# Predicting Credit Card Defaults EECS 433 Final Project

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#### Abstract

This paper uses multiple machine learning algorithms, such as K-nearest neighbor, Logistic regression, Discriminant analysis, Nave Bayesian, and Classification tree, to predict credit card defaults from a sample of n=30,000. It uses baseline techniques and seeks to show how selected improvements to the algorithms can be made that result in slightly better model accuracy, as judged by the Receiver Operating Characteristic area under curve metric. The paper concludes with a discussion of the strengths and weaknesses of the algorithms, and the reason why the Nave Bayesian approach yielded the best model performance.

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Label	Attribute	Notes
X1	Credit Given	NT Dollar currency
X2	$\operatorname{Gender}$	1 = male, 2 = female
Х3	Education	1 = grad. school; 2 = university; 3 = high school
X4	Marital Status	1 = married; 2 = single
X5	Age	years
X6	Repayment Status- Sept	$-1 = \text{pay duly}; 1 = 1 \text{mo payment delay}; \dots$
X7	Repayment Status- Aug	$\dots 9 = 9$ mo payment delay or greater
X8	Repayment Status- July	-
X9	Repayment Status- June	-
X10	Repayment Status- May	-
X11	Repayment Status- April	-
X12	Bill Statement- Sept	NT Dollary currency
X13	Bill Statement- Aug	-
X14	Bill Statement- July	-
X15	Bill Statement- June	-
X16	Bill Statement- May	-
X17	Bill Statement- April	-
X18	Bill Payment- Sept	NT Dollary currency
X19	Bill Payment- Aug	-
X20	Bill Payment- July	-
X21	Bill Payment- June	-
X22	Bill Payment- May	-
X23	Bill Payment- April	-

Table 1: Explanatory Variables

## 1 Introduction & Motivation

You will almost certainly start with an introductory description of the topic that you investigated in your assignment. Discuss any goals, motivation, or examples of the subject; the key is to provide the reader with any information that is necessary to understand why your topic was worth investigating. This descriptive section should also allow the reader to understand the subsequent detail sections on the subject.

## 2 Problem Description

#### 2.1 Description of the Data

The data is comprised of 23 explanatory variables (X1-X23) and one response variable (Y). Y denotes whether the borrower defaulted on credit card debt repayment, with Y = 1 denoting default. In the sample size of n = 30,000, only 6,636 (22%) defaulted.

### 2.2 Measuring Model Accuracy

When the explanatory variable is skewed towards one binary value, as is the case here, measuring the accuracy of a model via its error rate is insufficient. Consider a naive model that

estimated  $\hat{y}=1$  regardless of the values of the explanatory variables. Despite this being a naive and model that added little value, it would have a decent error rate: Consider n=100, this model would then have  $\approx 22$  misclassifications, resulting in an error rate of 22%. That's not half-bad!

While error rate is often a good measure of model accuracy, it is clearly insufficient here. A better measure of model accuracy involves using a lift curve. Let's consider a sample of n=100 with probility of y of 22%. Three lines comprise a lift curve: i) the prior probability line which represents a guess; this line would start at (0,0), and extend to (100,22) with slope 11/50. ii) The hypothetical best-model, which would start at (0,0), extend to (22,22) with slope 1, and then extend to (100,22) with slope 0. This curve represents 100% accuracy, or the ability to pick out which of the 100 samples have response variable equal to one. Lastly, iii) represents the model. This would hopefully be able to ascertain which of the n=100 are likely to yield y=1, and pick those first. The accuracy measure uses the ratio between the lines ((iii) & (i)) divided by ((ii) & (i)). A good model will be closer to the hypothetical best line than to the guess line, so it will have a ratio approaching 1.

Receiver operating characteristic (ROC) area under curve is also a good measure of model accuracy. An ROC curve measures the discriminability of a model. It plots the true positive rate as a function of the false positive rate. Each point represents a specificity pair; the curve has higher slope initially because in a gaussian distribution, there are values on both sides of the bell curve that are easy to classify. The slope approaches 0 as the curve gets closer to 100% true sensitivity rate, as there will always be instances that are very tough to classify, for which the model would yield false positives before it found a true positive. The area under the curve represents the quality of the model, where 1 is the hypothetical best model. The ROC curves for the models utilized in this paper are presented in Figure 1. The best performing model had an area under curve ratio of 75%.

#### 2.3 Not all Misclassifications are Equal

The section above treats a false positive and a false negative equal in the eyes of the model accuracy rates. However, this is not the case in actuality; one misclassification may be considerably more costly to the end user of the model than another type of misclassification. Consider a radiologist screening for cancer; a false positive would scare a patient, but a false negative is far worse - it could lead to the cancer going untreated. Similarly, consider a bank using the credit card data to decide whether to issue credit to a customer. A false positive would represent major loss from default on debt (Figure 2 - upper right quadrant), whereas a false negative would represent a minor loss of revenue from the client under consideration (Figure 2 - lower left quadrant).

#### 3 Baseline Methods

This section will the discuss the baseline methods used to predict credit card defaults.

#### 3.1 Classification Tree

Splitting the data set of n = 30,000 into n = 15,000 for training and n = 15,000 for testing; a decision tree classifier was trained with the training set. A decision tree starts at the root of the tree; each attribute is considered for its *information gain*; whichever attribute best splits the yes / no classifications correctly is chosen as the root of the subtree. This represents a greedy algorithm since it is based on making a series of locally-best decisions until a base case

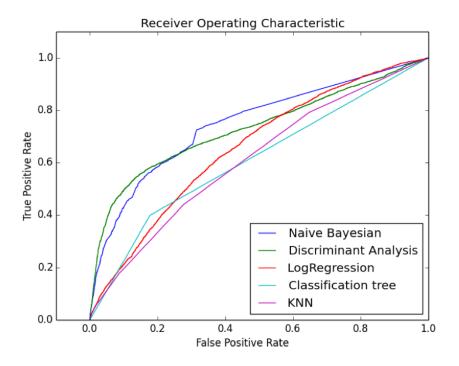


Figure 1: Receiver Operating Characteristic

22,296 (model correctly predicted non-default)	1,068 (false positive)
4,426 (false negative)	2,210 (model correctly predicted default)

Figure 2: Confusion Matrix - KNN

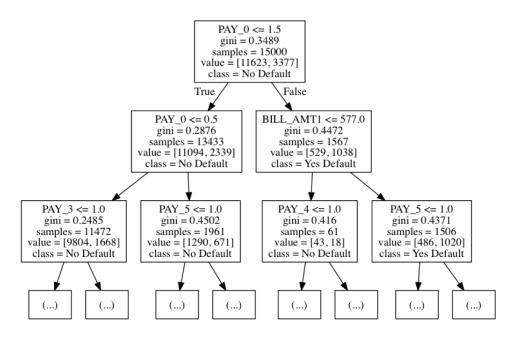


Figure 3: Decision Tree - prior to feature selection

is reached; in a decision tree, the base case is correct classification; however, pruning can be used to prevent *overfitting* and a model that generalizes better.

### 3.2 K-Nearest Neighbor

xyz

#### 3.3 Logistic Regression

xyz

#### 3.4 Discriminant Analysis

xyz

### 3.5 Naive Bayesian

xyz

## 4 Improvements

#### 4.1 Feature Selection

xyz

Column 1	Column 2	Column 3
a	b	c
d	e	f
g	h	i

Table 2: A sample table

#### 4.2 10-Fold Cross Validation

xyz

### 4.3 Principal Component Analysis

xyz

#### 5 Conclusion

Wrap up your paper with an "executive summary" of the paper itself, reiterating its subject and its major points. If you want examples, just look at the conclusions from the literature.

#### 6 Course Feedback

Professor Wu is clearly an accomplished researcher and this course is very advanced and well taught; I particularly liked the demos on the chalkboard. Students would have benefited from mandatory assignments from the book to solidify the materials taught in lecture; applying what we've learned helps reenforce learning new material. Similarly, weekly office hours, a teaching assistant, and piazza, would have led to discussions that would have benefited all students and furthered learning. A really solid background in linear algebra would have helped me more-easily understand the fast-moving lectures. I'm pleased I took the course, and it has opened doors for future statistical pattern recognition learning down-the-road.

#### 7 Latex Features

#### 7.1 Tables and Figures

LATEX has full support for tables and figures. Table 2 shows a sample table and Figure ?? shows a sample figure. Note the built-in support for captions and the automated numbering functionality. Lists of tables and figures can also be automatically generated, as seen at the beginning of this document.

One very important thing to remember about how LATEX handles tables and figures by default: you don't have to worry about where they go exactly. The general rule is that you insert them in the source after your first reference to them, and LATEX determines their final position. It also makes decisions on how much page space to devote to them. This all follows LATEX's overall theme of focusing on the content of your paper, and not its format.

Just so you can see a second table, Table 3 is provided.

Column 1	Column 2	Column 3
a	b	С
d	e	f
g	h	i

Table 3: Another sample table

#### 8 Latex features

Perhaps the most important functionality to learn for the paper is L<sup>A</sup>T<sub>E</sub>X bibliography support. Citations and references are handled automatically by L<sup>A</sup>T<sub>E</sub>X through its companion program, BibT<sub>E</sub>X. All you have to do is provide a bibliography file that provides the reference information and internal keys (very much like variable names) that you use in your document. <sup>1</sup>

BibTeX supports virtually all kinds of references, including books [?, ?, ?, ?], parts of books [?], articles [?, ?, ?, ?], and conference proceedings [?, ?, ?, ?, ?], to name a few. If not already included in your LaTeX distribution, download and install the url package to support formatting of URLs; you can usually mention these in the *note* or *howpublished* fields of your BibTeX file.

Like Section 1, a background, preliminary, and related work section is also almost certainly needed for your paper. In this section, describe any history, work, or projects that serve as direct contributors to the subject of your research paper. Look at other papers in the literature to see how they organized, presented, and discussed prior work.

The Shneiderman/Plaisant text [?] provide some pointers to seminal or key works; because they made it into the textbook they aren't necessarily "bleeding edge," but they likely provide the foundation for your chosen subject matter.

#### 9 Another Section

We're adding another section just so you can see how that looks. Plus there are a few more LATEX features to illustrate.

#### 9.1 Bulleted and Numbered Lists

LATEX is very good at providing clean lists. Examples are shown below.

- Bulleted items come out properly indented and spaced, every time.
  - Sub-bullets are a virtual no-brainer: just nest another itemize block.
  - Note how the bullet character automatically changes too.
- Just keep on adding \items...
- ... until you're done.

Numbered lists are almost identical, except that you specify enumerate instead of itemize. List items are specified in exactly the same way (thus making it easy to change list types).

- 1. A list item
- 2. Another list item

<sup>&</sup>lt;sup>1</sup>And always remember to run LATEX at least twice after running BibTEX.

Figure 4: Another sample figure

- 3. A list item with multiple nested lists
  - Nested lists can be of mixed types.
  - That's a lot of power and flexibility for the price of learning a handful of directives.
    - (a) Like nested bullet lists, nested numbered lists also "intelligently" change their numbering schemes.
    - (b) Meanwhile, all you have to write is \item. LATEX does the rest.
- 4. Back to your regularly scheduled list item

#### 9.2 Subsection with Another Figure

We may as well include a second figure also, shown in Figure 4. The same image file is used, but note how it can be resized. Again, observe how the positions of the tables and figures do not necessarily match their positions in the source file, reiterating the aforementioned LaTeX functionality for deciding where these items go in the final document. You provide an approximate location, and LaTeX does the rest.