## Chapter 9 Gaussian

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Q9.3.6: The probability that a student is not a For pdf calculation swimmer is  $\frac{1}{5}$ . Then the probability that out of five students, four are swimmers

1) 
$${}^5C_4\left(\frac{4}{5}\right)^4\frac{1}{5}$$

2) 
$$\left(\frac{4}{5}\right)^4 \frac{1}{5}$$

3) 
$${}^{5}C_{1}\frac{1}{5}\left(\frac{4}{5}\right)^{4}$$

## 4) None of these

**Solution:** The pmf of X is,

Parameter	Value	Description
n	5	number of students
q	1/5	probability for not a swimmer
p	4 5	probability for a swimmer
k	4	number of swimmers

TABLE 4 GIVEN INFORMATION

$$p_X(k) = {}^nC_k p^k q^{n-k} \tag{1}$$

and the desired probability is

$$p_X(4) = {}^{5}C_4 \left(\frac{4}{5}\right)^4 \left(\frac{1}{5}\right)^{5-4} \tag{2}$$

$$= 0.4096$$
 (3)

Let Y be gaussian variable

$$u = np \tag{4}$$

$$=4 \tag{5}$$

$$\sigma^2 = npq \tag{6}$$

$$=\frac{4}{5}\tag{7}$$

Using Normal distribution at X = 4.

$$Z = \frac{X - \mu}{\sigma} \tag{8}$$

$$=\frac{4-4}{\sqrt{\frac{4}{5}}}\tag{9}$$

$$=0 (10)$$

$$f_Y(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$
 (11)

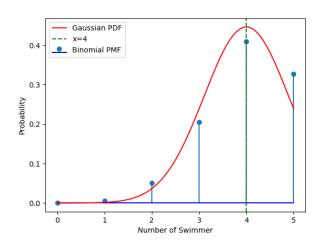


Fig. 4. Binomial pmf vs Gaussian pdf

From the plot, pmf is close to normal distribution pdf.

$$p_Y(4) = p_Z(0) (12)$$

$$= 0.44603$$
 (13)

From (3) and (13),

$$p_X(4) \approx p_Y(4) \tag{14}$$

Hence, option (3)