

binary - base 2 - 0 1

decimal - base 10 - 0 1 2 3 4 5 6 7 8 9

987

9 | 8 | 7  
hundreds tens ones

- 1 0 1

1 0 1 0<sub>2</sub>

eights	fours	twos	ones
1	0	1	0
=	-	=	-

binary  
octal 8  
decimal 10  
hexadecimal 16

$$1010_2 = 10_{10}$$

byte

$2^7 = 128$	$2^6 = 64$	$2^5 = 32$	$2^4 = 16$	$2^3 = 8$	$2^2 = 4$	$2^1 = 2$	$2^0 = 1$
0	0	0	0	1	0	1	0
7	6	5	4	3	2	1	0

$$2^7 = 128 \cdot 0 = 0$$

$$2^3 = 8 \cdot 1 = 8$$

$$2^2 = 4 \cdot 0 = 0$$

$$2^6 = 64 \cdot 0 = 0$$

$$2^5 = 32 \cdot 0 = 0$$

$$2^4 = 16 \cdot 0 = 0$$

$$2^1 = 2 \cdot 1 = 2$$

$$2^0 = 1 \cdot 0 = 0$$

→

$2^7 = 128$	$2^6 = 64$	$2^5 = 32$	$2^4 = 16$	$2^3 = 8$	$2^2 = 4$	$2^1 = 2$	$2^0 = 1$
1	1	1	1	1	1	1	1
7	6	5	4	3	2	1	0

$$2^7 = 128 \cdot 1 = 128$$

$$2^3 = 8 \cdot 1 = 8$$

$$2^6 = 64 \cdot 1 = 64$$

$$2^2 = 4 \cdot 1 = 4$$

$$2^5 = 32 \cdot 1 = 32$$

$$2^1 = 2 \cdot 1 = 2$$

$$2^4 = 16 \cdot 1 = 16$$

$$2^0 = 1 \cdot 1 = 1$$

$$\begin{array}{r} 128 \\ 64 \\ \hline 192 \end{array}$$

$$\begin{array}{r} 192 \\ 32 \\ \hline 224 \end{array}$$

$$\begin{array}{r} 224 \\ 16 \\ \hline 240 \end{array} \quad \begin{array}{r} 240 \\ 8 \\ \hline 248 \end{array}$$

$$\begin{array}{r} 248 \\ 4 \\ \hline 252 \end{array}$$

$$\begin{array}{r} 252 \\ 2 \\ \hline 254 \end{array}$$

$$\begin{array}{r} 254 \\ 1 \\ \hline 255 \end{array}$$

128	64	32	16	8	4	2	1
0	1	0	1	1	0	1	0
.		.					

64  
16  
8  
2

$$133/2 = 63 \text{ r } 1$$

$$63 \cdot 2 = 126$$

$$132/2 = 66 \text{ r } 0$$

$$66/2 = 33 \text{ r } 0$$

$$33/2 = 16 \text{ r } 1$$

$$16/2 = 8 \text{ r } 0$$

$$8/2 = 4 \text{ r } 0$$

$$\begin{array}{r} 63 \\ \hline 12641 = \end{array}$$

$$4/2 = 2 \text{ r } 0$$

$$2/2 = 1 \text{ r } 0$$

$$1/2 = 0 \text{ r } 1$$

1 0 0 0 0 1 0 0

128 64 32 16 8 4 2 1  
1 0 0 0 0 1 0 0

$$5/2 = 2 \text{ r } 1$$

$$2/2 = 1 \text{ r } 0$$

$$1/2 = 0 \text{ r } 1$$

$$\begin{array}{r} 4 \quad 2 \quad 1 \\ 1 \quad 0 \quad 1 \end{array}$$

$$\begin{array}{r} 4 \quad 2 \quad 1 \\ 1 \quad 1 \quad 1 \end{array}_2 = 7$$

$$\begin{array}{r} \phantom{1} \phantom{0} \phantom{0} \phantom{0} \phantom{1} \\ \phantom{1} \phantom{0} \phantom{0} \phantom{0} \phantom{1} \\ 1 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{1} \\ \hline 1 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{1} \end{array} \quad \begin{array}{r} 7 \\ 10 \\ \hline 17 \end{array}$$

$$17$$

$$\begin{array}{c|c|c|c|c} 16 & 8 & 4 & 2 & 1 \\ \hline 1 & 0 & 0 & 0 & 1 \end{array}$$

$$\begin{array}{r|l} 8 & 1 \\ 4 & 1 \\ 2 & 1 \\ 1 & 0 \end{array}$$

$$\begin{array}{r} 111 \\ 111 \\ \hline 1110 \end{array}$$

$$\begin{array}{r} 7 \\ 7 \\ \hline 14 \end{array}$$

Base Ten - Decimal

0 1 2 3 4 5 6 7 8 9

8 eight

Base Two - Binary

0 1

Bit

$2^3$			$2^4$		
2			10		
0	0	0	0	0	0
1	1	1	1	1	1
10	10	10	2	2	2
11	11	11	3	3	3
100	100	100	4	4	4
101	101	101	5	5	5
110	110	110	6	6	6
111	111	111	7	7	7

$2^3$			$2^3$		
hundreds			ones		
4	9	7	4	9	7

$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$
128	64	32	16	8	4	2	1
1	0	0	1	1	1	0	1
7	6	5	4	3	2	1	0

$$10011101_2 = 157_{10}$$

128 - 1	+ 8 - 1	128	
<del>+ 64 - 0</del>	+ 4 - 1	16	156
<del>+ 32 - 0</del>	+ 2 - 0	144	+ 1
+ 16 - 1	+ 1 - 1	8	157
		152	
		4	
		156	

$$11100001_2 = 225_{10}$$

$$1 \cdot 128 \quad \cancel{+ 0 \cdot 8}$$

$$128$$

$$64$$

$$+ 1.64$$

~~$$+ 0.4$$~~

$$+ 1.32$$

~~$$+ 0.2$$~~

~~$$+ 0.16$$~~

$$+ 1.1$$

$$\begin{array}{r} 192 \\ 32 \\ \hline 224 \\ 1 \\ \hline 225 \end{array}$$

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$$225_{10} =$$

$$q \quad r \quad 2$$

$$225/2 = 112 \text{ r } 1$$

$$66 \cdot 2 = 132$$

$$112/2 = 56 \text{ r } 0$$

$$56/2 = 28 \text{ r } 0$$

$$28/2 = 14 \text{ r } \underline{0}$$

$$14/2 = 7 \text{ r } 0$$

$$7/2 = 3 \text{ r } 1$$

$$3/2 = \underline{1} \text{ r } 1$$

$$1/2 = 0 \text{ r } 1$$

hundreds	tens	ones
2	2	5



twos    ones  
 |   |   |   0   0   0   0   1

1110   0001

$$\begin{array}{r} 0 \\ 70 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 1 \\ +0 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 0 \\ 71 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ +1 \\ \hline 10 \end{array}$$

$$\begin{array}{r} 1 \\ +1 \\ \hline 11 \end{array}$$

$$\begin{array}{r} 10 - 2 \\ 10 - 2 \\ \hline 100 \quad 4 \\ \pi \end{array}$$

$$\begin{array}{r}
 11 \\
 11 \\
 \hline
 110 \\
 42
 \end{array}$$

$$\begin{array}{r}
 11 \\
 11 \\
 \hline
 6
 \end{array}$$

$$\begin{array}{r}
 1184 \\
 1101 \\
 8420 \\
 \hline
 110112 = 27_{10}
 \end{array}$$