

# Computational Tool for Optimal Expansion of Transmission Networks

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JUAN LUIS BARBERÍA, MARIANO TOMAS ANELLO, ALBERTO DEL ROSSO

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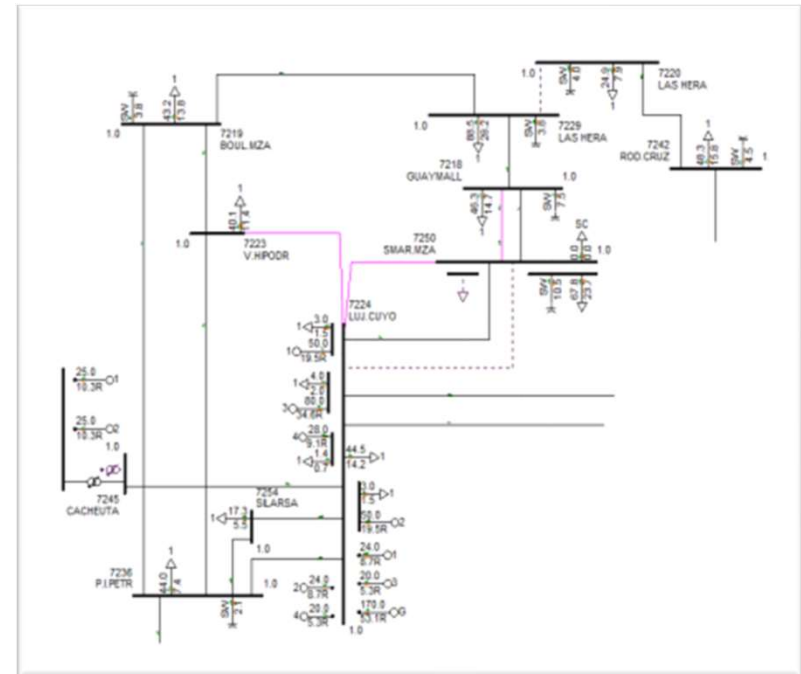
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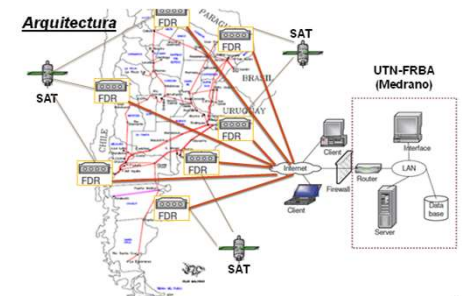


# About us

Investigation group since 2004

Universidad Tecnológica  
Nacional, Fac. Buenos Aires

Methodologies and tools for  
transmission expansion planning

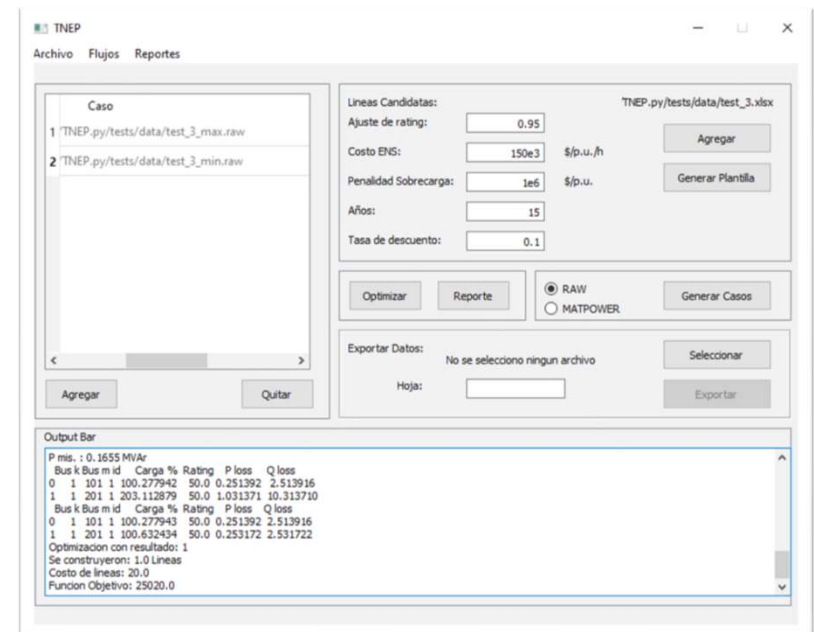


# Motivation: TNEP.py

Computational tool for  
transmission system expansion

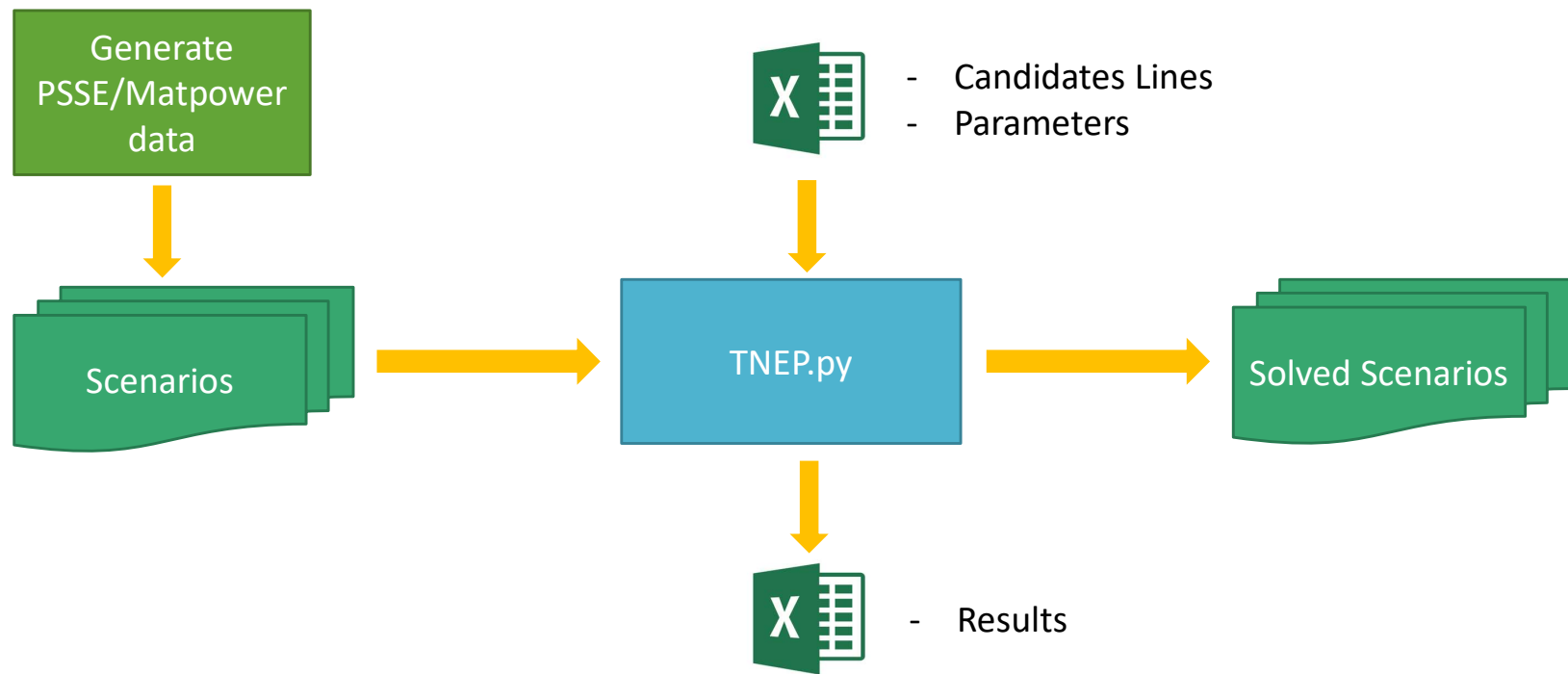
Requirements:

- Easy to use
- Handles multiples load scenarios
- Integration with other tools

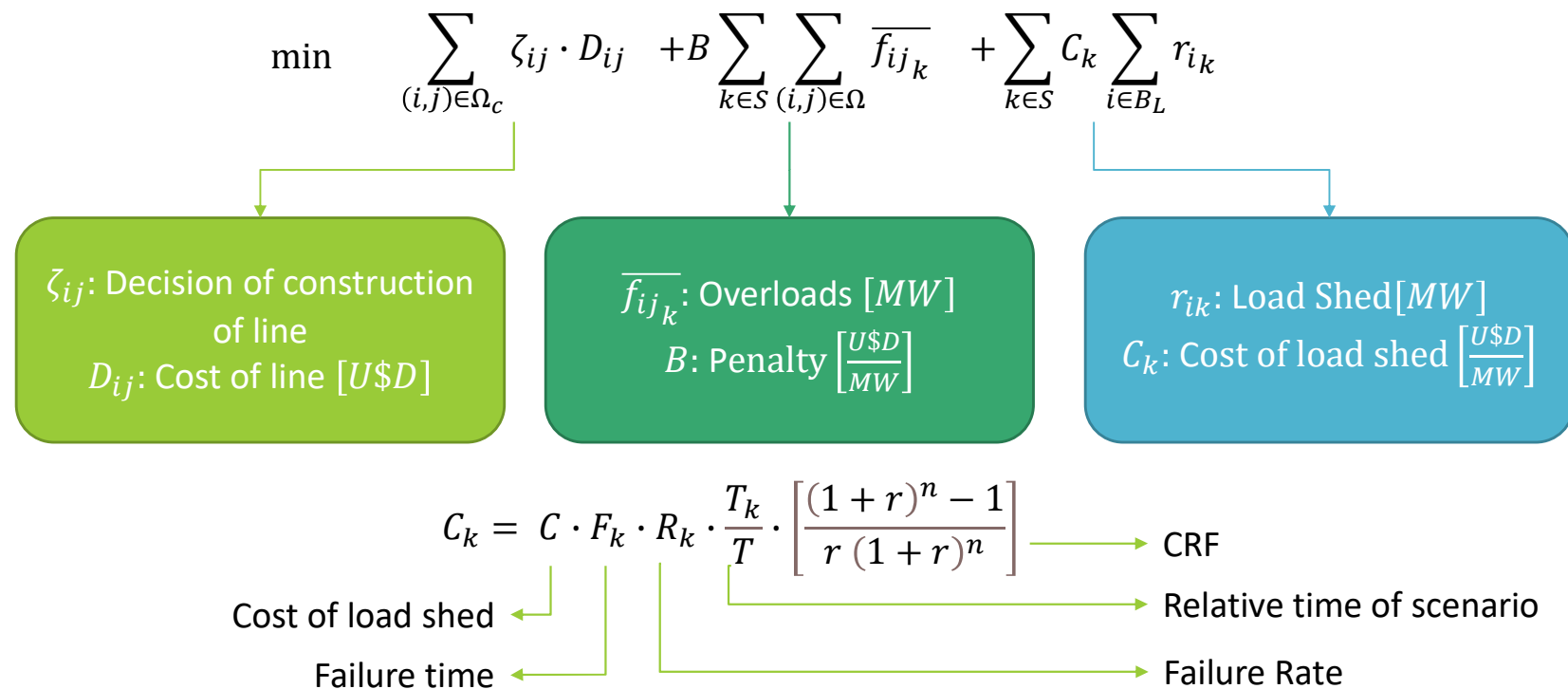


# Description: Workflow

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# Problem description: Transmission Network Expansion Planning



# Problem description: Transmission Network Expansion Planning

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$$\min \sum_{(i,j) \in \Omega_c} \zeta_{ij} \cdot D_{ij} + B \sum_{k \in S} \sum_{(i,j) \in \Omega} \overline{f_{ij_k}} + \sum_{k \in S} C_k \sum_{i \in B_L} r_{i_k}$$

subject to:

$$p_{i_k} - d_{i_k} + r_{i_k} - \sum_{(i,j) \in \Omega_i} f_{ij_k} = 0, \quad i \in B$$

$$f_{ij_k} = -b_{ij}(\theta_{i_k} - \theta_{j_k}), \quad (i,j) \in \Omega \setminus \Omega_c$$

$$|f_{ij_k} + b_{ij}(\theta_{i_k} - \theta_{j_k})| \leq (1 - \zeta_{ij})M, \quad (i,j) \in \Omega_c$$

$$|f_{ij_k}| \leq f_{ij}^{max} + \overline{f_{ij_k}}, \quad (i,j) \in \Omega_m, \quad k \in S$$

$$|f_{ij_k}| \leq \zeta_{ij} f_{ij}^{max} + \varphi_{ij_k}, \quad (i,j) \in \Omega_c$$

$$|\varphi_{ij_k} - \overline{f_{ij_k}}| \leq (1 - \zeta_{ij})M, \quad (i,j) \in \Omega_c$$

$$|\varphi_{ij_k}| \leq \zeta_{ij}M, \quad (i,j) \in \Omega_c$$

Physical Constraints

Engineering Constraints

# Problem description: Transmission Network Expansion Planning

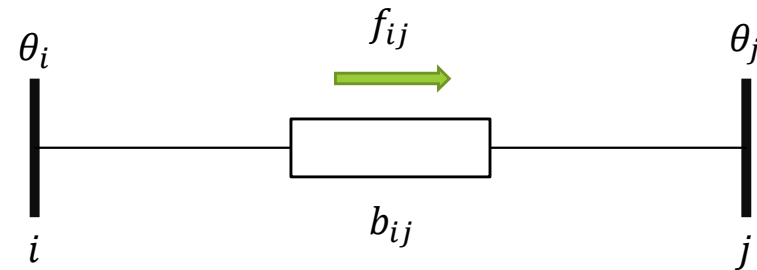
How to handle build decision variables

$\zeta_{ij} = 1 \Rightarrow$  Build Line

$$|f_{ij_k} + b_{ij}(\theta_{i_k} - \theta_{j_k})| \leq \cancel{(1 - \zeta_{ij})} M$$

$$|f_{ij_k} + b_{ij}(\theta_{i_k} - \theta_{j_k})| \leq 0$$

$$f_{ij_k} = b_{ij}(\theta_{i_k} - \theta_{j_k})$$

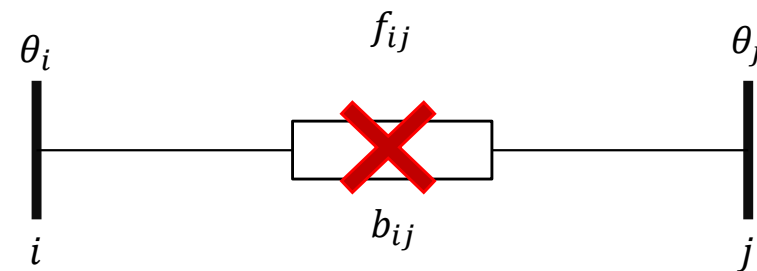


$\zeta_{ij} = 0 \Rightarrow$  Not build

$$|\varphi_{ij_k}| \leq \cancel{\zeta_{ij}} M$$

$$|f_{ij_k}| \leq \cancel{\zeta_{ij}} f_{ij}^{max} + \varphi_{ij_k}$$

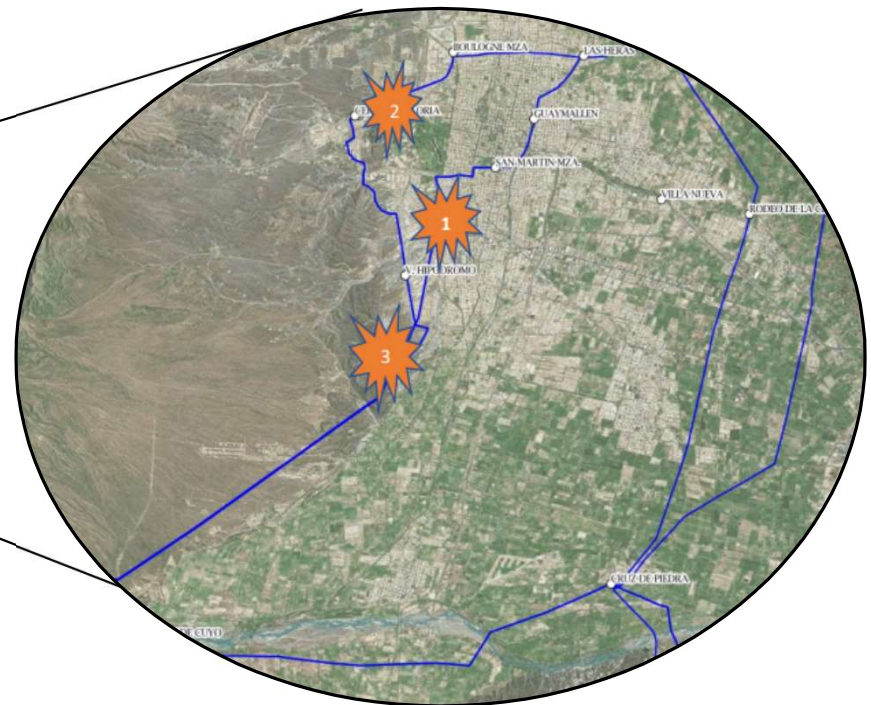
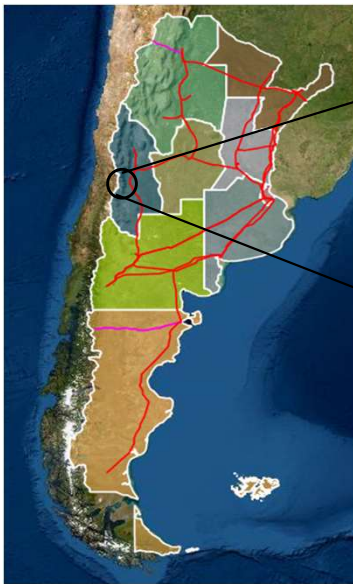
$$f_{ij_k} = 0$$



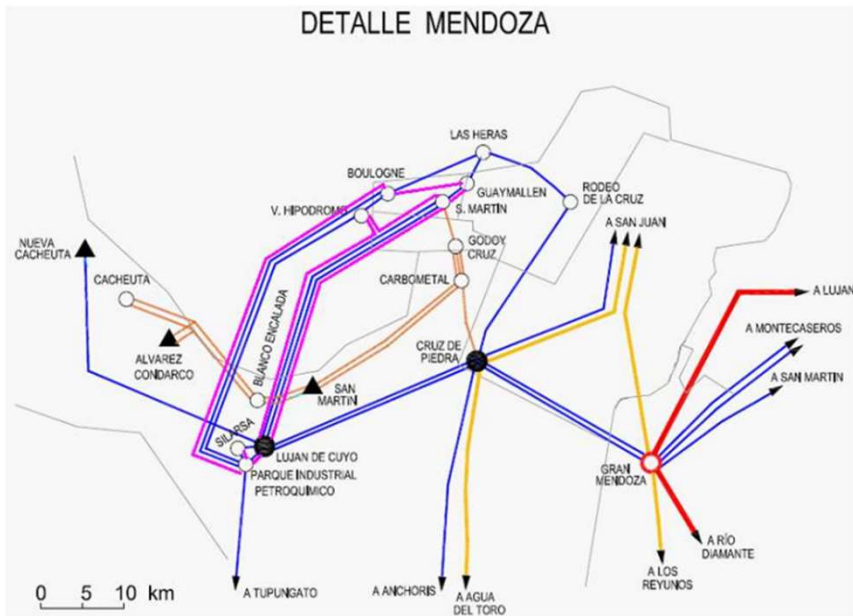


# Study case: Power System Scenarios

- Argentinean electric power system (SADI)
- 3 scenarios with different line contingency
- Avoid overloads in Cuyo area



# Study Case: Line Projects

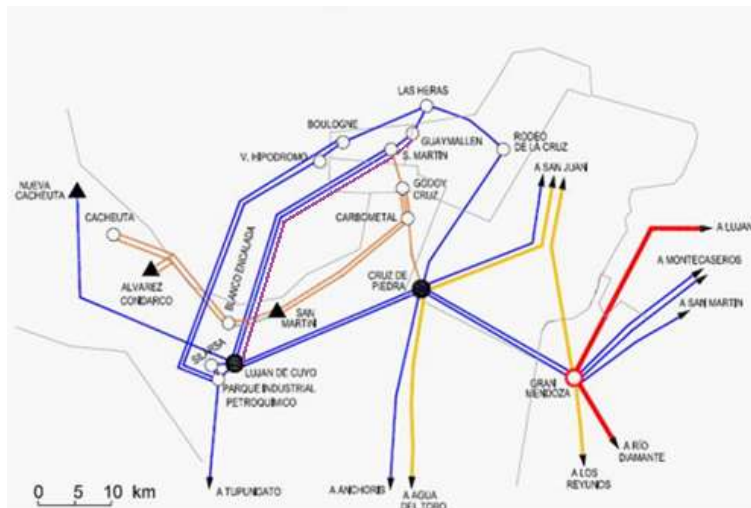


- Eight 132kV lines projects
- Six buses with possibility of load shed (20%)

[illegible]

# Study Case: Results

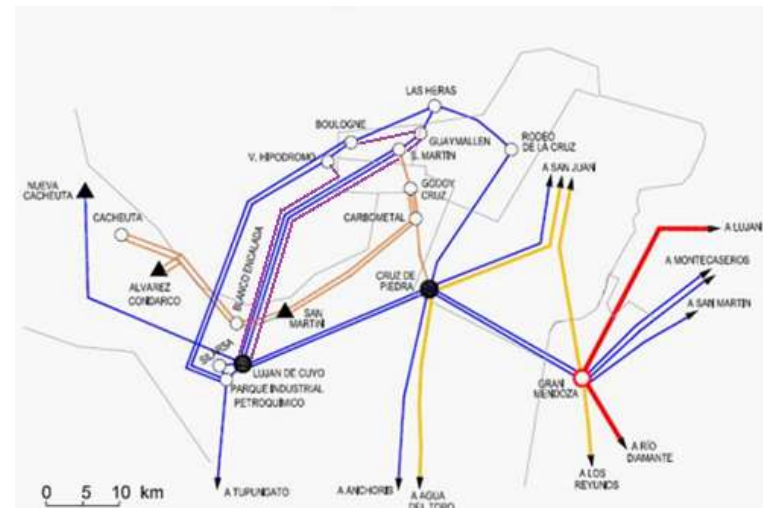
With load shed



- Lines build: 3
- Cost: U\$D 20.6M

23.7 % of difference

Without load shed



- Lines build: 4
- Cost: U\$D 27M

# Conclusions

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TNEP.py incorporates control policies (load shed) to achieve a lower inversion cost

The computational tool can handle country sized power systems

The results can be used with another power systems analysis tools