1

Problem 1.1.5

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question : The normal form of the equation of $\bf AB$ is

$$\mathbf{n}^{\mathsf{T}} \left(\mathbf{x} - \mathbf{A} \right) = 0 \tag{1}$$

where

$$\mathbf{n}^{\mathsf{T}}\mathbf{m} = \mathbf{n}^{\mathsf{T}} \left(\mathbf{B} - \mathbf{A} \right) = 0 \tag{2}$$

or,

$$\mathbf{n} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \mathbf{m} \tag{3}$$

Find the normal form of the equations of **AB BC** and **CA**

Solution: : The normal equation for the side BC is

$$\mathbf{n}^{\mathsf{T}} \left(\mathbf{x} - \mathbf{B} \right) = 0 \tag{4}$$

$$\implies \mathbf{n}^{\mathsf{T}}\mathbf{x} = \mathbf{n}^{\mathsf{T}}\mathbf{B} \tag{5}$$

Now our task is to find the \boldsymbol{n} so that we can find $\boldsymbol{n}^{\mathsf{T}}.$ As given in the question

$$\mathbf{n} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \mathbf{m} \tag{6}$$

Here $\mathbf{m} = \mathbf{C} - \mathbf{B}$ for side \mathbf{BC}

$$\implies \mathbf{m} = \begin{pmatrix} -3 \\ -5 \end{pmatrix} - \begin{pmatrix} -4 \\ 6 \end{pmatrix}$$

$$= \begin{pmatrix} 1 \\ -11 \end{pmatrix}$$
(8)

Now as we have obtained vector \mathbf{m} , we can use this to obtain vector \mathbf{n}

$$\mathbf{n} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ -11 \end{pmatrix} = \begin{pmatrix} -11 \\ -1 \end{pmatrix} \tag{9}$$

The transpose of \mathbf{n} is

$$\mathbf{n}^{\top} = \begin{pmatrix} -11 & -1 \end{pmatrix} \tag{10}$$

Hence the normal equation of side BC is

$$\begin{pmatrix} -11 & -1 \end{pmatrix} \mathbf{x} = \begin{pmatrix} -11 & -1 \end{pmatrix} \begin{pmatrix} -4 \\ 6 \end{pmatrix} \tag{11}$$

$$\implies (-11 \quad -1)\mathbf{x} = 38 \tag{12}$$

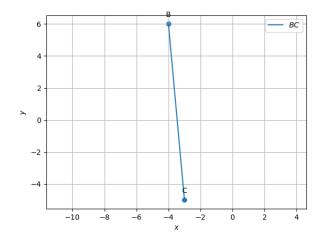


Fig. 0. The line **BC** plotted using python