

Event=an outcome or defined collection of outcomes of a random experiment

DM 1st Law: $(A \cup B)' = A' \cap B'$, DM 2nd Law: $(A \cap B) = A' \cup B'$.

Mutually exclusive = two or more events that cannot occur at the same time. If one of the outcomes occurs, it is not possible for the other event outcome to occur.

Axiom 1: For any event A, $P(A) \geq 0$. Axiom 2: $P(\text{Sample Space}) = 1$. Axiom 3: If A_1, A_2, A_3 is an infinite collection of disjoint events, then $P(\text{Union of all } A\text{'s}) = \text{Sum of } P(a\text{'s})$. $P(\text{empty set}) = 0$.

Complement Rule: $P(A) = 1 - P(A')$. Addition Rule: $P(A \cup B) = P(A) + P(B) - P(A \cap B)$.

$nPk = n! / (n-k)!$. $nCk = n! / k!(n-k)!$. Condition Prob.: $P(A|B) = P(A \cap B) / P(B)$. $P(A \cap B) = P(A|B)P(B)$. $P(A_1 \cap A_2 \cap A_3) = P(A_3 | (A_1 \cap A_2))P(A_1 \cap A_2) = P(A_3 | (A_1 \cap A_2))P(A_1 | A_2)P(A_2)$

Bayes' Theorem: $P(A|B) = P(B|A)P(A) / P(B)$

Independent if $P(A|B) = P(A)$, and they are dependent otherwise. $P(A \cap B) = P(A)P(B)$

If $A \cap C$ & $A \cap B$ are independent, this does not imply that $B \cap C$ are independent! Check all.

$P(A \cap B) = P(A) + P(B) - P(A \cup B)$.. 3 components $P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B) - P(A \cap C) - P(B \cap C) + P(A \cap B \cap C)$... $P(A \cap B') = P(A) - P(A \cap B)$... $P(A' \cap B) = P(B) - P(A \cap B)$...

PROOFS: 1) Write all formulas you know. 2) Substitute!! 3) Look for compliments 4) When in doubt draw a Venn diagram.

If you are trying to count the number of ordered pairs/tuples of objects:

1. Define n_1, n_2, \dots

2. Use the Fundamental Counting Principle ($n_1 \times n_2 \times \dots$)

1. Define n and k

- n is the number of distinct objects

- k is the number of objects selected

2. List out some sample space elements

3. Determine replacement: Can the n objects can be selected more than once per element (with replacement) or not (without replacement)?

4. Determine order: Does the sequence of each element matter (is $\{1,2,3\}$ meaningfully different than $\{2,1,3\}$)?

5. Use the box below to identify the correct counting technique

6. Remember that when you are computing a probability, you should have the same number of things accounted for in the numerator and the denominator.

	Order Matters	Order Does Not Matter	
With replacement	FCP or n^k	$\binom{n+k-1}{k}$	
Without replacement	FCP or $\frac{n!}{(n-k)!}$	$n C_k = \frac{n!}{k!(n-k)!}$	$n \geq k$