

### Kombinatorika – cvičení 3:

Uveďte podmínky a určete množinu kořenů:

$$1) \binom{10}{1} \binom{x}{x-2} - \binom{x+3}{x+1} = 15 \binom{x}{0}$$

$$2) \binom{n}{2} = 93 - \binom{n+3}{n+1} - \binom{n+6}{2}$$

$$3) \binom{6}{5} \binom{x+1}{x-1} - \binom{6}{4} \binom{x+2}{x+1} = \binom{4}{2}$$

$$4) \binom{x}{x-2} = \frac{5x}{2} - \binom{x}{x-1}$$

$$5) \binom{x}{1} = 2x - 3 - \binom{x-3}{x-4}$$

$$6) \binom{x-1}{x-3} - 2 \binom{x-2}{x-4} = 0$$

$$7) 2 \binom{x+6}{x+4} - \binom{x+4}{x+2} = 4! + \binom{5}{2} \cdot x$$

$$8) \binom{x+1}{x+1} + \binom{5}{3} \cdot \binom{x+1}{x} - \binom{4}{3} \cdot \binom{x+1}{x-1} = 1$$

$$9) 5 \binom{x+8}{x+7} - \binom{x}{1} = 2 \binom{x}{0} \binom{x+1}{x} \binom{x}{x-1}$$