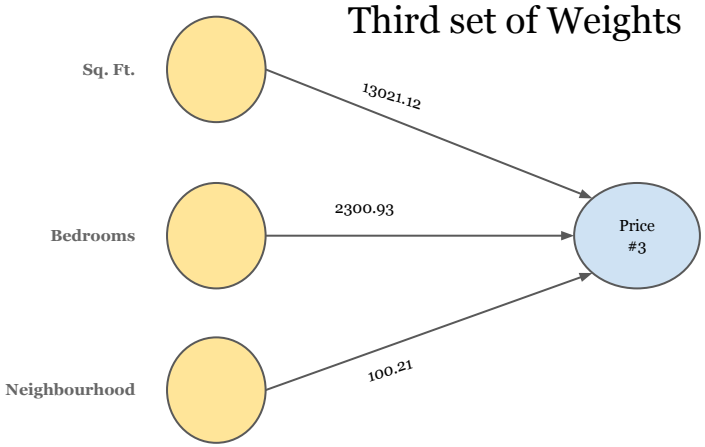
Second Set of Weights

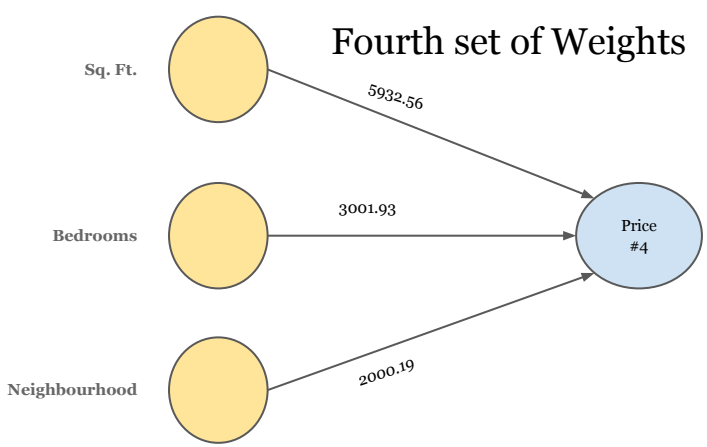
Learn ANOTHER logic in data





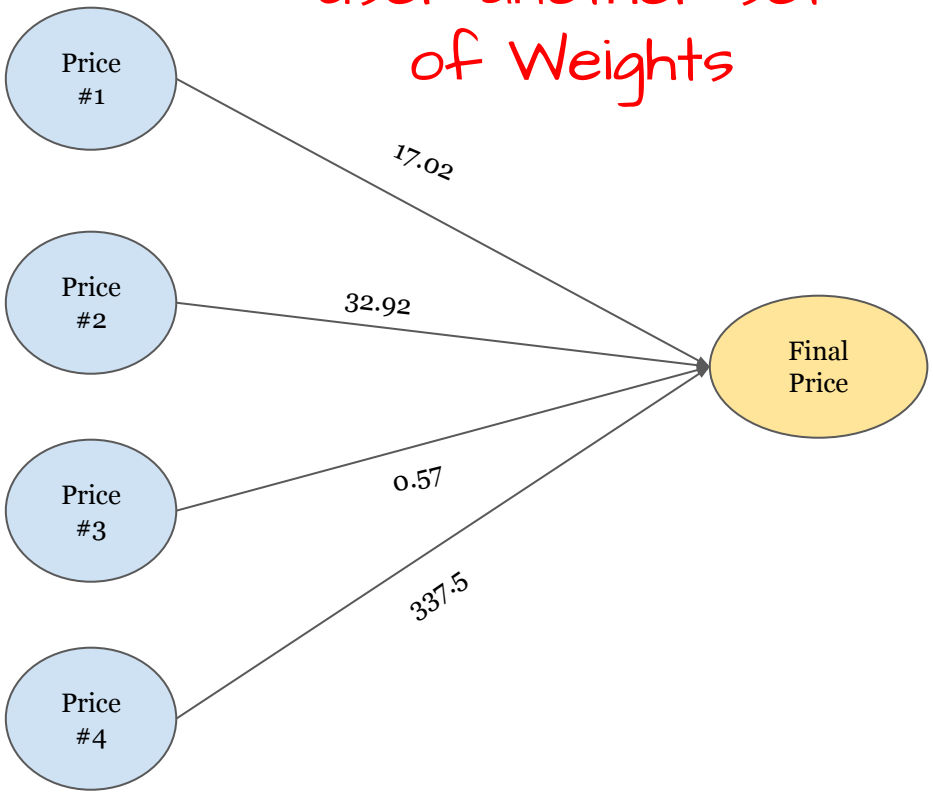
Learn more and more

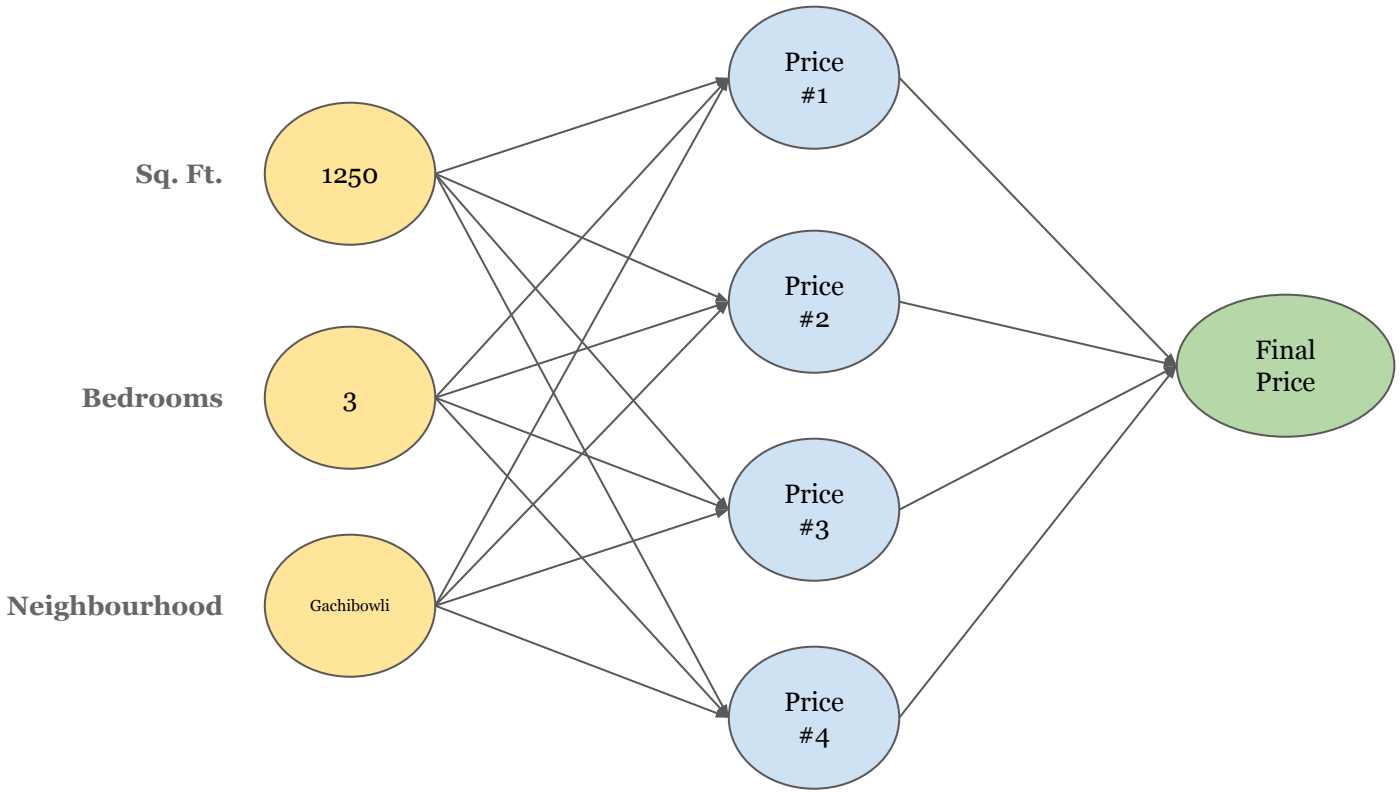




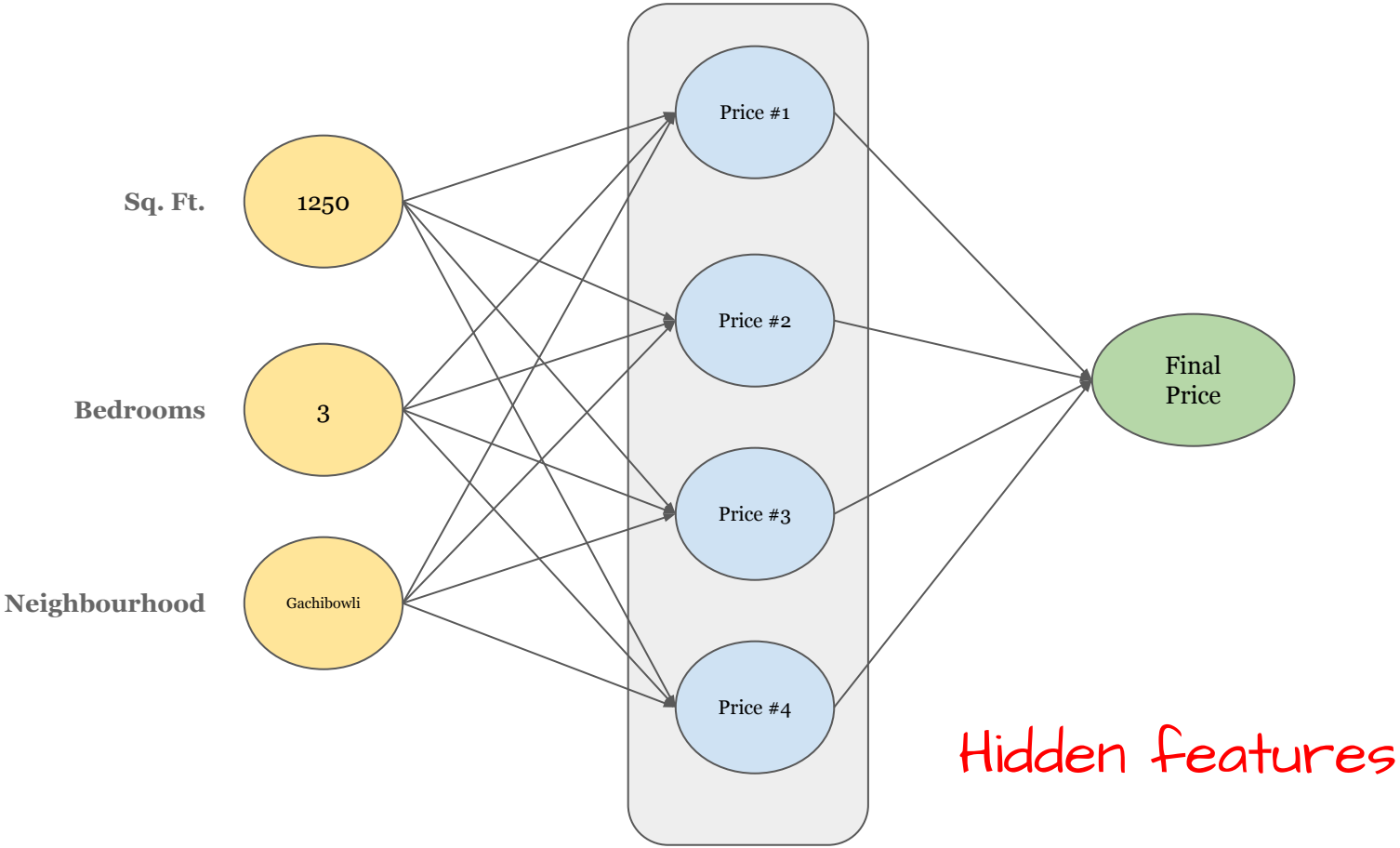
What to do with all the Prices?

User another set of Weights




Sq. Ft.
1250
Bedrooms
3
Neighbourhood
Gachibowli
Price #1
Price #2
Price #3
Price #4
Final Price

What do Price# 1, 2, 3 and 4 represent?

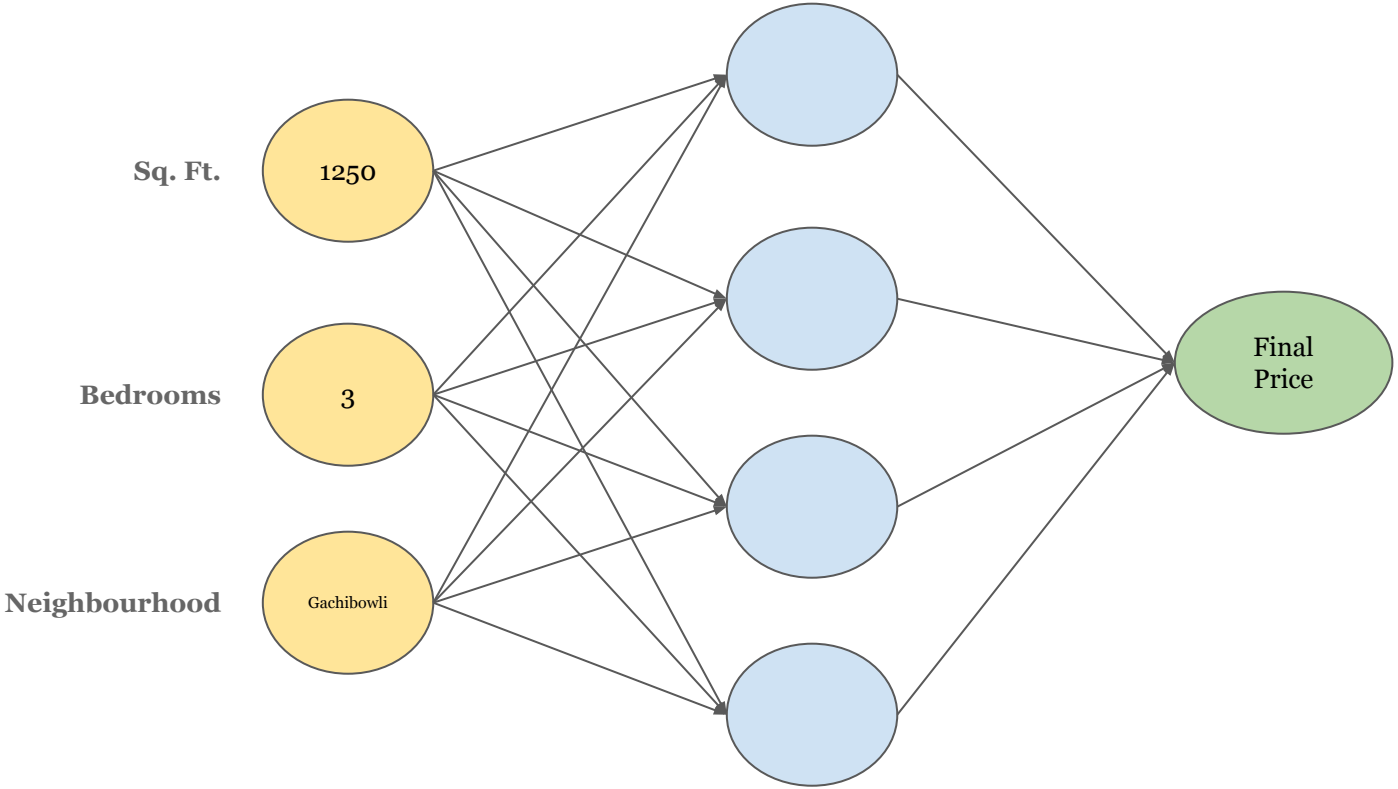

Sq. Ft.
1250
Bedrooms
3
Neighbourhood
Gachibowli
Price #1
Price #2
Price #3
Price #4
Final Price
Hidden features

What are these hidden features?

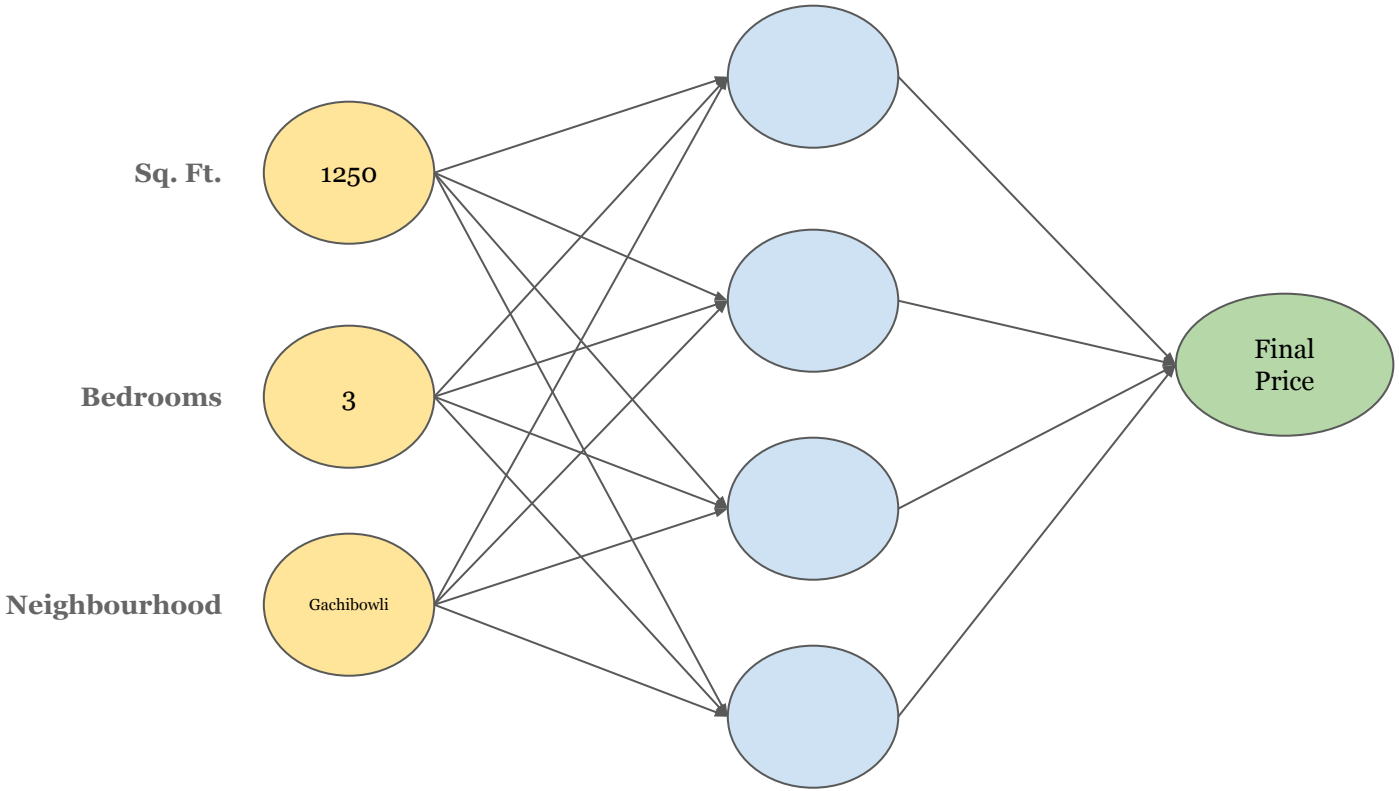
What are these hidden features?

We, humans, do not really understand them

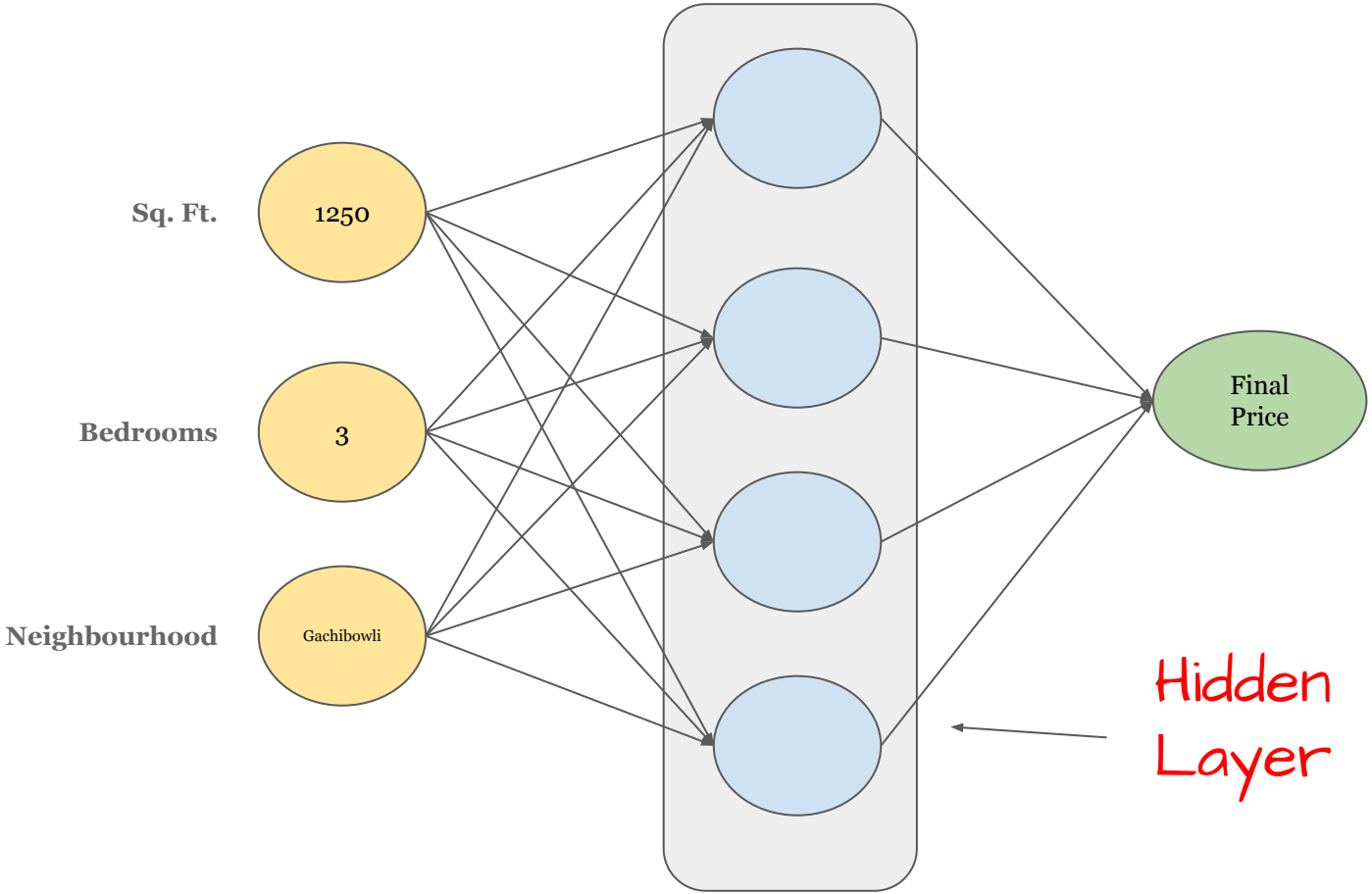
It’s like ‘Lego’

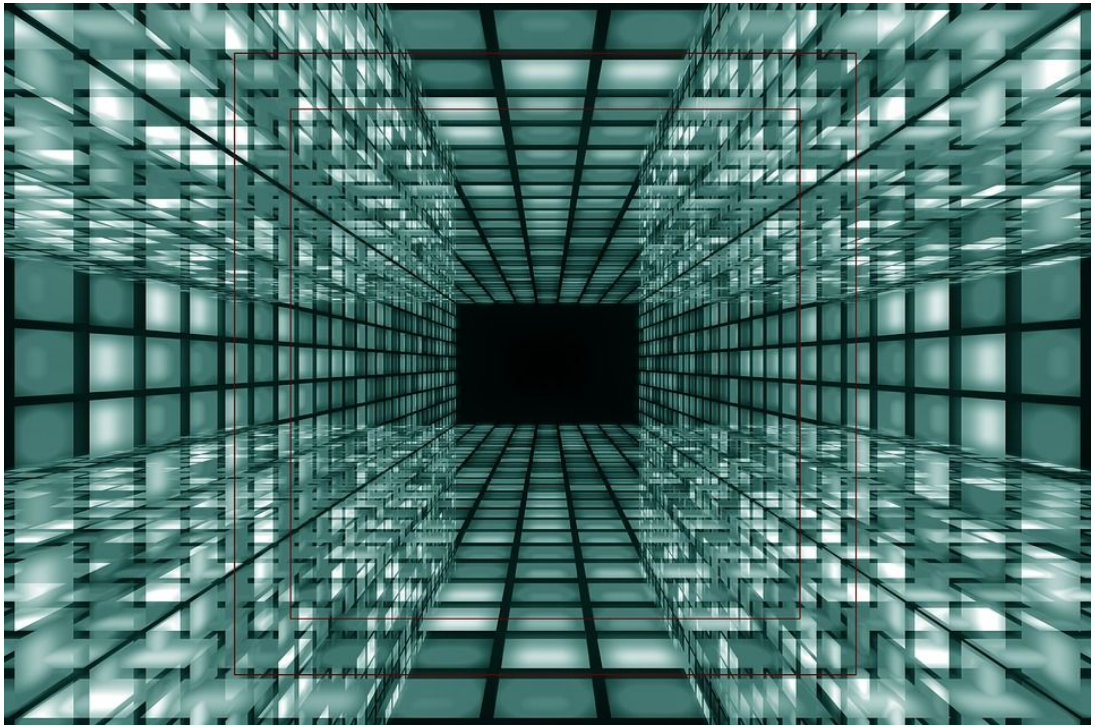


What is this structure?



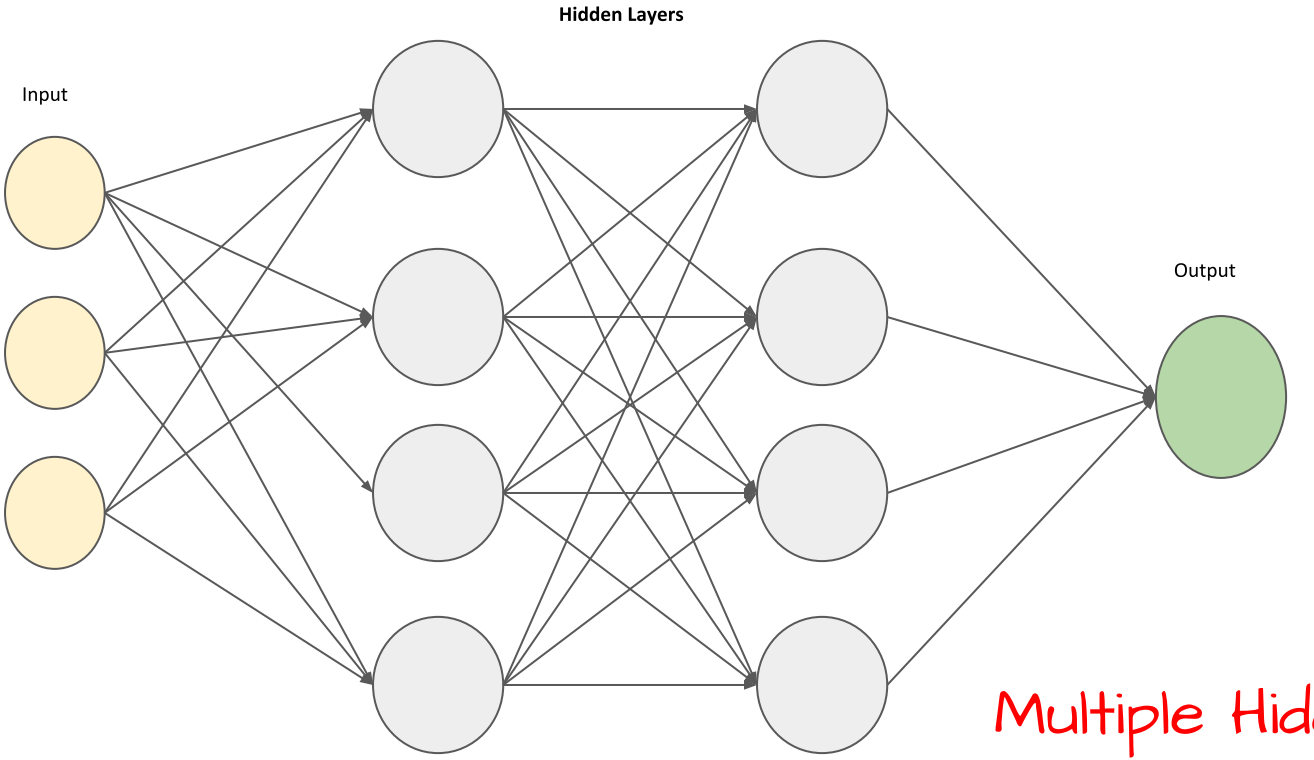
Neural Network


Sq. Ft.
1250
Bedrooms
3
Neighbourhood
Gachibowli
Final Price
Hidden Layer



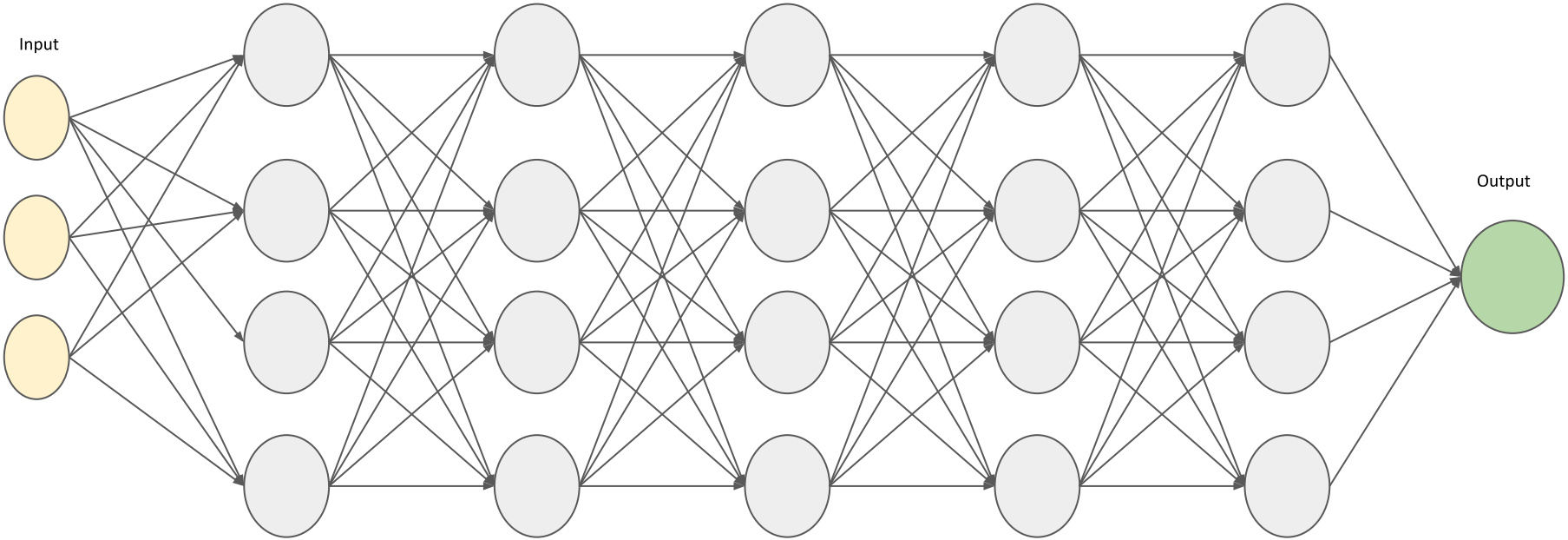
What is Deep Learning

Deep Neural Network



Multiple Hidden Layers

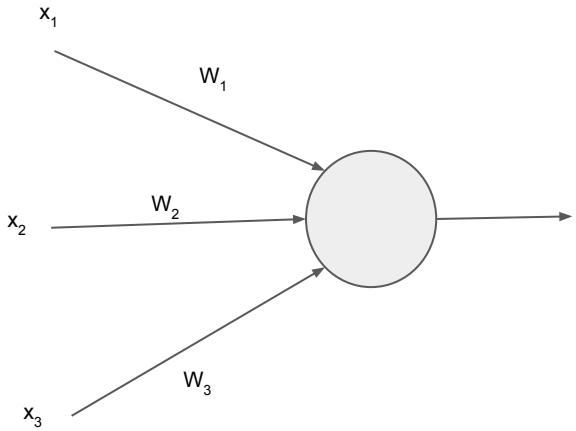
Deep Neural Network



Adding non-linearity to Decision making

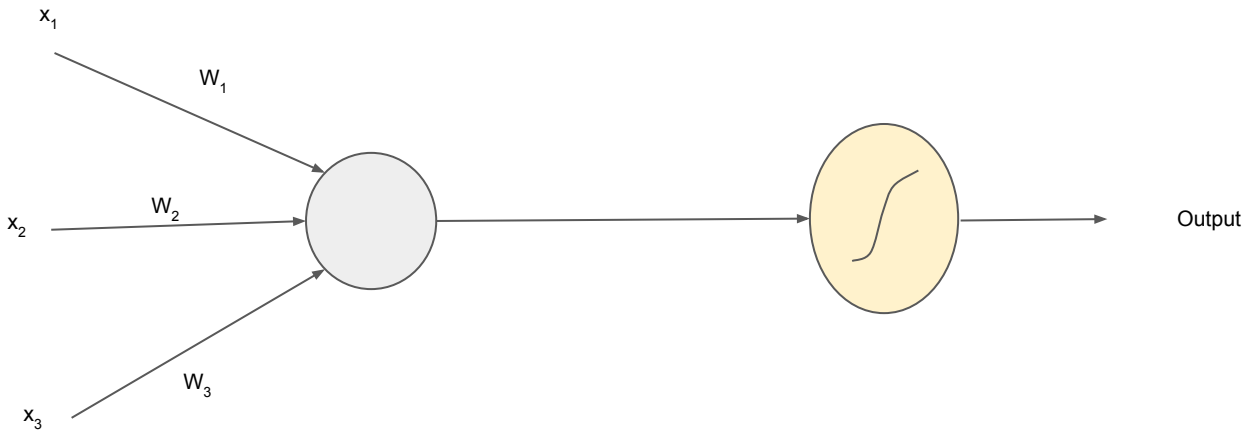
Activation function

Neuron output

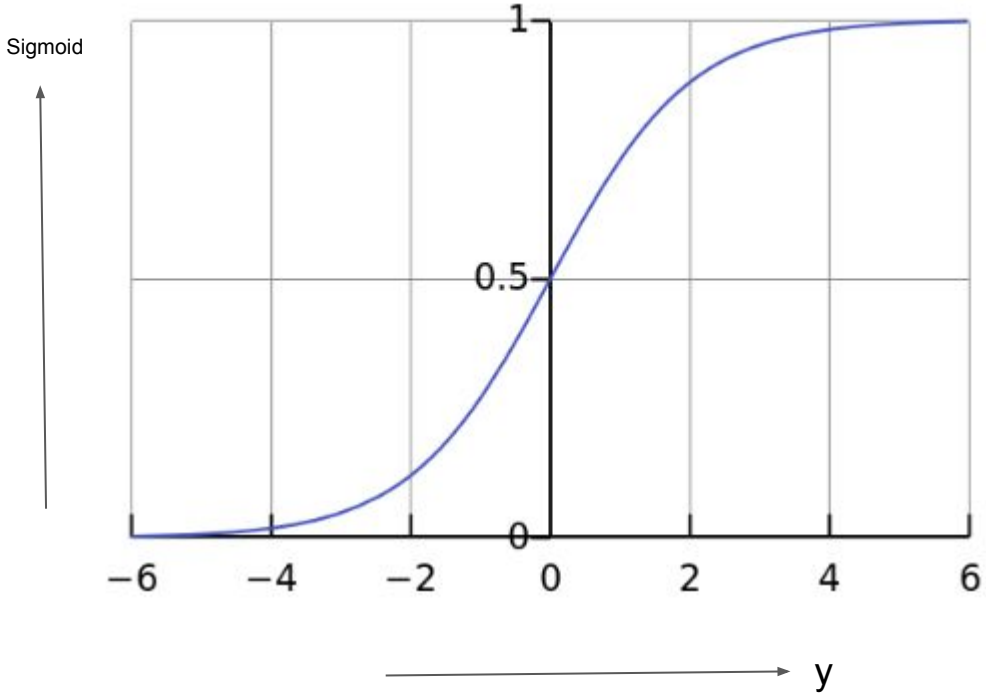


$$y = w_1 x_1 + w_2 x_2 + w_3 x_3 + b$$

Controlling Neuron firing



Sigmoid Function

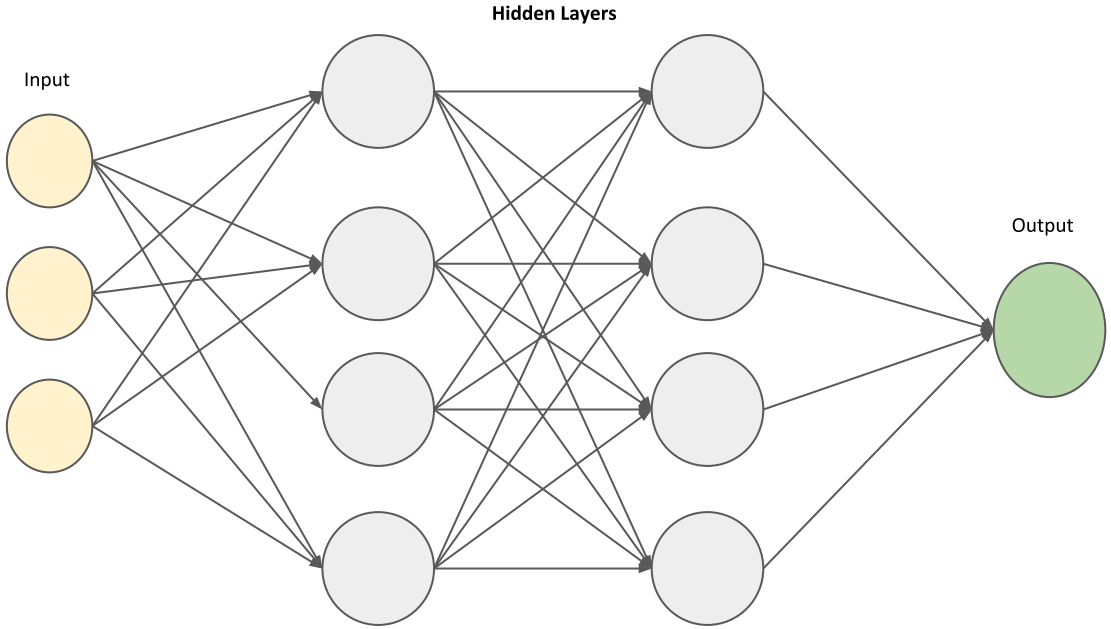


$$sigmoid(y) = \frac{1}{1 + e^{-y}}$$

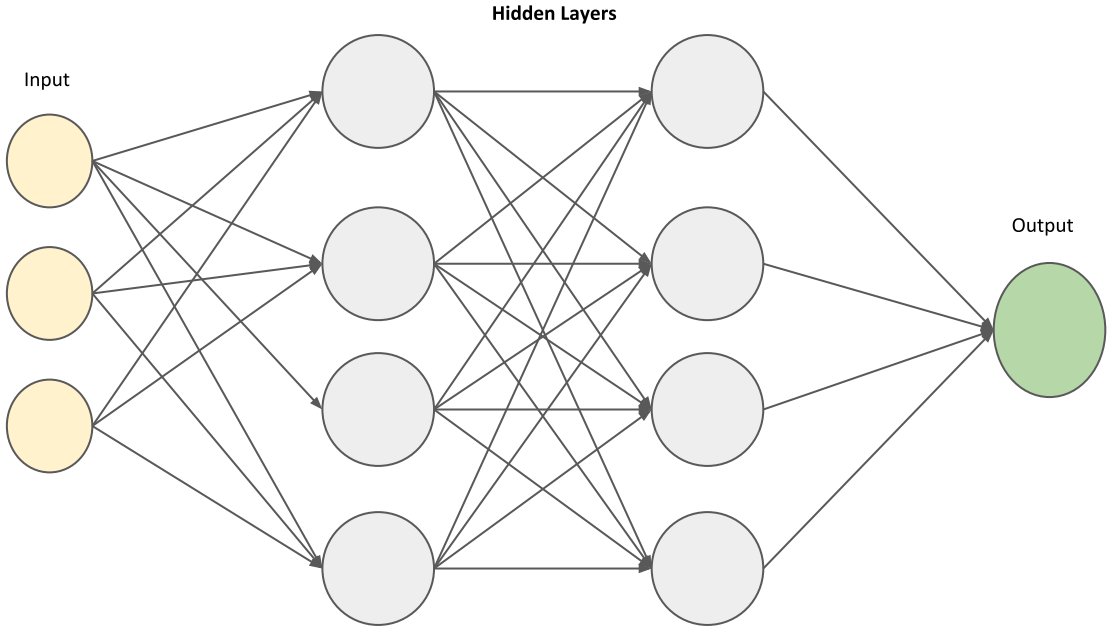
$$y = \sum wx + b$$

How do we update weights?

Number of weights

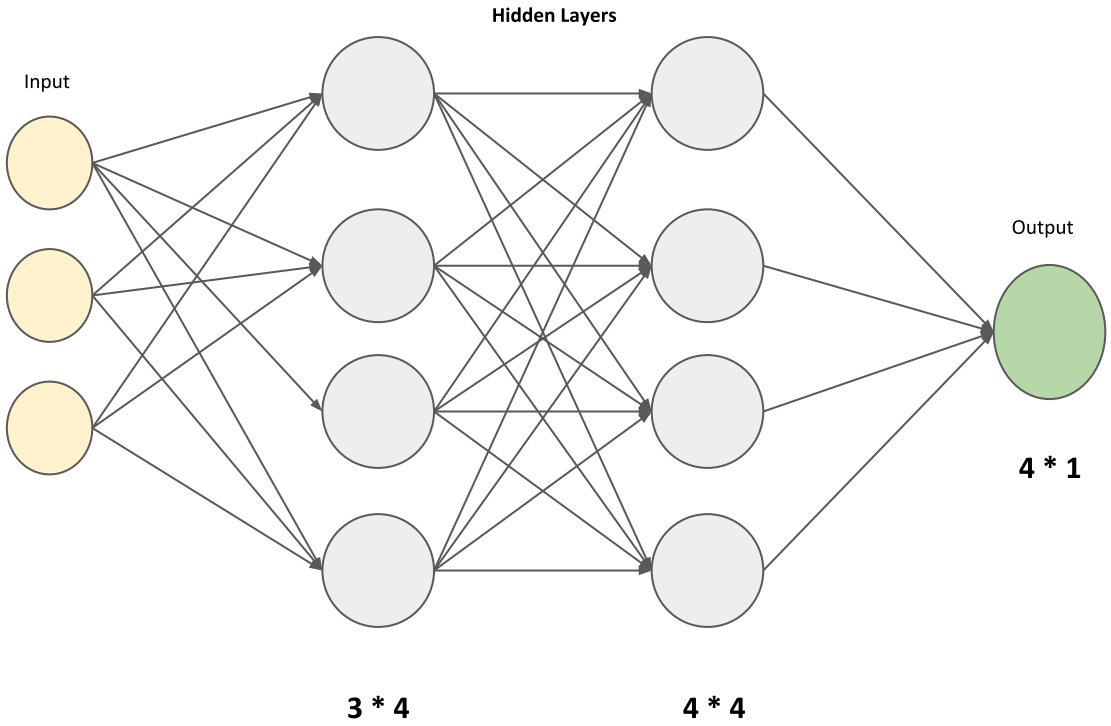


Number of weights



3 * 4

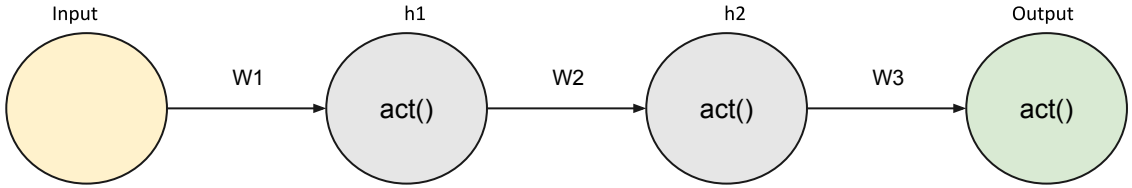
Number of weights



Function Derivative

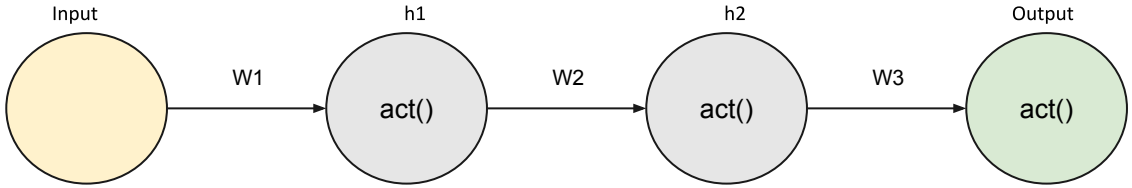
$$w_{new} = w_{old} - \eta \frac{d}{dw} J(w_{old})$$

Output in Neural Network



$$Output = act(w3 * h2)$$

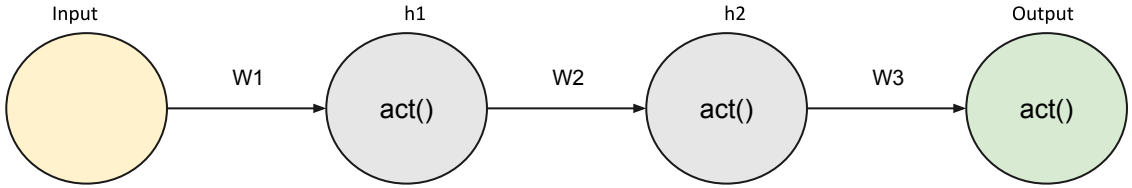
Output in Neural Network



$$Output = act(w3 * h2)$$

$$h2 = act(w2 * h1)$$

Output in Neural Network

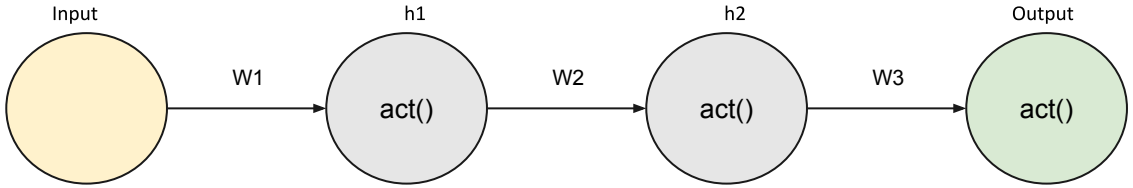


$$Output = act(w3 * h2)$$

$$h2 = act(w2 * h1)$$

$$h1 = act(w1 * input)$$

Output in Neural Network



$$Output = act(w3 * h2)$$

$$h2 = act(w2 * h1)$$

$$h1 = act(w1 * input)$$

$$Output = act(w3 * act(w2 * act(w1 * input)))$$

Derivative of Output function w.r.t w1

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$$Chain\ rule \rightarrow \frac{d\,f(g(x))}{dx} = \frac{df}{dg} * \frac{dg}{dx}$$

Derivative of Output function w.r.t w1

$$Chain\ rule \rightarrow \frac{d\,f(g(x))}{dx} = \frac{df}{dg} * \frac{dg}{dx}$$

$$f(w1) = output(h2(h1(w1)))$$

Derivative of Output function w.r.t w1

$$Chain\ rule \rightarrow \frac{d\,f(g(x))}{dx} = \frac{df}{dg} * \frac{dg}{dx}$$

$$f(w1) = output(h2(h1(w1)))$$

$$\frac{d\,f(w1)}{d\,w1} = \frac{d\,output}{d\,h2} * \frac{d\,h2}{d\,h1} * \frac{d\,h1}{d\,w1}$$

Loss function w.r.t Weights

Loss function w.r.t Weights

$$\frac{d\,LOSS}{d\,w3} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,w3}$$

Loss function w.r.t Weights

$$\frac{d\,LOSS}{d\,w2} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,h2} * \frac{d\,h2}{d\,w2}$$

$$\frac{d\,LOSS}{d\,w3} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,w3}$$

Loss function w.r.t Weights

$$\frac{d\,LOSS}{d\,w1} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,h2} * \frac{d\,h2}{d\,h1} * \frac{d\,h1}{d\,w1}$$

$$\frac{d\,LOSS}{d\,w2} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,h2} * \frac{d\,h2}{d\,w2}$$

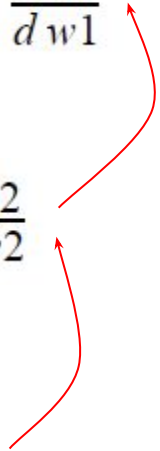
$$\frac{d\,LOSS}{d\,w3} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,w3}$$

Loss function w.r.t Weights

$$\frac{d\,LOSS}{d\,w1} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,h2} * \frac{d\,h2}{d\,h1} * \frac{d\,h1}{d\,w1}$$

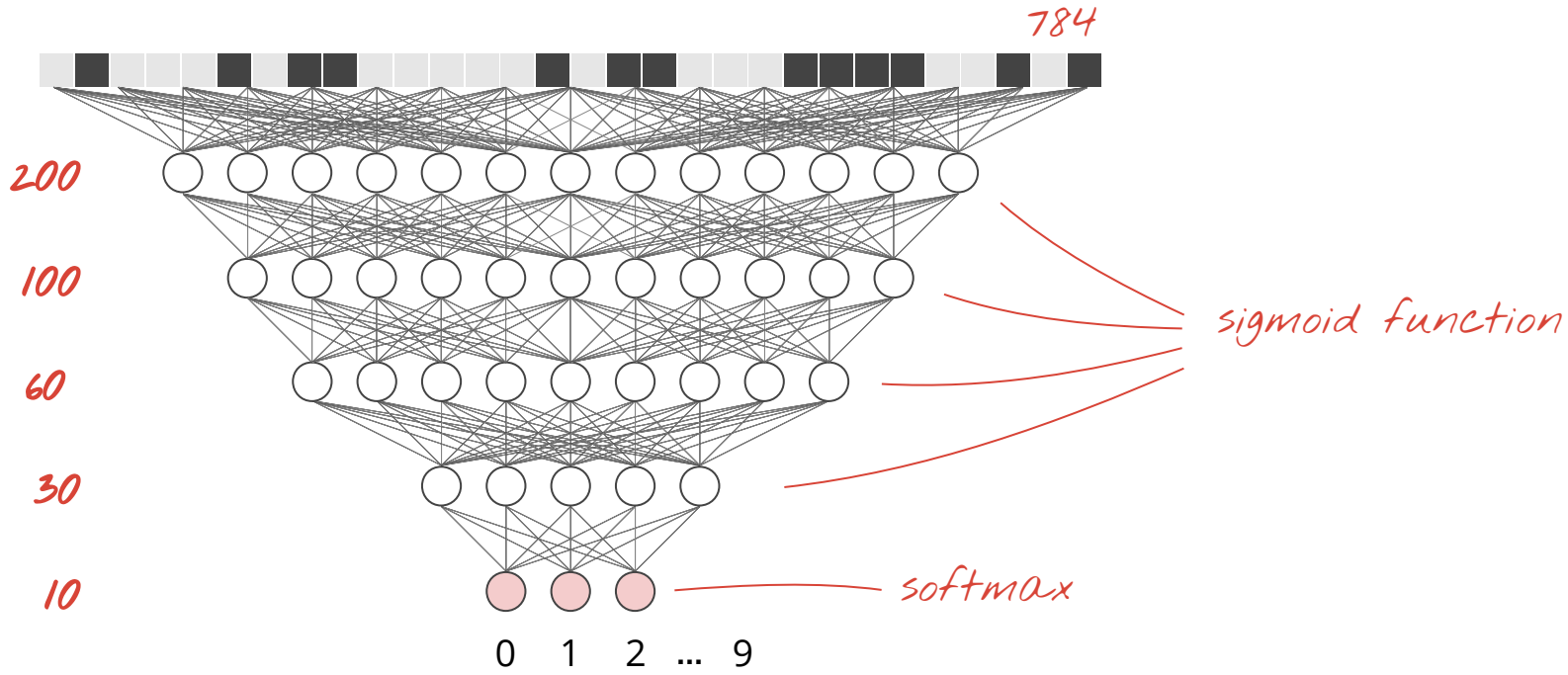
$$\frac{d\,LOSS}{d\,w2} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,h2} * \frac{d\,h2}{d\,w2}$$

$$\frac{d\,LOSS}{d\,w3} = \frac{d\,Loss}{d\,output} * \frac{d\,output}{d\,w3}$$



Backpropagation Algorithm

Applying Deep Learning on MNIST


784
200
100
60
30
10
sigmoid function
softmax
0 1 2 ... 9