Lab 1

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This lab is due 11:59 PM Satuday 2/9/19.

You should have RStudio installed to edit this file. You will write code in places marked "TO-DO" to complete the problems. Some of this will be a pure programming assignment. The tools for the solutions to these problems can be found in the class practice lectures. I want you to use the methods I taught you, not for you to google and come up with whatever works. You won't learn that way.

To "hand in" the homework, you should compile or publish this file into a PDF that includes output of your code. Once it's done, push by the deadline to your repository in a directory called "labs".

• Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
#TO-DO
options(digits = 10)
pi
```

[1] 3.141592654

• Sum up the first 100 terms of the series $1 + 1/2 + 1/4 + 1/8 + \dots$

```
#TO-DO
sum(2^(0:-99))
```

[1] 2

```
sum((1/2)^{(0:99)})
```

[1] 2

• Find the product of the first 100 terms of 1 * 1/2 * 1/4 * 1/8 * ...

```
#TO-DO
prod(.5^(0:99))
```

[1] 0

• Find the product of the first 500 terms of 1 * 1/2 * 1/4 * 1/8 * ... Answer in English: is this answer correct?

```
#TO-DO
prod(.5^(0:499))
```

[1] 0

• Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
#TO-DO
-log10(2)*sum(0:499)
```

```
## [1] -37553.49196
```

```
# this gives the log of what we want
# so 10^this should be more accurate

# 10^(-375353.49196) # would be more accurate

10^.49196
```

```
## [1] 3.104273661
```

```
# roughly 3.104273661e-375353
```

• Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle size 1e-6.

```
#TO-DO

# 1e-6*sum(seq(0,1-1e^-6, by = 1e-6)^2)

1e-6*sum(seq(0,(1-0.000001), length.out = 10000000)^2)
```

[1] 3.333326833

• Calculate the average of 100 realizations of standard Bernoullis in one line using the sample function. sample

```
#TO-DO
mean(sample( c(0,1),size = 100, replace = TRUE))

## [1] 0.46
# mean(rbinom(100,1,0.5)) #n-obs=100, n=1, p=0.5
```

• Calculate the average of 500 realizations of Bernoullis with p = 0.9 in one line using the sample function.

```
mean(sample(c(0,1),size = 500, replace = TRUE, prob = c(0.1,0.9)))
```

[1] 0.904

• Calculate the average of 1000 realizations of Bernoullis with p = 0.9 in one line using rbinom.

```
mean(rbinom(1000,1,0.5)) #n-obs=100, n=1, p=0.9
```

[1] 0.498

• Use the strsplit function and sample to put the sentences below in random order.

```
lorem = "Lorem ipsum dolor sit amet, consectetur adipiscing elit. Morbi posuere varius volutpat. Morbi
#TO-DO
lorem_split = strsplit(lorem,".", fixed = TRUE)
k = c(lorem_split[[1]][1:10])
sample(k,10,replace=FALSE)
```

- ## [1] " Integer dapibus mi lectus, eu posuere arcu ultricies in"
- ## [2] " Aenean nulla ante, iaculis sed vehicula ac, finibus vel arcu"
- ## [3] " Cras suscipit id nibh lacinia elementum"
- ## [4] " Curabitur est augue, congue eget quam in, scelerisque semper magna"
- ## [5] " Mauris at sodales augue"
- ## [6] " Donec at tempor erat"
- ## [7] "Lorem ipsum dolor sit amet, consectetur adipiscing elit"
- ## [8] " Morbi posuere varius volutpat"
- ## [9] " Donec vehicula sagittis nisi non semper"
- ## [10] " Morbi faucibus ligula id massa ultricies viverra"
 - In class we generated the variable criminality with levels "none", "infraction", "misdimeanor" and "felony". Create a variable x_2 here with 100 random elements (equally probable) and ensure the proper ordinal ordering.

```
#TO-DO
criminality_levels = c("none","infraction","misdemeanor","felony")
#x_2f = factor(criminality_levels, levels = criminality_levels, ordered = TRUE)
#print(x_2f)
# x_2 = sample(x_2f, 100, replace = TRUE)
```

```
x_2 = factor(sample(rep(criminality_levels,100/4)), levels = criminality_levels, ordered = TRUE)
x_2
##
     [1] felony
                    infraction misdemeanor misdemeanor infraction
##
     [6] infraction infraction infraction felony
                                                        misdemeanor
    [11] misdemeanor misdemeanor none
##
                                            felony
                                                        felony
    [16] none
                    infraction felony
                                            infraction felony
##
   [21] felony
                    misdemeanor infraction misdemeanor misdemeanor
   [26] none
                    misdemeanor infraction infraction infraction
##
  [31] none
                                misdemeanor none
                                                        misdemeanor
                    none
   [36] misdemeanor felony
                                infraction felony
                                                        none
##
  [41] felony
                    infraction felony
                                            infraction infraction
##
  [46] felony
                    misdemeanor none
                                            felony
                                                        infraction
## [51] none
                    misdemeanor misdemeanor misdemeanor felony
## [56] misdemeanor felony
                                infraction none
## [61] none
                    none
                                misdemeanor infraction felony
## [66] misdemeanor infraction none
                                            misdemeanor none
## [71] none
                    none
                                misdemeanor misdemeanor felony
## [76] felony
                    infraction felony
                                            felony
                                                        infraction
## [81] infraction felony
                                misdemeanor misdemeanor infraction
## [86] none
                    infraction felony
                                            none
                                                        none
## [91] none
                    none
                                felony
                                            felony
                                                        felony
## [96] none
                    none
                                misdemeanor none
                                                        infraction
## Levels: none < infraction < misdemeanor < felony
  • Convert this variable to binary where 0 is no crime and 1 is any crime. Answer in English: is this the
    proper binary threshold?
\#x_2n = as.numeric(x_2)
x 2b = rep(0,100)
for(i in 1:100){
 if(as.numeric(x_2[i])-1 > 0){x_2b[i] = 1}
 else{x_2b[i] = 0}
}
x_2b
     [1] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 0 1
   [71] 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 0 0 0 0 1 1 1 0 0 1 0 1
\# x \ 2b = as.numeric(x \ 2 > 0)
# It is a proper thereshold to say if someone has any infractions, but not a good threshold to determin
  • Convert this variable to an unordered, nominal factor variable.
x_2uno = factor(x_2,levels = levels(x_2), ordered = FALSE)
x_2uno
##
     [1] felony
                    infraction misdemeanor misdemeanor infraction
    [6] infraction infraction infraction felony
                                                        misdemeanor
##
  [11] misdemeanor misdemeanor none
                                            felony
                                                        felony
  [16] none
                    infraction felony
                                            infraction felony
## [21] felony
                    misdemeanor infraction misdemeanor misdemeanor
## [26] none
                    misdemeanor infraction infraction infraction
## [31] none
                    none
                                misdemeanor none
                                                        misdemeanor
## [36] misdemeanor felony
                                infraction felony
                                                        none
```

```
[41] felony
                    infraction felony
                                            infraction infraction
##
   [46] felony
                    misdemeanor none
                                            felony
                                                        infraction
                    misdemeanor misdemeanor felony
##
   [51] none
   [56] misdemeanor felony
##
                                infraction none
                                                        none
##
   [61] none
                    none
                                misdemeanor infraction felony
##
   [66] misdemeanor infraction
                                            misdemeanor none
                                none
   [71] none
                    none
                                misdemeanor misdemeanor felony
   [76] felony
##
                    infraction felony
                                            felony
                                                        infraction
##
   [81] infraction felony
                                misdemeanor misdemeanor infraction
##
  [86] none
                    infraction
                                felony
                                            none
                                                        none
  [91] none
                    none
                                felony
                                            felony
                                                        felony
## [96] none
                                                        infraction
                    none
                                misdemeanor none
## Levels: none infraction misdemeanor felony
```

• Convert this variable into three binary variables without any information loss and put them into a data matrix

```
x_2mtx = matrix(data = rep(0,100*3), nrow = 100, ncol = 3)
for(i in 1:100){
    j = as.numeric(x_2[i])-1
    if (j != 0){ x_2mtx[i,j] = 1}
}
x_2mtx
```

```
[,1] [,2] [,3]
##
##
      [1,]
               0
                     0
                           1
##
      [2,]
               1
                     0
                           0
##
      [3,]
               0
                     1
                           0
##
      [4,]
                     1
                           0
               0
##
      [5,]
                     0
                           0
               1
##
      [6,]
               1
                     0
                           0
##
      [7,]
                     0
                           0
               1
##
      [8,]
               1
                     0
                           0
      [9,]
                     0
##
               0
                           1
##
    ſ10.]
               0
                     1
                           0
##
    [11,]
                           0
               0
                     1
    [12,]
                     1
                           0
##
    [13,]
               0
                     0
                           0
##
    [14,]
                     0
                           1
               0
    [15,]
                     0
##
               0
                           1
    [16,]
                     0
##
               0
                           0
##
    [17,]
               1
                     0
                           0
##
    [18,]
               0
                     0
                           1
                     0
                           0
##
    [19,]
##
    [20,]
               0
                     0
                           1
    [21,]
                     0
##
               0
                           1
##
    [22,]
               0
                     1
                           0
##
    [23,]
                     0
                           0
##
    [24,]
               0
                     1
                           0
##
    [25,]
               0
                     1
                           0
   [26,]
                     0
                           0
##
               0
   [27,]
                     1
                           0
               0
                           0
##
    [28,]
               1
                     0
##
    [29,]
               1
                     0
                           0
##
   [30,]
                     0
                           0
```

шш	[24]	0	0	0
## ##	[31,] [32,]	0	0	0
##	[33,]	0	1	0
##	[34,]	0	0	0
		0	1	0
##	[35,]	0	1	
##	[36,]			0
##	[37,]	0	0	1
##	[38,]	1	0	0
##	[39,]	0	0	1
##	[40,]	0	0	0
##	[41,]	0	0	1
##	[42,]	1	0	0
##	[43,]	0	0	1
##	[44,]	1	0	0
##	[45,]	1	0	0
##	[46,]	0	0	1
##	[47,]	0	1	0
##	[48,]	0	0	0
##	[49,]	0	0	1
##	[50,]	1	0	0
##	[51,]	0	0	0
##	[52,]	0	1	0
##	[53,]	0	1	0
##	[54,]	0	1	0
##	[55,]	0	0	1
##	[56,]	0	1	0
##	[57,]	0	0	1
##	[58,]	1	0	0
##	[59,]	0	0	0
##	[60,]	0	0	0
##	[61,]	0	0	0
##	[62,]	0	0	0
##	[63,]	0	1	0
##	[64,]	1	0	0
##	[65,]	0	0	1
##	[66,]	0	1	0
##	[67,]	1	0	0
##	[68,]	0	0	0
##	[69,]	0	1	0
##	[70,]	0	0	0
##	[71,]	0	0	0
##	[72,]	0	0	0
##	[73,]	0	1	0
##	[74,]	0	1	0
##	[75,]	0	0	1
##	[76,]	0	0	1
##	[77,]	1	0	0
##	[78,]	0	0	1
##	[79,]	0	0	1
##	[80,]	1	0	0
##	[81,]	1	0	0
##	[82,]	0	0	1
##	[83,]	0	1	0
##	[84,]	0	1	0
πĦ	[O±,]	J	1	U

```
##
    [85,]
              1
                    0
                         0
##
    [86,]
                    0
                         0
              0
##
    [87,]
                    0
                         0
                    0
##
    [88,]
              0
                         1
##
    [89,]
              0
                    0
                         0
##
    [90,]
              0
                    0
                         0
    [91,]
                    0
                          0
##
              0
    [92,]
##
              0
                    0
                          0
##
    [93,]
              0
                    0
                          1
                    0
##
   [94,]
              0
                         1
  [95,]
##
              0
                    0
                         1
##
   [96,]
                    0
                         0
              0
##
   [97,]
              0
                    0
                         0
## [98,]
                         0
              0
                    1
## [99,]
              0
                    0
                         0
## [100,]
                    0
                          0
#T0-D0
```

• What should the sum of each row be (in English)? Verify that.

```
# the sum of each row should be 0 or 1
# this should match writing the data as a binary crime or no crime, as before
rowSums(x_2mtx)
```

• How should the column sum look (in English)? Verify that.

```
# the column sums should be the frequency of each category
colSums(x_2mtx)
```

```
## [1] 25 25 25
```

• Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column in exponential with lambda of 9, the fifth column is binomial with n = 20 and p = 0.12 and the sixth column is a binary variable with 24% 1's.

```
n00 = 100

datafill = c(
    rnorm(n00, mean = 17, sd = sqrt(38)),
    runif(n00, min = -10, max = 10),
    rpois(n00, lambda = 6),
    rexp(n00, rate = 1/9),
    rbinom(n00, size = 20, prob = 0.12),
    sample(c(rep(1,round(n00*.24)),rep(0,round(n00*(1.00-.24)))),size = n00, replace = FALSE)
)

mtx_B = matrix(datafill, nrow = n00, ncol = n00, byrow = FALSE)
```