

Correlation and Chi Square

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1 Load packages

```
library(tidyverse)
library(see)
library(car)
library(patchwork)
library(ggsci)
library(ggthemes)
library(performance)
library(Hmisc) #for correlation matrix
library(corrplot)#to visualize correlation matrices
library(car) #contains some statistical tests we need to assess assumptions
```

2 Correlation between numerical variables

Often in science, it can be useful to assess the correlation between numerical variables (how does a change in one variable impact a change in another?). We may use these correlations to tell us which variables to include or exclude from more complex models and we can also use

these correlations to understand relationships between variables and thus, possibly search for mechanisms to explain said relationships.

2.1 Correlation Coefficients

A **correlation coefficient (r)** tells us the relationship (strength and direction) between two variables. These coefficients can be positive or negative and will range from 0 to 1 (or negative 1). Values nearer to 1 (or negative 1) indicate stronger correlations and values closer to 0 indicate weaker correlations

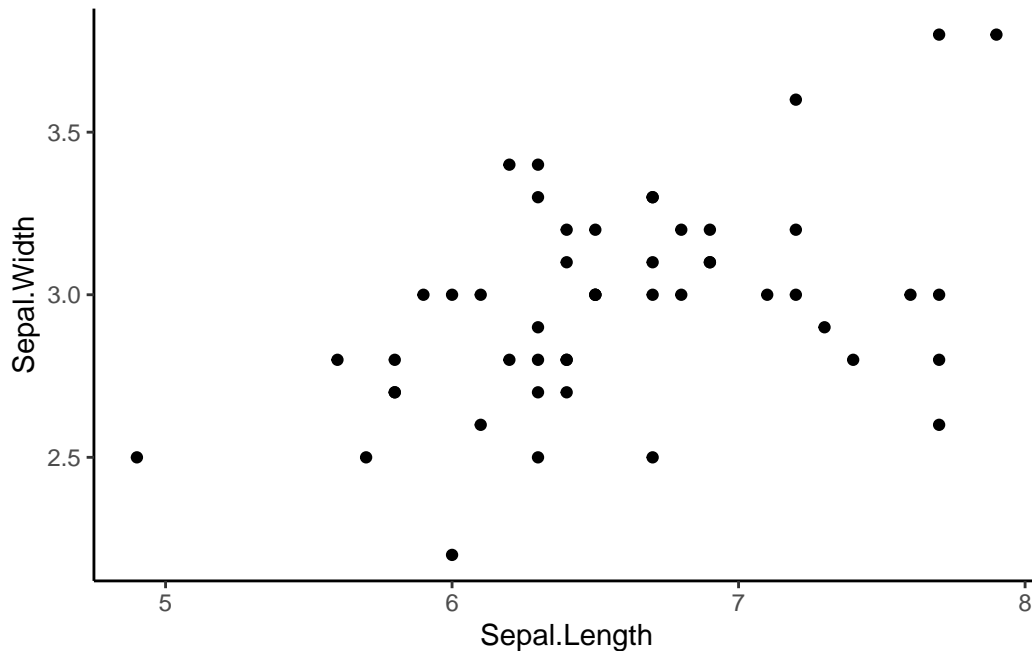
Let's try out some correlations using the iris data.

Is there a correlation between sepal length and sepal width? Let's test each species separately for now.

Step 1: make a scatterplot

```
#filter down to a single species
virg<-iris %>%
  filter(Species=='virginica')

#make a plot
ggplot(virg, aes(x=Sepal.Length, y=Sepal.Width))+
  geom_point()+
  theme_classic()
```



Step 2: Calculate a correlation coefficient (r)

```
cor(virg$Sepal.Length, virg$Sepal.Width)
```

```
[1] 0.4572278
```

This value ($r=0.45$) positive and middle of the road/strong. This tells us that some correlation likely exists.

Step 3: Do a hypothesis test on the correlation Spearman's Test

H0: The correlation between these two variables is 0

Ha: The correlation $\neq 0$

```
cor.test(virg$Sepal.Length, virg$Sepal.Width, method="spearman")
```

```
Warning in cor.test.default(virg$Sepal.Length, virg$Sepal.Width, method =
"spearman"): Cannot compute exact p-value with ties
```

Spearman's rank correlation rho

```
data:  virg$Sepal.Length and virg$Sepal.Width
S = 11943, p-value = 0.002011
alternative hypothesis: true rho is not equal to 0
sample estimates:
      rho
0.4265165
```

The above output gives us the r value (cor=0.457) AND a p-value for a hypothesis test that the two correlations do not differ. If $p < 0.05$ we can reject our H_0 and say that the correlation differs from 0. Here, $p = 0.0008$ so we can reject H_0 and suggest that we have a significant positive correlation! Rho is similar to r and in this case our correlation coefficient (0.42). It is slightly lower than the r we calculated above.

2.2 Multiple Correlations

```
iris2<-iris[,c(1:4)] #filter iris so we only have the numerical columns!

iris_cor<-cor(iris2, method="spearman")

iris_cor
```

| | Sepal.Length | Sepal.Width | Petal.Length | Petal.Width |
|--------------|--------------|-------------|--------------|-------------|
| Sepal.Length | 1.0000000 | -0.1667777 | 0.8818981 | 0.8342888 |
| Sepal.Width | -0.1667777 | 1.0000000 | -0.3096351 | -0.2890317 |
| Petal.Length | 0.8818981 | -0.3096351 | 1.0000000 | 0.9376668 |
| Petal.Width | 0.8342888 | -0.2890317 | 0.9376668 | 1.0000000 |

The above correlation matrix shows r (correlation coefficient) not p values!

Getting r and p values

```
mydata.rcorr = rcorr(as.matrix(iris2))
mydata.rcorr #top matrix = r, bottom matrix = p
```

| | Sepal.Length | Sepal.Width | Petal.Length | Petal.Width |
|--------------|--------------|-------------|--------------|-------------|
| Sepal.Length | 1.00 | -0.12 | 0.87 | 0.82 |
| Sepal.Width | -0.12 | 1.00 | -0.43 | -0.37 |
| Petal.Length | 0.87 | -0.43 | 1.00 | 0.96 |

| | | | | |
|-------------|------|-------|------|------|
| Petal.Width | 0.82 | -0.37 | 0.96 | 1.00 |
|-------------|------|-------|------|------|

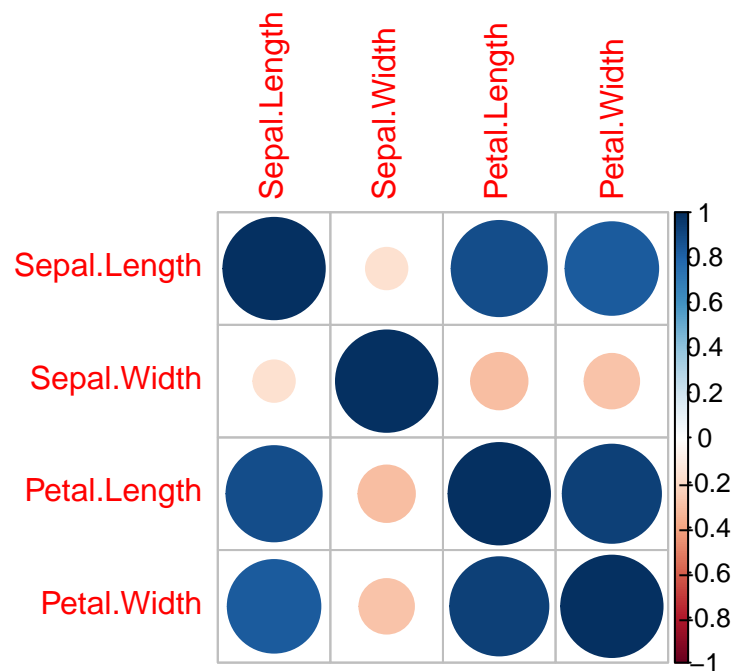
n= 150

P

| | Sepal.Length | Sepal.Width | Petal.Length | Petal.Width |
|--------------|--------------|-------------|--------------|-------------|
| Sepal.Length | | 0.1519 | 0.0000 | 0.0000 |
| Sepal.Width | 0.1519 | | 0.0000 | 0.0000 |
| Petal.Length | 0.0000 | 0.0000 | | 0.0000 |
| Petal.Width | 0.0000 | 0.0000 | 0.0000 | |

Plotting our correlations

```
corrplot(iris_cor)
```



2.3 Categorical correlations (Chi-Square)

A Chi-square test is a statistical test used to determine if two categorical variables have a significant correlation between them. These two variables should be selected from the same population. An example - Is the color of a thing red or green? Is the answer to a simple

question yes or no?

Data format Technically, a chi-square test is done on data that are in a contingency table (contains columns (variables) in which numbers represent counts. For example, here is a contingency table of household chore data (exciting)

```
chore <- read.delim("http://www.sthda.com/sthda/RDoc/data/housetasks.txt", row.names=1)
chore
```

| | Wife | Alternating | Husband | Jointly |
|------------|------|-------------|---------|---------|
| Laundry | 156 | 14 | 2 | 4 |
| Main_meal | 124 | 20 | 5 | 4 |
| Dinner | 77 | 11 | 7 | 13 |
| Breakfeast | 82 | 36 | 15 | 7 |
| Tidying | 53 | 11 | 1 | 57 |
| Dishes | 32 | 24 | 4 | 53 |
| Shopping | 33 | 23 | 9 | 55 |
| Official | 12 | 46 | 23 | 15 |
| Driving | 10 | 51 | 75 | 3 |
| Finances | 13 | 13 | 21 | 66 |
| Insurance | 8 | 1 | 53 | 77 |
| Repairs | 0 | 3 | 160 | 2 |
| Holidays | 0 | 1 | 6 | 153 |

H₀ = The row and column data of the contingency table are independent (no relationship)

H_a= Row and column variables are dependent (there is a relationship between them)

The test

```
chorechi<-chisq.test(chore)
chorechi
```

Pearson's Chi-squared test

data: chore

X-squared = 1944.5, df = 36, p-value < 2.2e-16

This result demonstrates that there is a significant association between the columns and rows in the data (they are dependent).

A second example

Let's try to assess correlation between two categorical variables in a dataframe we know! We will use mtcars

```
head(mtcars)
```

| | mpg | cyl | disp | hp | drat | wt | qsec | vs | am | gear | carb |
|-------------------|------|-----|------|-----|------|-------|-------|----|----|------|------|
| Mazda RX4 | 21.0 | 6 | 160 | 110 | 3.90 | 2.620 | 16.46 | 0 | 1 | 4 | 4 |
| Mazda RX4 Wag | 21.0 | 6 | 160 | 110 | 3.90 | 2.875 | 17.02 | 0 | 1 | 4 | 4 |
| Datsun 710 | 22.8 | 4 | 108 | 93 | 3.85 | 2.320 | 18.61 | 1 | 1 | 4 | 1 |
| Hornet 4 Drive | 21.4 | 6 | 258 | 110 | 3.08 | 3.215 | 19.44 | 1 | 0 | 3 | 1 |
| Hornet Sportabout | 18.7 | 8 | 360 | 175 | 3.15 | 3.440 | 17.02 | 0 | 0 | 3 | 2 |
| Valiant | 18.1 | 6 | 225 | 105 | 2.76 | 3.460 | 20.22 | 1 | 0 | 3 | 1 |

```
#make a contingency table
cartab<-table(mtcars$carb, mtcars$cyl)

chisq.test(cartab)
```

Warning in chisq.test(cartab): Chi-squared approximation may be incorrect

Pearson's Chi-squared test

```
data: cartab
X-squared = 24.389, df = 10, p-value = 0.006632
```

```
#note that we don't NEED to make the table. We can just do this
chisq.test(mtcars$carb, mtcars$cyl)
```

Warning in chisq.test(mtcars\$carb, mtcars\$cyl): Chi-squared approximation may be incorrect

Pearson's Chi-squared test

```
data: mtcars$carb and mtcars$cyl
X-squared = 24.389, df = 10, p-value = 0.006632
```

Both tests above are the same (just two options for you). We see that $p < 0.05$, thus we have evidence to reject H_0 and suggest that carb and cyl are dependent / correlated.