Part 3

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Agenda

- 1. Recap of Movie Analysis
- 2. Multiple Regression
- 3. Categorical Predictors

Recap of Movie Analysis

```
require(tidyverse)
mv <- readRDS('../data/mv.Rds')</pre>
```

- Theory: the more a movie costs, the more it should make
 - If not, Hollywood would go out of business!
- X: budget
- *Y*: gross

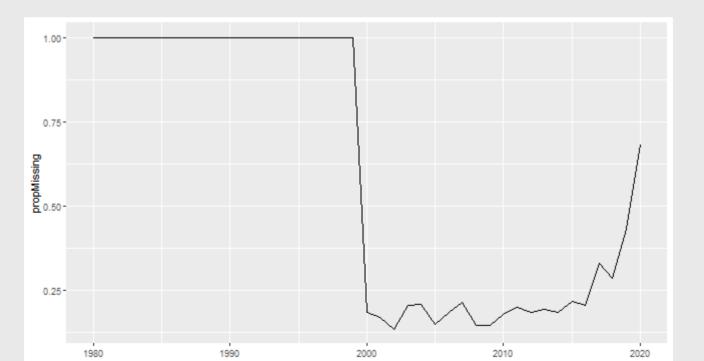
Step 1: Look

summary(mv %>% select(gross,budget))

```
budget
##
       gross
##
   Min.
          :7.140e+02
                      Min.
                                   5172
##
   1st Qu.:1.121e+07
                      1st Qu.: 16865322
##
   Median :5.178e+07
                     Median : 37212044
                    Mean : 57420173
##
   Mean :1.402e+08
                    3rd Qu.: 77844746
##
   3rd Qu.:1.562e+08
##
   Max. :3.553e+09
                     Max. :387367903
##
   NA's :3668
                      NA's :4482
```

Step 1: Look

```
mv %>%
  mutate(missing = ifelse(is.na(gross) | is.na(budget),1,0)) %>%
  group_by(year) %>%
  summarise(propMissing = mean(missing)) %>%
  ggplot(aes(x = year,y = propMissing)) +
  geom_line()
```



Some quick wrangling

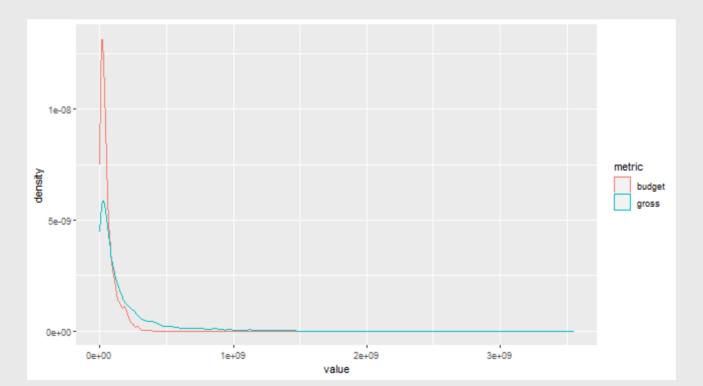
```
mv <- mv %>%
  drop_na(gross,budget)

mv %>%
  select(gross,budget) %>%
  glimpse()
```

```
## Rows: 3,179
## Columns: 2
## $ gross <dbl> 73677478, 53278578, 723586629, 11490339, 62...
## $ budget <dbl> 93289619, 10883789, 160147179, 6996721, 139...
```

Step 2: Univariate Viz

```
mv %>%
  select(title,gross,budget) %>%
  gather(metric,value,-title) %>%
  ggplot(aes(x = value,color = metric)) +
  geom_density()
```



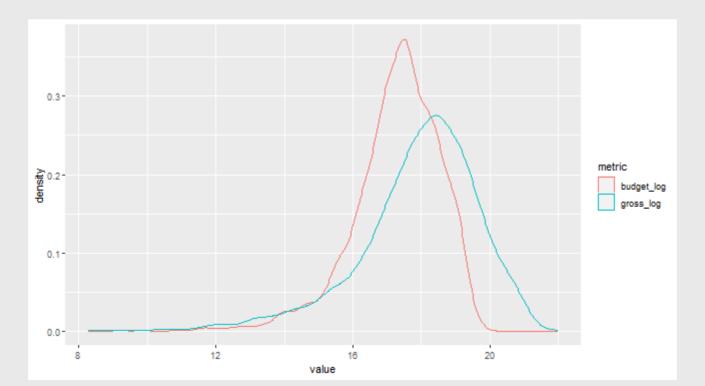
More Wrangling?

- Univariate visualization higlights significant skew in both measures
 - Most movies don't cost a lot and don't make a lot
 - But there are a few blockbusters that pull the density way out
- Let's wrangle two new variables that take the log of these skewed measures
 - Logging transforms skewed measures to more "normal" measures

```
mv <- mv %>%
  mutate(gross_log = log(gross),
        budget_log = log(budget))
```

Step 2: Univariate Viz

```
mv %>%
  select(title,gross_log,budget_log) %>%
  gather(metric,value,-title) %>%
  ggplot(aes(x = value,color = metric)) +
  geom_density()
```

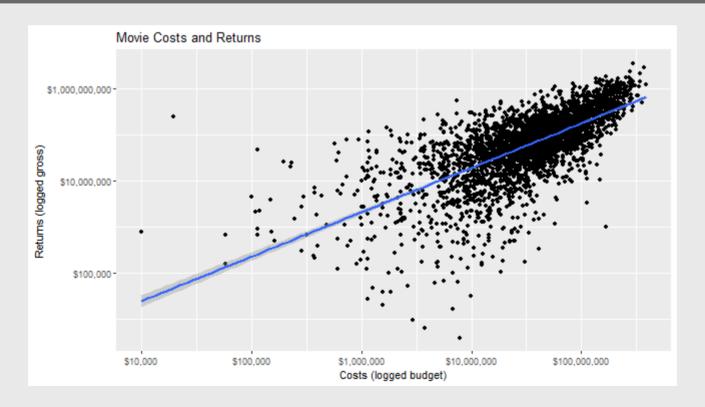


Step 3: Multivariate Viz

Step 3: Multivariate Viz

```
pClean + geom_smooth(method = 'lm')
```

```
## geom_smooth() using formula = 'y ~ x'
```



Step 4: Regression!

```
m <- lm(gross_log ~ budget_log,data = mv)
summary(m)</pre>
```

```
##
## Call:
  lm(formula = gross log ~ budget log, data = mv)
##
## Residuals:
##
      Min 1Q Median 3Q Max
## -8.2672 -0.6354 0.1648 0.7899 8.5599
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.26107 0.30953 4.074 4.73e-05 ***
## budget log 0.96386 0.01786 53.971 < 2e-16 ***
##
## Signif. codes:
## 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.281 on 3177 degrees of freedom
## Multiple R-squared: 0.4783, Adjusted R-squared: 0.4782
## F-statistic: 2913 on 1 and 3177 DF, p-value: < 2.2e-16
```

Step 5.1: Univariate Viz of Errors

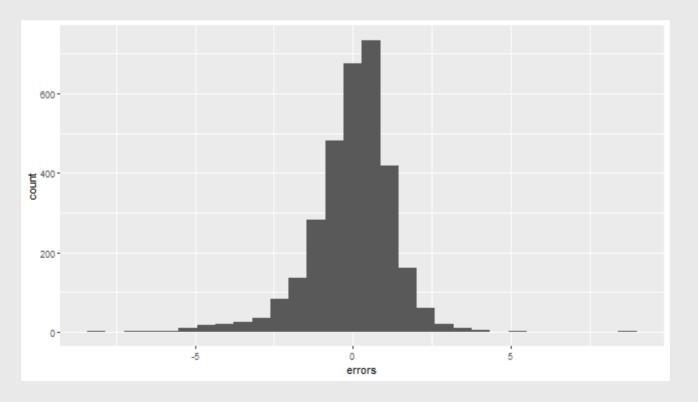
- Errors $\varepsilon = Y \hat{Y}$
 - In R, can also get them via resid() function

```
mv %>%
  mutate(errors_manual = gross_log - predict(m),
        errors_resid = resid(m))
```

```
## # A tibble: 3,179 × 24
     title rating genre year relea...¹ score votes direc...²
##
     ##
##
  1 Almost F... R Adve... 2000 Septem... 7.9 2.6 e5 Camero...
## 2 American... R Come... 2000 April ... 7.6 5.14e5 Mary H...
## 3 Gladiator R Acti... 2000 May 5,... 8.5 1.4 e6 Ridley...
##
   4 Requiem ... Unrat... Drama 2000 Decemb... 8.3 7.86e5 Darren...
## 5 Memento
                    Myst... 2000 May 25... 8.4 1.2 e6 Christ...
              R
  6 Cast Away PG-13 Adve... 2000 Decemb... 7.8 5.42e5 Robert...
##
   7 Scary Mo... R
                 Come... 2000 July 7... 6.2 2.38e5 Keenen...
##
   8 The Perf... PG-13 Acti... 2000 June 3... 6.4 1.6 e5 Wolfga...
##
   9 Coyote U... PG-13 Come... 2000 August... 5.7 1.08e5 David ...
##
              PG-13 Acti... 2000 July 1... 7.4 5.82e5 Bryan ...
## 10 X-Men
## # with 3 169 more rows 16 more variables: writer /chr
```

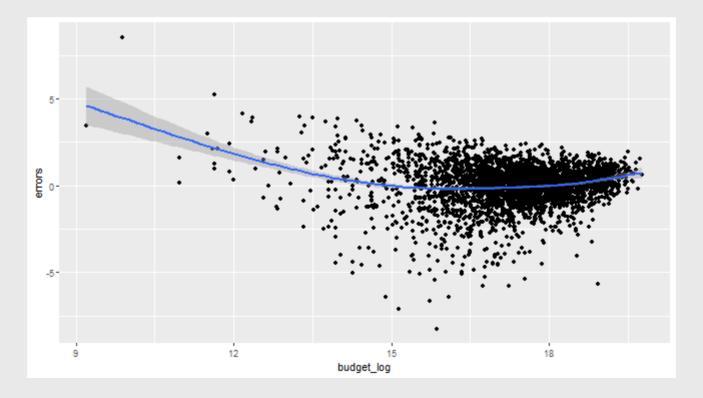
Step 5.1: Univariate Viz of Errors

```
mv %>%
  ggplot(aes(x = errors)) +
  geom_histogram()
```



Step 5.2: Multivariate Viz of Errors

```
mv %>%
  ggplot(aes(x = budget_log,y = errors)) +
  geom_point() +
  geom_smooth()
```



Step 5.3: Cross Validated RMSE

```
set.seed(123)
rmseBudget <- NULL
for(i in 1:100) {
  inds <- sample(1:nrow(mv), size = round(nrow(mv)/2), replace = F)</pre>
  train <- mv %>% slice(inds)
  test <- mv %>% slice(-inds)
  mTrain <- lm(gross log ~ budget log,train)</pre>
  test$preds <- predict(mTrain,newdata = test)</pre>
  rmse <- sqrt(mean((test$gross log - test$preds)^2,na.rm=T))</pre>
  rmseBudget <- c(rmseBudget,rmse)</pre>
mean(rmseBudget)
```

```
## [1] 1.279899
```

Thinking like a scientist

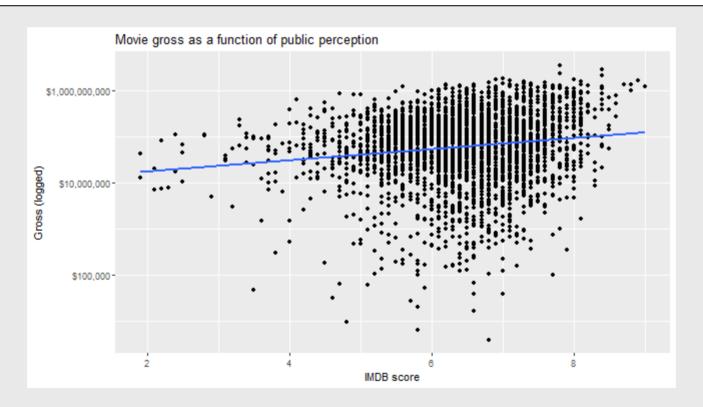
- Our previous model predicted gross as a function of budget
- Theoretically, is this sensible?
 - 1. Bigger budgets → famous actors → mass appeal → more tickets
 - 2. Bigger budgets → advertising money → mass appeal → more tickets
- But what if the movie is just...not good?

Alternative Theory

- Good movies make more money
 - Theory: good movies → recommendations → more tickets
- Predict gross with IMDB rating (score)

Alternative Model

pIMDB



Evaluating the Model

- Let's go straight to RMSE
 - We can have R calculate errors for us with residuals() command

```
m2 <- lm(gross_log ~ score,mv)
error <- residuals(m2)
(rmseScore <- sqrt(mean(error^2)))</pre>
```

[1] 1.753146

Even worse!

Multivariate Regression

• Recall that we can **model** our outcome with multiple **predictors**

$$Y = \alpha + \beta_1 X_1 + \beta_2 X_2 + \cdots + \varepsilon$$

How much better can we predict gross with BOTH budget and score?

```
m3 <- lm(gross_log ~ budget_log + score,mv)
error <- residuals(m3)
(rmseBudgScore <- sqrt(mean(error^2)))</pre>
```

```
## [1] 1.248817
```

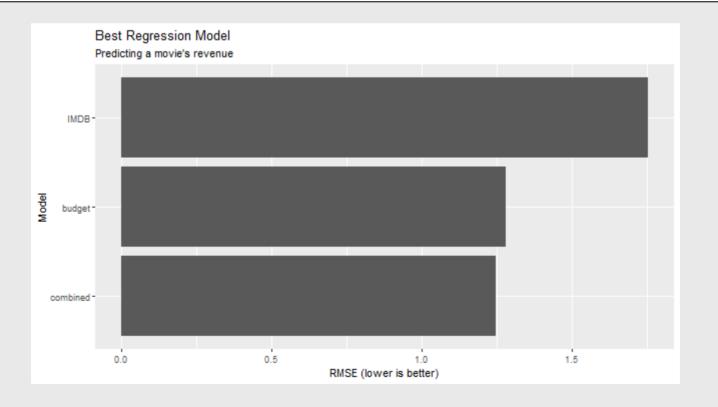
Comparing Models

Which model best predicts movie revenues?

Comparing Models

• Which model best predicts movie revenues?

р



Why RMSE?

- Want to understand how good / bad our model is
- Can use it to compare models

Why RMSE?

Do we improve our model with score?

```
set.seed(123)
bsRes <- NULL
for(i in 1:100) {
  inds <- sample(1:nrow(mv), size = round(nrow(mv)/2), replace = F)</pre>
  train <- mv %>% slice(inds)
  test <- mv %>% slice(-inds)
  mB <- lm(gross log ~ budget log,train)</pre>
  mS <- lm(gross log ~ score, train)</pre>
  mC <- lm(gross log ~ budget log + score, train)</pre>
  hsRes <- test %>%
    mutate(pB = predict(mB, newdata = test),
           pS = predict(mS, newdata = test),
           pC = predict(mC, newdata = test)) %>%
    summarise(Budget = sqrt(mean((gross log - pB)^2,na.rm=T)),
               Score = sqrt(mean((gross log - pS)^2,na.rm=T)),
               Combined = sqrt(mean((gross log - pC)^2,na.rm=T))) %>%
    bind rows(bsRes)
```

ASIDE: alternative code

• sample_n() and anti_join()

```
set.seed(123)
bsRes <- NULL
for(i in 1:100) {
  train <- my %>%
    sample n(size = round(nrow(.)*.8), replace = F)
  test <- mv %>%
    anti join(train)
  mB <- lm(gross log ~ budget log,train)</pre>
  mS <- lm(gross log ~ score, train)
  mC <- lm(gross log ~ budget log + score, train)</pre>
  bsRes <- test %>%
    mutate(pB = predict(mB, newdata = test),
           pS = predict(mS, newdata = test),
           pC = predict(mC,newdata = test)) %>%
    summarise(Budget = sqrt(mean((gross log - pB)^2,na.rm=T)),
              Score = sqrt(mean((gross log - pS)^2,na.rm=T)),
              Combined = sqrt(mean((gross_log - pC)^2,na.rm=T))) %>%
    bind rows(bsRes)
```

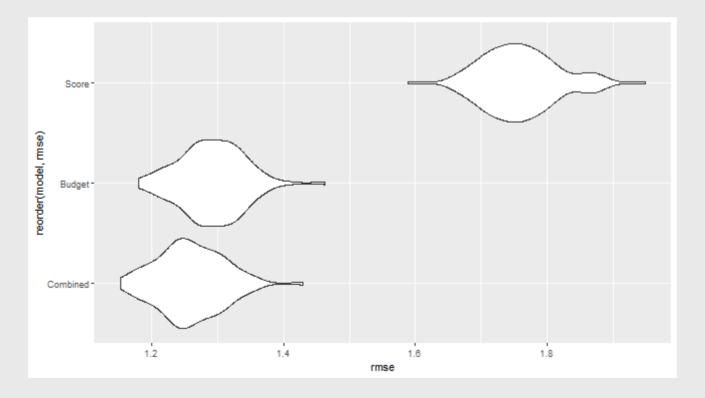
Why RMSE?

```
bsRes %>%
  summarise_all(mean,na.rm=T)
```

```
## # A tibble: 1 × 3
## Budget Score Combined
## <dbl> <dbl> <dbl>
## 1 1.29 1.76 1.26
```

Visualizing

```
bsRes %>%
  gather(model,rmse) %>%
  ggplot(aes(x = rmse,y = reorder(model,rmse))) +
  geom_violin()
```



Categorical Data

- Thus far, only using continuous variables
- But we can do regression with categorical data too!
- The Bechdel Test: 3 questions of a movie
 - 1. Does it have two women in it?
 - 2. Who talk to each other?
 - 3. About something other than a man?

```
mv %>%
  count(bechdel score)
```

```
## # A tibble: 5 × 2
     bechdel score
             <dbl> <int>
                     141
                    526
                 2 206
##
                    1185
##
                    1121
```

Research Question

- Do movies that pass the Bechdel Test make more money?
 - Theory: Women are ~50% of the population. Movies that pass the test are more appealing to women.
 - Hypothesis: Movies that pass the test make more money.
- Wrangling: Let's turn the bechdel_score variable into a binary

We can add the binary factor to our regression

```
summary(lm(gross_log ~ bechdel_factor,mv))
```

```
##
## Call:
  lm(formula = gross log ~ bechdel factor, data = mv)
##
  Residuals:
              10 Median
      Min
##
                            30
                                  Max
  -9.8817 -0.7918 0.2253 1.0831 3.8225
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
                   ## (Intercept)
  bechdel factorFail 0.15969 0.07423 2.151 0.0316 *
##
## Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  Residual standard error: 1.664 on 2056 degrees of freedom
    (1121 observations deleted due to missingness)
##
```

- Coefficient is positive
- What is the interpretation?
 - Movies that fail make more money...
 - ...than what?
 - Movies that pass the Bechdel Test
- Categorical variables are always interpreted in relation to the hold-out category!

- Movies that fail the test make more money!?
- REMEMBER: Correlation ≠ causation
 - What might explain this pattern?
 - Budgets in a sexist Hollywood!
 - Movies that fail the test get larger budgets
 - Budgets are positively associated with gross
- So we want to "control" for budget by adding it to our regression

```
mBechCtrl <- lm(gross_log ~ budget_log + bechdel_factor,mv)</pre>
```

summary(mBechCtrl)

```
##
## Call:
  lm(formula = gross log ~ budget log + bechdel factor, data = mv)
##
  Residuals:
             10 Median 30
##
     Min
                                 Max
## -8.6325 -0.5305 0.1287 0.6792 7.9370
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
                  2.30814 0.34497 6.691 2.85e-11 ***
## (Intercept)
## budget log 0.92089 0.01993 46.199 < 2e-16 ***
##
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.166 on 2055 degrees of freedom
    (1121 observations deleted due to missingness)
##
  Multiple R-squared: 0.5106, Adjusted R-squared:
```

- Our hypothesis is supported!
- What about non-binary categorical variables?

```
mv %>%
count(rating)
```

```
## # A tibble: 9 × 2
   rating
##
    <chr> <int>
##
  2 NC-17
  3 Not Rated
## 4 PG
               434
  5 PG-13
               1249
               1388
  6 R
  7 TV-MA
  8 Unrated
## 9 <NA>
```

• Let's first remove rarely-occurring ratings

```
mvAnalysis <- mv %>%
  filter(!rating %in% c('Approved','TV-14','TV-MA','TV-PG','X'))
```

```
summary(lm(gross_log ~ rating,mvAnalysis))
```

```
##
## Call:
  lm(formula = gross_log ~ rating, data = mvAnalysis)
##
  Residuals:
              10 Median
##
      Min
                            30
                                   Max
  -8.6749 -0.8189
                 0.1630 1.1082 5.2339
##
  Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
                19.1818
                            0.2177 88.113 < 2e-16 ***
##
  (Intercept)
  ratingNC-17
                 -2.4483 0.6884 -3.556 0.000381
  ratingNot Rated
                  -4.4322 0.3502 -12.655 < 2e-16 ***
  ratingPG
                  -0.3905
                            0.2308 -1.692 0.090784
##
  ratingPG-13
                  ratingR
                 -1.9123 0.2219 -8.618 < 2e-16 ***
  ratingUnrated
                            0.6426
                                    -7.246 5.38e-13 ***
                  -4.6564
##
  Signif. codes:
                   0.01 '*' 0.05 '.' 0.1 ' ' 1
         0.001
```

- Everything makes less money than the hold-out category!
 - "G"-rated movies are powered by children
- What if we wanted to compare to a different reference category?

summary(mRating2)

```
##
## Call:
  lm(formula = gross_log ~ rating, data = mvAnalysis)
##
  Residuals:
              10 Median
##
      Min
                             30
                                    Max
  -8.6749 -0.8184
                  0.1610 1.1082 5.2339
##
  Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
  (Intercept) 17.26952
                            0.04296 402.005 <2e-16 ***
  ratingPG-13 1.14905
                            0.06242 18.408 <2e-16 ***
  ratingPG
                 1.52178 0.08802 17.289 <2e-16 ***
  ratingG
                            0.22199 8.614
                                             <2e-16 ***
                  1.91231
                                             <2e-16 ***
  ratingNot Rated -2.51988
                            0.27782 -9.070
##
## Signif. codes:
    '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
  Residual standard error: 1.6 on 3154 degrees of freedom
```

Cross Validation

This is why sample_n() is useful

```
set.seed(123)
rmseRes_rating <- NULL
for(i in 1:100) {
   train <- mvAnalysis %>%
      group_by(rating) %>%
      sample_n(size = round(n()*.8),replace = F)
   test <- mvAnalysis %>% anti_join(train)

m <- lm(gross_log ~ rating,train)
rmseRes_rating <- test %>%
   mutate(preds = predict(m,newdata = test)) %>%
   summarise(rmse = sqrt(mean((gross_log - preds)^2,na.rm=T))) %>%
   bind_rows(rmseRes_rating)
}
```

```
## Joining, by = c("title", "rating", "genre", "year",
## "released", "score", "votes", "director", "writer", "star",
## "country", "budget", "gross", "company", "runtime", "id",
## "imdb_id", "bechdel_score", "boxoffice_a", "language",
## "gross_log", "budget_log", "errors", "bechdel_bin",
```

Quiz & Homework

- Go to Brightspace and take the 12th quiz
 - The password to take the quiz is ####
- Homework:
 - 1. Study for midterm!