A Bayesian Analysis of Abundance, Trend and Population Viability for Harbor Seals in Iliamna Lake, Alaska

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Abstract

Harbor seals in Iliamna Lake, Alaska, are a small, isolated population, and one of only two freshwater populations of harbor seals in the world, yet little is known about their abundance or risk for extinction. Bayesian hierarchical models were used to estimate abundance and trend of this population. Observational models were developed from aerial survey and harvest data, and they included effects for time-of-year and time-of-day on survey counts. Underlying models of abundance and trend were based on a Leslie matrix model that used prior information on vital rates from the literature. We developed three scenarios for variability in the priors and used them as part of a sensitivity analysis. The models were fitted using Markov chain Monte Carlo methods. The population production rate implied by the vital rate estimates was about 5\% per year, very similar to the average annual harvest rate. After a period of growth in the 1980s, the population appears to be relatively stable at around 400 individuals. A population viability analysis assessing the risk of quasi-extinction, defined as any reduction to 50 animals or below in the next 100 years, ranged from 1% to 3%, depending on the prior scenario. Although this is moderately low risk, it does not include genetic or catastrophic environmental events, which may have occurred to the population in the past, so our results should be applied cautiously.

KEY WORDS: quasi-extinction, Leslie matrix, demography, survival, hierarchical model

1 INTRODUCTION

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For the management of a natural population of animals, the goals of analysis often include learning about 1) demographic parameters, 2) the population's relationship to the environment, 3) abundance of the population, 4) trend of the population, and 5) viability of the population. All of these goals may be important when making decisions about a population's risk of extinction, such as a listing decision under the U.S. Endangered Species Act. Often, different data sets and analyses are used for the different goals. However, information on any component is typically expensive to collect and may not be readily available. In those cases, in order to make the best decision, it may be possible to develop prior distributions on various components from other literature and expert opinion. In addition, demography, 10 environment, abundance, trend, and viability are all related, and a single model that borrows 11 information from each component and treats uncertainty globally is preferred (Goodman, 12 2004). Although not the only approach, Bayesian models are attractive in this regard, and 13 have been used successfully in the past as integrated analyses (e.g., Goodman, 2002; Wade, 2002; Maunder, 2004). In this paper, we develop a Bayesian model for incorporating rel-15 atively sparse information on counts, harvests, demography, and environmental factors to 16 improve quantitative understanding of abundance, trend, and population viability for a small 17 population of harbor seals, *Phoca vitulina*, inhabiting a large freshwater lake in Alaska. 18

Iliamna Lake is located in southwest Alaska, and it is drained by the Kvichak River 19 to Bristol Bay. It is Alaska's largest freshwater lake, approximately 121 km long, up to 20 32 km wide and as deep as 300 m (Anderson, 1969; Hauser et al., 2008). The seals in 21 Iliamna Lake have been genetically confirmed as harbor seals and there has been no scientific 22 documentation of any rationale for considering them to be a subspecies other than the eastern North Pacific subspecies (P. v. richardii) (Burns et al., 2016). These are one of just five freshwater seal populations in the world, and one of just two harbor seal populations 25 (the other consisting of the subspecies P. v. mellonae, in the Lacs des Loups Marins of 26 the Ungava Peninsula, Québec) that persist in freshwater (Smith et al., 1996). The seals in 27 Iliamna Lake appear to be discrete, although there could potentially be interchange with the saltwater seal population in Bristol Bay via the Kvichak River. Genetic analysis and local understanding of the lake seals' isolation suggest that they are a separate population (Burns 30 et al., 2016; National Marine Fisheries Service, 2016). 31

Seals are observed in the lake year-round and the peak of births occurs in mid-July (Burns et al., 2016). The harbor seals in Iliamna Lake make use of abundant salmon runs

(Hauser et al., 2008), at least during the summer, as their main prey. Iliamna Lake typically freezes over for much or all of the winter and provides a unique challenge for year-round persistence. When ice covers the lake, fewer seals are observed and little is known about how seals adjust their behavior in response to the ice cover. During that time, harbor seals in the lake likely make use of near-shore leads, cracks, and spaces under the ice for breathing (Burns et al., 2016). In the winter, seals are occasionally observed resting on the ice, and harvest by Alaska Natives usually occurs on the ice in spring, before the ice cover breaks up.

The conservation and management of harbor seals in Iliamna Lake requires decisions that must be made with limited empirical data on demographic parameters, abundance, trend and population viability. Additionally, the data that are available originated from a variety of research projects and methodologies that were not necessarily designed for our objectives. We used aerial surveys of harbor seals in Iliamna Lake conducted by various agencies and organizations, and harvest information, also collected from a variety of sources. Our Bayesian analysis allows flexible inclusion of data from varied sources and allows us to borrow useful information from other harbor seal studies. This framework not only provides the basis for a population viability analysis but sheds light on this unusual ecological setting for harbor seals. We now summarize some of the literature that either informed our development of priors for the Bayesian model, or expresses our expectations about the results.

We examined two main factors associated with variation in observed seal numbers: time-of-year and time-of-day for aerial surveys. These factors are generally related to when seals haul out of the water. From studies of seals in saltwater, there is evidence that seals prefer to haul out near the middle of the day, or shortly thereafter (Boveng et al., 2003; Simpkins et al., 2003; Mathews & Pendleton, 2006; Ver Hoef et al., 2010). However, many other factors are also important, so the time-of-day effect may be weak and complex with considerable variation (Ver Hoef & Frost, 2003; London et al., 2012). Nonpup seals undergo molt each year, generally during the month of August in Alaska. It is well established (see literature listed above) that harbor seals in marine environments spend more time hauled out during molt, so we expected to see similar patterns for the harbor seals of Iliamna Lake, with a peak sometime in early to mid-August. We expected to see an earlier peak for pups, with peak pupping in mid-July. However, pups do not molt in their first summer and will start to spend more time foraging (less time hauled out) as they grow. In addition, the pups grow rapidly and are difficult to distinguish from adults by mid-August when they wean, so we expected their counts to decrease by the time non-pup counts were peaking.

No formal abundance estimates have been made for the harbor seals in Iliamna Lake.

Anecdotal evidence (Burns, 1978) suggested that there may have been around 300 individuals in the 1960s, and a subsequent drop to about 50 after a series of hard winters. Aerial surveys commenced in 1984 and have been conducted more frequently in recent years. Because 70 harbor seal counts typically vary greatly from day to day, Mathisen & Kline (1992) suggested 71 summing the highest counts from each haul-out site from multiple surveys in a short time 72 inverval, yielding an estimate of 137 seals in the lake in 1991. Later surveys indicated greater abundance to near 400 seals, with a maximum single-day count of 357 in 2008 (ABR, Environmental Research and Service, 2011). Summing the highest site-wise counts as recommended by Mathisen & Kline (1992) produced estimates of 367, 368, and 389 seals 76 in 2005, 2007, and 2009, respectively. All estimates lacked an explicit correction for seals 77 that were missed because they were in the water. In saltwater, Simpkins et al. (2003) 78 estimated that at least 20% to 35% of seals would be in the water, even when correcting to hypothetical ideal conditions (of date, time of day, tide, and weather) for hauling out. 80 Using just date, time of day, and tide information from satellite transmitters affixed to seals 81 in nearby Cook Inlet, Alaska, Ver Hoef et al. (2010) found that about 40% of seals would be hauled out under optimum conditions. Those data lacked information from the molt period because satellite transmitters were attached to hair, which falls off during molt. In summary, previous estimates based on counts are likely to be low, by perhaps 20% or more. Thus, our working hypothesis was that seal abundance was slightly over 400 individuals in 2005 - 2009. 86

With so little documentation of historical abundance, we could only surmise that the population trend may have encompassed an increase since the 1970s, from a low of around 50 seals to recent numbers of around 400. In addition to using observed changes in abundance to estimate trends, rates of survival and reproduction can be used to infer population trend. However, even less is known about these demographic parameters than abundance for harbor seals in Iliamna Lake. In fact, very little is known about demographic parameters of harbor seals along the Pacific Rim. An exception is a detailed study on survival for various sex and age classes at a nearby saltwater site, Tugidak Island, by Hastings et al. (2012). Little is known about reproduction as well, though Pitcher & Calkins (1979) provided data from females in the greater Gulf of Alaska region. Local residents along the lake perceived recent seal numbers to be relatively constant (Burns et al., 2016), so we predicted that new data and analysis would indicate a stable population.

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Even a population that has been stable faces certain risks if it is small. Shaffer (1981) outlined four main risks for species extinctions: genetic effects in small populations, demographic stochasticity, environmental stochasticity, and catastrophic events. All of these apply

to populations of any size, but genetic effects and demographic stochasticity are especially 102 important in small populations (Goodman, 1987). A general rule of thumb was established 103 by Franklin (1980) that a population size greater than 50 was necessary to avoid greatly 104 increased chances of extinction due to genetic effects (but see Taylor & Rojas-Bracho, 1999, 105 for caveats). After establishing such thresholds, one goal of population viability analysis is 106 to assess the risk, or probability of crossing such a threshold, often called quasi-extinction 107 (Ginzburg et al., 1982), based on current understanding of a population and the ability to 108 project it into the future. One-hundred years is a common time frame for assessing extinc-109 tion risk of animals, which represents about 11 generations for harbor seals (Swart et al., 110 1996). Based on the relatively small population size, we expected that the harbor seals in 111 Iliamna Lake are at considerable risk for crossing into a realm of critically low population size. 113

The goal of this paper was to develop a Bayesian hierarchical model based in part on a population process model that includes stochastic variation in vital rates and harvest of seals. Linked to the process model is an observational model for counts from aerial surveys that includes time-of-day and time-of-year effects, and the proportion of seals that are in the water and unavailable to be counted during surveys. From this model, we wished to obtain estimates of abundance and trend, and project the population into the future to assess the probability of quasi-extinction for different time horizons up to 100 years. We also wished to perform sensitivity analyses to better understand our prior assumptions. The practical goal of obtaining these results was to provide information for sound management of the harbor seal population in Iliamna Lake.

124 **DATA**

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We conducted aerial surveys of harbor seals in Iliamna Lake between 2008 and 2013. Sur-125 veys were conducted in collaboration with local community participants and researchers at 126 the University of Alaska (Burns et al., 2016). Surveys were flown using high-wing, twin-127 engine aircraft (Aero Commander 680, 690 or de Havilland Twin Otter). Survey altitude 128 was typically 330 m and aircraft speed was typically 120 kts. These abundance surveys were 129 performed several times yearly for most years (Table I). Surveys were timed so that one sur-130 vey was conducted while the lake was mostly frozen (Late March/early April), one during 131 pupping (mid-July), and often several during the August molt, when the greatest numbers of 132 seals typically haul out on shore and are visible to aerial observers. Over the years, a compre-133

hensive list of all known haulout sites was developed. These sites were searched extensively on each flight. Surveys were flown, weather allowing, in the mid- to late-afternoon, when the number of seals hauled out was expected to be highest. Aircraft flight tracks were recorded by GPS and all seals sighted were digitally photographed using a SLR camera (Nikon D700) with zoom lens (Nikkor 80-400mm). Time, date, latitude, longitude, and altitude were auto-matically embedded into the image metadata. The observer manually recorded weather and visibility information, though the surveys were typically conducted during good conditions and these variables were not used in our analysis. The total number of seals at each haul-out site was counted from the digital photographs. Pups were determined by their smaller size and close proximity (< 1 body length; either nursing or laying right next) to a larger seal. Pups were no longer recorded beyond about mid-August when many had been weaned. By that date the pups were large enough that they could not reliably be distinguished from yearlings and 2-year-olds, which we lumped into the non-pup age class for our analysis. In 2009, researchers from the Newhalen village provided 10 additional flights in collaboration with our survey project, and similar techniques were used.

We also used counts obtained prior to 2008 by other organizations. Between 2005 and 2008, ABR, Environmental Research and Service (2011) conducted a series of aerial surveys for harbor seals in Iliamna Lake. In addition, earlier counts from surveys conducted by Alaska Department of Fish and Game (ADFG) (Small, 2001) and surveys from 1984 to 1991 by Mathisen & Kline (1992) were incorporated into the analysis to expand the historical reach. Geographic coordinates were provided (or, when not provided, determined based on descriptions or physical maps) for each survey site and these sites were compared and merged with locations identified by us. In some cases, sites in very close geographic proximity were combined into a single site. In these surveys, as well as our own, seals observed in the shallow water near the haul-out site (typically, within 50 m) were included in the counts. It was rare to observe seals in the water away from haul-out sites, and the very few of those that were seen were not included in the counts. A consistent, collated dataset of all five survey projects served as the basis for our analysis. The data we used are archived with the National Centers for Environmental Information (Withrow et al., 2014) and available for download. Table I summarizes the aerial survey effort across the various agencies and researchers.

Seals in Iliamna Lake have cultural and nutritional importance to residents of the region (Burns et al., 2016) and are harvested by local Alaska Native hunters. Hunting primarily occurs in the late winter and early spring when the lake is still ice-covered. As the ice thins and cracks form, the seals haul out along the cracks and are accessible to hunters.

Some hunting may go on during summer, but these animals are taken more opportunistically while the earlier hunt is a directed subsistence activity. The numbers of seals harvested from Iliamna Lake have been estimated by household surveys of hunters in the local communities, 170 conducted by the ADFG Subsistence Division (Fall et al., 2006; Krieg et al., 2009; Burns 171 et al., 2016). We used harvest estimates for the various years between 1992 and 2011 (Ta-172 ble II), that were summarized by Burns et al. (2016). We also used estimates from Burns 173 et al. (2011), which were obtained separately from, but by similar methods to the ADFG studies. We did not use values from 1982–1991 that were reported by Burns et al. (2016) 175 because we were less certain about whether some of those harvests were from the Kvichak 176 River, rather than Iliamna Lake. Note that because not all households in each commu-177 nity were surveyed, harvest data were estimated such that the values are not necessarily 178 represented as whole numbers of seals per year.

3 ABUNDANCE, TREND AND POPULATION VIABILITY

In this section, we describe the basic model for the data, and priors for the model parameters.

We used Markov chain Monte Carlo (MCMC) methods for fitting the model (e.g., Gilks
et al., 1996), which provide a sample from the posterior distribution of the parameters, such
as survival and productivity. That sample also enables inference on derived quantities such
as abundance, trend and population viability.

3.1 The Model

For surveys in the earlier years when pups were not distinguished from non-pups, we denote the combined counts as $Z_{t,i}$ for the *i*th count in the *t*th year. Later, when pups were distinguished from non-pups, we denote pup counts as $X_{t,i}$ for the *i*th count in the *t*th year, and non-pup counts as $Y_{t,i}$. Harvest data, as given in Table II, are denoted by $H_{t,m}$ for the tth year and the *m*th village. We used the follow observational models for harbor seal counts 193 in Iliamna Lake,

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$$[X_{t,i}|\lambda_{t,i},\eta^{2}] = \mathcal{N}(\lambda_{t,i},\eta^{2}),$$

$$[Y_{t,i}|\mu_{t,i},\sigma^{2}] = \mathcal{N}(\mu_{t,i},\sigma^{2}),$$

$$[Z_{t,i}|\lambda_{t,i},\mu_{t,i},\eta^{2},\sigma^{2}] = \mathcal{N}(\lambda_{t,i}+\mu_{t,i},\eta^{2}+\sigma^{2}),$$

$$[H_{t,m}|\boldsymbol{\nu}_{m},C_{m}] = \mathcal{D}\mathcal{U}_{m}(1/C_{m}), H_{t,m} \in \{v_{1},\ldots,v_{C_{m}}\},$$
(1)

where $\mathcal{N}(a,b)$ is a Gaussian (normal) distribution with mean a and variance b, and $\mathcal{DU}(\cdot)$ is a discrete uniform where $H_{t,m}$ takes one of the values $\boldsymbol{\nu}_m = (v_1, \dots, v_{C_m})$ with equal probability $1/C_m$ for C_m different classes. Here, C_m is the number of different years with observations per village, and we simply allow for a discrete uniform distribution on the observed values for each village.

We built our model hierarchically (Cressie et al., 2009). We assumed that there is some true underlying population value for pups, P_t , and non-pups, A_t , for each year t. However, some part of the population is in the water, away from the haul-out sites, and unobservable, so we denote the proportion that is observable as ψ . This observed value is also affected by covariates; in this case day-of-year $d_{t,i}$ and hour-of-day $h_{t,i}$. The means of the observations in Equations (1) are set up as linear models,

$$\lambda_{t,i} = \psi P_t + \alpha_{d,1} d_{t,i} + \alpha_{d,2} d_{t,i}^2 + \alpha_{h,1} h_{t,i} + \alpha_{h,2} h_{t,i}^2,
\mu_{t,i} = \psi A_t + \beta_{d,1} d_{t,i} + \beta_{d,2} d_{t,i}^2 + \beta_{h,1} h_{t,i} + \beta_{h,2} h_{t,i}^2.$$
(2)

with regression parameters $\alpha_{d,1}$, $\alpha_{d,2}$, $\alpha_{h,1}$, and $\alpha_{h,2}$ that control how day-of-year and timeof-day affect pup counts, and $\beta_{d,1}$, $\beta_{d,2}$, $\beta_{h,1}$, and $\beta_{h,2}$, which control how day-of-year and time-of-day affect non-pup counts. Notice that we could model some interaction between $\alpha_{d,\bullet}$ and $\beta_{d,\bullet}$ because, as pups mature during the summer, they cannot be distinguished from non-pups. However, we have too little information and data for such estimates, and hence we leave $\alpha_{d,\bullet}$ and $\beta_{d,\bullet}$ as free parameters to capture such interactions.

Note that the construction ψP_t and ψA_t leads to a nonidentifiability problem in the model. Any increase in P_t can be counteracted by a decrease in ψ so that the product remains unchanged. We approached the problem as follows. First, we gave total abundance a lower bound by constraining $P_t + \alpha_{d,1} d_{t,i} + \alpha_{d,2} d_{t,i}^2 + \alpha_{h,1} h_{t,i} + \alpha_{h,2} h_{t,i}^2$ to be greater than $\max\{X_{i,t}\}/0.9$ for every t, and likewise $A_t + \beta_{d,1} d_{t,i} + \beta_{d,2} d_{t,i}^2 + \beta_{h,1} h_{t,i} + \beta_{h,2} h_{t,i}^2$ to be greater than $\max\{Y_{i,t}\}/0.9$ for every t, or their sum to be greater than $\max\{Z_{i,t}\}/0.9$, depending on how the data were collected in year t. Our justification for such a constraint follows from

Simpkins et al. (2003). They found that, under optimal conditions, the expected proportion of seals hauled out of the water was around 0.815, but the maximum that was observed across time was between 0.84 and 0.92 (for two different study areas). Thus, we used a value of 0.9. Note that, for consistency with surveys conducted by others previously, we have included seals seen in shallow water near the haul-out sites as part of the fraction of the population that is 'hauled out'. This differs slightly from the convention used in most studies of marine harbor seals, in which only seals actually hauled out on shore are considered to be hauled out and observable.

The nonidentifiability probem is still unsolved if abundance is uniformly distributed from the lower bound to infinity while ψ is constrained between zero and one. To solve this, we used an informative beta distribution as a prior for ψ . With a proper anchoring of ψ , there is some information on the haulout distribution from the surveys because the counts varied considerably. For example, if we could assume that the maximum number of counted seals reflected that 100% were hauled out, then a mean haul-out rate could be computed from all other surveys with less than the maximum count. The prior distribution helps anchor this distribution to realistic haul-out values, and we discuss our particular choice in the next section.

We also used a constant ψ rather than a temporally-varying ψ_t , for several reasons. First, the number of surveys per year varied considerably. Allowing ψ_t to vary yearly would allow abundance to essentially "track" the yearly maximum, regardless of the number of surveys in that year. The haul-out time study of Simpkins et al. (2003) was based on many time periods, so using the maximum across all years was more appropriate. Secondly, the issue of nonidentifiability exists for the annual variability of ψ_t as well, which would be confounded with the annual variability of P_t and A_t . While we do believe there is annual variability in ψ , because of the confounding we interpret ψ as an average across years and inter-annual variability is captured in the posterior variability of ψ .

Finally, note that we also tried formulating $X_{t,i}$, $Y_{t,i}$, and $Z_{t,i}$ in Equation (1) using negative binomial distributions, and then formulating Equation (2) as

$$\lambda_{t,i} = P_t \exp(\psi + \alpha_{d,1} d_{t,i} + \alpha_{d,2} d_{t,i}^2 + \alpha_{h,1} h_{t,i} + \alpha_{h,2} h_{t,i}^2),$$

$$\mu_{t,i} = A_t \exp(\psi + \beta_{d,1} d_{t,i} + \beta_{d,2} d_{t,i}^2 + \beta_{h,1} h_{t,i} + \beta_{h,2} h_{t,i}^2).$$

However, we found that this multiplicative formulation suffered from over-fitting and further confounding, where the regression coefficients $\alpha_{\bullet,\bullet}$ and $\beta_{\bullet,\bullet}$ would attempt to model the zero counts with unrealistic fits that increased P_t and A_t and decreased ψ in order to obtain the

fits. It seems that having ψ as a multiplicative effect, and $\alpha_{\bullet,\bullet}$ and $\beta_{\bullet,\bullet}$ as additive effects in Equation(2), allows for better identification in the model. Equation (2) is imperfect in the sense that it is not constrained to be nonnegative, nor are the normal distributions used in (1), even though our data are counts. We find this acceptable for the stability in model fitting, and it has no impact on our ability to project into the future based on the Leslie matrix model described next, and in Section 3.5.

We embedded a very simple population model that creates a time series and a relation between the numbers of pups and non-pups. The model included density dependence (Caswell, 2001, p. 511) for fecundity, as this is likely where density dependence occurs for seals,

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$$A_{t} = \delta_{t-1} A_{t-1} + \kappa_{t-1} P_{t-1} - H_{t-1},$$

$$P_{t} = c_{t-1} \phi_{t-1} A_{t-1},$$
(3)

where δ_{t-1} is an autoregressive parameter that, in a population model setting, is survival of non-pups from one year to the next; ϕ_{t-1} is fecundity, defined to be the proportion of non-pups that produce pups that survive to next year's survey period in mid-summer; $c_{t-1} = \exp(-\rho N_{t-1}/1000)$ is a density dependent factor for fecundity, scaled by a parameter ρ , that shrinks ϕ_{t-1} towards zero as $N_{t-1} = A_{t-1} + P_{t-1}$ increases; κ_{t-1} is the proportion of pups that survive from the survey period to become yearlings (and enter the non-pup age class); and H_{t-1} is the number of seals from the total population that were harvested in the previous year.

In Equation (3), absent the harvest, we have used a very simple two-component Leslie matrix model with density dependence (Caswell, 2001, p. 511), $\mathbf{n}_t = \mathbf{M}_{t-1}\mathbf{n}_{t-1}$, where

$$\mathbf{n}_t = \begin{pmatrix} P_t \\ A_t \end{pmatrix}, \quad \mathbf{M}_t = \begin{pmatrix} 0 & c_t \phi_t \\ \kappa_t & \delta_t \end{pmatrix}$$
 (4)

that matches the age class data that we have, namely, counts for pups and non-pups. The model is stochastic (Wade, 2002; Caswell, 2001, p. 452) because we allow δ_t , ϕ_t , and κ_t to vary randomly with year t. Early Bayesian approaches to population modeling that included Leslie matrix models include Raftery et al. (1995) and Poole & Raftery (2000). A review of embedding Leslie matrix models in a Bayesian inference framework, including stochastic demographic parameters, is provided by Gross et al. (2002) and Buckland et al. (2007). Other approaches using stochastic demographic parameters include Cáceres & Cáceres-Saez (2013), who studied effective growth rates when demographic parameters are known, or can

be assumed known, with random perturbations (whose distribution is part of the interest).
They show how to obtain a stable population state with the effective growth rate. Our interest centered more on abundance and trend, and not an estimate or a long-term stable state, which is not very informative with just two age classes in Equation (4).

Note that for harbor seal counts, population trends have often been modeled with 281 loglinear models, such as Poisson or negative binomial regression (see, e.g., Ver Hoef & 282 Frost, 2003; Small et al., 2003; Mathews & Pendleton, 2006), where the trend was a linear or quadratic function of time in the mean of the model. In those regression models, the 284 form of the trend component, and how it behaves near the end of the time sequence, largely 285 determines the trend into the future. There are advantages to demographic models, even 286 very simple ones, especially for population viability analysis. For example, suppose that the 287 trend in the data is slightly positive. A regression approach will continue the trend, and a population would never go extinct. However, a demographic model has such a possibility, 280 even for an overall positive trend, due to the stochastic nature of the parameters, which is a 290 more realistic property of populations. 291

292 **3.2** Priors

A summary of model parameters is given in Table III. To complete the model, we specified prior distributions on the stochastic components,

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[\eta] = \text{UNIF}(0, 30),

[\sigma] = \text{UNIF}(0, 100),

[\alpha_{d,1}] = [\alpha_{d,2}] = [\alpha_{h,1}] = [\alpha_{h,2}] = \text{UNIF}(-\infty, \infty),

[\beta_{d,1}] = [\beta_{d,2}] = [\beta_{h,1}] = [\beta_{h,2}] = \text{UNIF}(-\infty, \infty),

[P_1] = [A_1] = \text{UNIF}(0, \infty),

\{[\phi_t]; t = 1, \dots, 29\} = \text{i.i.d. UNIF}(0, 0.5), \text{ or Beta}(a,b) \text{ for two different scenarios,}

\{[\delta_t]; t = 1, \dots, 29\} = \text{i.i.d. UNIF}(0.5, 1), \text{ or Beta}(a,b) \text{ for two different scenarios,}

\{[\kappa_t]; t = 1, \dots, 29\} = \text{i.i.d. UNIF}(0.5, 1), \text{ or Beta}(a,b) \text{ for two different scenarios,}

[\rho] = \text{UNIF}(0, 1),

[\psi] = \text{Beta}(5, 5)^{30},
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where i.i.d. means independent and identically distributed. Note that in order to start the population model, we needed initial values for A_1 and P_1 , so each of these was given a flat uniform prior distribution.

Most Bayesian analyses require some discussion of the priors (Goodman, 2010). We used noninformative priors when we could, such as for η , σ , α , β , P_1 , and P_1 . However, our sample sizes were quite small, and the form and shape of the prior distribution had a large effect on the other parameters. To investigate those effects, and present a sensitivity analysis, we developed three scenarios for the demographic parameters fecundity (ϕ) , non-pup survival (δ) , and pup survival (κ) . A detailed development of these priors is given in the Appendix, and we give an overview here.

In Table IV, the "base-priors" scenario, was developed from demographic parameters of harbor seal survival and fecundity given in Hastings et al. (2012) and Pitcher & Calkins (1979), respectively. Survival estimates for both males and females, at two different stages of development for pups, and ages classes 1-3 and >3, were obtained from Hastings et al. (2012). Because estimates of pup survival were provided at two different stages, we were able to shift a detailed demographic model based on sex and age at the time of birth, to one based on the time of surveys, and collapse it to just two classes, pups and non-pups. In doing so, we preserved the stable age distribution and population growth rate of the non-shifted and uncollapsed matrix model, and we derived variance estimates for all parameters. Then, because ϕ , δ , and κ were constrained to greater than zero and less than one, we matched moments of the estimates and their variances with a beta distribution to provide a prior distribution that met the required constraints (see Appendix for details).

While the base-priors were derived from the best information that we had on demographic estimates, the associated variances represented sampling error and did not necessarily reflect the variability associated with annual variation in the demographic parameters. Also, the base-priors came from a separate, marine population of seals. The data can inform the posterior distributions of ϕ_t , δ_t , and κ_t , but when sample sizes are small there is some danger in making the priors too narrow because then those priors will largely determine the results. Hence, for the "wide-priors" scenario, we tripled the standard errors of "base-priors". Also, under base-priors, the expectation for population growth rate was around 4% annually. To be neutral on population growth rate, we also adjusted the prior means of ϕ_t , δ_t , and κ_t so that population growth rate was 0. The details are provided in the Appendix and are summarized in Table IV.

For a third scenario, "uniform-priors," we used constrained noninformative priors. For ϕ , it would be very unlikely for fecundity to exceed 50% of all non-pups, considering some of the non-pups are male and some are too young to produce pups. It would also be very unlikely for non-pup survival to be less than 50% given the few studies done on harbor

seals in Alaska (Hastings et al., 2012) and elsewhere (Härkönen & Heide-Jørgensen, 1990; Cordes & Thompson, 2014; Mackey et al., 2008), where they were all near 90%. We used a similar constraint for survival of pups from age at survey to non-pup status. Given these constraints, we assumed flat prior distributions (Table IV). Notice that under uniform-priors, the distribution on population growth rate is near -5% annually.

Finally, we considered the prior distribution for ψ , the expected proportion of seals that are observable. Research in ocean environments along coastal Alaska showed that haulout rates averaged from 41 - 50% (Pitcher & McAllister, 1981), with ranges from 20% to 80% along the west coast of North America (Sullivan, 1979; Huber et al., 2001; Simpkins et al., 2003; Ver Hoef et al., 2010). Using a prior of Beta(5,5) concentrated most of the prior mass between 0.2 and 0.8. Additionally, the prior was used multiple times, one for each year t, otherwise there was a tendency for P_t and A_t to increase without bound, driving the posterior distribution of ψ towards zero.

345 3.3 Fitting the Model

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The model was fitted with Markov Chain Monte Carlo (MCMC) methods using the Metropolis algorithm (Metropolis et al., 1953), which was custom coded in R (R Core Team, 2016). We used a burn-in of 50,000 iterations, and then kept each 10th sample from the next 100,000 iterations, yielding 10,000 samples. From the hierarchical model described in Section 3.1 and Section 3.2, we obtained a sample from the posterior distribution,

$$[\eta, \sigma, \boldsymbol{\alpha}, \boldsymbol{\beta}, P_1, A_1, \boldsymbol{\phi}, \boldsymbol{\delta}, \boldsymbol{\kappa}, \rho, \psi | \mathbf{x}, \mathbf{y}, \mathbf{z}, \mathbf{d}, \mathbf{h}],$$

where, from Equation (1), $\mathbf{x} = \{X_{t,i}\}$, $\mathbf{y} = \{Y_{t,i}\}$, and $\mathbf{z} = \{Z_{t,i}\}$, and from Equation (2), $\boldsymbol{\alpha} = (\alpha_{d,1}, \alpha_{d,2}, \alpha_{h,1}, \alpha_{h,2})$, $\boldsymbol{\beta} = (\beta_{d,1}, \beta_{d,2}, \beta_{h,1}, \beta_{h,2})$, $\mathbf{d} = \{d_{t,i}\}$, and $\mathbf{h} = \{h_{t,i}\}$. The samples from all posterior distributions were checked for convergence, and no problems were found (Jones et al., 2006).

There were missing values. In particular, we had harvest information for just 6 years. For the years that were missing harvest data, for each iteration of the MCMC algorithm, we imputed one of the observed values, and this was done by village. Recall that harvest was modeled as a discrete uniform distribution $\mathcal{DU}_m(1/C_m)$. For example in Iguigig where harvest data were 2, 5.4, and 4.2, all missing years were assigned one of these three values, at random for each year, with probability 1/3. Then, the total harvest for each year was computed as the sum across the observed and imputed values for all villages. Likewise, there

were a few seal counts that were missing hour-of-day values, and so for each iteration of the MCMC algorithm we randomly imputed one of the observed values. These imputations preserved the variation in the observed data for the missing values without explicitly modeling these variables, which were of no direct interest.

3.4 Trend and Abundance

Let $P_1^{[k]}$ and $A_1^{[k]}$ be the kth MCMC sample of the posterior distribution of the true, initial abundance of pups and non-pups, P_1 and A_1 . Then abundance in the following years is determined by the MCMC sample of the demographic parameters and the observed and imputed harvest values,

$$\begin{split} A_{t+1}^{[k]} &= \delta_t^{[k]} A_t^{[k]} + \kappa_t^{[k]} P_t^{[k]} - H_t^{[k]}, \\ P_{t+1}^{[k]} &= c_t^{[k]} \phi_t^{[k]} A_t^{[k]}, \end{split}$$

for t = 1, ... 29, where $\delta_t^{[k]}$, $\phi_t^{[k]}$, and $\kappa_t^{[k]}$ are the kth MCMC samples for δ_t , ϕ_t , and κ_t . The kth MCMC sample $c_t^{[k]}$ depends on the kth MCMC sample, $\rho^{[k]}$, along with A_t and P_t . The kth MCMC estimate of total abundance then is $N_t^{[k]} = P_t^{[k]} + A_t^{[k]}$ for any t.

We used two methods to estimate trend. To obtain a global estimate of trend for the model, we pooled all of the leading eigenvalues of $\mathbf{M}_t^{[k]}$ across both t and k. As a second method, we used simple linear regression on the the posterior distribution of the annual abundance estimates (Johnson & Fritz, 2014); that is, we simply regressed abundance on year. We did this for the last 5, 10, and 15 years. An estimate of trend for the most recent 5 years, taken from the kth MCMC sample, was computed as the slope of the regression of $N_t^{[k]}$; $t = 26, \ldots, 30$ on the integers $1, \ldots, 5$, which we denote as $\tau_5^{[k]}$. Likewise, an estimate of trend for the most recent 10 years, taken from the kth MCMC sample, was computed as the slope of the regression of $N_t^{[k]}$; $t = 21, \ldots, 30$ on the integers $1, \ldots, 10$, which we denote as $\tau_{10}^{[k]}$; and an estimate of trend for the most recent 15 years, taken from the kth MCMC sample, was computed as the slope of the regression of $N_t^{[k]}$; $t = 16, \ldots, 30$ on $1, \ldots, 15$, which we denote as $\tau_{15}^{[k]}$.

3.5 Population Viability

For population viability analysis, we wished to project the population for the next 100 years (e.g. Ver Hoef, 2002). Consider the MCMC samples of the posterior distributions of $\delta_t^{[k]}, \kappa_t^{[k]}, \phi_t^{[k]}; t = 1, \dots, 29; k = 1, \dots, 10000$. For each $t = 30, \dots, 129$, we resampled one year, t', independently from $t = 1, \dots, 29$, with replacement, and then set $\delta_t^{[k]} = \delta_{t'}^{[k]}, \kappa_t^{[k]} = \delta_{t'}^{[k]}, \kappa_t^{[k]}$

 $\kappa_{t'}^{[k]}, \phi_t^{[k]} = \phi_{t'}^{[k]}$ for $t = 30, \dots, 129$ and $k = 1, \dots, 10000$. We also extended harvest into the future. Initially, we drew $\tilde{H}_{t,m}^{[k]}$ randomly from $\mathcal{D}\mathcal{U}_m(1/C_m)$ for the mth village, and then summed them, $\tilde{H}_t^{[k]} = \sum_{m=1}^6 \tilde{H}_{t,m}$ for $t = 30, \dots, 129$ and $k = 1, \dots, 10000$. Based on analyses given in the subsequent sections, it appears that the harbor seal population averaged around 350–400 seals, so we allowed for simulated harvest rates (rather than simulated amounts) by scaling harvest to current abundance: $H_t^{[k]} = (\tilde{H}_t^{[k]}/350)N_t^{[k]}$, where $N_t^{[k]}$ is the current estimate of abundance, as described below. Thus, as the population increases, more seals would be harvested, and also as the population decreases, fewer seals would be harvested. This scaling seems natural, and keeps the population from becoming negative due to harvest.

The simulated population abundance, projected into the future for each k, t, is

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$$\begin{split} A_{t+1}^{[k]} &= \delta_t^{[k]} A_t^{[k]} + \kappa_t^{[k]} P_t^{[k]} - H_t^{[k]}, \\ P_{t+1}^{[k]} &= c_t^{[k]} \phi_t^{[k]} A_t^{[k]}, \end{split}$$

for $t=30,\ldots,129$ and $k=1,\ldots,10000$. For any t,k combination, the simulated total population is $N_t^{[k]}=P_t^{[k]}+A_t^{[k]}$, and note that $c_t^{[k]}$ is constant for $\rho^{[k]}$, but changing with N_t . Because $P_t^{[k,j]}$ and $A_t^{[k,j]}$ are positive, and always greater than $H_t^{[k,j]}$, the population will never reach 0. In this case, a threshold needs to be defined that reflects a notion of a critical size, below which the population is very unlikely to avoid extinction. We chose to illustrate the effects of using thresholds of 10, 50, and 100 individuals. Population viability analysis, then, is concerned with the cases when $N_t^{[k,j]}$ drops below a critical threshold, often called quasi-extinction. Statistical methods similar to those presented here can be found in Holmes et al. (2007). In the simulated predictions of population values, the first year that $N_t^{[k,j]}$ falls below such a threshold was recorded, for various thresholds. For each k, an indicator that the populations falls below ξ by year T is given by,

$$f(T, k, c) = \mathcal{I}\left(\sum_{t=1}^{T} \mathcal{I}(N_t^{[k]} < \xi) > 0\right),$$

where $\mathcal{I}(\cdot)$ is the indicator function, which is 1 when its argument is true, and 0 otherwise. Across all simulated populations, the proportion of times that a threshold is crossed, accumulated by year, provides an estimate of the probability of crossing the threshold in the years following 2013. That is, an estimate of crossing some threshold ξ by time T is,

$$\hat{q}(T,c) = \frac{1}{10,000} \sum_{k=1}^{10,000} f(T,k,\xi).$$
 (5)

Note that other uses of PVA include estimating time to extinction (Taylor, 1995), which we do not consider here.

419 4 RESULTS

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We first show posterior distributions for the demographic parameters and covariate effects to confirm that the values are reasonable with respect to our understanding of harbor seal biology. We then turn our attention to derived quantities from the model, such as abundance, trend and population viability analysis.

4.1 Distributions of Demographic Parameters

The main drivers of trend and abundance are the demographic parameters, δ_t , c_t , ϕ_t , and 425 κ_t (see Table III). Smoothed posterior densities for each of these quantities are given in 426 Figure 1. For each parameter, all values across the t years were pooled, so the subscript is dropped when discussing these results. The first column in Figure 1 contains the results under the base-priors scenario (Table IV). Note that there is very little change from the 429 prior distributions to the posteriors, indicating a lack of information in the data compared 430 to the priors. The average values of the posterior for non-pup annual survival rates (δ ; first 431 row, first column) was 0.893, for fecundity (ϕ ; second row, first column of Figure 1) was 0.232, and for pup survival to non-pup status, κ , it was 0.778. The posterior distribution of the density dependent scaling factor, c (third row, first column of Figure 1), depends on the 434 posterior distribution of ρ and various values of N_t . We show the posterior distribution of c 435 for $N_t = 300,600,1200$, which illustrates how fecundity $c\phi$ declines with increasing values of 436 N_t due to density dependence.

The prior distributions were somewhat broader for the wide-priors scenario, and the resulting posteriors diverged more from the priors, shown in the second column of Figure 1. Here, the average of the posterior values for δ was 0.861, for ϕ was 0.268, and for κ was 0.782. The posterior for c for the wide-priors scenario was very similar to that for the base-priors scenario.

The prior distributions were very wide for the uniform-priors scenario, and the resulting posteriors diverged substantially from the priors, as seen from the third column of Figure 1. The average of the posterior values for δ was 0.851, for ϕ was 0.313, and for was was 0.782. Once again, the posterior distribution of c was similar to both base-priors and wide-priors scenarios. In all three cases, most of the posterior distribution for c is very near 1.0 for sample sizes less than 1000.

449 4.2 Effects of Date and Time of Day

As expected, there was a strong effect of day-of-year on pup counts (Figure 2A). The mean 450 day-of-year for pup counts was 206 (26 July), and the estimated date of peak pup numbers 451 was 20 July. Counts as early as day 110 (21 April), and as late as day 301 (29 October), are 452 expected to have around 30 fewer pups than at the peak. The uncertainty in these temporal patterns is reflected in the variation in the fitted (grey) curves of Figure 2A. Note that the 454 simple quadratic model may not be fitting very well near the ends of the data, because we 455 would not expect to see any pups at those dates, nor at any dates more than about 3 weeks 456 from the peak. In early April, no pups are born yet, and by late October, they are large 457 enough to be difficult to distinguish from older seals, so these changes reflect both the annual pupping cycle and the decline in observability of older pups. There was a minor peak in 459 the effect of time-of-day on pup counts at about 15:00, which was one hour later than the 460 mean time of the surveys (14:00, Figure 2B). However, substantial variation among MCMC 461 samples indicated there is little evidence that more pups are expected to be counted at any 462 particular time of day. 463

The peak in expected counts of non-pups occurred later than for pups, on 10 August (Figure 2C). In comparison to the pups, counts of non-pups decreased more rapidly away from peak counts. Note that these are expected changes in absolute number, and there are many more non-pups than pups in the population, which can allow for greater increases and declines. The peak count of non-pups was at 13:00 (Figure 2D), one hour earlier than the mean time of surveys. However, there was considerable variation in the curves and, similar to pup counts, there was only weak evidence for a peak time of day in non-pup counts.

$_{\scriptscriptstyle 1}$ 4.3 Abundance

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For each MCMC sample k, the abundance estimates $N_t^{[k]}$ for years $t=1,\ldots,30$ are shown in Figure 3A, with priors on the demographic parameters from the base-priors scenario

(Table IV). For each t, the k different averaged values are denoted as \hat{N}_t . Notice the effect of the constraint that $N_t^{[k]}$ must be greater than the maximum observed count in any year, inflated by a factor of 1/0.9. The highest counts in 1998 and 2008 were largely responsible for determining how many seals were missed due to being in the water, from average counts (note that the year ticks are set to 1 January, but surveys generally occurred in summer, and hence the offset in time). The thin solid line that is fit to the observed data is essentially $\psi \hat{N}_t$, with some correction for covariate effects, reflecting the expected number of seals that are "observable" (i.e., at haul-out sites). The posterior distribution of ψ is shown in Figure 3B. Notice that although most of the mass of the prior was between 0.2 and 0.8, the posterior distribution of ψ had most of its mass between 0.35 and 0.5, with a mean of 0.417, indicating that on average slightly more than half of the seals were missed.

Figure 3C shows the same information as in Figure 3A, but using the wide-priors on the demographic parameters. Even with the same prior on ψ , the greater uncertainty in the prior demographic parameters led to more uncertainty in the abundance, as might be expected (Figure 3C). Also note that this greater uncertainty allowed the abundance estimates to "wrap" around, to a greater extent, the highest observed values in 1998 and 2008. For the wide-priors scenario, the posterior distribution of ψ is shown in Figure 3D, and it appears to be quite similar to that from the base-priors scenario (Figure 3B), with a mean of 0.423.

Figure 3E shows the same information as given in Figures 3A,B, but using the uniform-priors scenario for the demographic parameters. This scenario had the greatest uncertainty in the prior demographic parameters and led to the greatest uncertainty in the abundance, especially in those years with few or no surveys. For uniform-priors scenario, the posterior distribution of ψ (Figure 3F) again appears to be quite similar to those from the other scenarios, with a mean of 0.434.

4.4 Trend

For each MCMC sample k, the values $\delta_t^{[k]}$, $c_t^{[k]}$, $\phi_t^{[k]}$, and $\kappa_t^{[k]}$ can be used to form the matrix \mathbf{M}_t (Equation 4) for each time period t, yielding 290,000 such matrices. The posterior distributions of the leading eigenvalues from \mathbf{M}_t are given in the first column of Figure 4 (matching the situations in Figure 3). The leading eigenvalue is the annual factor of increase at the stable age distribution for each Leslie matrix. Despite the fact that wide-priors scenario had parameters of \mathbf{M}_t leading to zero growth, and the uniform-priors scenario had

parameters of \mathbf{M}_t leading to negative growth, the posteriors in all three scenarios had means showing positive growth: base-priors scenario = 1.062, wide-priors scenario = 1.055, and uniform-priors scenario = 1.074. The base-priors scenario had the least variability, and uniform-priors scenario had the most.

Linear regression estimates of trend were described in Section 3.4. In particular, the posterior distribution of the most recent 15 years, using the sample of $\tau_{15}^{[k]}$, $k=1,\ldots,10000$, is given in the second column of Figure 4. For the base-priors scenario, there was a posterior probability of 0.5075 of a decreasing trend, indicating little evidence that the population was decreasing over this time period. For the wide-priors scenario, there was a posterior probability of 0.8266, and for uniform-priors, there was a posterior probability of 0.7867, of decreasing trends, neither of which provide strong evidence for a decline. Nevertheless, these values highlight the difference between the annual factors of population increase computed from the Leslie matrix eigenvalues, which were positive and uncorrected for harvest, and linear trends on the last 15 years of abundance, which were negative and included harvest.

The posterior distributions of trend for the most recent 10 years, using the sample of $\tau_{10}^{[k]}; k=1,\ldots,10000$, are given in the third column of Figure 4. For the base-priors scenario, there was a posterior probability of 0.4055 of a decreasing trend, very weak evidence that the population was decreasing over this time period. For the wide-priors scenario, there was a 0.6004 posterior probability, and for uniform-priors a 0.3949 posterior probability, of a decreasing trend, neither of which provides much support for a trend.

The posterior distributions of trend for the most recent 5 years, using the sample of $\tau_5^{[k]}$; k = 1, ..., 10000, are given in the last column of Figure 4. For the base-priors scenario there was a 0.4961 posterior probability, for wide-priors a 0.584 posterior probability, and for uniform-priors a 0.1383 posterior probability, of a decreasing trend; the latter indicates modest evidence of an increasing trend in the last 5 years.

4.5 Population Viability Analysis

When projecting into the future, as described in Section 3.5, the survival and fecundity rates estimated under the base-priors scenario producted little variability (Figure 5A). Note that for the first 30 years, the lines $N_t^{[k]}; t = 1, \ldots, 30$ for $k = 1, \ldots, 10000$, are the same as in Figure 3A, but plotted on the log scale. The population predictions become more variable when projecting into the future, $N_t^{[k,j]}; t = 31, \ldots, 130; k = 1, \ldots, 10000$. Under this scenario, there was almost no chance that the population would drop below any of the

thresholds, $\hat{q}(T,c)$ (Equation 5), of 10, 50, or 100 individuals (Figure 5B). Parameters from 538 the wide-priors scenario produced more variability (Figure 5C). Under this scenario, some of 539 the future population trajectories crossed the various thresholds. The cumulative probability 540 that the population would drop below 100 by year 100 is about 9%, and there is a 1-2\% 541 chance of dropping below 50 (Figure 5D). Under the more variable uniform-priors scenario 542 (Figure 5E), the cumulative probability that the population would drop below 100 is about 543 5% within 30 years, and around 15% by year 100 (Figure 5F). There is also about a 4% chance that the population could drop below 50 by year 100, but still very little chance that 545 the population would drop below 10. 546

547 5 DISCUSSION AND CONCLUSIONS

548 5.1 Demographic Parameters

Hastings et al. (2012) compared their survival and productivity estimates to other literature 549 on harbor seals in Alaska and elsewhere. Using their estimates in our base-priors scenario, 550 along with the precision of those estimates, the data did little to move the posterior distri-551 butions from the prior distributions (Figure 1, top row). However, with our wide-priors and 552 uniform-priors, there was some evidence that both adult survival, δ , and fecundity, ϕ , were 553 higher than the prior values (Figure 1, bottom two rows). This may not be surprising based 554 on traditional knowledge of hunters around Iliamna Lake, who assert that seals in the lake are larger and fatter than their saltwater counterparts (Burns et al., 2016). Indeed, in all 556 three scenarios, the posterior distribution of the annual factor of increase (i.e., population 557 growth rate) implied by the Leslie matrix parameters was greater than the prior; (base-priors 558 = 1.062, wide-priors = 1.055, uniform-priors = 1.074). These growth rates make sense in 559 light of the harvest information (note that the harvest data in the model helped determine them). On average, Table II indicates about 20 seals are harvested per year. Based on a 561 population of approximately 400, that indicates about 5\% harvest rate, which essentially 562 balances the production rate, consistent with the apparent near-equilibrium in numbers over 563 the past several decades.

565 5.2 Effects of Date and Time of Day

The influence of time-of-day and day-of-year on harbor seal counts in Iliamna Lake mostly matched our expectations from patterns described for marine harbor seals. Despite consid-

erable uncertainty, there was a weak peak just after mid-day for both pups and non-pups 568 around 1400 local time, (Figure 2B,D), which is very near solar mid-day for this location and 569 exactly the peak time expected from marine harbor seal studies (e.g., Simpkins et al., 2003). 570 There was a much stronger relationship to day-of-year. The August peak in Figure 2C gen-571 erally matched our expectations, based on the greater amount of time that harbor seals tend 572 to spend ashore when they are most actively molting their pelage. Pupping generally peaks 573 around mid-June in Alaska (Mathews & Pendleton, 2006), but aerial counts are confounded by changes in the absolute numbers of pups, the time that they spend in the water, and 575 the difficulty in distinguishing them from non-pups as they grow during the summer, which 576 generally explains the broad peak in Figure 2A. A third covariate often modeled for seal 577 counts in marine populations is the effect of tide, which is not present in Iliamna Lake. 578

579 5.3 Abundance and Trends

The results in Figure 3 suggest a minimum of around 300 seals occurred in the mid-late 1980s, 580 but there was a large amount of uncertainty, with only a few, relatively low counts obtained 581 during that period (e.g., 77 seals in 1984). It is likely that the population grew through 582 the 1990s and has stabilized at around 400 individuals. Using the wide-priors scenario as shown in Figure 3C,D, the most recent abundance estimate, in 2013, was 398 with the 95\% 584 credible interval ranging from 326 to 485. The peak abundance estimate in the recent years 585 of increased monitoring occurred in 2008 and was estimated at 460, with the 95% credible 586 interval ranging from 412 to 536. This corresponds reasonably well with the 389 estimate by ABR, Environmental Research and Service (2011), which would be expected to be lower because it did not include a correction (ψ) for the proportion of seals in the water. 580

590 5.4 Population Viability

The probability of quasi-extinction in the next 100 years, using 50 as a threshold, was estimated to be around 1% under wide-priors and 4% for uniform-priors. We generally disregard the base-priors scenario, as the variances in those priors were developed based on sampling error alone, and not on annual stochastic variation in demographic parameters. In the Introduction, we reported that the concept of extinction risk due to demographic stochasticity is often separated from environmental stochasticity. However, our analysis includes both because the variation in estimated demographic parameters includes normal environmental variation. That leaves genetic and catastrophic effects as unmodeled. A

quasi-extinction threshold of 50 may be large enough to avoid genetic effects somewhat, but we acknowledge that populations of long-lived animals that remain at such low levels for very long will likely incur genetic challenges (Frankham, 1996). Finally, it is important to consider catastrophic events. For example, catastrophic population declines in otariids due to El Niño or unknown causes (Gerber & Hilborn, 2001). Our results are based on a span of 30 years, which is a relatively long time for monitoring a marine mammal population. However, a population's risk may depend on rare events that occur less frequently than any observed during the sampling time frame. Based on accounts by local residents, Burns (1978) and Mathisen & Kline (1992) reported that the numbers of seals in Iliamna Lake dropped after extremely severe winters in 1970-71 and 1971-72, to approximately 40 to 50 individuals. Although the evidence is anecdotal, harbor seals in Iliamna Lake may be subject to such catastrophic events, which increases their risk beyond those that are modeled in this paper. It is difficult to quantify such catastrophic risk (but see Ward et al. (2007) for a quantitative approach when there are better data), so any management decisions should consider the risk presented in this paper as the minimum risk, and our model could be used to evaluate the effects of hypothetical scenarios for the likelihood of various kinds of catastrophes.

For our data, changes in assumptions (priors) sometimes led to relatively large changes in inference. For example, the population parameters contained in the scenarios as shown in Figure 1, led to the different trends (Figure 4) and population trajectories (Figure 5), with differing chances of crossing a quasi-extinction threshold. As such, these scenarios should be considered a compromise between projections and predictions, in the sense of Keyfitz (1972) and Caswell (2001, pg. 29). That is, a prediction is an inference on what will happen, and a projection on what could happen given a certain set of assumptions. Here, the data modify the starting assumptions somewhat, but not enough to overwhelm those assumptions. We have presented several reasonable scenarios through the specification of prior distributions. The results largely match the hypotheses and expectations that we outlined in the Introduction, but the analysis quantified their values and illustrated the uncertainty stemming from the relatively sparse data available for this poorly documented seal population. This should form a basis for current management decisions, designing future sampling efforts, and a comparison point for future analyses.

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638 DATA AND CODE ACCESSIBILITY

An R (R Core Team, 2017) package called IliamnaSealsTrendPVA was created that contains all data, code, and analyses. This document was created using knitr (Xie, 2014, 2015, 2016), and the manuscript combining LATEX and R code is also included in the package. The package can be downloaded at

https://github.com/jayverhoef/IliamnaSealsTrendPVA.git,

with instructions for installing the package.

References

- ABR, Environmental Research and Service, 2011. Chapter 16. Wildlife and habitat,
 Bristol Bay drainages. In Pebble Project Environmental Baseline Document 2004
 through 2008. Pebble Limited Partnership, http://www.arlis.org/docs/vol2/Pebble/20042008%20EBD/CH16%20Wildlife%20Habitat%20BB.pdf.
- Anderson, J. W., 1969. Bathymetric measurements of Iliamna Lake and Lake Clark, Alaska.
 Technical Report 69-17, Fisheries Research Institute, College of Fisheries, University of
 Washington.
- Boveng, P. L., J. L. Bengtson, D. E. Withrow, J. C. Cesarone, M. A. Simpkins, K. J. Frost
 and J. J. Burns, 2003. The abundance of harbor seals in the Gulf of Alaska. Marine
 Mammal Science 19(1):111–127.

- Buckland, S. T., K. B. Newman, C. Fernández, L. Thomas and J. Harwood, 2007. Embedding
 population dynamics models in inference. Statistical Science 22:44–58.
- Burns, J. J., 1978. Unpublished letter to the marine mammal commission. Technical report,
 Alaska Department of Fish and Game.
- Burns, J. M., H. Chythlook, C. Gomez, T. Askoak and D. Withrow, 2011. Iliamna Lake
 freshwater seal study: characterizing local use patterns, local traditional knowledge, and
 seal population ecology. Technical report, North Pacific Research Board Final Report
 Project 916, 30 pp.
- Burns, J. M., J. M. Van Lanen, D. Withrow, D. Holen, T. Askoak, H. Aderman, G. O'CoreyCrowe, G. Zimpelman and B. Jones, 2016. Integrating local traditional knowledge and
 subsistence use patterns with aerial surveys to improve scientific and local understanding
 of the iliamna lake seals. Technical report, Alaska Department of Fish and Game, Division
 of Subsistence, Technical Paper No. 416., 182 p.
- Cáceres, M. O. and I. Cáceres-Saez, 2013. Calculating effective growth rate from a random
 leslie model: Application to incidental mortality analysis. Ecological modelling 251:312–
 322.
- Caswell, H., 2001. Matrix Population Models, 2nd Edition: Construction, Analysis, and
 Interpretation. Sunderland, Mass.: Sinauer Associates.
- Cordes, L. S. and P. M. Thompson, 2014. Mark-recapture modeling accounting for state
 uncertainty provides concurrent estimates of survival and fecundity in a protected harbor
 seal population. Marine Mammal Science 30(2):691–705.
- Cressie, N., K. A. Calder, J. S. Clark, J. M. Ver Hoef and C. K. Wikle, 2009. Accounting for
 uncertainty in ecological analysis: The strengths and limitations of hierarchical statistical
 modeling. Ecological Applications 19:553–570.
- Dorfman, R., 1938. A note on the δ -method for finding variance formulae. The Biometric Bulletin 1:129–137.
- Fall, J. A., D. L. Holen, B. Davis, T. Krieg and D. Koster, 2006. Subsistence harvests and uses
 of wild resources in Iliamna, Newhalen, Nondalton, Pedro Bay, and Port Alsworth, Alaska,
 2004. Technical report, Alaska Department of Fish and Game, Division of Subsistence
 Technical Paper No. 302, Juneau, Alaska.

- Frankham, R., 1996. Relationship of genetic variation to population size in wildlife. Conservation Biology **10**(6):1500–1508. 686
- Franklin, I. R., 1980. Evolutionary change in small populations. In M. Soulé & B. Wilcox, 687 editors, Conservation Biology: An Evolutionary-Ecological Perspective, pages 135–149.
- Sinauer Associates, Sunderland, Massachusetts.

688

- Gerber, L. R. and R. Hilborn, 2001. Catastrophic events and recovery from low densities in 690 populations of otariids: implications for risk of extinction. Mammal Review 31(2):131-691 150. 692
- Gilks, W. R., S. Richardson and D. J. Spiegelhalter, 1996. Introducing Markov chain Monte 693 Carlo. In Markov chain Monte Carlo in Practice, pages 1–19. Chapman and Hall. 694
- Ginzburg, L. R., L. B. Slobodkin, K. Johnson and A. G. Bindman, 1982. Quasiextinction 695 probabilities as a measure of impact on population growth. Risk Analysis 2(3):171-181.
- Goodman, D., 1987. The demography of chance extinction. In M. E. Soulé, editor, Viable 697 populations for conservation, pages 11–34. Cambridge University Press, Cambridge, UK. 698
- Goodman, D., 2002. Predictive Bayesian population viability analysis: a logic for listing 699 criteria, delisting criteria, and recover plans. In S. R. Beissinger & D. R. McCullough, ed-700 itors, Population Viability Analysis, pages 447–469. University of Chicago Press, Chicago, 701 Illinois, USA. 702
- Goodman, D., 2004. Methods for joint inference from multiple data sources for improved 703 estimates of population size and survival rates. Marine Mammal Science 20(3):401–423. 704
- Goodman, D., 2010. Taking the prior seriously: Bayesian analysis without subjective proba-705
- bility. In M. L. Taper & S. R. Lele, editors, The Nature of Scientific Evidence: Statistical, 706
- Philosophical, and Empirical Considerations, pages 379–409. University of Chicago Press, 707
- Chicago, Illinois, USA. 708
- Goodman, L. A., 1960. On the exact variance of products (Corr: V57 p917). Journal of the 709 American Statistical Association **55**:708–713. 710
- Gross, K., B. A. Craig and W. D. Hutchison, 2002. Bayesian estimation of a demographic 711 matrix model from stage-frequency data. Ecology 83(12):3285–3298. 712

- Härkönen, T. and M.-P. Heide-Jørgensen, 1990. Comparative life histories of east atlantic and other harbour seal populations. Ophelia **32**(3):211–235. 714
- Hastings, K. K., R. J. Small and G. W. Pendleton, 2012. Sex-and age-specific survival 715 of harbor seals (*Phoca vitulina*) from Tugidak Island, Alaska. Journal of Mammalogy 716 **93**(5):1368–1379. 717
- Hauser, D. D., C. S. Allen, H. B. Rich and T. P. Quinn, 2008. Resident harbor seals (*Phoca* 718 vitulina) in Iliamna Lake, Alaska: Summer diet and partial consumption of adult sockeye 719 salmon (Oncorhynchus nerka). Aquatic Mammals **34**(3):303–309. 720
- Holmes, E. E., J. L. Sabo, S. V. Viscido and W. F. Fagan, 2007. A statistical approach to 721 quasi-extinction forecasting. Ecology Letters 10(12):1182–1198. 722
- Huber, H. R., S. J. Jeffries, R. F. Brown, R. L. Delong and G. Vanblaricom, 2001. Correcting aerial survey counts of harbor seals (phoca vitulina richardsi) in washington and oregon. 724 Marine Mammal Science 17(2):276–293. 725
- Johnson, D. S. and L. Fritz, 2014. agTrend: A bayesian approach for estimating trends of 726 aggregated abundance. Methods in Ecology and Evolution 5(10):1110–1115. 727
- Jones, G. L., M. Haran, B. S. Caffo and R. Neath, 2006. Fixed-width output analy-728 sis for Markov Chain Monte Carlo. Journal of the American Statistical Association 729 **101**(476):1537–1547. 730
- Keyfitz, N., 1972. On future population. Journal of the American Statistical Association 731 **67**:347–363. 732
- Krieg, T. M., D. L. Holen and D. Koster, 2009. Subsistence harvests and uses of wild 733 resources in Igiugig, Kokhanok, Koliganek, Levelock, and New Stuyahok, Alaska, 2005. 734 Technical report, Alaska Department of Fish and Game, Division of Subsistence Technical 735 Paper No. 322, Dillingham, Alaska.
- London, J. M., J. M. Ver Hoef, S. J. Jeffries, M. M. Lance and P. L. Boveng, 2012. Haul-737 out behavior of harbor seals (*Phoca vitulina*) in Hood Canal, Washington. PLoS ONE 738 7(6):e38180. doi:10.1371/journal.pone.0038180. 739
- Mackey, B., J. Durban, S. Middlemas and P. Thompson, 2008. A bayesian estimate of 740 harbour seal survival using sparse photo-identification data. Journal of Zoology 274(1):18-741
- 27. 742

736

- Mathews, E. A. and G. W. Pendleton, 2006. Declines in harbor seal (*Phoca vitulina*) numbers in Glacier Bay National Park, Alaska, 1992–2002. Marine Mammal Science **22**(1):167–189.
- Mathisen, O. A. and T. C. Kline, 1992. Harbor seals in Iliamna Lake, Bristol Bay, Alaska (final report on aerial census in 1991, jcdos 9203). Technical report, Juneau Center for Fisheries and Ocean Sciences, University of AlaskaFairbanks.
- Maunder, M. N., 2004. Population viability analysis based on combining Bayesian, integrated, and hierarchical analyses. Acta Oecologica **26**(2):85–94.
- Metropolis, N., A. W. Rosenbluth, M. N. Rosenbluth, A. H. Teller and E. Teller, 1953.

 Equation of state calculations by fast computing machines. The Journal of Chemical
 Physics 21(6):1087–1092.
- National Marine Fisheries Service, 2016. Endangered and threatened species; determination on whether to list the harbor seals in Iliamna Lake, Alaska as a threatened or endangered species. Federal Register 81:81074–81086, U.S. Federal Government.
- Pitcher, K. and D. McAllister, 1981. Movements and haulout behavior of radio-tagged harbor seals, *Phoca vitulina*. Canadian Field-Naturalist **95**(3):292–297.
- Pitcher, K. W. and D. G. Calkins, 1979. Biology of the harbor seal, *Phoca vitulina richardsi*,
 in the Gulf of Alaska. Technical Report Research Unit 229, Contract 03-5-002-69, US. Department of Commerce, National Oceanic and Atmospheric Administration, Outer Continental Shelf Environmental Assessment Program Final Report 19(1983), Anchorage, AK.
- Poole, D. and A. E. Raftery, 2000. Inference for deterministic simulation models: the Bayesian melding approach. Journal of the American Statistical Association **95**(452):1244–1255.
- R Core Team, 2016. R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Vienna, Austria. URL http://www.R-project.org.
- R Core Team, 2017. R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Vienna, Austria. URL http://www.R-project.org.
- Raftery, A. E., G. H. Givens and J. E. Zeh, 1995. Inference from a deterministic population dynamics model for bowhead whales. Journal of the American Statistical Association 90(430):402–416.

- Shaffer, M. L., 1981. Minimum population sizes for species conservation. BioScience 31(2):131–134.
- Simpkins, M. A., D. E. Withrow, J. C. Cesarone and P. L. Boveng, 2003. Stability in the proportion of harbor seals hauled out under locally ideal conditions. Marine Mammal Science 19(4):791–805.
- Small, R. J., 2001. Harbor seal investigations in Alaska (Annual report for NOAA award
 NA87FX0300). Technical report, Alaska Department of Fish and Game, Division of
 Wildlife Conservation, Anchorage, Alaska.
- Small, R. J., G. W. Pendleton and K. W. Pitcher, 2003. Trends in abundance of Alaska harbor seals, 1983–2001. Marine Mammal Science **19**(2):344–362.
- Smith, R. J., K. A. Hobson, H. N. Koopman and D. M. Lavigne, 1996. Distinguishing
 between populations of fresh-and salt-water harbour seals (*Phoca vitulina*) using stableisotope ratios and fatty acid profiles. Canadian Journal of Fisheries and Aquatic Sciences
 53(2):272–279.
- Sullivan, R. M., 1979. Behavior and ecology of harbor seals, *Phoca vitulina*, along the open coast of northern California. Unpublished masters thesis.
- Swart, J. A. ., P. J. H. Reijnders and W. Van Delden, 1996. Absence of genetic variation in harbor seals (*Phoca vitulina*) in the Dutch Wadden Sea and the British Wash.

 Conservation Biology pages 289–293.
- Taylor, B. L., 1995. The reliability of using population viability analysis for risk classification
 of species. Conservation Biology 9(3):551–558.
- Taylor, B. L. and L. Rojas-Bracho, 1999. Examining the risk of inbreeding depression in a naturally rare cetacean, the vaquita *Phocoena sinus*. Marine Mammal Science **15**(4):1004–1028.
- Ver Hoef, J. M., 2002. Population viability analysis. In Encyclopedia of Environmetrics, pages 1625–1627. John Wiley & Sons.
- Ver Hoef, J. M., 2012. Who invented the delta method? The American Statistician **66**:124–127.

- Ver Hoef, J. M. and K. J. Frost, 2003. A Bayesian hierarchical model for monitoring harbor seal changes in Prince William Sound, Alaska. Environmental and Ecological Statistics 10(2):201–219.
- Ver Hoef, J. M., J. M. London and P. L. Boveng, 2010. Fast computing of some generalized linear mixed pseudo-models with temporal autocorrelation. Computational Statistics 25:39–55.
- Wade, P. R., 2002. Bayesian population viability analysis. In S. R. Beissinger & D. R.
 McCullough, editors, Population Viability Analysis, pages 213–238. University of Chicago
 Press, Chicago, Illinois, USA.
- Ward, E. J., R. Hilborn, R. G. Towell and L. Gerber, 2007. A state–space mixture approach for estimating catastrophic events in time series data. Canadian Journal of Fisheries and Aquatic Sciences **64**(6):899–910.
- Withrow, D. E., J. M. London, K. M. Yano and P. L. Boveng, 2014. Aerial survey counts of harbor seals in Lake Iliamna, Alaska, 1984-2013 (NODC Accession 0123188). Version 2.3. National Oceanographic Data Center, NOAA. Dataset. doi:10.7289/V5H41PCQ. http://data.nodc.noaa.gov/cgi-bin/iso?id=gov.noaa.nodc:0123188. Accessed: 2016-07-27.
- Xie, Y., 2014. knitr: a comprehensive tool for reproducible research in R. In V. Stodden, F. Leisch & R. D. Peng, editors, Implementing Reproducible Computational Research, pages 3 32. Chapman and Hall/CRC. URL http://www.crcpress.com/product/isbn/9781466561595. ISBN 978-1466561595.
- Xie, Y., 2015. Dynamic Documents with R and knitr. 2nd edition. Chapman and Hall/CRC,
 Boca Raton, Florida. URL http://yihui.name/knitr/. ISBN 978-1498716963.
- Xie, Y., 2016. knitr: A General-Purpose Package for Dynamic Report Generation in R. URL http://yihui.name/knitr/. R package version 1.15.1.

TABLES

Table I: Summary of Iliamna Lake aerial surveys conducted by various agencies and re-

searchers from 1984 to 2013.

Data Source	Year	First Survey	Last Survey	No. of Surveys
MK92	1984	1984-08-06	1984-08-06	1
MK92	1987	1987-08-29	1987-09-10	2
MK92	1988	1988-07-05	1988-07-05	1
MK92	1991	1991-08-23	1991-08-27	8
ADFG	1998	1998-08-13	1998-08-23	2
ADFG	1999	1999-08-23	1999-08-23	1
ADFG	2003	2003-08-07	2003-08-07	1
ABR/Pebble	2005	2005-03-30	2005-12-13	20
MML	2005	2005-08-11	2005-08-11	1
ABR/Pebble	2007	2007-05-22	2007-10-11	9
ABR/Pebble	2008	2008-08-02	2008-08-18	7
MML	2008	2008-07-24	2008-08-20	6
MML	2009	2009-05-09	2009-08-22	7
Newhalen	2009	2009-06-18	2009-09-19	10
MML	2010	2010-04-03	2010-11-03	6
MML	2011	2011-04-14	2011-11-08	6
MML	2012	2012-04-03	2012-08-10	3
MML	2013	2013-04-05	2013-08-08	5

ADFG: Alaska Department of Fish and Game

MK92: Mathisen & Kline (1992) Newhalen: Community of Newhalen

MML: Marine Mammal Laboratory, NOAA Alaska Fisheries Science Center

ABR/Pebble: ABR, Environmental Research and Service (2011)

Table II: Harvest data for various communities (column headings) on or near Iliamna Lake. Table entries are the estimated number of seals harvested by each community for various years. Fractions occur due to the estimation method, and due to households sharing seal harvest.

Year	Igiugig	Iliamna	Kokhanok	Levelock	Newhalen	Pedro Bay
1992^{1}	2		11	0		
1996^{1}						0
2004^{1}		8.5			17.9	0
2005^{1}	5.4		4.8	0		
2009^{2}			7		7^{3}	
2010^{1}			0		2	
2011^{1}	4.2	2.4	6.6	0	7.9	1.3

 $^{^{1}}$ Burns et al. (2016)

Table III: Table of model parameters, a short description, and a link to the formula where they $\underline{\text{are defined.}}$

<u> </u>		
Parameter	Description	Formula
η^2	observation variance of pups	(1)
σ^2	observation variance of non-pups	(1)
$\alpha_{d,1}; \alpha_{d,2}$	pup regression parameters for day-of-year	(2)
$\alpha_{h,1}; \alpha_{h,2}$	pup regression parameters for time-of-day	(2)
$\beta_{d,1}; \beta_{d,2}$	non-pup regression parameters for day-of-year	(2)
$\beta_{h,1}; \beta_{h,2}$	non-pup regression parameters for time-of-day	(2)
ψ	expected proportion of seals hauled out during counts	(2)
P_t	annual abundance of pups	(2),(3),(4)
A_t	annual abundance of non-pups	(2),(3),(4)
δ_t	annual survival of non-pups	(4)
κ_t	annual survival of pups to non-pup class	(4)
ϕ_t	annual fecundity of non-pups	(4)
c_t	density dependence for non-pups	(4)
ρ	scaling factor for density dependence for non-pups	(4)

²Burns et al. (2011)

³Burns, Jennifer, Personal Communication, 29 May 2014

Table IV: Three scenarios for priors on demographic parameters derived from literature values, with sampling variation along (base-priors), variation broadened from consideration of other expected sources of variation (wide-priors), and uninformative variation (uniform-priors). These are described in the text and fully developed in the Appendix. The parameters, non-pup survival (δ) , fecundity (ϕ) , and pup survival (κ) are components of Equation (3). The columns labeled a and b are the beta distribution parameters, derived using moment matching from the mean and variance in the previous columns (see Appendix for details). The uniform distribution in the uniform-priors extend from 0 to 0.5 for ϕ_t , and 0.5 to 1 for κ_t and δ_t .

Scenario	Parameter	Mean	Variance	a	b
base-priors	δ	0.891	0.000317	272.63	33.52
base-priors	ϕ	0.227	0.001075	36.86	125.43
base-priors	κ	0.773	0.003300	40.34	11.85
wide-piors	δ	0.843	0.002857	38.25	7.14
wide-priors	ϕ	0.215	0.009675	3.53	12.91
wide-priors	κ	0.731	0.029702	4.11	1.51
uniform-priors	δ	0.750	0.020833		
uniform-priors	ϕ	0.250	0.020833		
uniform-priors	κ	0.750	0.020833		

FIGURES

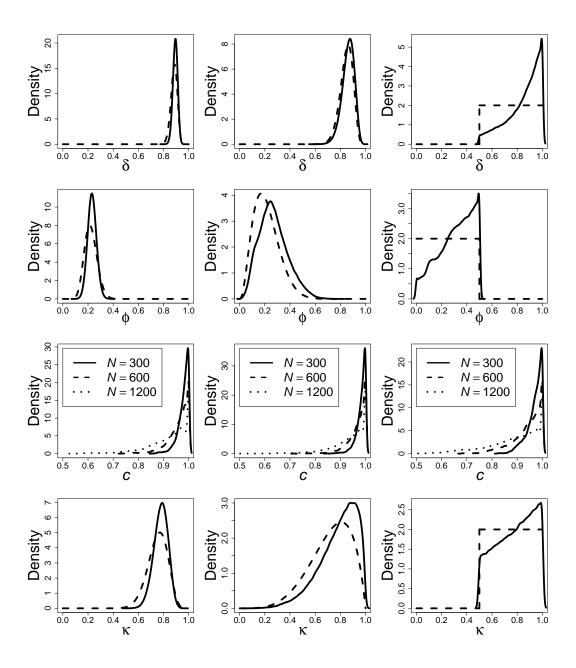


Figure 1: Prior (dashed lines) and posterior (solid lines) densities for adult survival δ , fecundity ϕ , and pup survival κ . The posterior densities for density dependence c are also shown for various population sizes N. The first column of plots use parameters from the base-priors scenario, and the second and third columns of plots use parameters from wide-priors and uniform-priors, respectively.

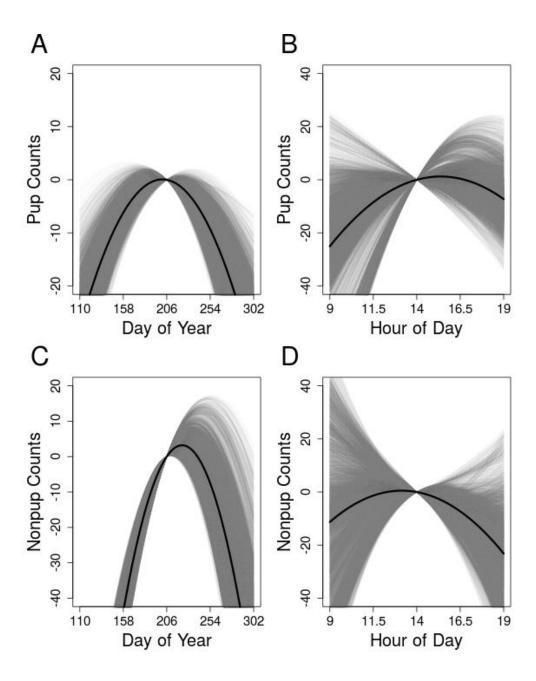


Figure 2: The effect of covariates on counts, where each grey line is computed from one MCMC sample of parameters among the 10000 samples from the posterior distribution. The thick black line is the average value among the 10000 curves. Each curve shows the expected change in counts as a function of the covariate, where all curves pass through the mean covariate value. (A) Day-of-year effect on pup counts, (B) hour-of-day effect on pup counts, (C) day-of-year effect on non-pup counts, and (D) hour-of-day effect on non-pup counts.

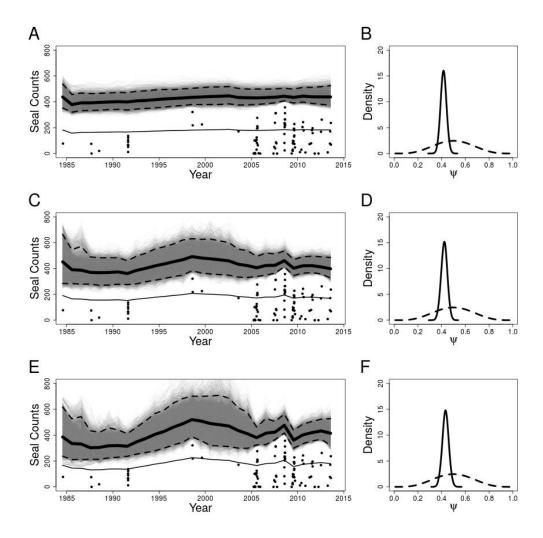


Figure 3: Series of annual abundance estimates (grey lines) for base-priors (A), wide-priors (C), and uniform-priors (E) from 10000 MCMC samples from the posterior distribution. The thick black line is the average value over all 10000 samples, the dashed lines form the 2.5% and 97.5% point-wise credible intervals, and solid black circles are observed counts. The thin solid line is the average annual abundance estimate times the average ψ value. Both solids lines are adjusted to optimum covariate conditions. In subfigures B), D), and F), the dashed line is the prior distribution for ψ , and the solid line is the posterior distribution, for base-priors, wide-priors, and uniform-priors, respectively.

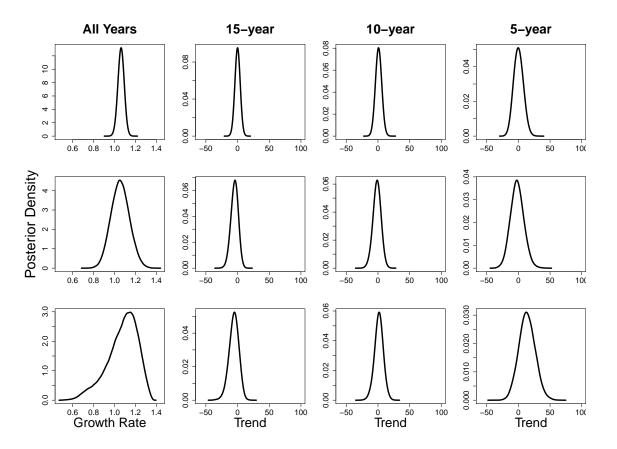


Figure 4: Trend summaries from the posterior distribution, computed from the 10000 MCMC samples. The first column is the posterior density of the first eigenvalue of the Leslie matrix, computed on the samples of δ , ϕ , and κ and used in Equation 4. The first row is from the base-priors scenario, and rows two and three are from the wide-priors and uniform-priors, respectively. The second through fourth columns are least-squares linear trends (individuals/year) through the abundance estimates (all of the grey lines in Figure 3), for the last 15, 10, and 5 years of abundance estimates, respectively. All posterior densities were smoothed with a kernel density estimator.

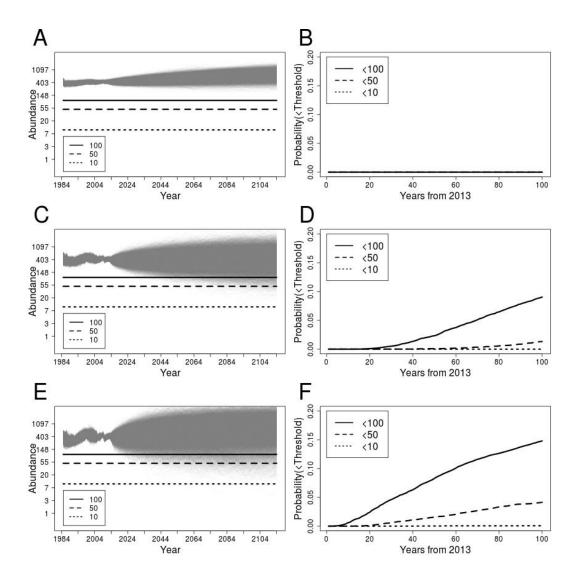


Figure 5: Simulated population trajectories (10000 of them) for the next 100 years after year 2013, under the base-priors (A), wide-priors (C), and uniform-priors (E) scenarios. The trajectories for 1984–2013 match those in Figure 3. Each population projection line is mostly transparent, so darker areas have more trend lines through them. Horizontal lines are thresholds for population sizes of 10, 50, and 100. Posterior probabilities of quasi-extinction, defined for thresholds of 10, 50, and 100, for various time horizons, are shown in (B), (D), and (F).

Appendix: Priors for Demographic Parameters

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To develop informative priors, we used the detailed information of sex and age-specific survival obtained from Hastings et al. (2012), and the information on female productivity contained in Pitcher & Calkins (1979), which are given in Table A.1.

Table A.1: Demographic parameters used to develop informative priors.

Parameter	Estimate	Standard Error
Survival Small Male Pups	0.405	0.089
Survival Large Male Pups	0.717	0.088
Survival Male 1-3	0.782	0.035
Survival Male 3+	0.879	0.038
Survival Small Female Pups	0.549	0.093
Survival Large Female Pups	0.820	0.069
Survival Female 1-3	0.865	0.027
Survival Female 3+	0.929	0.026
Fecundity Female 3+	0.733	0.041

The average female fertility rate for all females of age ≥ 3 was obtained from Pitcher & Calkins (1979) in a study of harbor seals in the Gulf of Alaska, the nearest available source for such data. They collected 165 females aged 3+ at various times in the annual cycle between ovulation (early July) and the next pupping-weaning-ovulation season. Among those 165 individuals, 143 had ovulated. Pitcher & Calkins (1979) found that implantation of the embryo took place around early October. There were 132 females in their sample that were collected between the time of implantation and the birth season; 14 of those either failed to become fertilized or lost their embryo or fetus. We estimated the raw birth rate, then, as the ovulation rate (143/165 = 0.867) minus the pregnancy failure rate (14/132 = 0.106), which equals 0.761. Because the females collected for evidence of ovulation and failure of pregnancy were collected at various (unspecified) times in the annual cycle, this raw birth rate accounts incompletely for females that would not have been available to be sampled because of mortality during the interval (i.e., the data are censored). To adjust for this, we applied one-half of the annual mortality rate for the 3+ age class, (1-0.929)/2=0.036, to the raw birth rate to yield a fecundity rate appropriate for use in a Leslie-type population projection matrix, 0.761 * (1 - 0.036) = 0.733). The variance was developed assuming indepenent binomial proportions for raw birth rate and pregnancy failure, and used the result on direct products (Goodman, 1960), assuming again that mortality rate was independent of birth rates and pregnancy failures.

We began with a full sex- and age-specific Leslie matrix model for harbor seals, then adjusted it for the timing of our surveys, and finally collapsed it to the two classes for which we had information: pups and non-pups. The full Leslie matrix model, developed from data in Hastings et al. (2012) and Pitcher & Calkins (1979), is $\mathbf{n}_{i+1} = \mathbf{M}\mathbf{n}_i$, where \mathbf{M} is given by

and \mathbf{n}_i is

$$\begin{pmatrix} n_{M,0,i} \\ n_{M,1,i} \\ n_{M,2,i} \\ n_{M,3+,i} \\ n_{F,0,i} \\ n_{F,1,i} \\ n_{F,2,i} \\ n_{F,3+,i} \end{pmatrix}, \tag{A.2}$$

where n is the number of animals in various sex/age classes, "M" indicates male, "F" indicates female, "0" indates age as birth, "1" indicates first birthday, "2" indicates second birthday, and "3+" indicates birthdays 3 and older. All of the survival values in this model were taken from Hastings et al. (2012, Table 2, part a). We chose these values because they were from a detailed study of well-marked seals, temporally and geographically close to our study in Iliamna Lake. Note that, from genetic considerations, we assumed that the productivity rate was split equally between production of male and female pups, resulting in an expected 0.367 probability of a male pup, and the same probability of a female pup, per female aged 3+.

Our surveys generally occurred around early August. If not, counts were modeled as being adjusted by a covariate for date as if they were counted in early August. Hence, there is a misalignment with the demographic parameters in Equation A.1 and our observations because seal pups are born prior to aerial surveys. We corrected for that as follows. Hastings et al. (2012) gave two survival rates for pups; from the time they are very small, and from the time that they are large. We take these to be equivalent to the time of birth, and the time of our surveys. Harbor seal pups grow rapidly, and some time in August it becomes unreliable to distinguish pups from non-pups in aerial surveys, so the survival of large pups

aligns very well with our survey period. For male pups, survival from birth to yearling is 872 reported as 0.405, but survival from a large pup to yearling is 0.717, and hence we take the 873 estimate of survival from small to large pup as 0.405/0.717 = 0.565. Likewise, the female 874 survival from small to large pup is 0.549/0.82 = 0.67. We adjusted the productivity values 875 then not for birth, but for the production of pups that survive to the time of surveys. Hence, 876 females aged 3+ have a 0.367*0.565=0.207 probability of producing a male pup that survives 877 to the survey period, and females aged 3+ have a 0.367*0.67=0.245 probability of producing 878 a female pup that survives to the survey period. This requires modifying Equation A.1 as, 879

There are several characteristics of this population model. The first (dominant) eigenvalue of the matrix, for both matrices A.1 and A.3 is 1.0566, indicating an annual growth rate of 5.66%. The first eigenvector associated with the dominant eigenvalue for matrix A.3, when scaled so that all elements sum to one, is,

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$$\mathbf{v} = \begin{pmatrix} 0.081 \\ 0.055 \\ 0.041 \\ 0.179 \\ 0.096 \\ 0.074 \\ 0.061 \\ 0.413 \end{pmatrix} = \begin{pmatrix} n_{\mathrm{M,s,\infty}} \\ n_{\mathrm{M,1-2,\infty}} \\ n_{\mathrm{M,2-3,\infty}} \\ n_{\mathrm{M,3+,\infty}} \\ n_{\mathrm{F,s,\infty}} \\ n_{\mathrm{F,s,\infty}} \\ n_{\mathrm{F,1-2,\infty}} \\ n_{\mathrm{F,2-3,\infty}} \\ n_{\mathrm{F,3+,\infty}} \end{pmatrix} / \mathrm{sum}(\mathbf{n}), \tag{A.4}$$

which is the stable age distribution, shown with $i = \infty$ for the vector, \mathbf{n} , of the number of animals in each sex/age class. Note that we have changed the notation on \mathbf{n} to reflect the shift away from birthdays to the time of surveys, indicated by the subscript s on the pup class, and the survey time between birthdays using a dash for other age classes.

Our objective was to collapse the Leslie matrix in A.3 into two classes. That is, we seek a simplified model

$$\begin{pmatrix} n_{\text{pups},i+1} \\ n_{\text{non-pups},i+1} \end{pmatrix} = \begin{pmatrix} 0 & \phi \\ \kappa & \delta \end{pmatrix} \begin{pmatrix} n_{\text{pups},i} \\ n_{\text{non-pups},i} \end{pmatrix},$$

where ϕ is the probability, among all non-pups alive at one annual survey, of producing a pup that survives to the time of next year's surveys, κ is the survival of those pups from the time of aerial surveys to the non-pup class, and δ is the survival of the non-pups to stay within that class. Assuming the population is at a stable age distribution, from Equation A.3 and A.4, we used the following weighted averages:

$$\delta = \frac{\mathbf{v}_{2}\mathbf{M}_{3,2} + \mathbf{v}_{3}\mathbf{M}_{4,3} + \mathbf{v}_{4}\mathbf{M}_{4,4} + \mathbf{v}_{6}\mathbf{M}_{7,6} + \mathbf{v}_{7}\mathbf{M}_{8,7} + \mathbf{v}_{8}\mathbf{M}_{8,8}}{\mathbf{v}_{2} + \mathbf{v}_{3} + \mathbf{v}_{4} + \mathbf{v}_{6} + \mathbf{v}_{7} + \mathbf{v}_{8}},
\kappa = \frac{\mathbf{v}_{1}\mathbf{M}_{2,1} + \mathbf{v}_{5}\mathbf{M}_{6,5}}{\mathbf{v}_{1} + \mathbf{v}_{5}},
\phi = \frac{\mathbf{v}_{8}(\mathbf{M}_{1,8} + \mathbf{M}_{5,8})}{\mathbf{v}_{2} + \mathbf{v}_{3} + \mathbf{v}_{4} + \mathbf{v}_{6} + \mathbf{v}_{7} + \mathbf{v}_{8}}.$$
(A.5)

895 This yields the matrix

$$\begin{pmatrix} 0 & \phi \\ \kappa & \delta \end{pmatrix} = \begin{pmatrix} 0.000 & 0.227 \\ 0.773 & 0.891 \end{pmatrix}. \tag{A.6}$$

Notice that, because we used weighted averages of the stable distribution of matrix A.3, the eigenvalue of matrix A.6 is 1.0566, which is exactly the same as that for matrix A.3, and the stable proportion of pups from matrix A.6 is 0.177, which is exactly the sum of the male and female stable proportions from A.4.

We also developed the variances for the parameters estimated in A.6. To do so, we used the delta method (Dorfman, 1938; Ver Hoef, 2012) twice. First, consider the following Taylor series approximation for a vector of functions of random variables,

$$f(x) \approx f(\mu) + D(x - \mu),$$
 (A.7)

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$$\mathbf{f}(\mathbf{x}) = \begin{pmatrix} f_1(\mathbf{x}) \\ f_2(\mathbf{x}) \\ \vdots \\ f_{\ell}(\mathbf{x}) \end{pmatrix}, \quad \mathbf{f}(\boldsymbol{\mu}) = \begin{pmatrix} f_1(\boldsymbol{\mu}) \\ f_2(\boldsymbol{\mu}) \\ \vdots \\ f_{\ell}(\boldsymbol{\mu}) \end{pmatrix}, \quad \mathbf{D} = \begin{pmatrix} \frac{\partial f_1(\mathbf{x})}{\partial X_1} & \dots & \frac{\partial f_1(\mathbf{x})}{\partial X_m} \\ \frac{\partial f_2(\mathbf{x})}{\partial X_1} & \dots & \frac{\partial f_2(\mathbf{x})}{\partial X_m} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_{\ell}(\mathbf{x})}{\partial X_1} & \dots & \frac{\partial f_{\ell}(\mathbf{x})}{\partial X_m} \end{pmatrix},$$

and $\mathbf{x} = (X_1, \dots, X_m)'$ for random variables X_i , and $\boldsymbol{\mu} = E(\mathbf{x})$ where the *i*th column of $\boldsymbol{\mu}$ is μ_i . Then if Σ is the covariance matrix of \mathbf{x} , then

$$cov(\mathbf{f}(\mathbf{x})) \approx \mathbf{D}\mathbf{\Sigma}\mathbf{D}'. \tag{A.8}$$

Notice that there are 8 unique entries in A.3, but some of them are functions of the quantities

in Table A.1. We assume that all variables in Table A.1 are independent, so that the 907 covariance matrix is diagonal. However, using Equation A.8 for the functions of the estimates 908 in Table A.1 contained in A.3 results in the following covariance matrix, 909

among the unique entries in A.3, where we order them $\mathbf{m} = (M_{2,1}, M_{3,2}, M_{4,4}, M_{6,5}, M_{7,6},$ 910 $M_{8,8}, M_{1,8}, M_{5,8}$). 911

Next, notice that δ , ϕ , and κ are functions of the entries in M, but that function is 912 complicated and nonlinear because some entries occur multiple times in M, and because of 913 the scaled eigenvector v. In fact, we can write them showing the dependence on m as $\delta(\mathbf{m})$, 914 $\phi(\mathbf{m})$, and $\kappa(\mathbf{m})$, where the exact dependencies are given in Equation A.5. We need the 915 derivatives of $\delta(\mathbf{m})$, $\phi(\mathbf{m})$, and $\kappa(\mathbf{m})$ with respect to every element of \mathbf{m} . If we write $f_i(m_i)$, 916 where m_i is the jth element of **m** and $f_i(\mathbf{m})$ is the ith function, which is one of $\delta(\mathbf{m})$, $\phi(\mathbf{m})$, 917 or $\kappa(\mathbf{m})$, then the i, jth component of the matrix **D** will be a numeric approximation to the 918 derivative by letting $\mathbf{D}_{i,j} = (f_i(m_j + h) - f_i(m_j))/h$ for some small value of h. We used 1×10^{-5} for both positive and negative values of h for all i and j, and tried 1×10^{-4} and 1×10^{-6} but found there was very little change in **D** for smaller values of h. Then, using Equation A.8 again, with Σ as given in A.9, we obtained the following covariance matrix 922 among the estimates of δ , ϕ , and κ ,

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$$\hat{\nabla} \hat{\nabla} \begin{pmatrix} \hat{\delta} \\ \hat{\phi} \\ \hat{\kappa} \end{pmatrix} = \begin{pmatrix} 0.000317 & 0.000171 & -0.000017 \\ 0.000171 & 0.001075 & 0.000325 \\ -0.000017 & 0.000325 & 0.003300 \end{pmatrix}.$$
(A.10)

Finally, the prior distributions for these probabilities should to be constrained between 924 0 and 1. We did this by matching moments with a beta distribution. A beta distribution, given as 926

$$f(x|a,b) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} x^{a-1} (1-x)^{b-1},$$

₉₂₇ has

$$E(X) = \frac{a}{a+b},$$

$$var(X) = \frac{ab}{(a+b+1)(a+b)^2}.$$

For example, using $\hat{\delta}$ and $\hat{\text{var}}(\hat{\delta})$, we obtained

$$a = \frac{\hat{\delta}^2 (1 - \hat{\delta}) - \hat{\delta} \hat{\text{var}}(\hat{\delta})}{\hat{\text{var}}(\hat{\delta})},$$

929 and then

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$$b = \frac{a(1-\hat{\delta})}{\hat{\delta}}.$$

For the estimated value of δ in (A.5), and its variance in (A.10), we obtained a=272.63 and b=33.52. For developing priors, we did not use the estimated covariances among $\hat{\delta}$, $\hat{\phi}$, and $\hat{\kappa}$.

Using this basic framework, we developed three prior scenarios. "Base-priors" used the parameters as estimated above, and moment matching to a beta distribution. However, notice that the variances in base-priors are estimates for parameters that are assumed fixed, and from a nearby saltwater location. Our model allows for annual variation in the demographic parameters, and there is little reason to assume that the variance of estimation is related to annual variation. Therefore, it would be prudent to allow the variation to be wider. We decided to triple the standard errors (nine times the variance of each parameter). In addition, the base-priors biased the population towards positive growth because the dominant eigenvalue is 1.0566. In "wide-priors", we wanted to be neutral on population growth. Therefore, we wished to scale matrix A.6 so that the eigenvalue was 1. That is, we wanted to find some α such that

 $\left| \mathbf{I} - \lambda \begin{pmatrix} 0 & \alpha \phi \\ \alpha \kappa & \alpha \delta \end{pmatrix} \right| = 0.$

Notice that when $\alpha = 1$, λ is the eigenvalue of the matrix, so $\alpha = 1/\lambda$ yields an eigenvalue of 1. For the values in A.6, it is easily determined that $\alpha = 0.946$ creates the desired matrix. These values, and the variance for wide-priors are given in Table IV, along with the derived a and b parameters for the beta distribution. As a third scenario, "uniform-priors", we used flat uniform priors over the interval 0.5 to 1 for δ and κ , and over the interval 0 to 0.5 for ϕ . Note that using the mean for each of these parameters yields a dominant eigenvalue of 0.948, biasing the population towards negative growth, but has the widest prior variances. Our three scenarios are summarized in Table IV in the main body of the manuscript.