

To the Graduate Council:

I am submitting herewith a thesis written by Jason Bane entitled “The EMC Effect in A=3 Nuclei.” I have examined the final paper copy of this thesis for form and content and recommend that it be accepted in partial fulfillment of the requirements for the degree of Doctor of Philosophy, with a major in Nuclear Physics.

Nadia Fomin, Major Professor

We have read this thesis
and recommend its acceptance:

Jamie Coble

Kate Jones

Thomas Papenbrock

Soren Soreson

Accepted for the Council:

Carolyn R. Hodges

Vice Provost and Dean of the Graduate School

To the Graduate Council:

I am submitting herewith a thesis written by Jason Bane entitled “The EMC Effect in A=3 Nuclei.” I have examined the final electronic copy of this thesis for form and content and recommend that it be accepted in partial fulfillment of the requirements for the degree of Doctor of Philosophy, with a major in Nuclear Physics.

Nadia Fomin, Major Professor

We have read this thesis
and recommend its acceptance:

Jamie Coble

Kate Jones

Thomas Papenbrock

Soren Soreson

Accepted for the Council:

Carolyn R. Hodges

Vice Provost and Dean of the Graduate School

(Original signatures are on file with official student records.)

The EMC Effect in A=3 Nuclei

A Thesis Presented for
The Doctor of Philosophy
Degree

The University of Tennessee, Knoxville

Jason Bane

December 2018

© by Jason Bane, 2018

All Rights Reserved.

Contents

List of Tables	v
List of Figures	vi
1 Introduction	1
1.1 Electron scattering	2
1.1.1 Deep inelastic scattering	5
1.2 EMC Effect	6
1.3 MARATHON	9
2 Experimental Setup	10
2.1 Thomas Jefferson Lab	10
2.1.1 CEBAF	10
2.1.2 Hall A	12
2.2 Target	17
2.3 High Resolution Spectrometers	19
2.3.1 Vertical Drift Chambers	20
2.3.2 Scintillators	22
2.3.3 Cherenkov	22
2.3.4 Shower Calorimeter	22
2.3.5 Pion Rejector	22
2.3.6 FPP Chambers	22

2.4	Trigger Setup	22
2.5	DAQ - Data Acquisition System	22
2.6	Kinematic Settings	22
3	Calibration	24
3.1	Beam Line	24
4	Data Analysis	27
4.1	Efficiencies	27
4.1.1	Computer and electronic Lifetime	27
4.1.2	Particle Identification Efficiency	28
4.1.3	31
4.1.4	32
4.2	Background Subtraction	34
4.2.1	End Caps	34
4.2.2	Pair Produced Electrons	34
5	Results	35
6	Simulation	36
6.1	Investigation	36
6.2	Transformation	37
6.3	Results	39
7	Conclusion	42
	Bibliography	43

List of Tables

4.1 Livetime during the MARATHON experiment calculated using trigger 2.	28
--	----

List of Figures

1.1	Simple Feynman diagram of an electron scattering from a proton [7].	3
1.2	Graph of the ratio of A/D structure functions vs x for Carbon [10].	7
1.3	EMC effect from EMC, SLAC, and BCDMS [17]	8
1.4	Graph of the ratio of A/D structure functions vs x for Carbon [10].	9
2.1	Schematic Layout of CEBAF.	11
2.2	A 3D drawing of Hall A.	12
2.3	A schematic layout of the beam line in Hall. [1]	13
2.4	BPM design diagram, from JLab instrumentation group. Beam direction is from left to right [23].	14
2.5	BPM design diagram, looking down the beam line[23].	14
2.6	Hall A Current Monitor components [4].	16
2.7	Target Images	18
2.8	A side view of a HRS [1].	20
2.9	A view of both the left(top) and right(bottom) detector stacks inside the left and right HRS [1].	21
2.10	A sketch of the two VDC planes in the HRSs with a particle traveling through the detector at 45° .[6].	22
2.11	A sketch of the two VDC planes in the HRSs with a particle traveling through the detector at 45° .[6].	23
3.1	A schematic layout of a harp fork [23]	25

3.2	The X and Y position for a Bulls eye scan for BPM calibration.	26
4.1	Two dimensional plot of the cherenkov sum versus Total Energy deposited, including electron sampling in teal and non-electron sampling in red.	29
4.2	Electrons and other back ground particles identified via cuts in the total calorimeter and the gas cherenkov shown in the individual layers of the calorimeters and the cherenkov. Sampling cuts for Electrons in teal and Non-Electrons in red.	30
4.3	The PID efficiency for the cherenkov and both layers of the calorimeter,including the overall total PID efficiency for each of the gas targets at all of the kinematics.	31
4.4	Trigger efficiency of trigger 2 for different targets at all kinematics calculated via sampling from trigger 1.	32
4.5	Tracking efficiency of the VDCs for different targets at all kinematics.	33
6.1	Example of the electron beam(red) with a energy of 2.5 GeV and the proton(blue) with angle of 45° in respect to the electron and with a momentum of 0.5 GeV/c.	37
6.2	Vector representations of the momentum for the incoming electron(red) and target proton(blue) with units of GeV for each phase of their transformations before scattering.	38
6.3	Vector representations of the momentum for the incoming electron(red) and target proton(blue) with units of GeV for each phase of their transformations after scattering).	40
6.4	Simulation results for fixed momentum protons. Three runs with unique proton momentum.	41

Chapter 1

Introduction

Understanding the world around us is the goal of every scientist, from the chemist that experiments with the formation of atoms to the geologist exploring the process of rock formations. Nuclear physicists focus on studying the fundamental constituents of matter, the building blocks of nature. Physicist use scattering experiments at accelerator facilities, like CERN in Switzerland, DESY in Germany, BATES in Massachusetts, JLAB in Virginia, and many others, to study the protons and neutrons and their constituents that make up a nucleus. These experiments allow physicists to observe the internal structure of the nucleus and to investigate the interactions between the quarks and gluons. Many of the experiments are design to confirm a existing results while also expanding on unique ideas.

In the last century, there have been numerous breakthroughs in the fields of nuclear and particle physics. Rutherford discovered the proton by bombarding light nuclei with alpha particles to produce



This reaction allowed Rutherford to conclude that the Hydrogen nucleus was a constituent of an atomic nuclei [18]. In the late 1950s, experimental results published

by W. McAllister and R. Hofstadter exposed some of the eternal structure of the proton [7, 15]. The European Muon Collaboration(EMC) produced results in the early 1980s showing a differences between the internal structure of the deuterium nucleus and Iron [20, 10]. The data received from scattering experiments using alpha particles contain information about the target, the beam, and the interaction between the two. Deciphering and analyzing this data can be convoluted because the cross-section contains information about the internal structure of the target and the beam along with the interaction and forces between the two [18].

1.1 Electron scattering

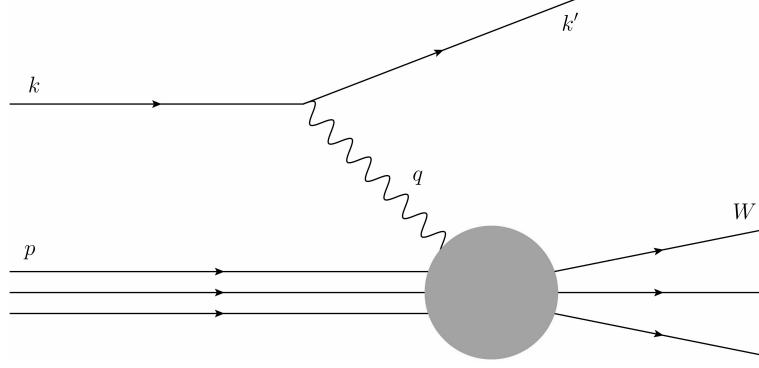
In order to remove some of the complexity in scattering experiments, one may employ highly relativistic electrons. Electrons being point-like particles without any internal structure allow the elimination of some of the analysis difficulties with using alpha particles in scattering experiments due to their complex internal structure. Electrons and the target nucleus, nucleon, or quarks interact via the exchange of a virtual photon. Using quantum electrodynamics (QED), these interactions can accurately be described by the well known electromagnetic interaction. Higher order terms of this process contribute very little due to the coupling constant $\alpha \approx 1/137$, being much smaller than one.

Figure 1.1 represents an electron scattering from a proton. The incoming or incident electron's four-momentum is described as $k = (E, \vec{k})$ and the scattering electron's four-momentum is represented by $k' = (E', \vec{k}')$. The exchange of the virtual photon in this electromagnetic interaction is defined by the four-momentum transfer q :

$$Q^2 \equiv -q^2 = 4EE' \sin^2(\theta/2). \quad (1.2)$$

In equation 1.2, E and E' are the electron energy before and after the scattering interaction. Theta is the angle that describes the deflection of E' from the electron's original path.

Figure 1.1: Simple Feynman diagram of an electron scattering from a proton [7].



Along with Q^2 , the variables ν , W , and x_B are used to narrate the evolution of the electron scattering process. ν , defined as $p \cdot q/M$. In the rest frame of the target, ν can be described by:

$$\nu = E - E'. \quad (1.3)$$

Simply, ν is the magnitude of energy loss by the electron during the scattering interaction. The invariant mass of the system, W , defines the hadronic state produced by the scattering event.

$$W^2 \equiv (q + p)^2 = M^2 + 2M\nu - Q^2. \quad (1.4)$$

A scattering event with the invariant mass equal to the square of the mass of the nucleon, (M^2), falls in the regime of elastic scattering. W above M^2 will transform the scattering interaction from an elastic scattering to inelastic scattering due to the excited state of the scattered byproduct. x_B , the Bjorken scaling variable is a dimensionless quantity that measures the inelastically of a scattering process. x_B is defined as: $x := \frac{Q^2}{2M\nu}$.

The intrinsic likelihood of an event with a certain Q^2 , ν , and W is defined by the scattering cross section. An electron scattering off of a target with a charge of $Z * e$ can be described by the Rutherford cross-section. Povh et. al. details the Rutherford cross section as:

$$\left(\frac{d\sigma}{d\Omega}\right)_{Rutherford} = \frac{(zZe^2)^2}{(4\pi\epsilon_0)^2 * (eE_{kin})^2 \sin^4(\theta/2)}. \quad (1.5)$$

In the early 1920s, German physicists Stern and Gerlach performed an experiment that confirmed the presence of electron angular momentum. Later a discovery of electron spin was made by Uhlenbeck and Goudsmit. The Rutherford cross-section neglects the spin of an electron and its target. The Mott cross-section is the evolved version of the Rutherford cross-section. It has been modified to include the intrinsic spin of the target and electron. The Mott cross-section is: [12, 18]

$$\left(\frac{d\sigma}{d\Omega}\right)_{Mott} = \frac{4Z^2\alpha^2(\hbar c)^2 E'^2}{|\mathbf{q}_c|^4} \cos^2(\theta/2). \quad (1.6)$$

There is an agreement between the measured cross section and the theoretical Mott cross-section when in the limit of $|\mathbf{q}| \rightarrow 0$ for scattering events of electrons off of a target nuclei. As $|\mathbf{q}|$ climbs further from zero, the experimentally measured cross sections systematically decreases [18]. Increasing the $|\mathbf{q}|$ of an interaction reduces the size of the wavelength of the virtual photon that mediates the electromagnetic interaction between the electron and target nuclei and increases the resolution of the probe. The wavelength of this virtual photon is inversely proportional to $|\mathbf{q}|$, and can be described by the following: $\lambda = \frac{\hbar}{|\mathbf{q}|}$ [18]. Increasing the amount of momentum transferred in an electromagnetic reaction allows one to study deeper into the nucleus.

Studying the internal structure of a nucleus with the electromagnetic interaction requires increasing the momentum transferred. Pushing $|\mathbf{q}|$ to be comparable with the mass of a nucleon adds more complexity to the details of the scattering interaction.

At the appropriate levels of $|\mathbf{q}|$ to study the nucleons in the nucleus, the Mott cross-section equation requires modifications to include additional factors that incorporate information about the target. The Rosenbluth formula is based on the Mott cross section and embraces target recoil, magnetic moment, and charge and current distributions. Povh writes the Rosenbluth formula as:

$$\left(\frac{d\sigma}{d\Omega}\right) = \left(\frac{d\sigma}{d\Omega}\right)_{Mott} * \left[\frac{G_E^2(Q^2) + \tau G_M^2(Q^2)}{1 + \tau} + 2\tau G_M^2(Q^2) \tan^2 \frac{\theta}{2} \right]. \quad (1.7)$$

Equation 1.7 contains $G_E^2(Q^2)$ and $G_M^2(Q^2)$, the electric and magnetic form factors. τ is used in the Rosenbluth formalism to account for the magnetic moment of a nucleon and is defined as: $\tau = \frac{Q^2}{4M^2c^2}$ [18]. In the general case of electron scattering off of a free proton or neutron elastically, the scattered energy of the electron will be a function of the incident electron's energy and the scattered angle of the electron, shown in the following equation.

$$E' = \frac{E}{1 + \frac{E}{Mc^2}(1 - \cos\theta)} \quad (1.8)$$

1.1.1 Deep inelastic scattering

The first generation of electron scattering experiments achieving a significantly large $|\mathbf{q}|$ used a linear accelerator with a 25 GeV maximum beam energy, and following generations increased the total interaction energy to substantially higher thresholds. At these high incident beam energies, individual resonances cannot be separated in the invariant mass spectrum above 2.5 GeV. Observations made into this convoluted invariant mass spectrum has shown that many strongly interacting particles are produced, known as hadrons. Scattering interactions that generate these hadrons are considered to be inelastic. Inelastic scattering events contain the possibility of conceiving additional resultants and increase the complexity of a scattering interaction. Inelastic scattering events occur when the wavelength of the virtual photon is comparable to the radius of the struck nucleon or when $Q^2 R^2 \lesssim 1$ [18]. Increasing the amount of transferred momentum so that $Q^2 R^2 \gtrsim 1$,

increase the resolution of the probe to a level that allows for the interacting with the charge constituents within the nucleon. When the scattering event probes the fundamental elements of a nucleon, the scattering process is titled deep inelastic scattering(DIS). Due to the increase in complexity, an additional degree of freedom has to be introduced into the scattering cross section equation. Modifying the Rosenbluth formula to include the inelastic scattering structure functions $F_1(Q^2, \nu)$ and $F_2(Q^2, \nu)$ evolves the Rosenbluth formula to contain the needed complexity of an inelastic event. These modifications are shown in equation 1.9.

$$\frac{d^2\sigma}{d\Omega dE'} = \left(\frac{d\sigma}{d\Omega} \right)_{Mott} \left[\frac{F_2(Q^2, \nu)}{\nu} + \frac{2F_1(Q^2, \nu)}{M} \tan^2 \frac{\theta}{2} \right] \quad (1.9)$$

The F_1 and F_2 structure functions provide the details for describing the internal composition of the nucleon [18].

$$F_2(x) = x \mathbf{1} \cdot \sum_f z_f^2 (q_f(x) + \bar{q}_f(x)) \quad (1.10)$$

[21] [13]

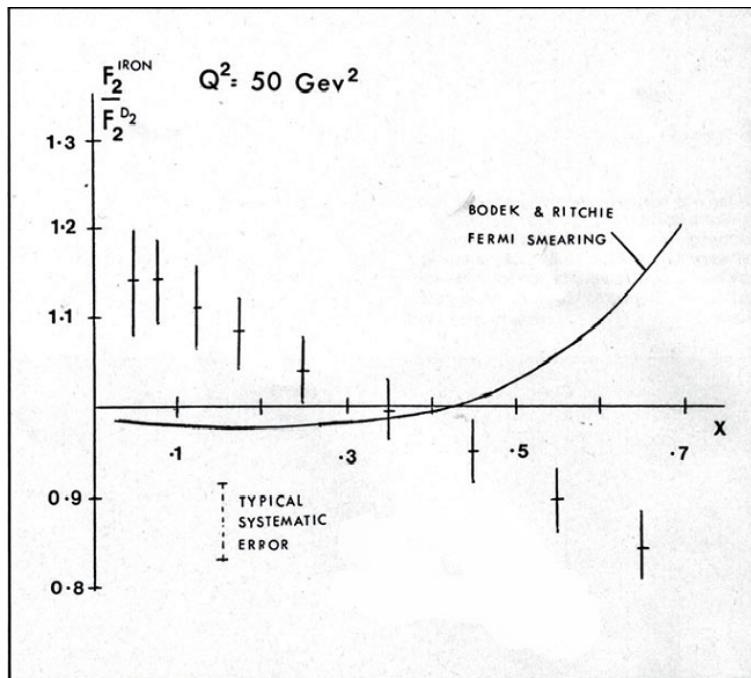
1.2 EMC Effect

The European Muon Collaboration (EMC) performed a deep inelastic measurement with 120-280 GeV muons on iron and deuteron targets [14]. The EMC extracted A/D structure function ratios versus the Bjorken scaling variable, x . The relationship originally expected by the EMC contained the sum of the structure functions of each nucleon in a nucleus. Each nucleus has a certain number of neutrons (N) and a amount of protons (Z). The expected structure function for a nucleus could be written as:

$$F_A = N F_2^N + Z F_2^P. \quad (1.11)$$

The EMC compared the extracted structure functions from iron and deuterium. Their results are shown in Figure 1.2. The $\frac{A}{D}$ structure function ratio showed an unexpected downward slope. This phenomenon was titled the EMC effect. This finding demonstrated to the EMC that their understanding of the nucleus was incorrect. A nucleon's structure function and thereby, the constituent quark distributions may be altered by the nucleus.

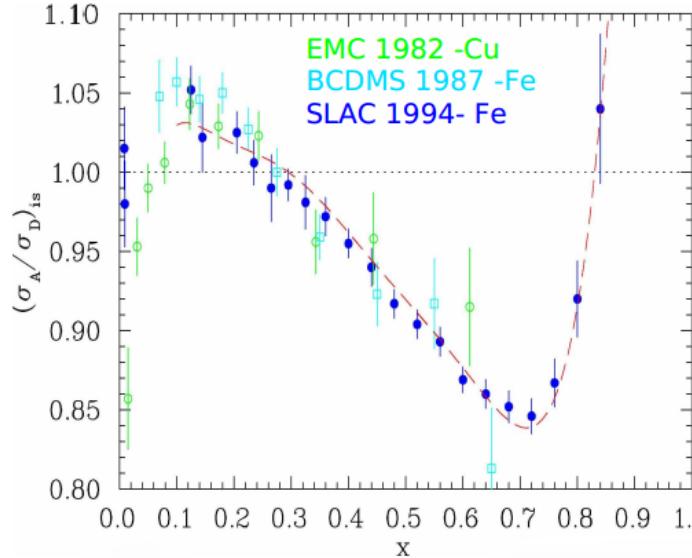
Figure 1.2: Graph of the ratio of A/D structure functions vs x for Carbon [10].



Ever since the European Muon Collaboration discovered the depletion of quarks at high x for $A > 2$ nuclei, physicists have tried to discover its cause. Scientists at SLAC extracted structure function ratios for many nuclei including; ${}^4\text{He}$, ${}^9\text{Be}$, ${}^{12}\text{C}$, ${}^{27}\text{Al}$, ${}^{40}\text{Ca}$, ${}^{56}\text{Fe}$, ${}^{108}\text{Ag}$, and ${}^{197}\text{Au}$. There were slightly different results for each nucleus. The magnitude of the EMC effect, taken to be the A/D ratio at $x = 0.6$, was found to be different for the various nuclei, and roughly scaled with the size or density of the nuclei. The NMC (New Muon collaboration), another group at CERN, gathered precise data in order to construct the inclusive cross section of deuterium and protons.

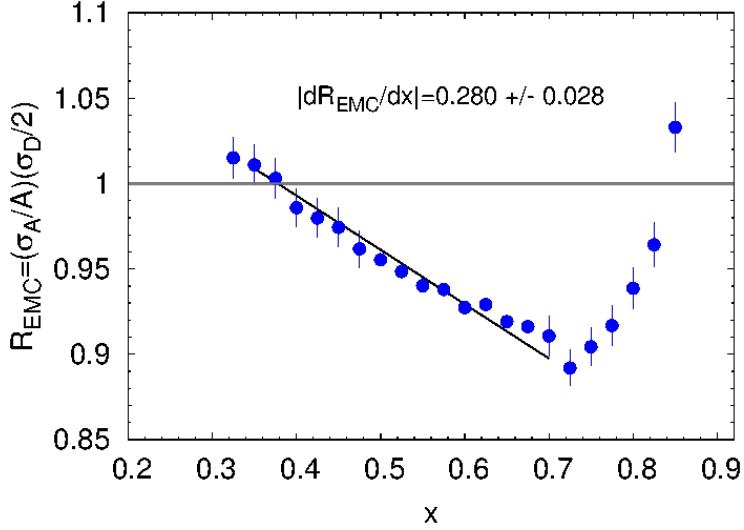
BCDMS collaboration extracted data for N and Fe structure function ratios. Figure 1.3 shows some of the data from SLAC and BCDMS on the EMC effect for Iron and Cu. Figure 1.4 shows this result from a recent JLab EMC measurement, most precise to date. Many models over the years have been able to reproduce the shape of the A/D ratios. These models can contain traditional nuclear physics effects like momentum distribution or pion-charge contributions. Some models also describe the EMC effect through quark momentum distribution or modification of the internal structure [17, 5, 2, 8, 9]. However, no single model has provided a complete picture of the possible underlying physics. Precise data from Jlab's E03-103 experiment has revitalized this research. This experiment focused on precision measurements in light nuclei and added ${}^3\text{He}$ as a target nucleus. Instead of taking the A/D ratio at a certain x -value to be the magnitude of the EMC effect, this analysis looked at the slope instead. This eliminated sensitivity to normalization uncertainties.

Figure 1.3: EMC effect from EMC, SLAC, and BCDMS [17]



In Figure , ${}^9\text{Be}$ was found not to follow the previously observed scaling with nuclear density. This result from Jefferson Lab determined that the previous idea

Figure 1.4: Graph of the ratio of A/D structure functions vs x for Carbon [10].



of a dependence on A or nuclear density in the EMC effect to be incorrect [20]. This result spawned a drive to determine another explanation for the EMC effect and understand what clue the ${}^9\text{Be}$ outlier was providing. The structure of this nucleus is made up of two high-density alpha particles and a single neutron [3]. The regions of higher density that are contained in a comparatively large volume may be able to explain why ${}^9\text{Be}$ does not follow the expected trend. This suggests that the EMC effect could be a function of local nuclear density [20].

1.3 MARATHON

Experiment E12-010-102, MARATHON (MeAsurement of the $F2^n/F_2^p, d/u$ RAtios and A=3 EMC Effect in Deep Inelastic Electron Scattering Off the Tritium and Helium MirOr Nuclei), will use deep inelastic scattering off of the mirror nuclei ${}^3\text{H}$ and ${}^3\text{He}$ to measure the EMC effect for both ${}^3\text{H}$ and ${}^3\text{He}$, to determine the ratio of the neutron to proton inelastic structure functions, and to find the ratio of the down to up quark distributions in the nucleon.

Chapter 2

Experimental Setup

2.1 Thomas Jefferson Lab

Thomas Jefferson Lab (Jlab) in Newport News, Virginia hosted the MARATHON experiment in the Fall of 2017 and Spring of 2018. Jlab uses support from the U.S. Department of Energy(DOE) and the state of Virgina to complete the lab's mission of delivering productive research by exploring the atomic nucleus and its fundamental constituents, including precise tests of their interactions. Along with applying an advanced particle accelerator, particle detectors and other technologies to develop new basic research capabilities and to address the challenges of a modern society.

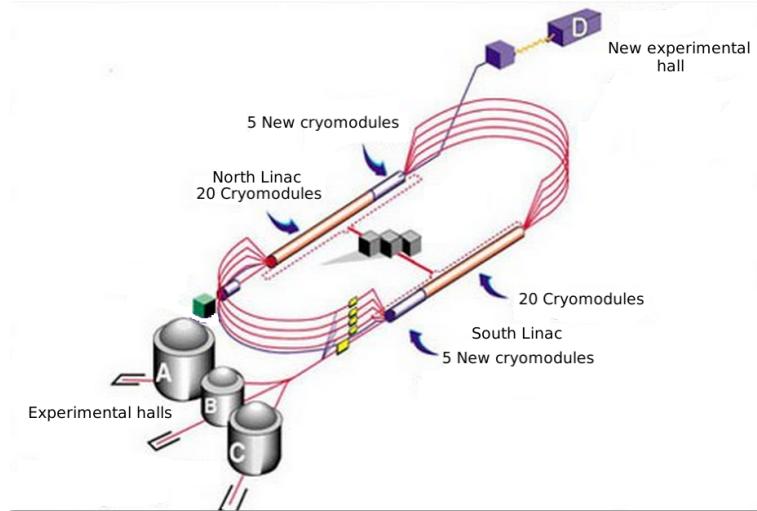
2.1.1 CEBAF

The Continuous Electron Beam Accelerator Facility (CEBAF) was recently upgraded to a 12 GeV accelerator, upgrading it to be able to supply a 11 GeV beam of continuous electrons of up to $200 \mu\text{A}$ of current to three experimental halls (A,B,C) and 12 GeV to the recently constructed hall D. After being accelerated to 45 MeV by a polarized electron gun or a thermionic injector, the electrons are injected into the North linear accelerator (LINAC), shown in figure 2.1. The polarized gun can supply electrons with up to 80% polarization and the polarization direction can be controlled

by a wien filter. To ensure the level of polarization, a 5 MeV Mott polarimeter may be used to measure the level of polarization[1].

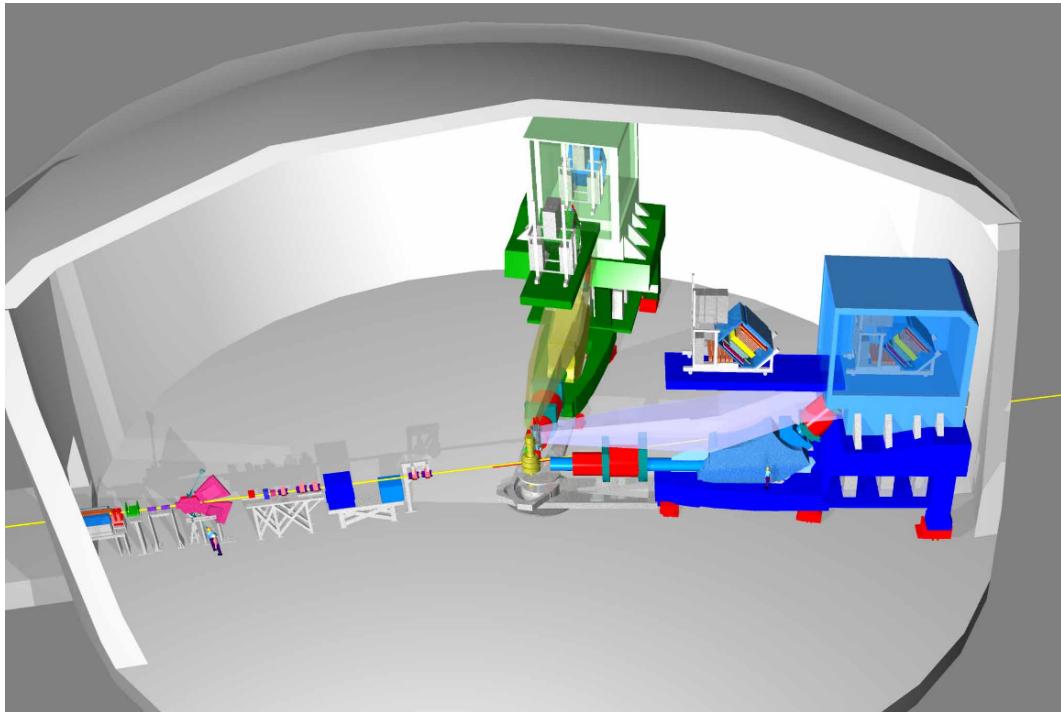
The electrons are conveyed through two LINACs and two bending arcs per complete pass of the accelerator. Electrons traveling to Halls A, B, and C complete a maximum of four and a half revolutions around the accelerator. Electrons going to all D travel through the north LINAC for an extra boost. These particles receive approximately 2.2 GeV in energy for each cycle through the accelerator. The radio frequency (RF) cavities in each LINAC use an oscillating electromagnetic field to supply a force to accelerate the passing electrons. These Niobium RF cavities are cooled to 2 K in order to create conditions that allow the cavities to be superconducting [1].

Figure 2.1: Schematic Layout of CEBAF.



2.1.2 Hall A

Figure 2.2: A 3D drawing of Hall A.

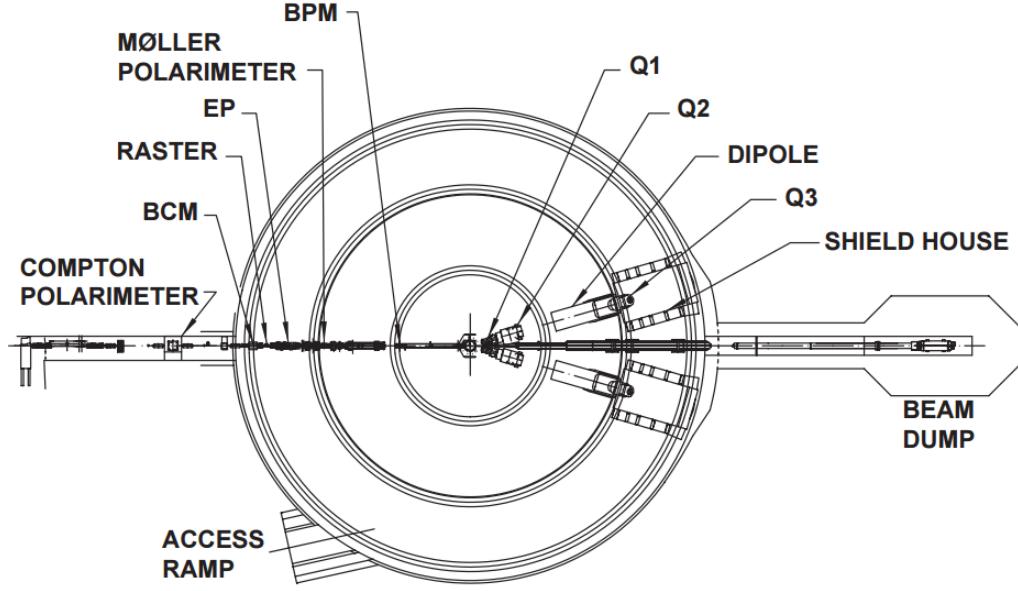


The experimental Hall A and the scientific equipment used were designed for detailed investigations of the internal structure of nuclei. Two high resolution spectrometers in Hall A use the inclusive (e, e') and exclusive ($e, e' p$) reactions to gain a greater understanding of the structure of the nucleus. Completing detailed studies with high resolution and extreme accuracy requires knowing the beam position, size, energy, current, direction, and polarization when the beam strikes the target. The instrumentation used in the precise measurement of these quantities in Hall A are shown in figure 2.3 [1].

A pair of Beam Position Monitors(BPM)s are used to measure the relative beam position without affecting the beam. The two Hall A BPMs are located at 7.524 m and 1.286 m away from the target. Using the standard difference-over-sum technique, the relative beam position is determined with an accuracy of $100 \mu\text{m}$ with a beam

current of at least $1 \mu\text{A}$ [1]. The BPMs' positional data is recorded in two ways. Every second of beam time, the beam position average over 0.3 seconds is logged into the Experimental Physics and Industrial Control System (EPICS) database. The BPMs also transmit data event-by-event to the CEBAF online Data Acquisition system(CODA).

Figure 2.3: A schematic layout of the beam line in Hall. [1]



The main beam line components of the BPMs consist of four open-ended antennas. Figure 2.4 shows a BPM chamber and figure 2.5 shows the layout of the four antennas as you look down the beam line. In this chamber, the design of three of the four antennas can be seen. The antennas are titled u_+ , u_- and v_+ , v_- . The antennas receive an induced signal as electrons pass to determine the beam position in the u and v directions. The direction of the beam is determined by using the two BPMs in conjunction with timing information provided. The accuracy of the BPMs requires an absolute measurement of the electron beam's position to calibrate the BPMs and a internal input oscillation measurement names twiddle to supply BPM signal coefficients. [19, 23].

Figure 2.4: BPM design diagram, from JLab instrumentation group. Beam direction is from left to right [23].

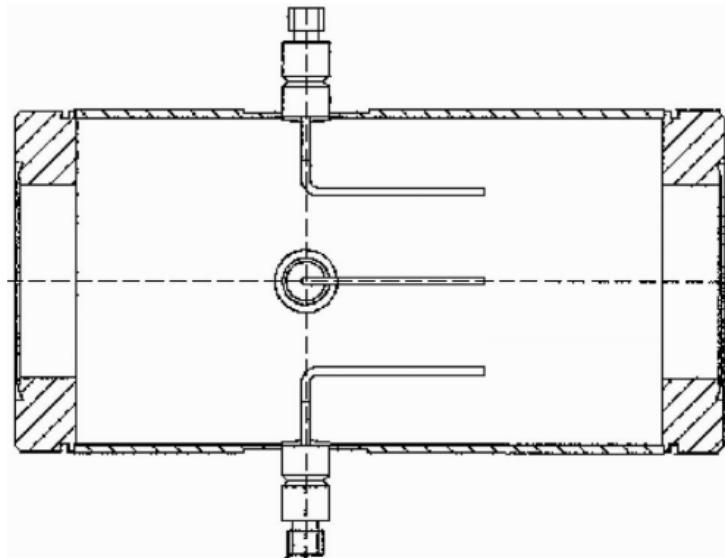
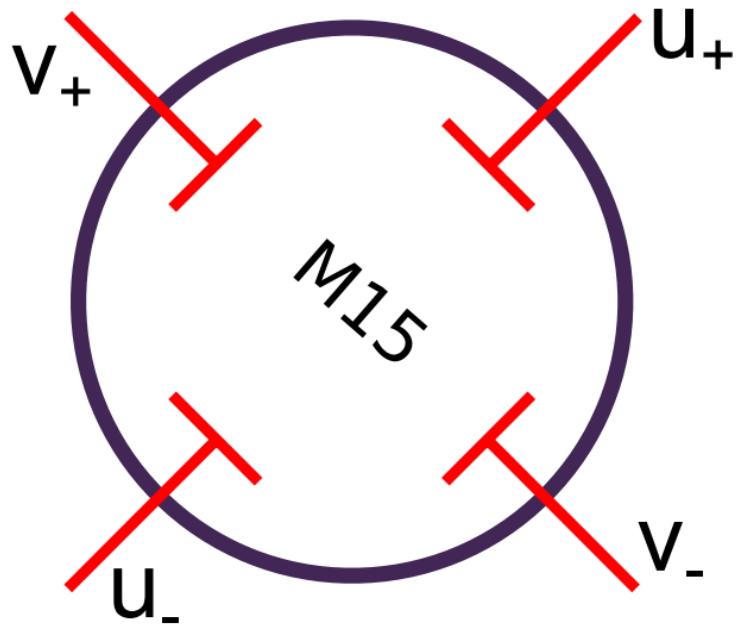


Figure 2.5: BPM design diagram, looking down the beam line[23].



Damage to a target system from intense beam can cause extreme fluctuations in the target's temperature and density. A raster was used to counteract the damage

caused by a focused beam. The raster used two magnetic fields produced by two dipoles to spread the electron beam out. This produces a large rectangle interaction area on the front face of the target container. A triangle wave of 25 kHz was used to control the coils of the dipole magnets. The raster systems are located \approx 17 meters before the target chamber (upstream of the target[23]). The rasters position can be seen in figure 2.2. Safety constraints administrated by the target group at JLAB limited the minimum size of the raster spot for the MARATHON experiment to two millimeters by two millimeters. This limit was installed has a safety concern for the tritium target.

The Hall A raster system consists of four dipoles. Two dipoles produce magnetic fields in the horizontal direction of the lab frame and two in the vertical. The upstream raster and downstream rasters include one vertical and one horizontal dipole. The relative change in position of the incoming electrons are controlled by the current supplied to the dipoles. In order to obtain the change in beam position due to the rasters, a calibration between the raster current and measured beam position were obtained.

The electron beam energy is located in many of the equations used in an electron scattering experiment. This can cause a noticeable increase in systematic error if the beam energy measurement is not made precisely. At JLAB for the MARATHON experiment, the beam energy was measured in two ways. In Hall A, the beam energy was measured by using the (e,e/p) method. On the beam line, 17 meters upstream from the target an ep scattering chamber is located. The beam was directed into the target containing a rotating 10-30 μm thick tape of CH_2 . The scattering angle of the electron and the recoil angle of the proton are used to determine the beam energy using equation 2.1. Where M_p is the mass of the proton and θ_p, θ_e are the scattered

angle of the proton, electron respectively.

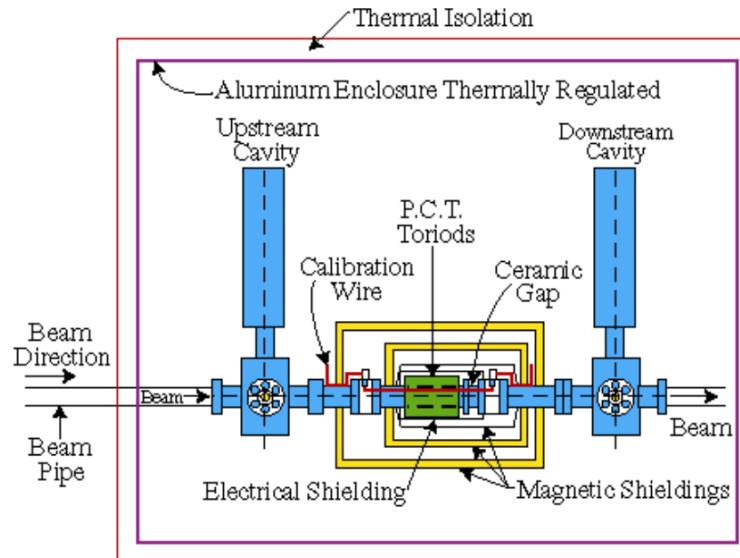
$$E = Mp \frac{\cos\theta_e + \frac{\sin\theta_e}{\tan\theta_p} - 1}{1 - \cos\theta_e} \quad (2.1)$$

The beam energy was also measured using the ark measurement method [7]. This method uses changes in beam position and precise measurements of the magnetic fields around the beam line to determine the energy of the electron beam. The angle at which the electrons are bent through is related to the momentum of the electrons,

$$p = k \frac{\int \vec{B} \cdot d\vec{l}}{\theta}. \quad (2.2)$$

In equation 2.2, p is the momentum of the electrons, θ is the bend angle, and \vec{B} is the magnetic field the electron experiences. Then using the momentum of the electron, the energy of the beam can be extracted. The error on the beam energy measurement is $\delta E/E \approx 2 * 10^{-4}$ [22, 7]. The MARATHON experiment used both methods to accurately determine the electron beam energy.

Figure 2.6: Hall A Current Monitor components [4].



The main process of measuring the scattering yield for a calculation of a cross section looks at finding the ratio of the number of electrons scattered to the number of electrons sent. In order to accurately determine the number of electrons sent to scatter with our target system, Hall A use a highly accurate and non-invasive beam current monitor(BCM). The Hall A BCM has an absolute accuracy of 0.2 percent as long as the current is between 1 and 180 μ A. The BCM used in Hall A consists of three main components: a Parametric Current Transformer (PCT) and two pill box cavities. Figure 2.6 shows the components in the Hall A BCM. The BCM produces an RF signal that is proportional to the beam current. An 10 kHz down converter, RMS-to-DC converter, voltage-to-Frequency converter, and a scaler are used to inject the current signal into the Hall A DAQ. Proportionality constants are determined in the calibration process to correctly integrate the charge for a given amount of beam current[4]. Continue after the initial beam line components, an electron will enter into the target chamber, housing the target system.

2.2 Target

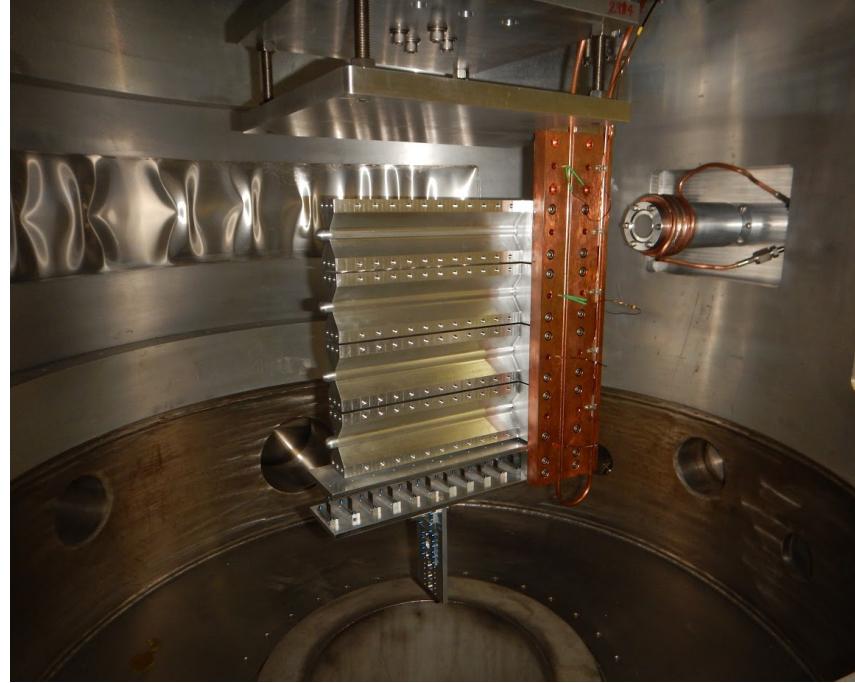
The Hall A Tritium Target(HATT) system was used for the Tritium run group of experiments. The HATT target chamber was repurposed from a previously used cryo-target chamber in order to reduce the financial cost of designing a new target chamber. The refurbishing of the cryo-target chamber consisted of adding in new safety features to prevent and mitigate a tritium leak. A 4 inch long collimator with an inner diameter of 0.4 inch was added inside of the target chamber but upstream of the target ladder to prevent the beam from striking the thin side wall of the aluminum cell. In case of a tritium leak in the target chamber, an exhaust system was installed to control the amount of tritium exposed to the Hall.[16] Figure 2.7 shows the HATT system with the target ladder in the home position and the scattering windows removed. A picture of the HATT ladder installed in the HATT system is shown if figure 2.7. The ladder contains both gaseous cells and solid targets. The MARATHON experiment had five

Figure 2.7: Target Images

(a) A image of the HATT. [11]



(b) Image of the Hall A Tritium Target Ladder. [11]



gas cells. The top four of the gas cells were filled with tritium, deuterium, hydrogen, and $^3\text{helium}$, from top to bottom respectively. Due to safety restricts the tritium cell was not installed until the HATT system could be closed. The bottom most cell was left empty, to complete end cap subtractions. The lower half of the target ladder contains the solid targets used during the MARATHON experiment. Listed from top to bottom, the solid targets used were a pair of thick aluminum foils, carbon multifoil, single carbon foil, and a carbon foil with a 2mm diameter hole. The thick Al foils were used to aid the target window background subtraction. The multifoil target also know has the optics target was used to calibrate the z-axis reconstruction of the optics matrix. The single carbon foil and carbon hole were used to calibrate the BPMs and rasters and to determine the off set of the central line of the detector.

2.3 High Resolution Spectrometers

Electrons that successfully scatter from the target may end up in either of the two HRSs(High Resolution Spectrometers). The HRSs were designed to detect charged particles with a high degree of precision. In order to achieve a high level of resolution in momentum and angle, the HRSs were designed with a magnet configuration of QQD_nQ (quadrupole, quadrupole, dipole, and quadrupole). The vertical bending dipole provides the field required to transport the scattered particles through the 45° bending angle to the detector hut. A drawing of an HRS can be seen in figure 2.8. The first quadrupole(Q1) focuses the incoming electrons in the vertical plane. The following two quadrupoles (Q2 and Q3 provide transverse focusing. This optical design allows the use of extended gas targets with no substantial loss in solid angle[1]. The spectrometers were designed to perform various functions which include: triggering the data acquisition system (DAQ) when certain requirements are met, gathering the position and direction of individual particles to reconstruct a track, provide precise timing information for time of flight calculations, and identify many different particle types that pass through the detector system. In order for both the Left HRS (LHRS) and Right HRS (RHRS) to complete the required task, they contain a myriad of detectors. The HRSs use drift chambers, scintillators, cerenkov detectors, and shower calorimeters. Both the Left and Right HRSs contain two planes of scintillators to function has the main trigger for the detector package. The vertical drift chambers (VDC) that lay at the front of the detector in conjunction with the Shower that lies in the back of the detector provide information for reconstructing the particle tracks and precise timing. Particles are identified by the cerenkov, shower calorimeters, and pion rejectors that are contained in the left or right HRS. The layout of the individual detectors that make up the left and right detector package are shown in figure 2.9 [1].

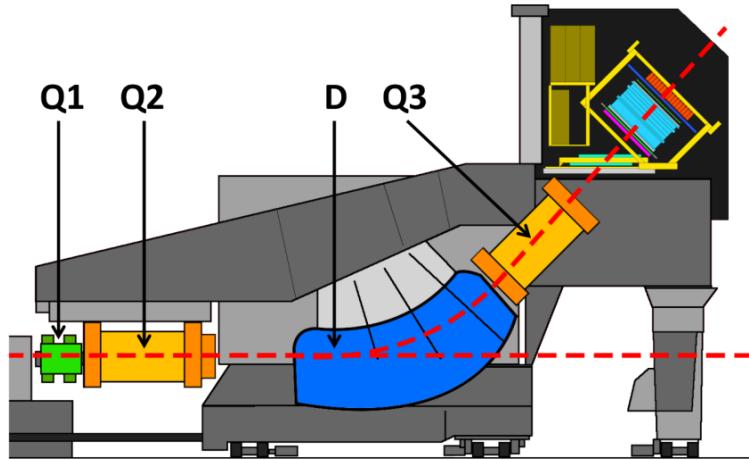


Figure 2.8: A side view of a HRS [1].

2.3.1 Vertical Drift Chambers

Each of the spectrometers housed in Hall A contains a vertical drift chamber(VDC). Each VDC contains two planes of crossing sense wires. Shown in figure 2.10, the two planes of the VDC lie a distance of 0.335m apart [6]. The lower plane of the VDC is positioned at the approximate focal plane of the HRS and lies in the horizontal plane of the Hall A coordinate system. The sense wires located in the VDCs cross orthogonally. They are offset by 45° in respect to the dispersive and non-dispersive directions.

[6]

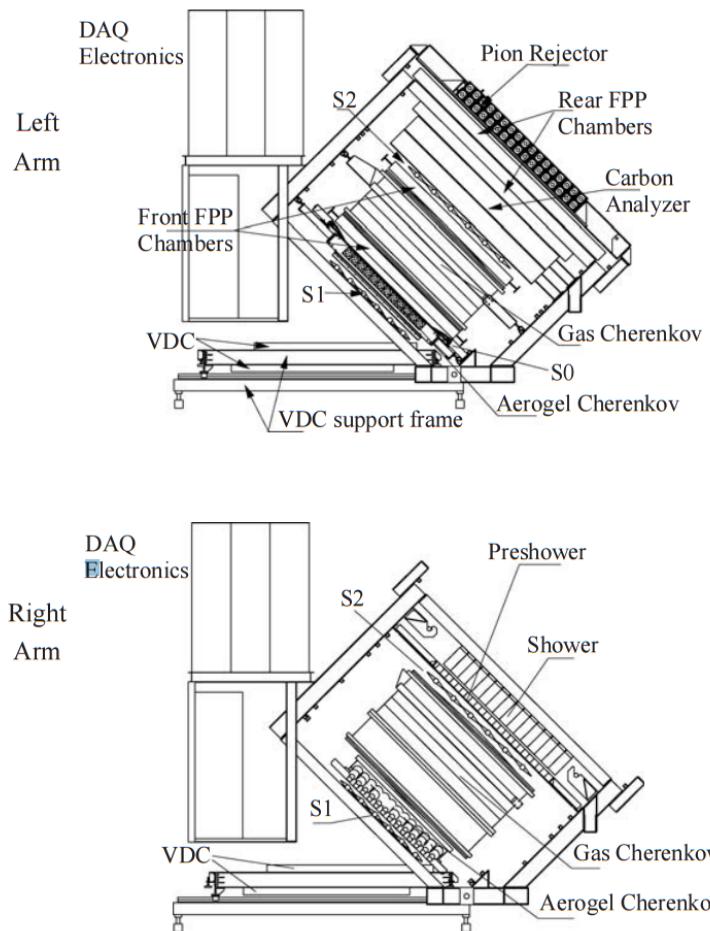


Figure 2.9: A view of both the left (top) and right (bottom) detector stacks inside the left and right HRS [1].

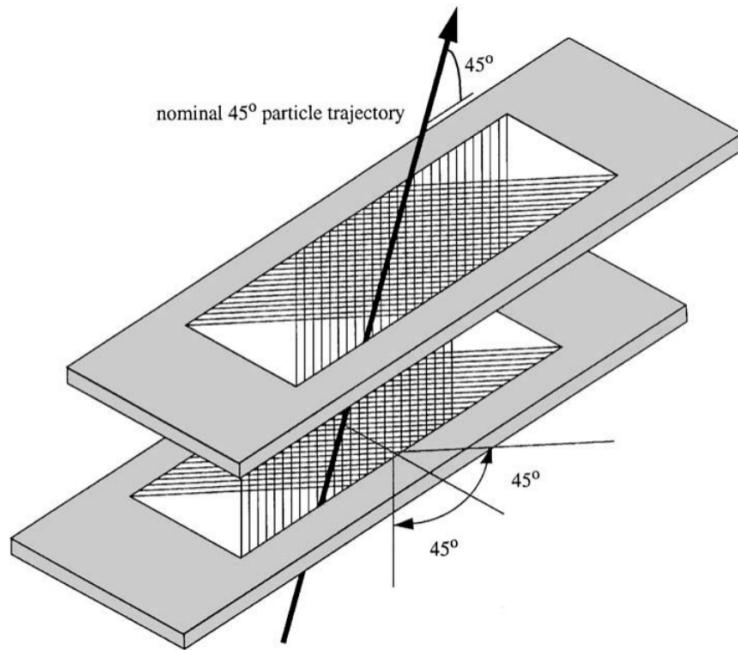


Figure 2.10: A sketch of the two VDC planes in the HRSs with a particle traveling through the detector at 45° .[6].

2.3.2 Scintillators

2.3.3 Cherenkov

2.3.4 Shower Calorimeter

2.3.5 Pion Rejector

2.3.6 FPP Chambers

2.4 Trigger Setup

2.5 DAQ - Data Acquisition System

2.6 Kinematic Settings

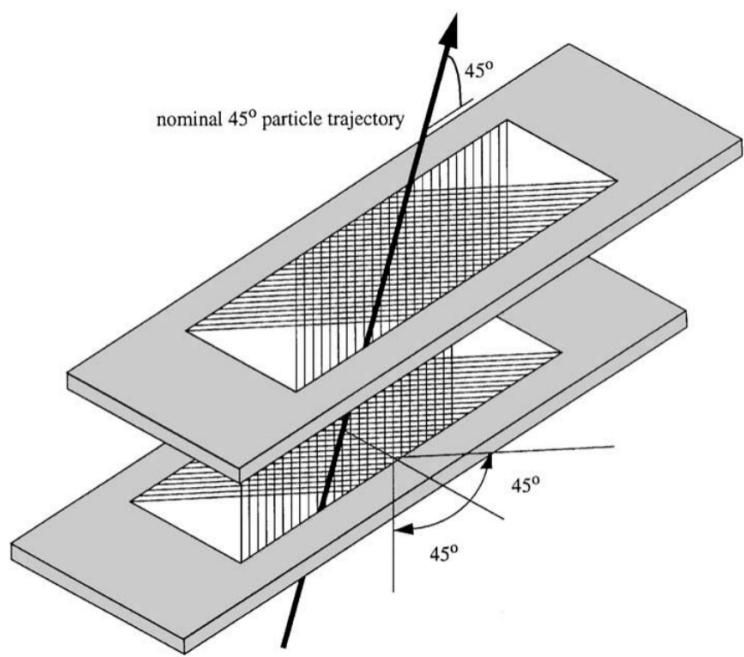


Figure 2.11: A sketch of the two VDC planes in the HRSSs with a particle traveling through the detector at 45° .[6].

Chapter 3

Calibration

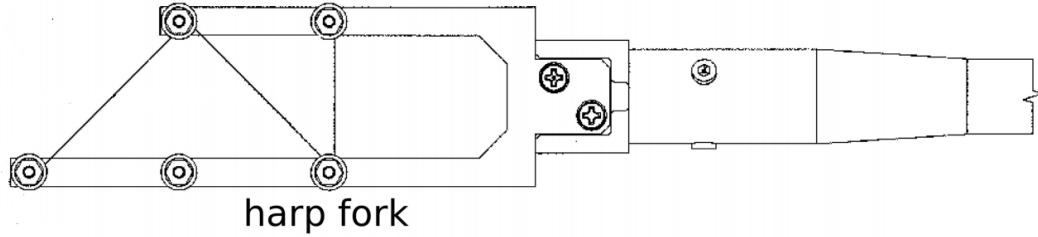
The information provided by the detectors originate through small changes in current and voltage sent through the DAQ electronics. These signals are transformed into useful information through calibration constants. The beam line elements and the individual detector components were calibrated to supply highly precise and accurate data.

3.1 Beam Line

The BPM signal coefficients are determined by a twiddle measurement. An RF module attached to the BPM antennas is used to pass a signal out of each of the antennas, one at a time. This will allow the determination of the conversion factor for the BPM signal to relative beam position. Two harps were used to provide the absolute measurement required for calibrating the BPMs. Figure 3.1 contains a drawing of the harps used in Hall A. The harps were moved into the beam line when calibration data is needed, but must be moved out for the production of experimental data because the harp wires are intrusive to the beam operation. The harp forks are aligned perpendicular to the beam line, to allow the harps to be moved in and out of the beam line. Three different wires are used to determine the horizontal and vertical position of the beam. Each wire has one of three orientations: vertical, sloped down

or sloped up. The two sloped wires are angled at 45° relative to the wire frame. As the harp fork is moved into the beam, the wires receive a signal as the beam interacts with the wires. The two sloped wires are used together to determine the vertical position of the beam. The vertical wire is used to determine the horizontal position of the beam [19, 23].

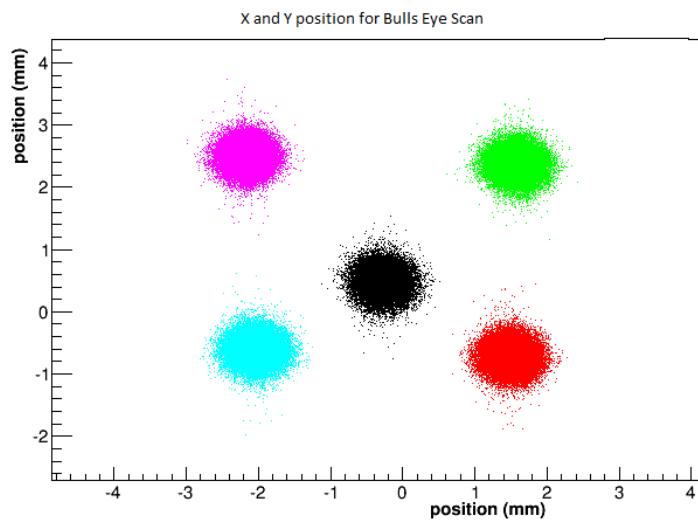
Figure 3.1: A schematic layout of a harp fork [23]



The location of the wires on the harp frame and the position of the harp fork were used to calculate the absolute beam position. The BPM calibration coefficients were determined by using a bulls eye scan, figure 3.2 shows an example of the five positions used to calculate the BPM calibration coefficients. The harp scan results are substituted into equation 3.1 for the X and Y positions. Using all five points and an R^2 regression technique, the coefficients can be determined with great accuracy. These highly accurate BPMs were crucial in reducing systematic error in the final results obtained from this experiment.

$$\begin{pmatrix} X_{position} \\ Y_{position} \end{pmatrix} = \begin{pmatrix} C(0, 0) & C(0, 1) \\ C(0, 0) & C(0, 1) \end{pmatrix} * \begin{pmatrix} X_{BPM} \\ Y_{BPM} \end{pmatrix} + \begin{pmatrix} X_{offset} \\ Y_{offset} \end{pmatrix} \quad (3.1)$$

Figure 3.2: The X and Y position for a Bulls eye scan for BPM calibration.



Chapter 4

Data Analysis

4.1 Efficiencies

The high resolution spectrometers are capable of detecting a myriad of particles that track through the detectors. The design of an experimental trigger uses the properties of the individual detectors to capture data of meaningful events. Many accidentals, background, and unwanted events trigger the data acquisition system, and some good electrons are missed by our DAQ. The removal of these unwanted events takes place during analysis via software cuts. Restricting the applicable signal from certain detectors through different cuts allows for the rejection of background particles and prevents contamination in the yield extraction.

4.1.1 Computer and electronic Lifetime

The signal from events that fire the DAQ travel through electronics like amplifiers and logic modules on its way to be recorded by the TDCs and ADCs. The processing of these signals require time at each stage. During that time another event will be discarded due to limitations in the hardware. This time when the DAQ system cannot handle another event is known as the dead-time of the system. Lifetime therefor is the percentage of time when an event can be recorded. The lost events need to be account

Livetime for each kinematic

Kin	1	2	3	4	5	7	9	11	13	15
LiveTime	0.947	0.969	0.981	0.986	0.992	0.996	0.997	0.998	0.998	0.998

Table 4.1: Livetime during the MARATHON experiment calculated using trigger 2.

for during the analysis process. The lifetime of the DAQ system for the MARATHON experiment was measured by determining the percentage of events that were recorded relative to the number of events that fired the corresponding trigger. The lifetime for the MARATHON experiment depended on the rate of events. The lifetime during the highest rate kinematic was determined to be 0.947, and climbs to 0.998 for the highest angle setting. Listed in table 4.1 are the calculated values for lifetime at each kinematic.

4.1.2 Particle Identification Efficiency

One of the largest sources of contamination for the MARATHON experiment are negatively charged pions. These pions are removed through software cuts made in the total signal from the ten cherenkov PMTs(photomultiplier tubes) and the energy deposited into the blocks of both layers of the calorimeter. Electrons can be identified by their behavior in the spectrometer. High-quality electrons will track through the entire detector stack to deposit most of their energy into the total calorimeter system and creating a large amount of light in the cherenkov. Though this knowledge tight cuts can be used to study the efficiency of the particle identification system. Plotting the signal in the cherenkov versus the energy deposited into both layers of the calorimeter allows for visual representation of the sampling cuts made in the efficiency studies, which can be seen in figure 4.1.

$$GE_{sample} = \text{Known electron sample from tight cut}$$

$$GE_{pass} = GE_{sample} \text{ and pass identification cut} \quad (4.1)$$

$$Electron_{eff} = \frac{GE_{pass}}{GE_{sample}}$$

Cherenkov sum versus Total Energy deposited

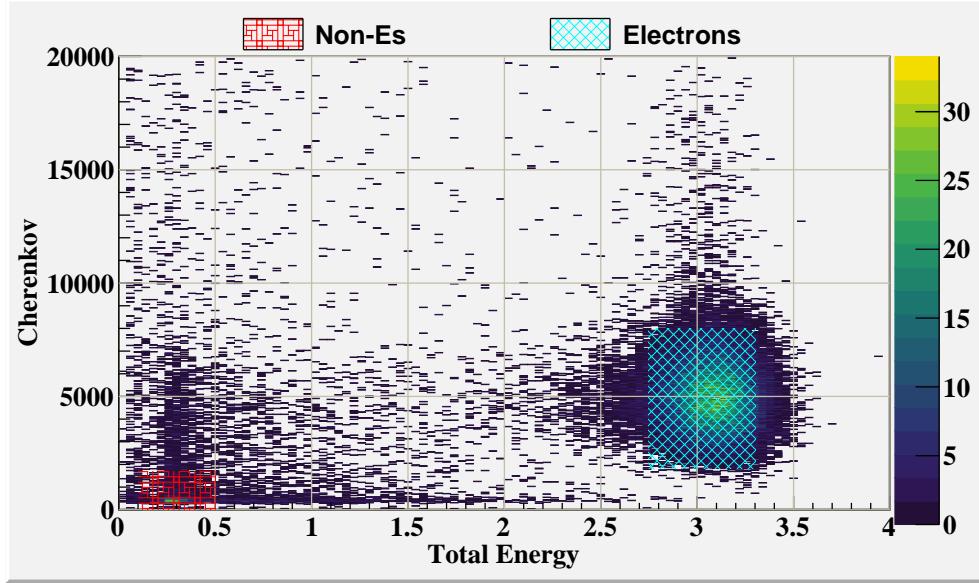


Figure 4.1: Two dimensional plot of the cherenkov sum versus Total Energy deposited, including electron sampling in teal and non-electron sampling in red.

The efficiencies of the spectrometer's particle identification(PID) detectors were determined by using the first calorimeter layer, the second calorimeter layer, and the cherenkov to provide samples of good electrons and other particles. The PID efficiency of the individual detectors was determined using equation 4.1. The good electron sample for calculating the efficiency of the single detector was defined by sampling through the other two detectors. Sampling through the two layers of the calorimeter is shown in figure 4.2a for the first layer of the calorimeter and 4.2b for the second layer. The cherenkov good electron sample is shown in figure 4.2c. The electron sample from the cherenkov is contaminated by delta particles and a combination of unknown particles. These unidentified background particles are known to be relativistic due to the amount of light seen in the cherenkov. However, the events do not deposit enough energy into the calorimeter system to be considered as a good electron that scatter from our target through the detector. Using sampling in one layer of the calorimeter

Particle ID and efficiency sampling for PID detectors

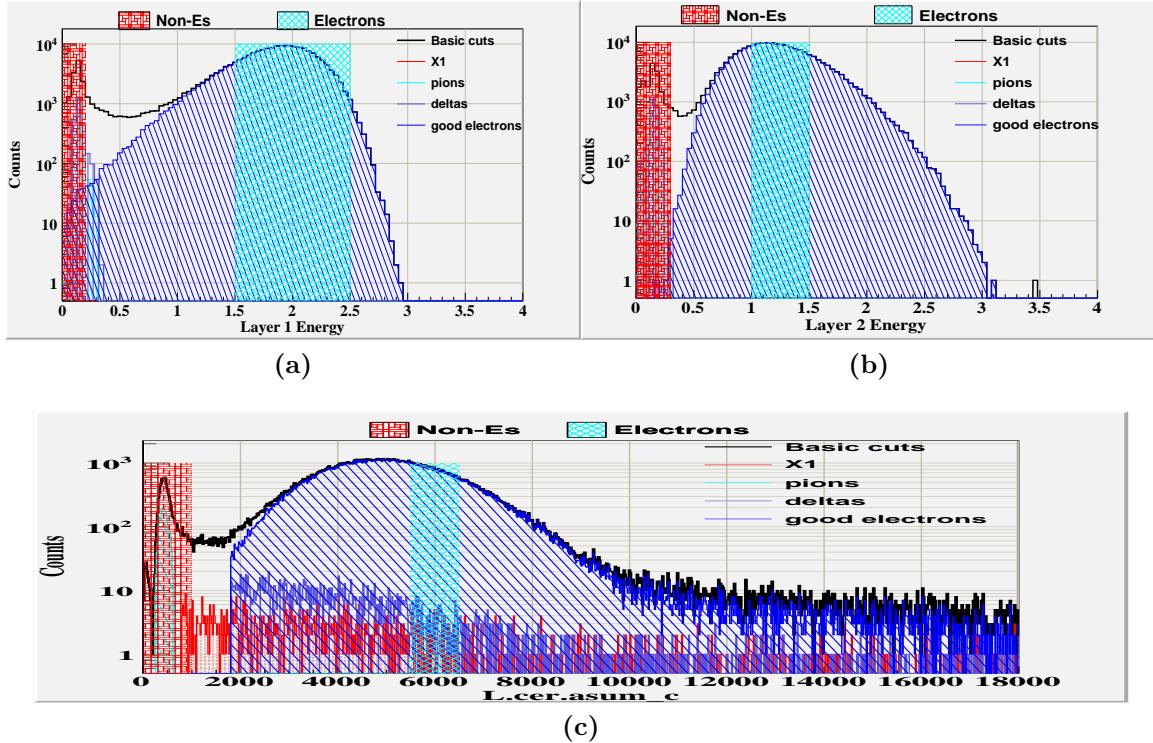


Figure 4.2: Electrons and other back ground particles identified via cuts in the total calorimeter and the gas cherenkov shown in the individual layers of the calorimeters and the cherenkov. Sampling cuts for Electrons in teal and Non-Electrons in red.

and the cherenkov, these unwanted low energy particles are rejected from sampling for efficiency calculations. The electron selection PID efficiency for the three PID detectors was determined at each kinematic setting to be approximately 98% . The efficiency was determined to be independent of the kinematic setting. Only small fluctuations were seen during the study, these small changes are due to decrease in statics, and all of the results fall within statical uncertainty of being independent of kinematic setting. The non-electron suppression efficiency was determined as part of this PID efficiency study to ascertain how many back ground particles leak into our sample of good electrons after cuts our made. The suppression efficiency of the cherenkov suffered due to the contamination of the relativistic low energy particles. Combining the two calorimeter detectors with the cherenkov increased the overall

PID efficiency for each detector for all kinematics.

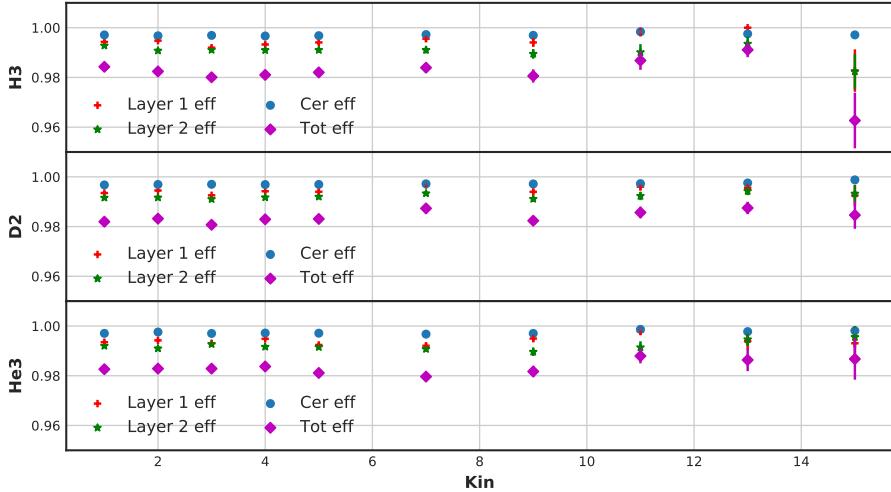


Figure 4.3: The PID efficiency for the cherenkov and both layers of the calorimeter,including the overall total PID efficiency for each of the gas targets at all of the kinematics.

suppression efficiency for the spectrometer to 99.9% over the entire kinematic range of the MARATHON experiment.

4.1.3 Trigger Efficiency

The process of capturing data from the two HRSs begins with the firing of a trigger. The trigger design for MARATHON focused on triggering for electrons and reducing the amount of other particles. Figure 2.11 describes the design of MARATHON's main trigger and efficiency triggers. MARATHON's main trigger, trigger 2, consist of a $(S_o \& S_2) \& Cer$. Due to inefficiencies of the electronics, logic, and detectors an event can produce a false trigger or a high quality electron may not fire the main trigger.

A low threshold in the cherenkov allows for an inclusive trigger limiting the overall number of quality electrons missed, but allows for a large quantity of false triggers. Software PID cuts prevent the contamination of false positives from trigger inefficiencies. The tight PID software cuts removes the false positive inefficiency

Trigger efficiency for the MARATHON experiment

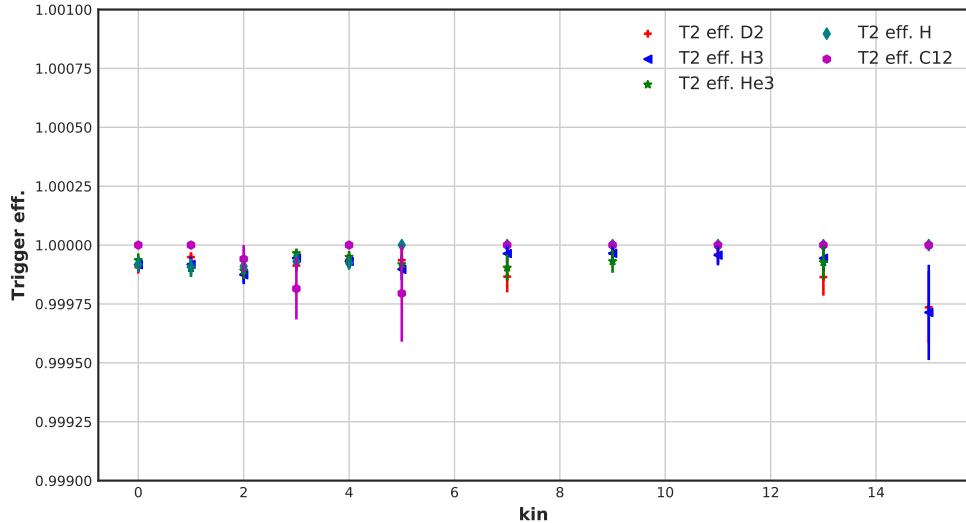


Figure 4.4: Trigger efficiency of trigger 2 for different targets at all kinematics calculated via sampling from trigger 1.

from the trigger design and is then considered in the PID efficiencies. The trigger inefficiency caused by missed high quality electrons was then calculated by sampling the high quality electrons in trigger 1, ($S_o \& S_2$). This ties the efficiency of trigger 2 with the performance of the scintillators. The efficiency of the two scintillating planes in conjunction is calculated by using sampling in trigger 3, ($S_o | S_2 \& Cer$) with strict PID cuts in both layers of the calorimeters and requiring a hit in the cherenkov. The two scintillator planes in conjunction have an efficiency greater than 99.7% for all kinematics. Combining the trigger efficiency of the main trigger shown in figure 4.4 with the performance of the scintillators give an over all efficiency for the trigger of the MARATHON experiment of greater than 99.6%.

4.1.4 Tracking Efficiency

Particles that travel through our detector could originated from sources wanted or unwanted. In order to control the source of the scatter electrons, we use a particle's track to identify its source. The signals received via the VDC is used to produce

Tracking efficiency for the MARATHON experiment

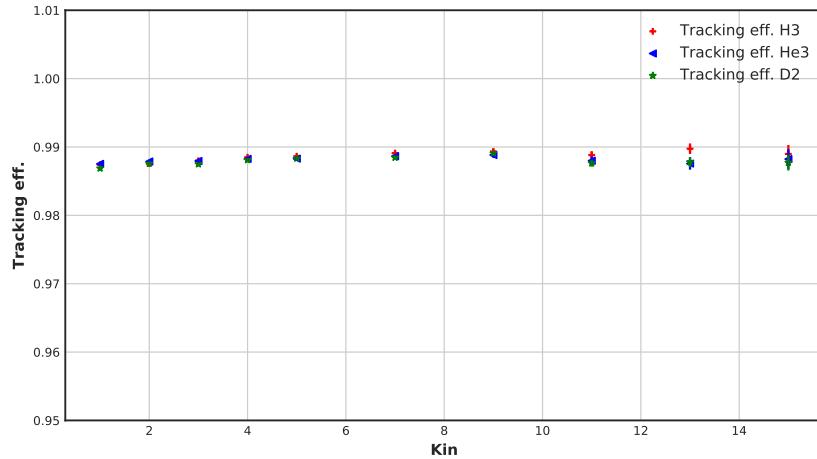


Figure 4.5: Tracking efficiency of the VDCs for different targets at all kinematics.

a particles track from the target to end of the spectrometer. The largest source of inefficiency for the VDCs are incorrectly identified tracks. High quality electrons that transverse the spectrometer should only have one good track, calculated via the tracking package in the analysis software. The capability of the VDCs to determine a good electron event's one good track is known as the one track efficiency for the VDCs. Quantitatively the one track efficiency (ϵ_{VDC}) can be obtained via:

$$\epsilon_{VDC} \equiv \frac{N_{1track}}{N_{0\&multitrack}} \quad (4.2)$$

Where the number of good electron events that have one good track is defined as N_{1track} , and $N_{0\&multitrack}$ are the good electron events that have not been assigned a good track or have more than one good track associated with that event. The good electron selection is made via PID cuts in the calorimeter and cherenkov, and cuts in the ADC and TDC of the scintillators. Direct cuts in the signal of the scintillators were made to include the nominal acceptance cuts, which were produced through tracking software. The tracking efficiency of HRSs during the MARATHON experiment is shown in figure 4.5 for the three gas targets during all kinematic ranges. The efficiency of the VDCs is not relative to the angle of the spectrometer. So the

uniform tracking efficiency across all kinematics is expected and helps eliminate any concerns of the performance of the VDCs during the experiment.

4.2 Background Subtraction

The purpose of this analysis is to study the DIS cross sections of deuterium, helium-3, and tritium. The sample of scattered events used to determine the cross section of a given nuclear then needs to be cleaned of any contamination produced from other targets and processes. The electrons detected by the spectrometers can be electrons that scattered from our chosen target, scattered from a source other than our target, or produced through process other than DIS scattering. The two sources of contamination for the MARATHON experiment are events scattered from the aluminum end caps of the target cell and pair produced electrons via photon interaction.

4.2.1 End Caps

The target cells used during the MARATHON experiment are shown in figure 2.7. The cells are filled with gaseous version of the chosen nuclear target.

4.2.2 Pair Produced Electrons

Chapter 5

Results

Chapter 6

Simulation

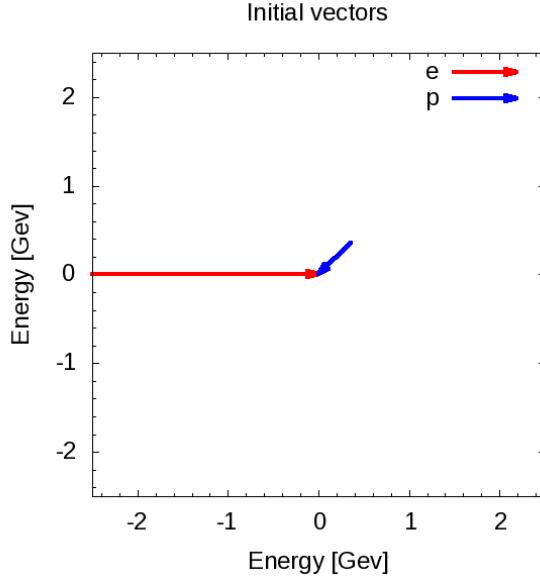
Nuclei are systems of nucleons that interact strongly. The characteristic scale for the nucleons momentum is approximately the Fermi momentum, $k_F \approx 200 - 270 \text{ MeV}/c$ [9]. However because of the strongly repulsive nature of the nucleon-nucleon interaction at short distances prevents two nucleons from laying in close proximately to each other. This strong interaction demands the presence of high-momentum components in the nuclear ground state wave function. A simulation was designed to phenomenologically study the effect of these high-momentum components on the nuclear EMC effect. This program was designed in two phases. The first phase used simple elastic scattering and a single value for the targets momentum to investigate overall effect of different target momentum on the yield in bins of x_B . The second phase of the simulation was created to lay out the effect of using different momentum distributions on the yield for the EMC effect region of x_B , 0.3 to 0.7.

6.1 Investigation

This simulation phenomenologically investigates the effect of a moving target on the EMC effect by scattering a beam of electrons off of a moving proton. The target protons are comprised of a directional vector of 0° to 360° in respect to the incoming electron beam and a momentum between 0 and 1 GeV/c. Figure 6.1 contains a

possible event for the simulation. The electron approaches with 2.5 GeV of energy and collides with a proton moving with a momentum of 0.5 GeV/c with an angle of 45° in respect to the electron trajectory.

Figure 6.1: Example of the electron beam(red) with a energy of 2.5 GeV and the proton(blue) with angle of 45° in respect to the electron and with a momentum of 0.5 GeV/c.



Using conservation of momentum and conservation of energy in elastic collisions, this simulation calculates the final state of the electron and proton after the scattering event by randomly selecting a scattered direction for the electron. The vector representation of the scattered products are shown in figure 6.3a. In order to make these calculations systematic and to study cross sections models the simulation transform each event into the rest frame of the target before scattering.

6.2 Transformation

The Simulation completes a set of Lorentz invariant rotations and boost for each event to transform the lab frame of the electron and proton collision into the rest frame of the proton. First the simulation takes the initial proton and electron vectors

and rotates them to align the proton vector to the horizontal axis, shown in figure 6.2b. This rotation uses the angle between the proton and the electron defined as λ . This allows for a straight forward calculations for the Lorentz factors β and γ and to boost into the rest frame of the target proton, figure 6.2c. Once in the boosted frame, the angle between the electron and the horizontal axis is defined as δ . Right before the simulation starts to calculate the scattered products, it completes one more rotation to align the electron vector with the horizontal axis, figure 6.2d, to make the scattering calculation systematic and unconditional.

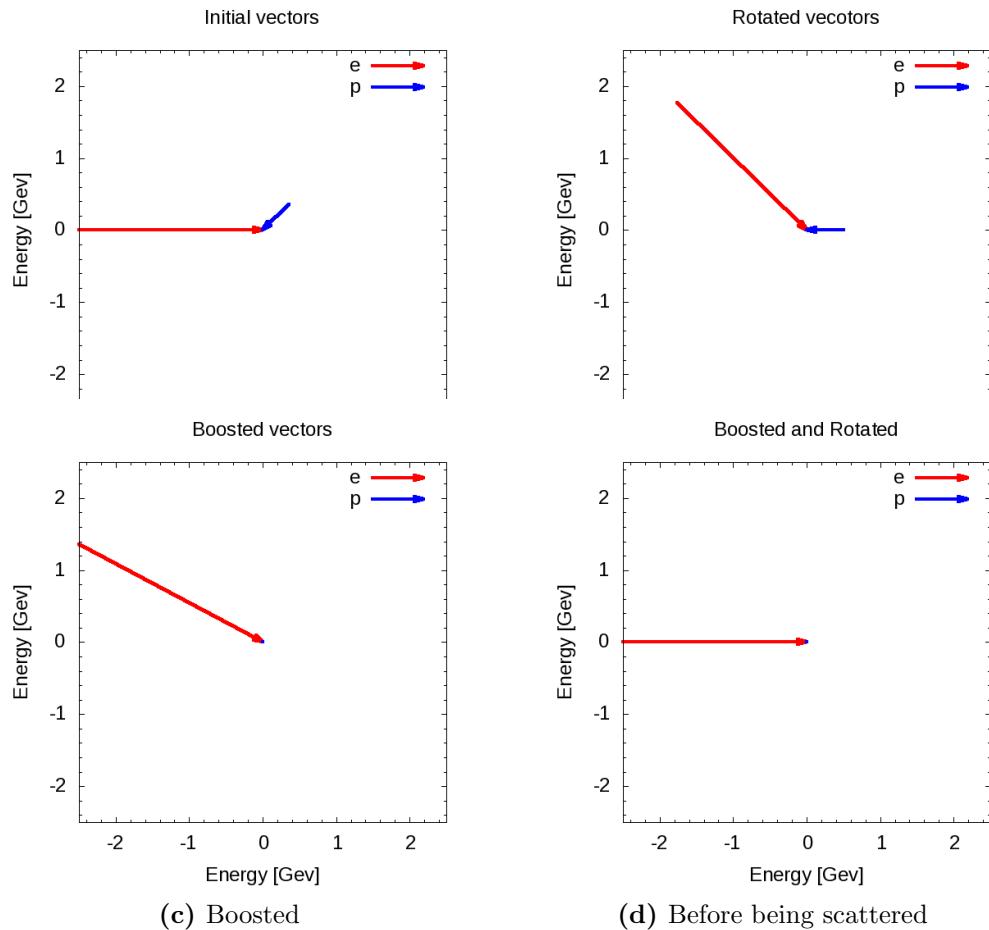


Figure 6.2: Vector representations of the momentum for the incoming electron(red) and target proton(blue) with units of GeV for each phase of their transformations before scattering.

In order to gain a more complete understanding of the scattering products, the program completes a set of transformations to move from the rest frame of the target proton to the beginning lab frame. After the simulation calculates the scattered products it begins to transform back by beginning with a rotation by the angle δ , figure 6.3b. Followed by the inverse of the previously used Lorentz boost. The last transformation, a rotation by λ , transforms the frame back into the lab frame. A proton vector and electron vector in the lab frame are the final products of the simulation. An image of the electron and proton vectors for each transformation can be found in figure 6.3. These vectors allow for calculation of kinematic variables such as Bjorken x and the four-momentum transfer (Q^2). This simulation will complete these steps for many electron and proton combinations.

6.3 Results

This electron scattering simulation produced results for two stages. The firsts stage used a fix proton momentum for each run to compare the yield in bins of x_B . Figure 6.4 shows the results for three different runs, each having a unique fixed proton momentum. The red histogram represents a run with a proton momentum of 0 Gev/c. The result is an elastic peak at x_B of one. The blue histogram contains the results having a fixed proton momentum of 0.25 GeV/c. Increasing the initial momentum of the proton spreads the events into two peaks. The scattering interactions that form the peak above 1 x_B are produced by events were the proton's initial directional vector are orientated towards the electron. The events that produce an x_B below 1 have a proton direction pointing away from the electron initially. Doubling the proton's initial momentum from 0.25 GeV to 0.50 GeV causes these peaks two spread out furtherer in x_B .

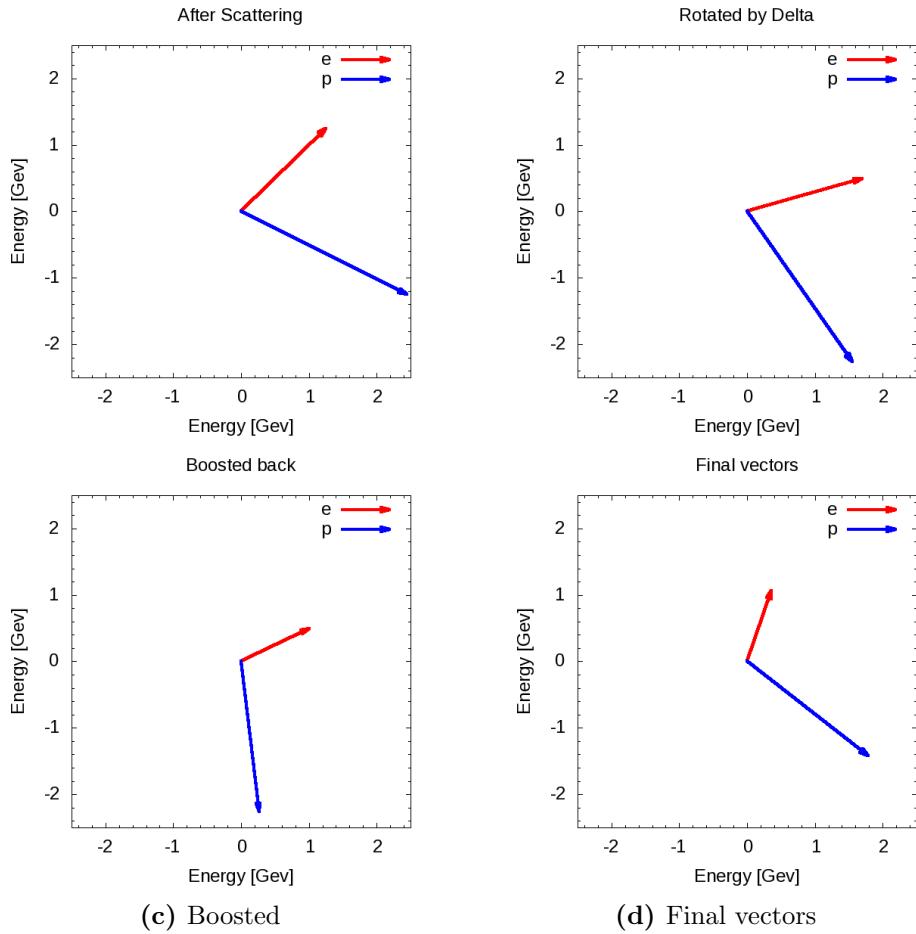
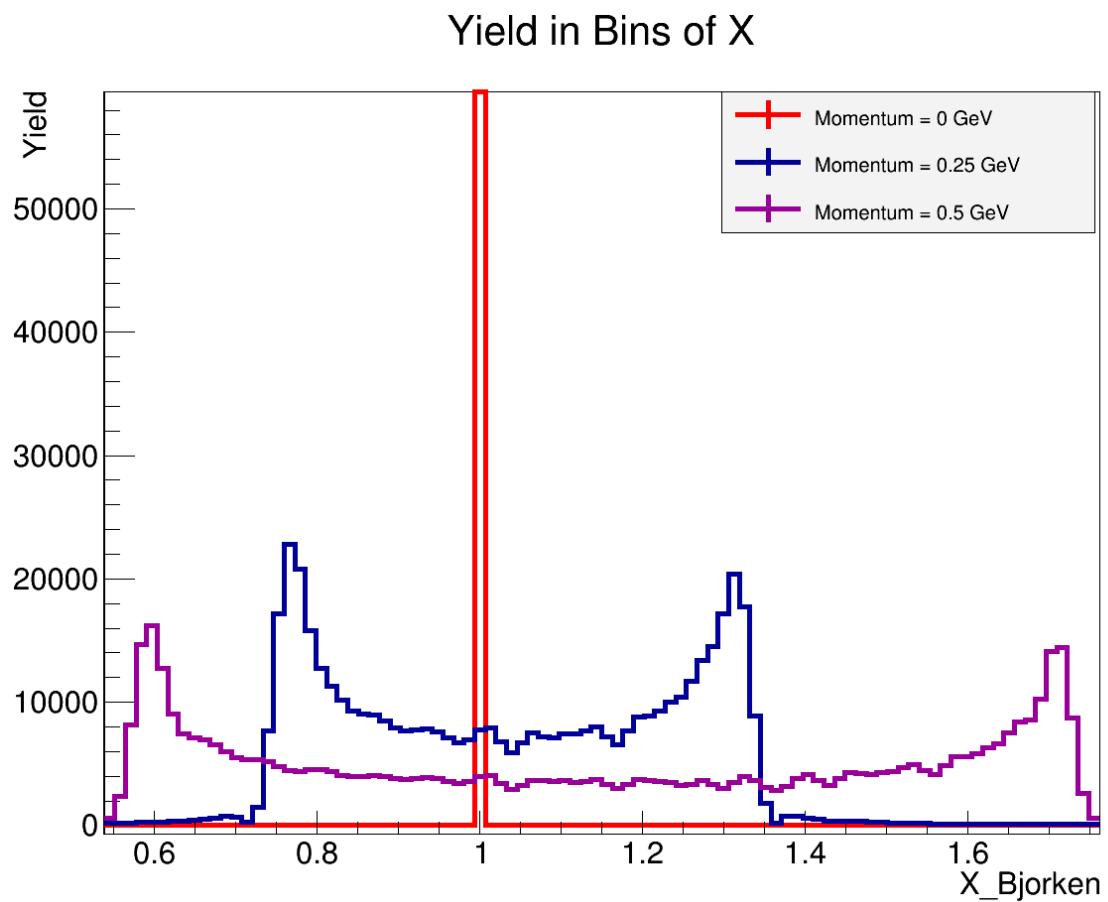


Figure 6.3: Vector representations of the momentum for the incoming electron(red) and target proton(blue) with units of GeV for each phase of their transformations after scattering).

Figure 6.4: Simulation results for fixed momentum protons. Three runs with unique proton momentum.



Chapter 7

Conclusion

Bibliography

Bibliography

- [1] J. Alcorn et al. Basic Instrumentation for Hall A at Jefferson Lab. *Nucl. Instrum. Meth.*, A522:294–346, 2004. [vi](#), [11](#), [12](#), [13](#), [19](#), [20](#), [21](#)
- [2] John Arrington, Aji Daniel, Donal Day, Nadia Fomin, Dave Gaskell, and Patricia Solvignon. A detailed study of the nuclear dependence of the EMC effect and short-range correlations. *Phys. Rev.*, C86:065204, 2012. [8](#)
- [3] A. Daniel, J. Arrington, and D. Gaskell. Measurements of the EMC effect in few-body nuclei at large x. *AIP Conf. Proc.*, 1369:98–105, 2011. [9](#)
- [4] J. Denard and J. Sahar. High accuracy beam current monitor system for cebaf’s hall a. Chicago, 2001. Particle Accelerator Conference. [vi](#), [16](#), [17](#)
- [5] J. Edelmann, G. Piller, Norbert Kaiser, and W. Weise. Resonances and higher twist in polarized lepton nucleon scattering. *Nucl. Phys.*, A665:125–136, 2000. [8](#)
- [6] K.G. Fissum et al. Vertical drift chambers for the hall a high-resolution spectrometers at jefferson lab. *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment*, 474(2):108 – 131, 2001. [vi](#), [20](#), [22](#), [23](#)
- [7] David J. Flay. *Measurements of the Neutron Longitudinal Spin Asymmetry A1n and Flavor Decomposition in the Valence Quark Region*. PhD thesis, Temple University, Philadelphia, PA, Aug 2014. [vi](#), [2](#), [3](#), [16](#)

- [8] D.F. Geesaman, K Saito, and A Thomas. The nuclear emc effect. *Annual Review of Nuclear and Particle Science*, 45(1):337–390, 1995. [8](#)
- [9] J. Gomez et al. Measurement of the A-dependence of deep inelastic electron scattering. *Phys. Rev.*, D49:4348–4372, 1994. [8, 36](#)
- [10] D. Higinbotham. The emc effect still puzzles after 30 years - cern courier. <http://cerncourier.com/cws/article/cern/53091>, April 2013. (Visited on 01/04/2016). [vi, 2, 7, 9](#)
- [11] Doug Higinbotham. Target images, December 2017. [18](#)
- [12] R Hofstadter. Nuclear and nucleon scattering of high-energy electrons. *Annual Review of Nuclear Science*, 7(1):231–316, 1957. [4](#)
- [13] Henry W. Kendall. Deep inelastic scattering: Experiments on the proton and the observation of scaling. *Rev. Mod. Phys.*, 63:597–614, Jul 1991. [6](#)
- [14] Simona Malace, David Gaskell, Douglas W. Higinbotham, and Ian Cloet. The Challenge of the EMC Effect: existing data and future directions. *Int. J. Mod. Phys.*, E23:1430013, 2014. [6](#)
- [15] R. W. McAllister and R. Hofstadter. Elastic scattering of 188-mev electrons from the proton and the alpha particle. *Phys. Rev.*, 102:851–856, May 1956. [2](#)
- [16] David Meekings. Hall a tritium target, 2017. [17](#)
- [17] P R Norton. The emc effect. *Reports on Progress in Physics*, 66(8):1253, 2003. [vi, 8](#)
- [18] Bogdan Povh, Klaus Rith, Christoph Scholz, and Frank Zetsche. *Particles and Nuclei: An Introduction to the Physical Concepts*. Springer, 2009. [1, 2, 4, 5, 6](#)
- [19] Tom Powers, Lawrence Doolittle, Rok Ursic, and Jeffrey Wagner. Design, commissioning and operational results of wide dynamic range bpm switched

electrode electronics. *AIP Conference Proceedings*, 390(1):257–265, 1997. [13](#), [25](#)

- [20] J. Seely et al. New measurements of the european muon collaboration effect in very light nuclei. *Phys. Rev. Lett.*, 103:202301, Nov 2009. [2](#), [9](#)
- [21] Richard E. Taylor. Deep inelastic scattering: The early years. *Rev. Mod. Phys.*, 63:573–595, Jul 1991. [6](#)
- [22] Hall A Tech. Ep method. http://hallaweb.jlab.org/equipment/beam/energy/ep_web.html. (Accessed on 06/28/2016). [16](#)
- [23] Pengjia Zhu et al. Beam Position Reconstruction for the g2p Experiment in Hall A at Jefferson Lab. *Nucl. Instrum. Meth.*, A808:1–10, 2016. [vi](#), [13](#), [14](#), [15](#), [25](#)

Appendix