# Assignment-1

# EE:23010 Probability and Random Processes Indian Institute of Technology, Hyderabad

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### I. Question 1.2.4

Verify that

$$\frac{BG}{GE} = \frac{CG}{GF} = \frac{AG}{GD} = 2 \tag{1}$$

#### II. Solution

In order to verify the above equation we first need to find **G**. **G** is the intersection of *BE* and *CF* Using the value of  $\mathbf{G}$  from (1.2.3).

$$\mathbf{G} = \begin{pmatrix} -2\\0 \end{pmatrix} \tag{2}$$

Also, We know that **D**, **E** and **F** are midpoints of BC, CA and AB respectively.

$$D = {B + C \over 2}, E = {C + A \over 2}, F = {A + B \over 2}$$
 (3)

 $\mathbf{D} = \frac{\begin{pmatrix} -4\\6 \end{pmatrix} + \begin{pmatrix} -3\\-5 \end{pmatrix}}{2}, \ \mathbf{E} = \frac{\begin{pmatrix} -3\\-5 \end{pmatrix} + \begin{pmatrix} 1\\-1 \end{pmatrix}}{2}, \ \mathbf{F} = \frac{\begin{pmatrix} 1\\-1 \end{pmatrix} + \begin{pmatrix} -4\\6 \end{pmatrix}}{2}$  The value of  $\frac{BG}{GE}$ 

$$\implies \mathbf{D} = \begin{pmatrix} \frac{-7}{2} \\ \frac{1}{2} \end{pmatrix}, \implies \mathbf{E} = \begin{pmatrix} -1 \\ -3 \end{pmatrix}, \implies \mathbf{F} = \begin{pmatrix} \frac{-3}{2} \\ \frac{5}{2} \end{pmatrix}$$
(5)

Taking direction vector of BG, GE, GF, CG, AG, GD

$$\mathbf{G} - \mathbf{B} = \begin{pmatrix} 2 \\ -6 \end{pmatrix} \tag{6}$$

$$\mathbf{E} - \mathbf{G} = \begin{pmatrix} 1 \\ 3 \end{pmatrix} \tag{7}$$

$$\mathbf{F} - \mathbf{G} = \begin{pmatrix} \frac{1}{2} \\ \frac{5}{2} \end{pmatrix} \tag{8}$$

$$\mathbf{G} - \mathbf{C} = \begin{pmatrix} 1 \\ 5 \end{pmatrix} \tag{9}$$

$$\mathbf{G} - \mathbf{A} = \begin{pmatrix} -3\\1 \end{pmatrix} \tag{10}$$

$$\mathbf{D} - \mathbf{G} = \begin{pmatrix} \frac{-3}{2} \\ \frac{1}{2} \end{pmatrix} \tag{11}$$

Using the equation, (6), (7), (8), (9), (10), (11) Taking norm of BG, GE, GF, CG, AG, GD

$$\|\mathbf{G} - \mathbf{B}\| = \sqrt{2^2 + (-6)^2} = \sqrt{40}$$
 (12)

$$\|\mathbf{E} - \mathbf{G}\| = \sqrt{1^2 + 3^2} = \sqrt{10}$$
 (13)

$$\|\mathbf{F} - \mathbf{G}\| = \sqrt{\left(\frac{1}{2}\right)^2 + \left(\frac{5}{2}\right)^2} = \frac{\sqrt{26}}{2}$$
 (14)

$$\|\mathbf{G} - \mathbf{C}\| = \sqrt{1^2 + 5^2} = \sqrt{26}$$
 (15)

$$\|\mathbf{G} - \mathbf{A}\| = \sqrt{(-3)^2 + 1^2} = \sqrt{10}$$
 (16)

$$\|\mathbf{D} - \mathbf{G}\| = \sqrt{\left(\frac{-3}{2}\right)^2 + \left(\frac{1}{2}\right)^2} = \frac{\sqrt{10}}{2}$$
 (17)

Now, using the equation (12), (13), (14), (15), (16),

value of 
$$\frac{BG}{GE}$$

$$\frac{BG}{GE} = \frac{\|\mathbf{G} - \mathbf{B}\|}{\|\mathbf{E} - \mathbf{G}\|} = \frac{\sqrt{40}}{\sqrt{10}} = 2$$
 (18)

2) The value of  $\frac{CG}{GF}$ 

$$\frac{CG}{GF} = \frac{\|\mathbf{G} - \mathbf{C}\|}{\|\mathbf{F} - \mathbf{G}\|} = \frac{\sqrt{26}}{\frac{\sqrt{26}}{2}} = 2 \tag{19}$$

3) The value of  $\frac{AG}{GD}$ 

$$\frac{AG}{GD} = \frac{\|\mathbf{G} - \mathbf{A}\|}{\|\mathbf{D} - \mathbf{G}\|} = \frac{\sqrt{10}}{\frac{\sqrt{10}}{2}} = 2$$
 (20)

Hence,

$$\frac{BG}{GE} = \frac{CG}{GF} = \frac{AG}{GD} = 2 \tag{21}$$