B461 Assignment 4: Relational Algebra

This assignment is designed to test your knowledge of the following lectures:

- Lecture 10: Relational Algebra
- Lecture 11: (Regular) Joins and semijoins
- Lecture 12: Set joins and Set semijoins in RA

For this assignment, you will need to submit 3 files. The first file is a .sql file that should contain all the SQL code relating to problems requesting the development of such code. The second file is a .txt file that should contain the output of the queries. The third file is a .pdf file that should contain your solutions for problems where RA expressions in their standard (i.e., non SQL) notation are requested. Ideally you should use latex to construct this .pdf file. Latex offers a convenient syntax to formulate RA expressions.

1 Formulating Queries in RA

1.1 Discussion

Before you solve the problems in this section, we briefly review how you can express RA expressions in SQL in a way that closely mimic their specifications as RA expressions in standard notation¹.

Consider a relation R(A,B) and a relation S(B,C) and consider the following RA expression F:

$$\pi_A(R) - \pi_A(\sigma_{B=1}(R \bowtie_{R.B=S.C} S))$$

Then we can write this query in SQL in a variety of ways that closely mimic its RA formulation. One way to write this RA expression in SQL is as follows:

```
SELECT DISTINCT A

FROM R

EXCEPT

SELECT A

FROM (SELECT DISTINCT A, B, C

FROM R JOIN S ON (R.B = S.C)

WHERE A = 1) q
```

An alternative way to write this query is to use the WITH statement of SQL.² To do this, we separate the RA expression F into sub-expressions as follows. (In this example, notice that each sub-expression corresponds to the application of a single RA operation. More generally, one can of course use sub-expressions that can contain multiple RA operations.)

¹By RA expressions in standard notation, we refer to expressions that use the notations $(A:\mathbf{a}), \sigma...(\cdot), \pi...(\cdot), \cup, \cap, -, \times, \bowtie, \bowtie..., \bowtie, \text{ and } \overline{\ltimes} \text{ for the RA operations. (For more detail, consult the lectures relating to RA and joins.)}$

²This is especially convenient when the RA expression is long and complicated.

Expression Name	RA expression
E_1	$\pi_A(R)$
E_2	$R\bowtie_{R.B=S.C} S$
E_3	$\sigma_{B=1}(E_2)$
E_4	$\pi_A(E_3)$
F	$E_{1}-E_{4}$

Then we can write the following SQL query. Notice how the expressions E1, E2, E3, and E4 occur as separate queries (temporary views) in the WITH statement and that the final query gives the result for the expression F.

WITH

```
E1 AS (SELECT DISTINCT A FROM R),
E2 AS (SELECT DISTINCT A, B, C FROM (R JOIN S ON (R.B = S.C)) e2),
E3 AS (SELECT A, B, C FROM E2 WHERE B = 1),
E4 AS (SELECT DISTINCT A FROM E3)
(SELECT A FROM E1) EXCEPT (SELECT A FROM E4);
```

In your answer to a problem, you may write the resulting RA expression with or without the WITH statement. (Your SQL query should of course closely resemble the RA expression it is aimed to express.). It should also be clear that in your solutions, you can not use the SQL set predicates [NOT] EXISTS, θ ALL, θ SOME, and [NOT] IN. You can also not use GROUP BY and aggregate functions.

 $^{^3}$ For better readability, I have used relational-name overloading. Sometimes, you may need to introduce new attribute names in SELECT clauses using the AS clause. Also, use DISTINCT were needed.

1.2 Problems

In the following problems, we will use the database schema that was used in Assignment 2 and Assignment3. To test your queries, you can use the data.sql file provided for this assignment.

Write the following queries as RA expressions in the standard RA notation.⁴ In the expressions, avoid using the \times operator. Rather, the use of the natural join \bowtie , the join \bowtie ..., the semijoin \ltimes , and the anti semijoin $\overline{\ltimes}$ operation is encouraged. It is also not required that you "optimize" the expressions. It is sufficient that they are correct.

When you formulate your RA expressions, you can use the following abbreviations for the relations:

Relation	Permitted abbreviations
Person	$P, P_1, P_2,$ etc
Company	C, C_1, C_2 etc
jobSkill	J, J_1, J_2 etc
Worksfor	$W, W_1, W_2, \text{ etc}$
Knows	$K, K_1, K_2,$ etc
PersonSkill	$S, S_1, S_2,$ etc

Submit your RA expressions for these queries in a .pdf document. (You are strongly encouraged to use Latex.)

Then, for each such RA expression, write a SQL query (possibly using the WITH statement) that mimics this expression as discussed in Section 1.1. Submit these queries in a .sql file as usual.

- 1. Find the pid and name of each person who (a) works for a company located in 'Bloomington' and (b) knows as person who lives in 'Chicago'. (Assignment 2, problem 1.)
- 2. Find each job skill that is not the job skill of any person who works for 'Yahoo' or for 'Netflix'. (Assignment 2, problem 7.)
- 3. Find the cname of each company which employs at least two different persons who have at least one common jobskill. (Assignment 2, problem 3.)
- 4. Find the pid and name of each person who knows another person who works for 'Google', but who does not know a person who works at 'Amazon' and has the 'Programming' skill. (Assignment 2, problem 2.)
- 5. Find the pid and name of each person who works for 'IBM' and who has a higher salary that any person with the 'Databases' skill and who also works at 'IBM'. (Assignment 2, problem 4.)

⁴Each of the problems relates back to a corresponding problem in Assignment 2 or in Assignment 3. You may find it useful to look at the SQL solutions for Assignment 2 and Assignment 3 as they may help you in formulating the queries as RA expressions.

- 6. Find the pid and name of each person who does not know any person who has a salary strictly above 55000. (Assignment 3, problem 8).
- 7. Find the cname of each company who only employs persons who make less than 55000. (Assignment 3, problem 10).
- 8. Find the pairs of job skills (s_1, s_2) such that each person with job skill s_1 also has job skill s_2 . (Assignment 2, problem 8.)

2 Theoretical Problems about RA

9. Consider two RA expressions E_1 and E_2 over the same schema. Furthermore, consider an RA expression F with a schema that is not necessarily the same as that of E_1 and E_2 .

Consider the following if-then-else query:

```
if F = \emptyset then return E_1 else return E_2
```

So this query evaluates to the expression E_1 if $F = \emptyset$ and to the expression E_2 if $F \neq \emptyset$.

We can formulate this query in SQL as follows⁵:

```
select e1.*
from E1 e1
where not exists (select distinct row() from F)
union
select e2.*
from E2 e1
where exists (select distinct row() from F);
```

Incidentally, the query

```
select distinct row() from F
```

returns the empty set if $F=\emptyset$ and returns the tuple () if $F\neq\emptyset.^6$ In RA, this query can be written as

$$\pi_{()}(F)$$
.

I.e., the projection of F on an empty list of attributes.

Write an RA expression, in function of E_1 , E_2 , and F, that expresses this if-then-else statement.

10. Let A(x) be a unary relation that can store a set of integers A. Consider the following boolean SQL query:

```
select not exists(select distinct row() from A) as A_isEmpty;
```

This boolean query returns the constant "true" if $A = \emptyset$ and returns the constant "false" otherwise. Using the insights you gained from Problem 9, solve the following problems:

 $^{^5}$ In this SQL query E1, E2, and F denote SQL queries corresponding to the RA expressions E_1 , E_2 , and F, respectively.

⁶The tuple () is often times referred to as the *empty tuple*, i.e., the tuple without com-

⁶The tuple () is often times referred to as the *empty tuple*, i.e., the tuple without components. It is akin to the empty string ϵ in the theory of formal languages. I.e., the string wihout alphabet characters.

Write an RA expression that expresses the above boolean SQL query.

Hint: recall that, in general, a constant value "a" can be represented in RA by an expression of the form (A: a). (Here, A is some arbitrary attribute name.) Furthermore, recall that we can express (A: a) in SQL as "select a as A". Thus RA expressions for the constants "true" and "false" can be the expressions (A: true) and (A: false), respectively.