

Quiz 6 Solutions

1a.) $4(10^{2\log(x)+1}) = 3$

$$10^{2\log(x)+1} = \frac{3}{4}$$

$$10^{2\log(x)} \cdot 10 = \frac{3}{4}$$

$$10^{2\log(x)} = \frac{3}{40}$$

$$10^{\log(x^2)} = \frac{3}{40}$$

$$x^2 = \frac{3}{40}$$

$$x = \sqrt{\frac{3}{40}} \approx .2738 \quad (\text{This the same value as the exam solution})$$

* Review exponent algebra *

b.) $e^{kx} = 2e^{x+2}$

$$\ln(e^{kx}) = \ln(2e^{x+2})$$

$$kx \ln(e) = \ln(2) + \ln(e^{x+2})$$

* This where many of you messed up *

$$kx = \ln(2) + (x+2) \ln(e)$$

$$* \ln(e) = \log_e(e) = 1 *$$

$$kx - x = \ln(2) + 2$$

$$x(k-1) = \ln(2) + 2$$

* Factored out x *

$$x = \frac{\ln(2) + 2}{k-1}$$

c.) $\log(100x) = 2 + 2\log(x^2)$

$$\log(100) + \log(x) = 2 + 2\log(x^2)$$

$$* \log(AB) = \log(A) + \log(B); A=100, B=x *$$

$$\log(100) + \log(x) = 2 + 4\log(x)$$

$$* \log(B^u) = u\log(B) *$$

$$\log(100) - 2 = 3\log(x)$$

$$* \log(100) = \log(10^2) = 2$$

$$0 = 3\log(x)$$

$$0 = \log(x)$$

$$10^0 = 10^{\log(x)}$$

* exponentiate by base of log (base=10) *

$$1 = x$$