

# Replication of "Transformers are RNNs: Fast Autoregressive Transformers with Linear Attention"

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## 1 Introduction

Transformers introduced by Vaswani et al. (2017) are the state-of-the-art in tasks like language understanding and image processing. However their quadratic memory complexity within the self-attention mechanism weakens the efficiency when dealing with long sequences. Consequently a number of so called "*X-former*"- models have been proposed, that improve the original Transformer in terms of computational and memory efficiency.

Aside from other approaches, such as Performer (Choromanski et al., 2020), Linformer (Wang et al., 2020) and Big Bird (Zaheer et al., 2020) the authors of "Transformers are RNNs" developed a Linear Transformer (Katharopoulos et al., 2020) to show how the quadratic complexity  $O(N^2)$  can be reduced to a linear complexity of  $O(N)$  without reducing the accuracy.

Standard Transformers use the following attention matrix:

$$Attention(Q, K, V) = V \cdot \text{softmax}\left(\frac{QK^T}{\sqrt{D_k}}\right) \quad (1)$$

with the queries  $Q \in \mathbb{R}^{N \times D_k}$ , keys  $K \in \mathbb{R}^{M \times D_k}$  and values  $V \in \mathbb{R}^{N \times D_v}$ , where  $N$  and  $M$  represent the lengths of queries and keys (or values) and  $D_k$  and  $D_v$  the dimensions of the keys (or queries) and values. The softmax function is applied rowwise to  $QK^T$ .

Katharopoulos et al. (2020) simplify this attention mechanism by generalizing equation (1) and replacing the softmax with the kernel feature map  $\phi(x) = \text{elu}(x) + 1$ :

$$V'_i = \frac{\phi(Q_i)^T \sum_{j=1}^i \phi(K_j) V_j^T}{\phi(Q_i)^T \sum_{j=1}^i \phi(K_j)} \quad (2)$$

Because of that  $\sum_{j=1}^i \phi(K_j) V_j^T$  and  $\sum_{j=1}^i \phi(K_j)$  can be computed once and reused for every query, this leads to a linear time and memory complexity of  $O(N)$ . Furthermore, by representing these cumulated sums as  $S_i$  and  $Z_i$ , they can be seen as states of an RNN for causal attention and computed from  $S_{i-1}$  and  $Z_{i-1}$  in constant time.

By testing, the Linear Transformer of Katharopoulos et al. (2020) performed an image generation task based on the CIFAR-10 dataset over 4,000 times faster than the normal transformer

with the same accuracy. These results seem to be extraordinary, which is why the Linear Transformer has been recognized in further scientific research as well as the paper *Transformers are RNNs* has been recited about 250 times in nearly two years.

Indeed, Linear Transformers seem to overpower the original Transformer using long sequences. In this paper, we attempt to replicate the copy task of *Transformers are RNNs* to investigate, whether Linear Transformer converges stably and scale linear with the sequence length. Furthermore, we want to find out at which sequence length a Linear Transformer is faster than a softmax-based Transformer.

## 2 Scope of reproducibility

Due to their linear complexity, Linear Transformers are said to be highly efficient when the sequence length increases. Katharopoulos et al. (2020) evaluate their Linear Transformer on image generation, automatic speech recognition and a copy task of numbers.

In order to examine computational cost and convergence property with growing sequence length, a copy task of number sequences is favourable because it is easy to increase the sequence length and to evaluate the results. Furthermore, an example of a copy task is already given in the Julia package Transformers.jl. We will use this example as a benchmark, that represents the performance of the Transformer by Vaswani et al. (2017). Based on that, we are going to replace the softmax-based attention function by a linear attention function. Then we apply different sequence lengths and examine, if the Linear Transformer performs faster but with the same precision as the original Transformer especially with high sequence lengths. All in all we focussing on the following claims:

- Claim 1: Linear Transformers converge stably and reach the same performance as the original Transformer.
- Claim 2: Linear Transformer scale linear with the sequence length.
- Claim 3: Linear Transformer perform faster than softmax-based Transformer.

## 3 Methodology

### 3.1 Model descriptions

A minimalistic model was developed to determine the convergence properties and computational cost of linear transformers. The transformer which was introduced by Vaswani et al. (2017) has been chosen as our baseline in this experiment. Unlike this aforementioned model which utilized softmax attention, the authors shifted the feature map into the module attention, computed the dot product of key and value instead of key and query so that the attention matrix never be explicitly computed and thus decrease the complexity from  $O(N^2 \max(D, M))$  to  $O(ND^2M)$ , where  $N > D^2$  in practice. Our target is to determine, whether linear attention converges stable, scales linear with the sequence length and runs faster than the softmax attention for different sequence lengths.

### 3.2 Data descriptions

For this synthetic task, we use sequences of 10 different symbols separated by a dedicated separator symbol and with different lengths. These sequences are randomly generated at the beginning

of the code.

### 3.3 Hyperparameters

We have mostly adjusted the hyperparameters of the given model in Transformers.jl according to the original paper. The number of head per Transformer is 8, with a head size of 64, which leads to the size of the whole Transformer of 512. The sequence length will be varied from 8 to 64, whereas the learning rate will stay constantly at  $10^{-3}$ . The batch size after being adjusted to fit the memory of our GPU will be kept at 8. We also maintain the number of training step at 3,000. We acknowledge that reducing the batch size could lead to a decreasing in precision at the end. However, our focus is to determine the performance particularly in respect to time complexity and therefore, it's not necessary to increase this parameter at the moment.

### 3.4 Implementation

The programming language used in the replication task is Julia. Due to a restriction of time, we have mainly taken most of the code from the package Transformers.jl as a template for the implementation. Other packages were:

- Flux: a library for machine learning functions for Julia
- CUDA: programming interface for working with NVIDIA CUDA GPUs using Julia
- Tullio: a flexible macro to calculate Einstein sums
- NNlib: a package that provides a library of functions useful for neural networks, such as softmax, sigmoid, batched multiplication, convolutions and pooling
- Plots: package to visualize data in Julia

For the synthetic task, we use a modified version of copy task based on the experiment which was used by Kitaev et al. (2020). As mentioned above in 3.1, what we do to implement linear attention is to replace the function attention of Transformers.jl with our own code called linattention, which has been translated from the original PyTorch code of the authors to Julia code. The original code requires in addition one more function called splitHeads to reshape the 3D tensor to 4D tensor, which we have also included in the script and which is shown below.

```
function splitHeads(x, batch_size, head, depth)
    x = reshape(x, (batch_size, :, head, depth))
end
```

Moreover, as the authors used the activation function  $\text{elu}(x) + 1$  in original paper instead of  $\text{relu}(x)$  as in the Transformers.jl, we also attempt to implement  $\text{elu}(x) + 1$  (which was called nelu in our script and is shown below) into the code to make sure that the performances of each model do not affected by different conditions and therefore they are comparable.

```
begin
    function oftf(x, y)
        oftype(float(x), y)
    end
    function nelu(x, =1)
        ifelse(x < 0, float(x)+1, @fastmath oftf(x, ) * (exp(x) - 1)+1)
    end
end
```

Also we have trimmed functions of the copy task of Transformers.jl that were only needed when using a softmax attention like *apply\_mask* for the sake of simplification. Lastly, instead of using Kullback-Leibler divergence as loss function, we apply cross entropy to calculate the loss for the gradient descent as given in the original work.

### 3.5 Experimental setup

Firstly, 8 random batches as training data will be created. They will go through 4 layers of encoders as well as 4 layers of decoders. At the end, the loss can be computed for each iteration, so that we can monitor the improvement of loss over each iteration. Furthermore, we can also observe the execute time of each model after a certain amount of iteration. To do so, we use an Nvidia Quadro P4000 with 8 GB of memory. Finally, we create test data randomly and give it in the trained model. The model then has to replicate the given sequence of numbers.

The Authors claimed, that their model can perform much better than the other implementation of Transformer for very long sequences due to the linearity property. Therefore, two models will be trained with increasing sequence length to verify this statement, namely Transformer with softmax attention and Linear Transformer with linear attention. Also we double the length of symbol sequence after each run, beginning with 8, 16, 32 and 64. The run time as well as convergency was reported afterwards.

Towards the convergency, both model do not always converge within 3000 steps. It might be due to the the very small batch size, as reducing batch size can result in worser performance of optimizer.

We implemented our code in a Pluto notebook and uploaded all our files in our GitHub repository <https://github.com/jbergner1/DM2022-LinearTransformers/>. In order to run our code we recommend reading the Read Me.

### 3.6 Computational requirements

Due to the linearity property as mentioned by the authors, we expect that the runtime of 3000 steps will just double after each run. We keep increasing the sequence length and keep other factors the same until the GPU reaches ist capacity. In this case, the maximal capacity can only be reached at  $seq\_len = 64$ . We also expected that Linear Transformer will perform better than Transformer with Softmax Attention in respect to computational time and convergency for long sequences.

## 4 Results

Due to the lack of memory capacity of the GPU, we can only set the sequence length to 64 at the maximum.

Table 1: Computational time of softmax and linear Transformer for given sequence lenghts

<b>Computational time in seconds</b>		
Seq_len	Softmax	Linear
8	221	1738
16	236	3004
32	287	5373
64	416	10071

The result can be seen in table 1 (this table is presented as a plot in the Supplementary Material).

As mentioned, we can not implement higher sequences to empirically determine the point where Linear Attention outperforms Softmax Attention. To tackle this deficiency, we apply a R-code using regression to determine the sequence length, from which Linear Attention takes advantage over Softmax Attention. First, we assume that the computational time in case of Softmax Attention has quadratic relation and Linear Attention has linear relation to sequence length. We do a regression of time on sequence length to calculate the coefficients, then try to use this coefficients to predict the possible output. At the end, we set the two terms equally and solve the quadratic equation resulting from it. A plot of that is shown in figure 1.

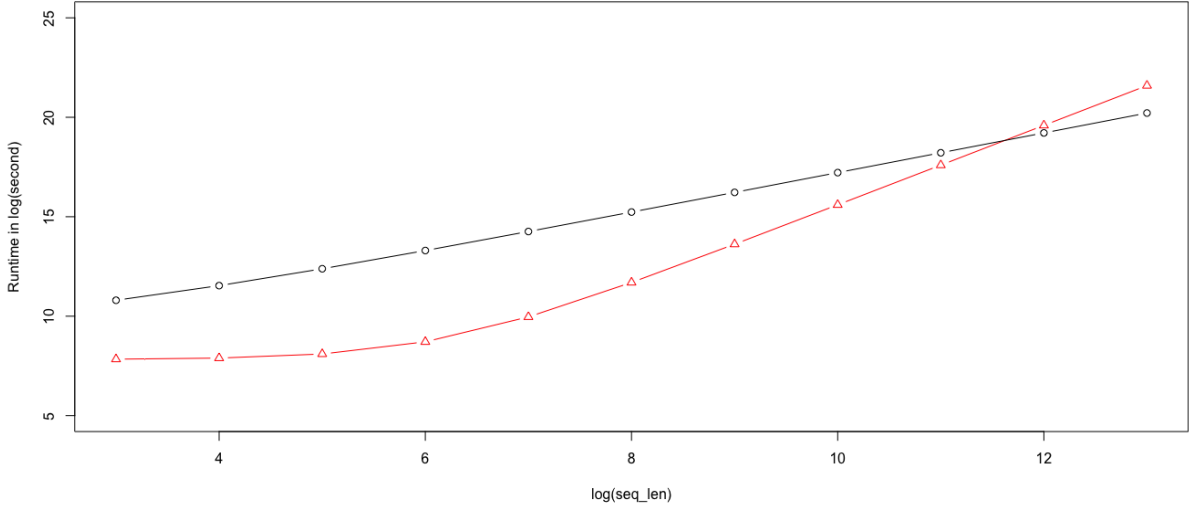


Figure 1: Computational time and sequence length prediction based on R-Code

## 4.1 Result 1

Katharopoulos et al. (2020) claim, that their Linear Transformer converges stable and reaches the same performance level as the original Transformer. Figure 2 shows the Convergence Plots of the Linear Transformer. Looking at these plots, a stable convergence does not occur. Even though the Linear Transformer converges to 0 at a sequence length of 8 and 32, the original Transformer converges to a loss that ranges from 10 to 18, whereas the Linear Transformer converges from 0 up to 70.

The original convergence plot of *Transformers are RNNs* contains 10,000 gradient steps. We could just analyze 3,000 steps, but looking at the original plot of the paper, linear attention has a higher loss than softmax attention on that point. Nevertheless, the original plot shows a range of the loss between  $10^{-2}$  and  $10^{-1}$ . This is something we can not replicate with our small batch size and number of gradient steps.

Consequently the Linear Transformer has much more variation in its losses and does not converge stably.

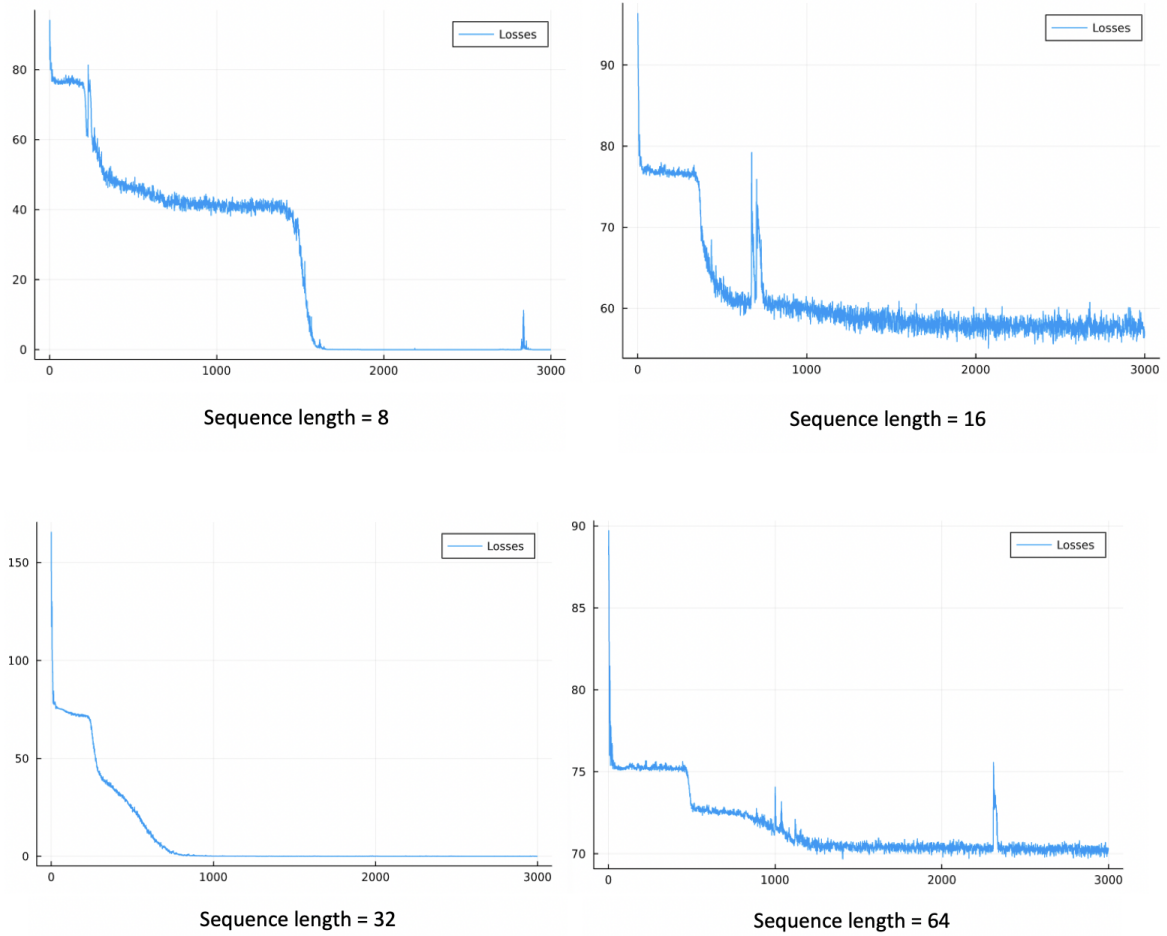


Figure 2: Convergence Plots of Linear Transformer with 3,000 gradient steps

## 4.2 Result 2

Like its name says, a Linear Transformer is supposed to scale linear to the sequence length. Our findings confirm this. Looking into table 1, each doubling of the sequence length approximately doubles the computational time of the Linear Transformer. So we were able to implement a linear complexity to the basic Transformer of Transformers.jl. Figure 1 also shows, that the Linear Transformer scales linear with the sequence length, whereas the softmax-based Transformer shows signs of quadratic complexity.

## 4.3 Result 3

Katharopoulos et al. (2020) often claim, that the Linear Transformer is faster than a softmax-based Transformer as a general statement. They analyze sequence lengths of  $2^9$  or higher and confirm that statement.

In contrast to *Transformers are RNNs* we analyzed smaller sequence lengths beginning at  $2^3$  and ending at  $2^6$ . As we expected, Softmax Attention does overperform Linear Attention by short sequences up to the length of  $2^6$ . This result shows, that linear attention performs only well with long sequences. So softmax attention is still advantageous on short sequences.

As a matter of fact that the capacity of our GPU was relatively restricted and that the code could have been implemented more efficiently, we cannot experiment with a higher sequence length to determine empirically the point where linear attention begins to outperform softmax attention. Because of that, we calculated the relationship between runtime and sequence length in R with our experimental data as the basis. According to the calculation, it is only worthwhile to use Linear Attention from a sequence length of 3149, i. e. between  $2^{11}$  and  $2^{12}$ . This result is not inline with the experiment in the original article, which claims that the outperformance of linear attention should already occur from a sequence length of  $2^9 = 512$ .

## 5 Discussion

Our experiments show, that Linear Transformer are faster than softmax-based Transformer with a quadratic complexity, but only when using long sequences. Katharopoulos et al. (2020) explain the problems of the original Transformer with growing sequence lengths and provide their Linear Transformer as a solution. In this regard they claim, that linear attention performs faster than softmax attention. Our replication finds, that this is only true with long sequences and not as a general statement. So as a consequence, the original Transformer is still more useful, when the sequences are small.

With our implementation, we were able to linearize the complexity of a Transformer to the sequence length. This shows that the mathematical trick that Katharopoulos et al. (2020) explain works and delivers results.

Nevertheless, we could not replicate a stable convergence of the Linear Transformer. Looking at Figure 2 our implementation of a Linear Transformer always converges with several steps. This is comparable to the convergence of the original Transformer. As we look at Figure 3, the convergence plots seem quite similar (apart from the Linear Transformer having a higher loss).

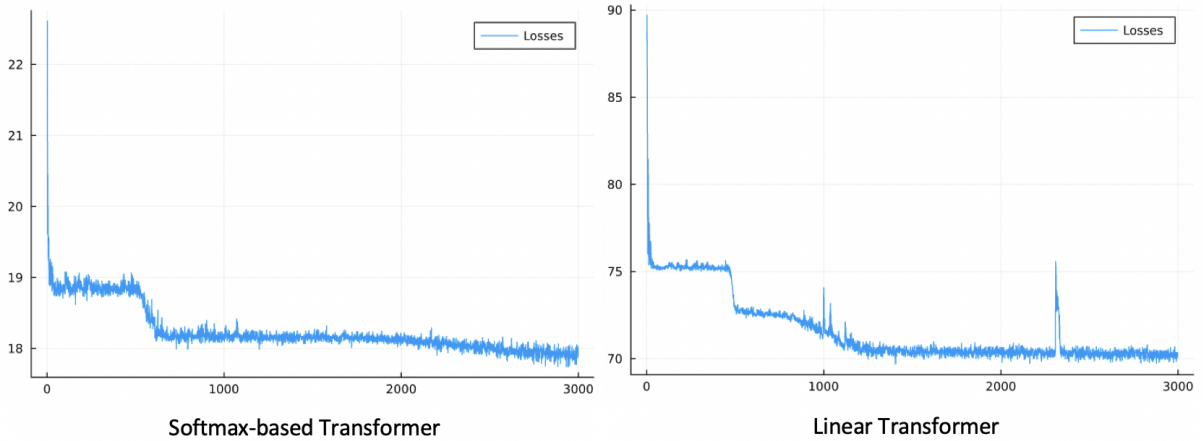


Figure 3: Convergence Plots of Original and Linear Transformer with 3,000 gradient steps and a Sequence length of 64

In Summary, we can conclude, that we were partly able to replicate the findings of *Transformers are RNNs* in our implementation of a Linear Transformer using Julia. We developed a Transformer that scales linear to the sequence length, just like proposed in the paper. However, we could not discover a stable convergence of the Linear Transformer and our Transformer

overpowers a softmax-based Transformer only above a sequence length of  $2^{12}$ , whereas the paper proposed this happens already at  $2^9$ .

Reasons for the failure of the replication could also be linked to our implementation itself. Our code in Julia could be further optimized and implemented more efficiently. Whereas the authors use PyTorch as a Python library with many functions for specific machine learning tasks, we had to either find equivalents in Julia or implement these functionalities ourself. This may sometimes resulted in a way that worked for our use case, but did the computation not in the best way. The code implementation of a Linear Transformer by Katharopoulos et al. (2020) differed in certain parts from the explanation of the paper. They used for example Einstein summation to compute the matrices more efficiently and some calculations were written in C++ in order to optimize them. Since we used plain Julia, this could be one reason for the underperformance of our Linear Transformer in comparison to the original.

In the GitHub repository of *Transformers are RNNs* it is rather described, how the repository can be used as a package in order to apply the Linear Transformer. On the other hand, it is a little bit unclear, how the Transformer was optimized and which function is necessary to implement it efficiently. Whereas the paper describes the proposed Transformer very detailed, the code implementation of it has quite a lack of explanation. So we can not be exactly sure whether our implementation uses the most efficient calculations.

The advantage of our approach was, that we could analyze different sequence lengths by modifying the amount of numbers on our copy task. Because of that we could create new findings in a fast way without many changes in the code. We mainly had to change the attention function of the Transformer provided by the package Transformers.jl. Therefore it was easy to change the existing softmax-based Transformer into a Linear Transformer.

Unfortunately we could not analyze sequence lengths above  $2^6$  because of limited GPU memory. Maybe with an optimized version of our Transformer, running with longer sequences would be possible.

We used a Transformer as our basis, which usually has a softmax attention. and is probably optimized for it. Maybe our result would be closer to the ones of *Transformers are RNNs* if we develop a Transformer that is basically planned to use linear attention. E.g. we had to reshape the structure of matrices in order to fit the requirements of our basic Transformer from Transformers.jl. This takes computation time, which could be lowered by implementing a Transformer that is more suitable for linear attention.

In our replication we only focused on the a copy task to compare linear and softmax attention. The paper also views the tasks image generation and automatic speech recognition. Maybe these tasks would have shown the differences between the original and the Linear Transformer more clearly and highlighted the strengths of the linear attention. All in all, we believe that the claims by Katharopoulos et al. (2020) are true and solve the problem of softmax attention with growing sequence length. Although our Linear Transformer did not perform as efficient as the one from the paper, we think that with further optimization it is possible to achieve similar results.

## 5.1 What was easy?

Katharopoulos et al. (2020) describe the mathematical simplification in order to achieve a linear complexity very detailed and justify each point understandable. So with an intermediate knowledge of matrix calculation and Transformers in general, the idea of the paper is perspicuous. This is supported by slides and videos of lectures about Linear Transformers which the authors provide on their website.

Furthermore Katharopoulos et al. (2020) provide code to their Linear Transformer on GitHub.



This repository is usable as a PyTorch package to apply Linear Transformers without an own implementation. Because of that, the GitHub repository is very extensive and contains useful information. The authors also refer to other repositories which use PyTorch as well as TensorFlow to implement a Linear Transformer. This wide number of templates was useful to create our own version of a Linear Transformer in Julia. Additionally the package Transformers.jl exists in Julia. It already contains an implementation of a softmax-based Transformer introduced by Vaswani et al. (2017). Moreover Transformers.jl had an example of a copy task which we used as the basis of our implementation. With an understanding of the tasks done in the paper and the code templates in Python it was possible for us to analyse the code of the copy task of Transformers.jl and mark sections, where changes are needed. Consequently, we changed the softmax-based attention function into a linear attention function. The rest of the example only needed minor changes in order to run our Linear Transformer.

At first we tried to run our code on a CPU, which resulted in a long time to carry out the experiments. Fortunately we were able to use the server provided by our University in order to run the code on a GPU. Because of that we could run code on several computers and procured results fast and effectively.

## 5.2 What was difficult?

The paper Transformers are RNNs seemed to support an implementation of Linear Transformers, because it contains an algorithm that explains how the calculation can be done using for-loops. However, the code differs from this algorithm. Instead of for-loops, Katharopoulos et al. (2020) use Einstein sums for calculation, which are never mentioned in the paper. With no knowledge of that specific mathematical operation it was challenging to discover how the matrices are computed. This was also caused by the reason, that the authors used the package torch to implement Einstein summation. This package does not exist in Julia, so we had to find a package that does the same calculation. For that we had to do further research in the computational function of Einstein summation and compare the one of torch with equivalent Julia packages. Lastly, after a consultation with our lecturer, we decided to use the package Tullio.jl. In addition to that, torch used another syntax to specify the input and the required transformation of the matrices. Consequently we needed to find a translation from the torch syntax to the one used in Tullio.

In general, it was a challenge to translate the code templates written in Python into Julia since Julia does not use classes like object-oriented languages. It was e.g. not possible to access values of a class, so we had to pass values within functions. Because of that, the code written in Julia is different than the Python template in some cases. Furthermore, many codes contained reshapes of the matrices, but did not mention which structure resulted from it. We had a lot of problems because of wrong matrix shapes, which were laborious to solve. We had e.g. to reference from other code source to find solutions.

Katharopoulos et al. (2020) published their experiments in a separate repository on GitHub, which is only mentioned in the issues section. There is no reference to this repository in the ReadMe, but on the other hand other references lead to non-existing pages that show a 404-error. In the repository, which can be used as a package, calculations are partially written C++. Because of that, the code published by the authors was all in all hard to understand.

We also ran the copy task provided in the experiment repository of Katharopoulos et al. (2020). Unfortunately, this code showed only the loss and accuracy of the model during the training, but did not give a plot or overview of the loss in the end. Furthermore, the ReadMe did not specify, how sequences of numbers can be applied in order to test the model. Finally, we were not able

to generate any findings from the provided code.

In order to use our Linear Transformer written in Julia on a GPU, we had to use CUDA. This package requires a Nvidia graphic card, which we could only access by using the University-servers. These servers did not always run stably, so that some experiments needed to be run again. The problem of using external servers to have a Nvidia GPU is an issue that may also affect multiple users.

At last but not the least, we wrote to the authors about our problems and questions, but have not received an answer yet. Looking at the issues section on the GitHub repository, it sometimes takes months to receive any responses from the authors.

### 5.3 Recommendations for reproducibility

In order to improve the replicability, Katharopoulos et al. (2020) should add comments to their code. Thereby it will be possible to explain the structure caused by the reshape of matrices and requirements of certain functions, which depends on the shape of a matrix. Furthermore, it should have been shown, which part of the paper is implemented in a certain line of code and why e.g. a package is used to do a calculation.

Although the authors answer question in the issues section in GitHub very well, they should add these answers to their repository to prevent, that these questions occur again. In our case it was always more useful to search in the issues section than in the ReadMe of the repository when we had questions.

## 6 Communication with original authors

Our contact to the authors was unanswered. However, the issues section in the GitHub Repository contains questions that are also interesting in our case.

The user gaceladri made his own implementation of a Linear Transformer and shared a plot that showed, that the loss of a Linear Transformer is higher than the loss of a softmax-based Transformer (in this case a BERT model) when the gradient steps are lower than 10,000. The user asked, if he has done something wrong regarding this discovery. Angelos Katharopoulos (username: angeloskath) answered, that this is possible, because the attention matrix of a Linear Transformer is low rank which leads to a harder learning process. The author further explains, that the whole point of Linear Transformers is an optimization of speed and memory. When these aspects are insignificant, using a softmax attention is probably better.

The user Yogurt928 asked, why Einstein sums are used in the code, whereas the paper uses buzz signs. Katharopoulos responds:

”The reason for using einsum instead of multiplication and summation is that it is faster since the large matrix does not need to ever be computed and kept in memory.”

At last, the user burcehan asked, why  $\text{elu}(x) + 1$  was used as the feature map. He recognized, that the convergence of his model is very slow using this function. Angelos Katharopoulos answers that the feature map needs to correspond to a non-negative similarity score. The question, whether other feature maps are better is an open research problem. In the tests for the paper, some feature maps achieved similar results, others not. All in all this depends on the analysed problem, but problems that require sparse attention patterns might be harder to learn using the  $\text{elu}(x) + 1$  feature map.

## References

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Supplementary Material

Computational time over gradient steps

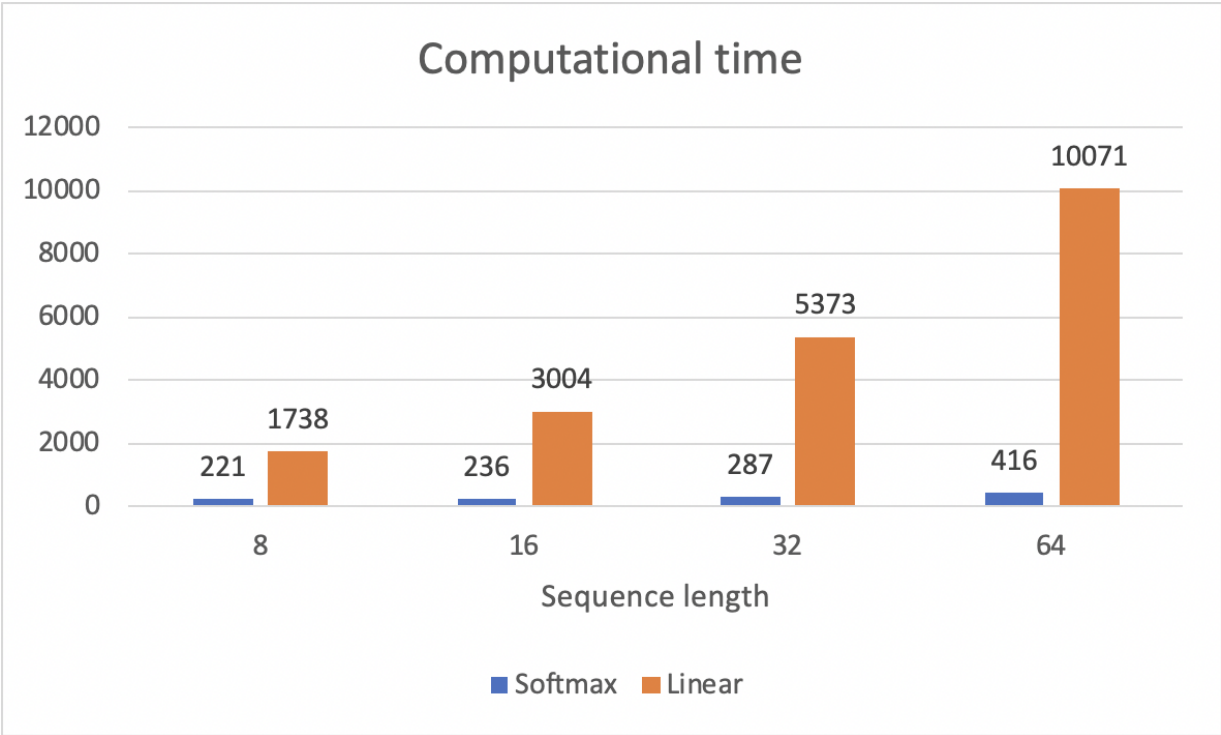


Figure 4: Computational time of softmax and linear attention over 3,000 gradient steps

## Convergence Plot of Softmax Transformer

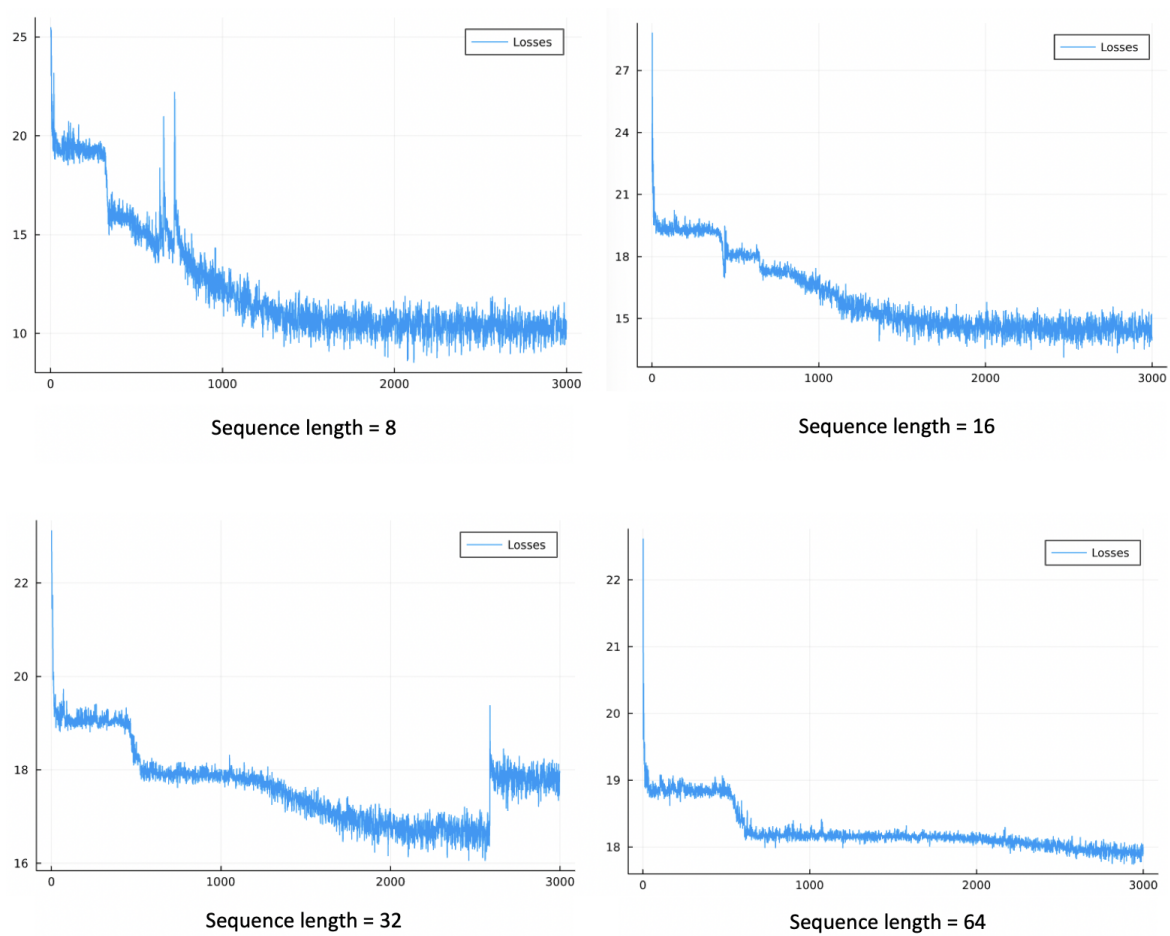


Figure 5: Convergence Plots of Softmax Transformer at 3,000 gradient steps

## Git History

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* 2f9a349 (HEAD -> main, origin/main, origin/HEAD) (clean up of code structure, 2022-03-28)
* 29c627d (Merge pull request #2 from jbergner1/JB-working, 2022-03-28)
| \
| * 3d4c420 (origin/JB-working, JB-working) (delete file for merge, 2022-03-28)
| * 43e7ba7 (changes for merge without conflicts, 2022-03-28)
| * 653f293 (change names for merge, 2022-03-28)
| * cfdc35c (add images to the article, 2022-03-28)
| * 2dcf813 (cleaning code, 2022-03-26)
| * a231bd4 (retry to run original code; further writing of article, 2022-03-25)
| * 239b8b0 (adjustments and optimization for GPU, 2022-03-24)
| * 17fce84 (changes in order to get 10-Element Vector, 2022-03-21)
| * 7f312fa (using nelu function, 2022-03-18)
| * 7c96da6 (finally training; optimization needed, 2022-03-17)
| * 77f4d7c (Training stops due to Error: "Mutating arrays is not supported", 2022-03-17)
| * 19b8aa9 (update of LinAtTransformer, 2022-03-14)
| * 74c8e8d (changes, but stil dimension mismatch, 2022-03-14)
| * a9af286 (tryouts of new attention function, 2022-03-14)
| * 1c44697 (finishing introduction, 2022-03-13)
| * 7a61cec (update of introduction, 2022-03-12)
| * 53afa90 (first paragraphs of introduction, 2022-03-11)
| * 8645799 (further tries of linear Attention in Julia; Beginning of writing Article, 2022-03-11)
| * 9274835 (create script for linear attention, 2022-03-08)
| * f62f405 (adding Transformer definitions and functions manually for changing, 2022-03-03)
| * 366ff7e (create Duplicate of Exercise 11 for testing purposes, 2022-03-02)
| * b6fe150 (documentation of changes, 2022-03-02)
| * c32adca (additional template, 2022-02-28)
| * a86fc2a (Initialization and upload of first tries, 2022-02-28)
* | b9321f6 (Merge pull request #1 from jbergner1/vado, 2022-03-28)
| \ \
| * | b8e9c39 (origin/vado, vado) (Create intersection_calculating.r, 2022-03-28)
| * | 3f81412 (Create LinTrans.jl, 2022-03-28)
| * | 188e8c7 (Update LinAt.ipynb, 2022-03-20)
| * | b30abaf (padding_mask, 2022-03-20)
| * | f36da33 (Fast am Ziel, 2022-03-16)
| * | f1fa358 (Create testattention.ipynb, 2022-03-16)
| * | 45ebf6e (Update LinearAttentionTransformer.ipynb, 2022-03-14)
| * | 95c02f4 (Update LinearAttentionTransformer.ipynb, 2022-03-14)
| * | 9baf89e (Create test.ipynb, 2022-03-14)
| * | a2eb13e (Create u11.ipynb, 2022-03-05)
| * | 2f5fca0 (relevant functions and possible changes, 2022-03-02)
| * | d15db5a (Transformer basic template upload, 2022-03-02)
| | /
| * | 4292b82 (Update README.md, 2022-03-26)
| * | bf04635 (Update README.md, 2022-03-26)
| * | fc26614 (Update README.md, 2022-03-26)
| * | 36e837d (Update README.md, 2022-03-26)
| /
* 67ccab4 (Initial commit, 2022-02-28)
```