WORKED EXAMPLE 10.1

Investigating Number Sequences



In this Worked Example, we investigate properties of number sequences. A number sequence can be a sequence of measurements, prices, random values, or mathematical values (such as the sequence of prime numbers). There are many interesting properties that can be investigated. For example, you can look for hidden patterns or test whether a sequence is truly random.

Problem Statement Investigate how the last digit of each value is distributed. For a given sequence of values, produce a chart such as



```
0: 105
1: 94
2: 81
3: 112
4: 89
5: 103
6: 103
7: 100
8: 108
9: 105
```

In order to produce arbitrary sequences, we declare an interface type with a single method:

```
public interface Sequence
{
    int next();
}
```

The LastDigitDistribution class analyzes sequences. It keeps an array of ten counters. Its process method receives a Sequence object and the number of values to process and updates the counters:

```
public void process(Sequence seq, int valuesToProcess)
{
   for (int i = 1; i <= valuesToProcess; i++)
   {
     int value = seq.next();
     int lastDigit = value % 10;
     counters[lastDigit]++;
   }
}</pre>
```

Note that this method has no knowledge of how the sequence values are produced.

To analyze a specific sequence, you provide a class that implements the Sequence interface. Here are two examples: the sequence of perfect squares (0 1 4 9 16 25 . . .) and a sequence of random integers.

```
public class SquareSequence implements Sequence
{
    private int n;

    public int next()
    {
        n++;
        return n * n;
    }
```

```
public class RandomSequence implements Sequence
{
   public int next()
   {
      return (int) (Integer.MAX_VALUE * Math.random());
   }
}
```

The following class demonstrates the analysis process. Note the pattern of the last digits of the sequence of perfect squares.

```
public class SequenceDemo
{
    public static void main(String[] args)
    {
        LastDigitDistribution dist1 = new LastDigitDistribution();
        dist1.process(new SquareSequence(), 1000);
        dist1.display();
        System.out.println();

        LastDigitDistribution dist2 = new LastDigitDistribution();
        dist2.process(new RandomSequence(), 1000);
        dist2.display();
    }
}
```

Program Run

```
0: 100
1: 200
2: 0
3: 0
4: 200
5: 100
6: 200
7: 0
8: 0
9: 200
0: 105
1: 94
2: 81
3: 112
4: 89
5: 103
6: 103
7: 100
8: 108
```

The complete program is contained in the ch10/worked_example_1 directory of the book's companion code.