

**Homework 11 (Assigned: 4/24/2020; Due: 5/6/2020, 11:59pm)**

1. Plot the loop gain Bode plot for the feedback systems with the following open-loop gain  $H_{OL}(s)$  and feedback factor  $f$ . Determine loop-gain phase margin for all parts.

(a)  $H_{OL}(s) = \frac{100}{1 + \frac{s}{10^5}} ; f = 1$

(b)  $H_{OL}(s) = \frac{200}{(1 + \frac{s}{10^4})(1 + \frac{s}{10^6})} ; f = 1$

(c)  $H_{OL}(s)$  same as (b); but with  $f = 1/2$

(d)  $H_{OL}(s)$  same as (b); but with  $f = 1/4$

(e)  $H_{OL}(s) = \frac{1000}{s(1 + \frac{s}{100})} ; f = 1/10$

(f)  $H_{OL}(s)$  same as (e); but with  $f = 1/2$

(g)  $H_{OL}(s)$  same as (e); but with  $f = 1$

2. Design the CMOS realization of the boolean expressions shown below.

(a)  $Y = \overline{A \cdot (B + C)}$

(b)  $Y = \overline{(A + (B \cdot C))}$

(c)  $Y = A \cdot B$

(d)  $Y = A \cdot \overline{B + C}$

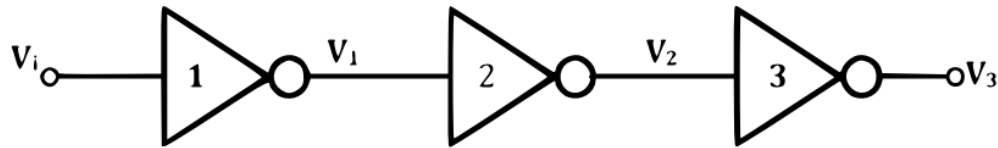
(e)  $Y = \overline{A \cdot B + B \cdot C + C \cdot A}$

(f)  $Y = \overline{((A \cdot B) + C) \cdot (D + E)}$

(g)  $Y = \overline{((A + B) \cdot C + D \cdot E)}$

(h)  $Y = \overline{A + B + C}$

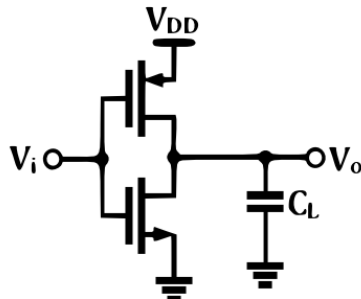
3. Consider the Inverter chain below:



Each inverter is identical to the others with  $V_{OH} = 1V$ ,  $V_{OL} = 0V$ ,  $NM_L = 0.3V$ ,  $NM_H = 0.5V$ .

- (a) Sketch a piecewise linear plot of the VTC(Voltage Transfer Function).
- (b) True or False: if  $V_i = V_{OL} + v_n$  with  $|v_n| < NM_L$ , then output  $V_3 = V_{OH}$ .
- (c) Determine  $V_3$  if  $V_i = V_{OL} + 0.4V$ . Is the output  $V_3$  correct? Does  $V_3 \in \{V_{OH}, V_{OL}\}$ ?
- (d) Determine  $V_3$  if  $V_i = V_{OL} + 0.45V$ . Is the output  $V_3$  correct? Does  $V_3 \in \{V_{OH}, V_{OL}\}$ ?
- (e) Which of the parts (b), (c), (d) demonstrate the noise-immunity property of the digital gates?
- (f) Which of the parts (b), (c), (d) demonstrate the restorative property of the digital gates?

4. Consider the CMOS inverter below:



Assume  $V_{DD} = 5V$ ,  $k'_n = 150\mu A/V^2$ ,  $k'_p = 75\mu A/V^2$ ,  $(W/L)_n = 1$ ,  $V_{THp} = -0.5V$ ,  $V_{THn} = 0.7V$ ,  $C_L = 0.5pF$ .

- (a) Determine the values of  $(W/L)_p$  such that  $V_M$  is 2.5V, 1.5V and 3.5V.
- (b) If  $(W/L)_p = 2$ , determine  $V_M$ ,  $t_{PLH}$ ,  $t_{PHL}$ , and the dynamic power dissipation  $P_D$  when operating at maximum switching frequency( $P_{Dmax}$ ).
- (c) If  $(W/L)_p = 4$  and  $(W/L)_n = 2$ , then relative to your answer in part (b), how will  $V_M$ ,  $t_{PLH}$ ,  $t_{PHL}$  and  $P_{Dmax}$  change?