Clustering

Part 1

Prof. Bisbee

Vanderbilt University

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Agenda

- 1. Structure in data
- 2. "Clustering"
- 3. Application

Structure

- Patterns in data
- Behind everything we've done thus far
 - Theory Testing: structure answers research question
 - Prediction: structure improves accuracy
- A third "camp" in data science: Learning

Learning

- No research question, no prediction goal
 - Just want to learn about structure of data
- Existing tools can do it
 - Run 1m regressions
 - Visualize a thousand variables
 - But these are slow
- This topic: letting algorithms learn for you!
 - Today: clustering

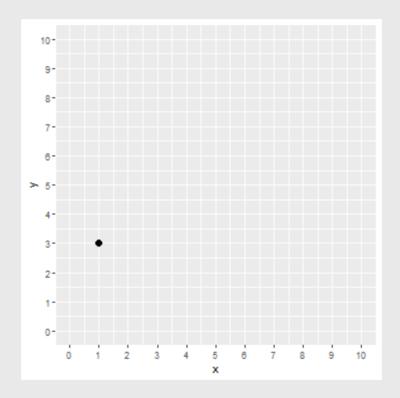
Clustering

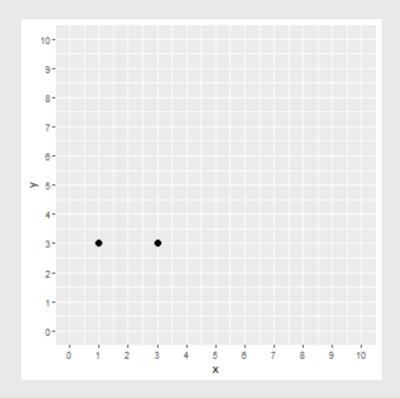
- Identify observations that belong to groups
 - Similarities → group belonging
- Part of broader set of methods to identify underlying "structure"
 - Today: *k*-means clustering algorithm

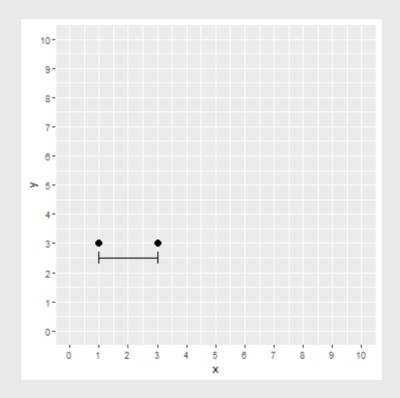
k-means Clustering

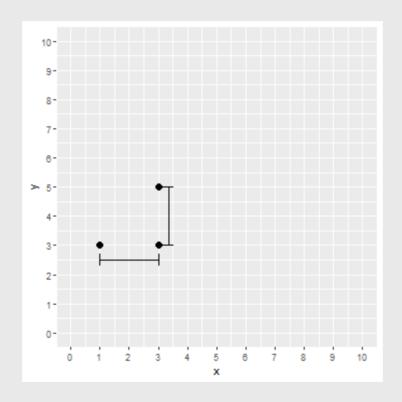
- k: number of clusters (i.e., groups)
- Algorithm assigns each observation to these \(1\dots k\) groups
 - 1. Choose initial "centroids" at random
 - 2. Assign observations to each centroid based on "Euclidean distance"
 - 3. Calculate new centroid based on mean of each variable
 - 4. Repeat until assignments stabilize

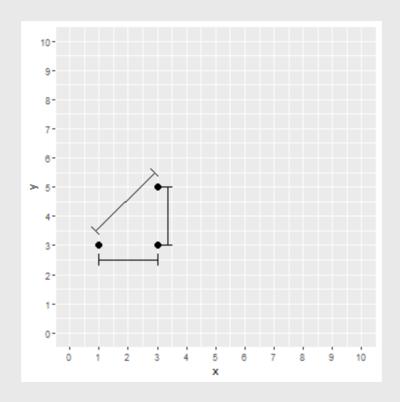


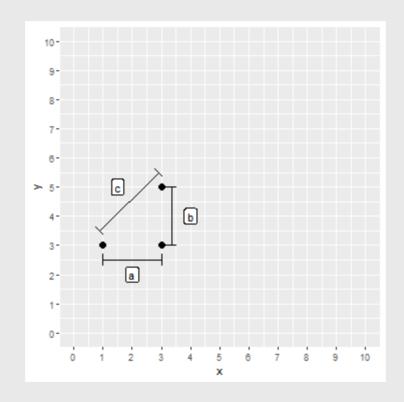








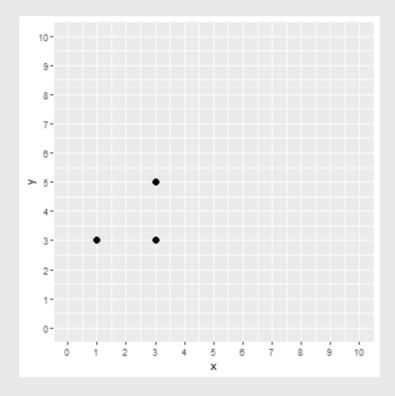




- $(c^2 = a^2 + b^2) \rightarrow (c = \sqrt{a^2 + b^2})$
- \(a^2 = $(x_2 x_1)^2 + (y_2 y_1)^2$ \) & \(b^2 = $(x_3 x_2)^2 + (y_3 y_2)^2$ \)
- General: \(\sqrt{\sum i (q i p i)^2}\)

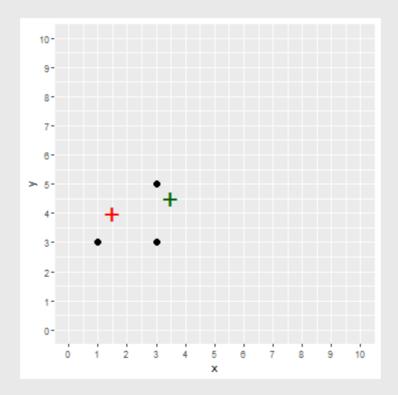
Centroids

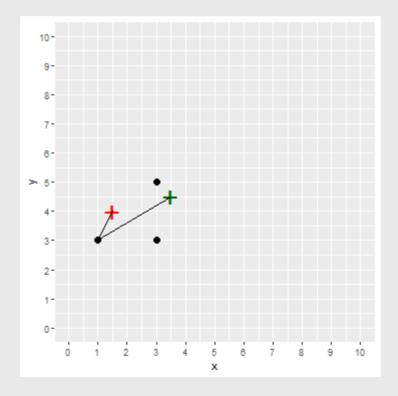
• The center of some data

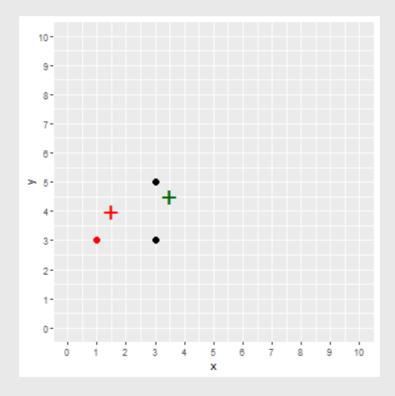


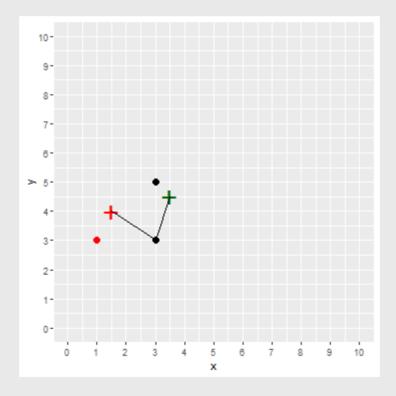
Centroids

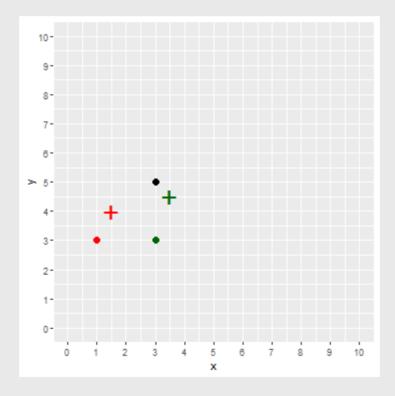
• Initially chosen at random by the algorithm

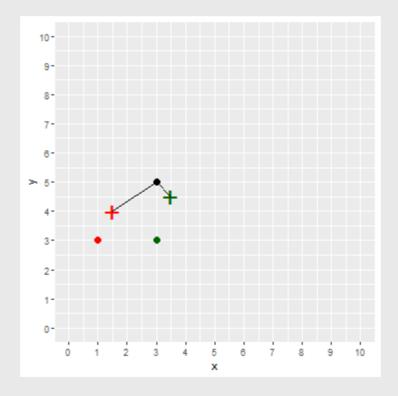


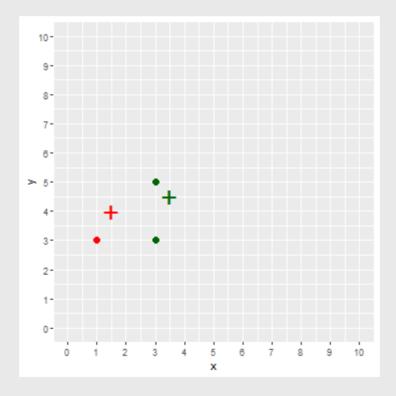






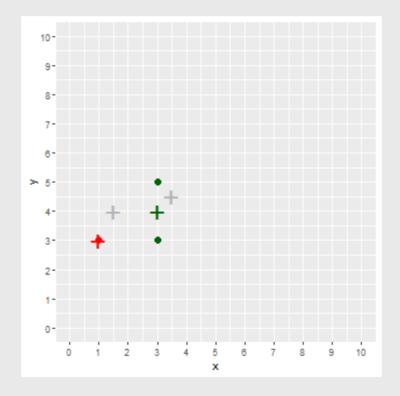






Recalculate Centroids

Set new centroids to mean of \(x\) and \(y\) among members



A simulation

Clustering to Learn about MCs

```
library(tidyverse)
dat <-
read_csv('https://raw.githubusercontent.com/jbisbee1/DS1000_S2024/main/
glimpse(dat)</pre>
```

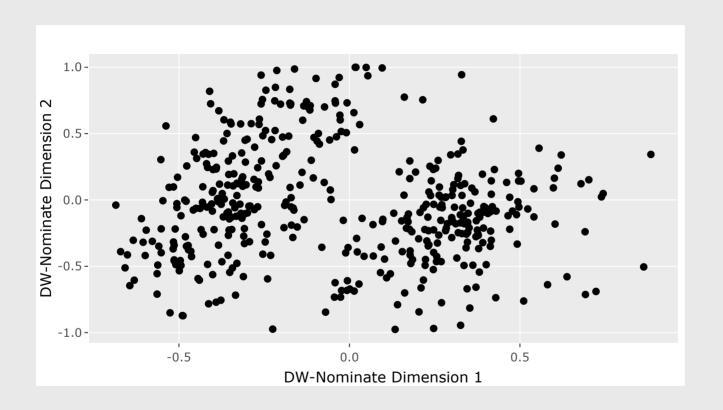
```
## Rows: 445
## Columns: 22
## $ congress
                                     <dbl> 97, 97, 97, 97, 97, ...
## $ chamber
                                     <chr> "President", "House"...
                                     <dbl> 99907, 10717, 10721,...
## $ icpsr
## $ state icpsr
                                     <dbl> 99, 41, 41, 41, 41, ...
## $ district code
                                     <dbl> 0, 2, 1, 4, 3, 5, 7,...
                                     <chr> "USA", "AL", "AL", "...
## $ state abbrev
## $ party code
                                     <dbl> 200, 200, 200, 100, ...
                                     <dbl> 0, 0, 0, 0, 0, 0, 0, ...
## $ occupancy
                                     <dbl> 0, 1, 1, 1, 1, 1, 1,...
## $ last means
## $ bioname
                                     <chr>> "REAGAN, Ronald Wils...
## $ bioguide id
                                     <chr> NA, "D000326", "E000...
## $ born
                                     <dbl> 1911, 1925, 1928, 19...
## $ died
                                     <dbl> 2004, 2008, 2019, 20...
## $ nominate dim1
                                     <dbl> 0.692, 0.398, 0.177,...
## $ nominate dim2
                                     <dbl> -0.713, -0.057, 0.16...
```

DW-NOMINATE

- DW-NOMINATE is a measure of how frequently different legislators vote together
- Often interpreted as "ideology"
- Two-dimensions:
 - 1. Standard left-right ideology (size of gov, redistribution, etc.)
 - 2. Second dimension changes, but typically salient social issues
- Can \((k\))-means clustering help us learn about legislators?

97th Congress (1981-1983)

97th Congress (1981-1983)



Intuition Check

- Can we see some clusters?
 - What do we think these are?
- Let's try estimating \((k\))-means!
- Function kmeans(x,centers,iter.max,nstart)
 - x is the data (only select the columns of interest!)
 - centers is the number of centroids
 - iter.max maximum amount of "steps"
 - nstart how many times to re-estimate

First, some light wrangling (convert numeric party code to character)

• Second, estimate kmeans() function

```
## K-means clustering with 2 clusters of sizes 214, 231
##
  Cluster means:
##
     nominate dim1 nominate dim2
         0.2607991
                        -0.2443271
## 1
        -0.3019524
                        0.1529177
##
##
   Clustering vector:
##
##
##
##
##
##
   [163<sup>-</sup>
```

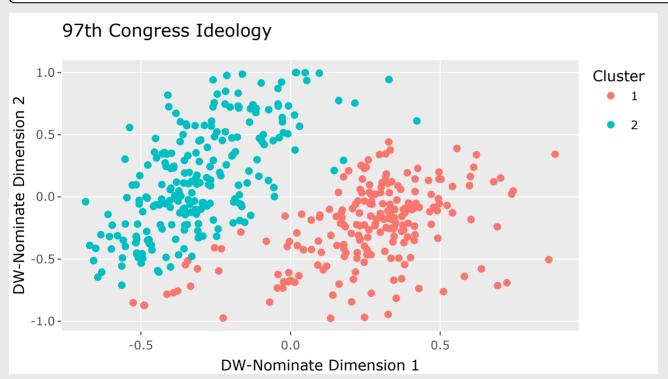
• Easier to see output with the help of tidymodels package

```
require(tidymodels)
tidy(m)
```

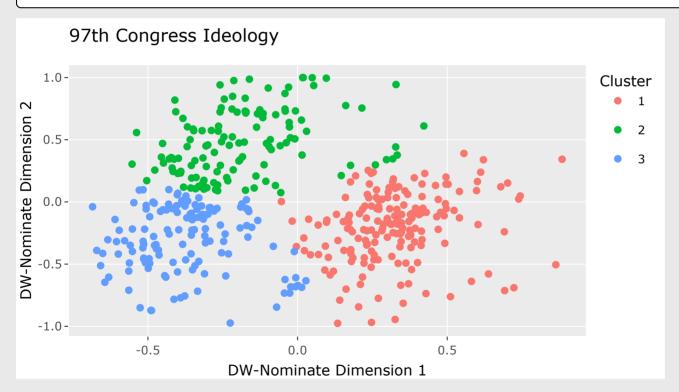
- First two columns are the locations of the centroids
- size is the number of observations associated with each group
- withinss is the errors each centroid makes

Third, plot points and color by cluster

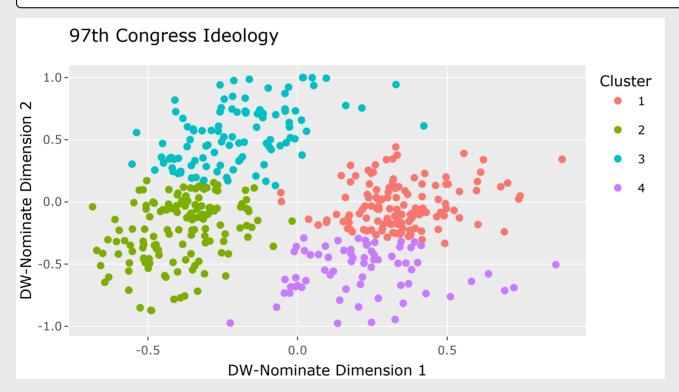
```
ggplotly(ggClust,tooltip = 'text')
```



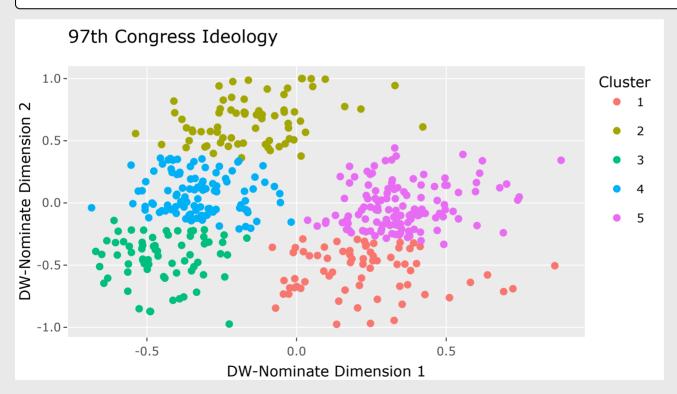
More Clusters



More Clusters

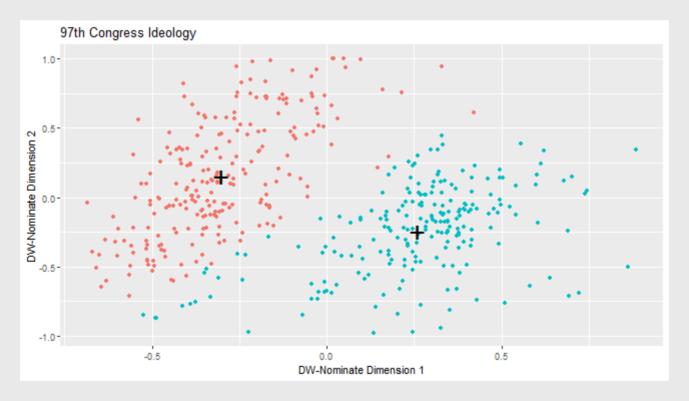


More Clusters



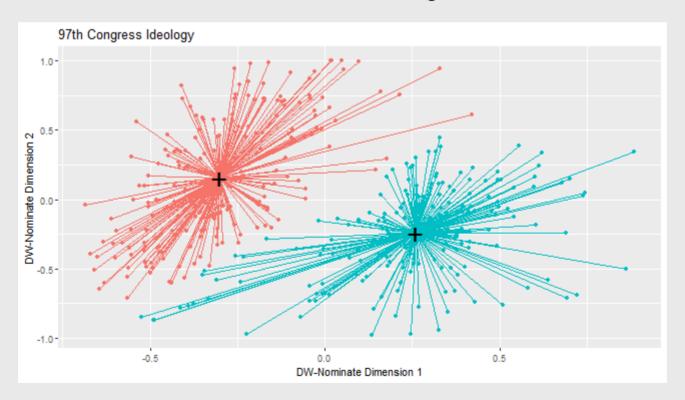
How many clusters?

- Recall from regression that we are interested in errors
- What are "errors" in the context of clustering?



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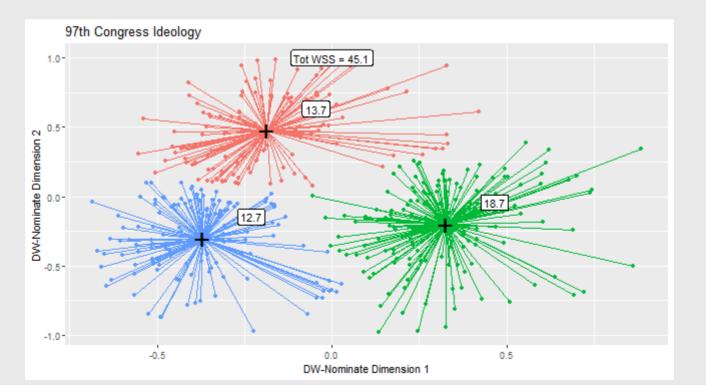


How many clusters?

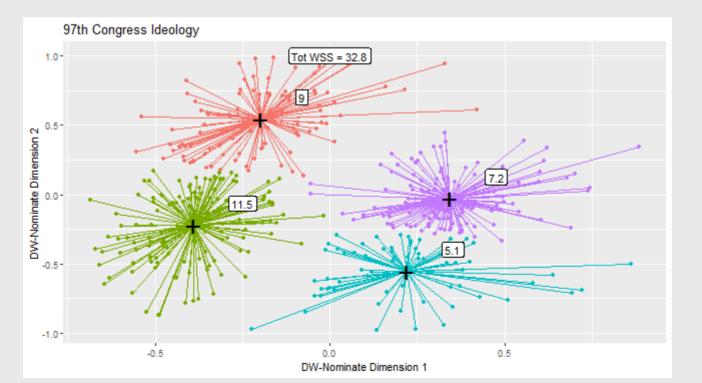
- Recall from regression that we are interested in errors
- What are "errors" in the context of clustering?
- Just the sum of each observation's distance from its centroid!
 - Within Sum of Squares (WSS)

```
tidy(m)
```

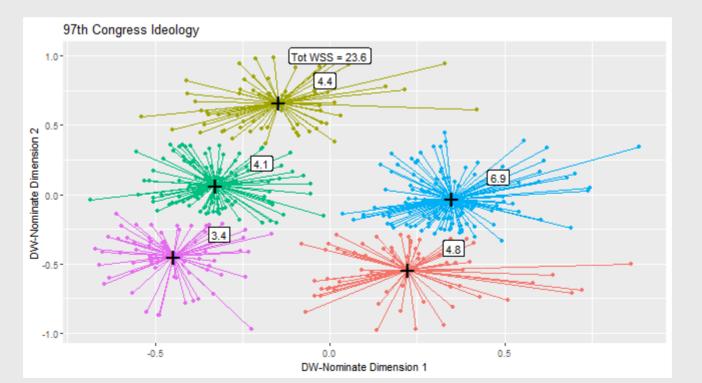
```
m.cluster <- datClust %>%
  select(-nameParty) %>% # Same as selecting two dimensions
  kmeans(centers = 3)
```



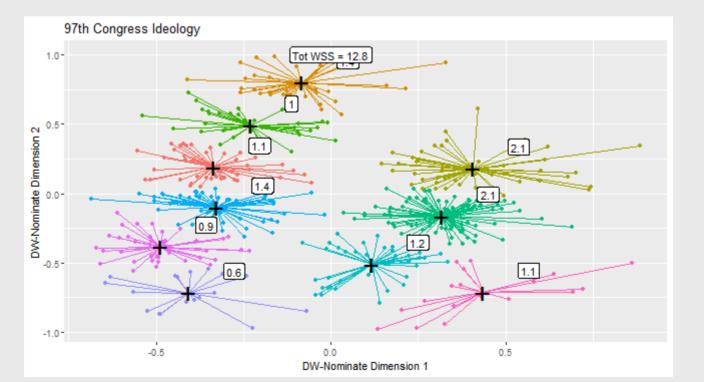
```
m.cluster <- datClust %>%
  select(-nameParty) %>%
  kmeans(centers = 4)
```



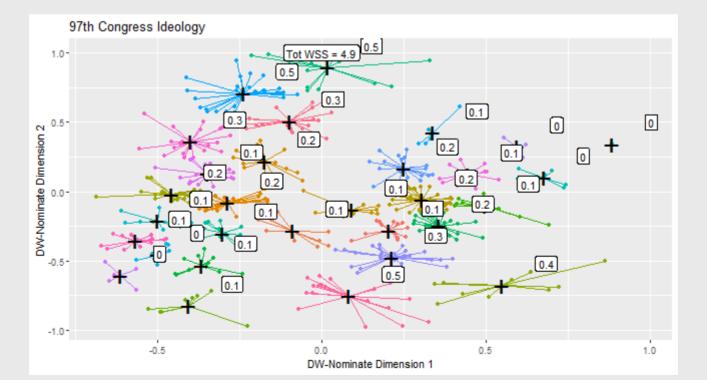
```
m.cluster <- datClust %>%
  select(-nameParty) %>%
  kmeans(centers = 5)
```



```
m.cluster <- datClust %>%
  select(-nameParty) %>%
  kmeans(centers = 10)
```



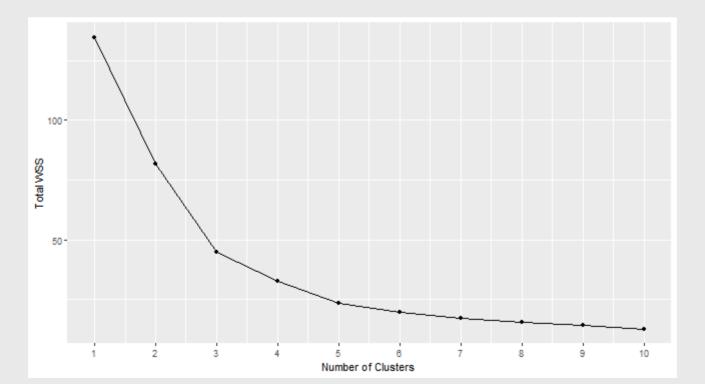
```
m.cluster <- datClust %>%
  select(-nameParty) %>%
  kmeans(centers = 30)
```

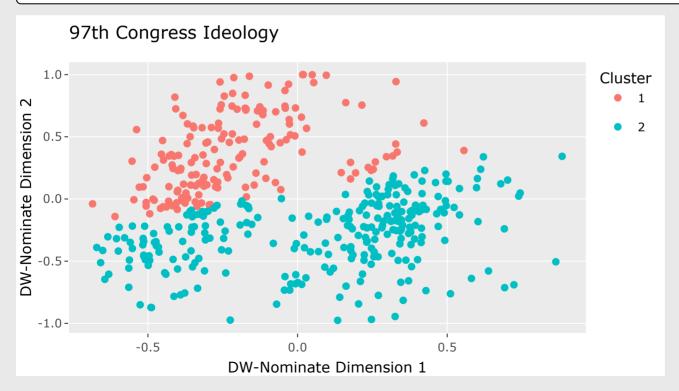


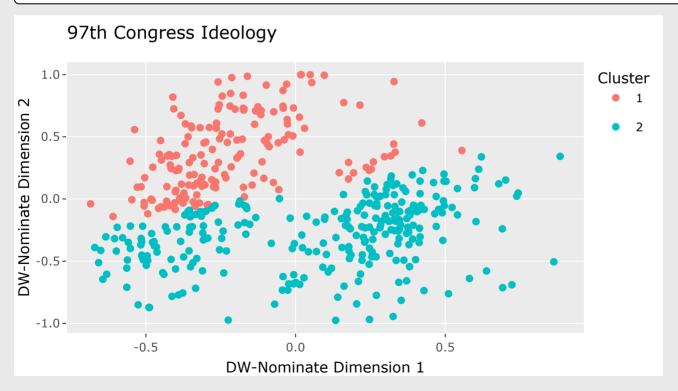
- But there's a trade-off!
 - Accuracy versus parsimony
- Simple rule: look for the "elbow"

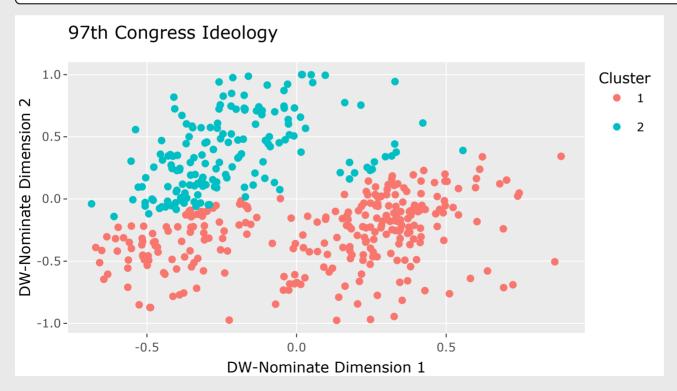
Looking for the "elbow"

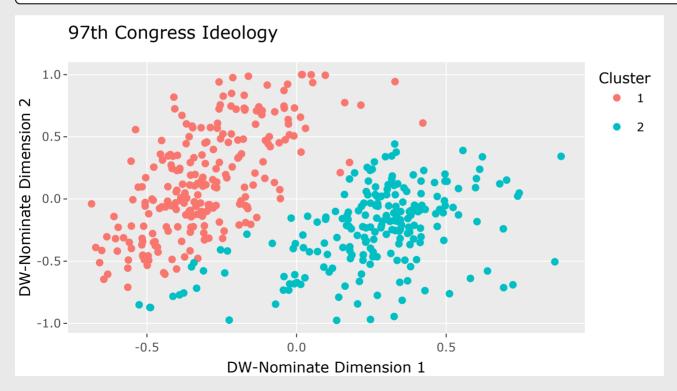
```
totWSS %>%
  ggplot(aes(x = k,y = totWSS)) +
  geom_line() + geom_point() +
  labs(x = 'Number of Clusters',y = 'Total WSS') +
  scale_x_continuous(breaks = 1:10)
```











Clustering Randomness

- Can overcome with nstart
 - Attempts multiple initial centroids and chooses the "best"

```
set.seed(42)
c1 <- kmeans(datClust %>% select(-nameParty),centers = 2,nstart = 25)
set.seed(123)
c2 <- kmeans(datClust %>% select(-nameParty),centers = 2,nstart = 25)
table(c1$cluster,c2$cluster)
```

```
##
## 1 166 0
## 2 0 279
```

Is Polarization Increasing?

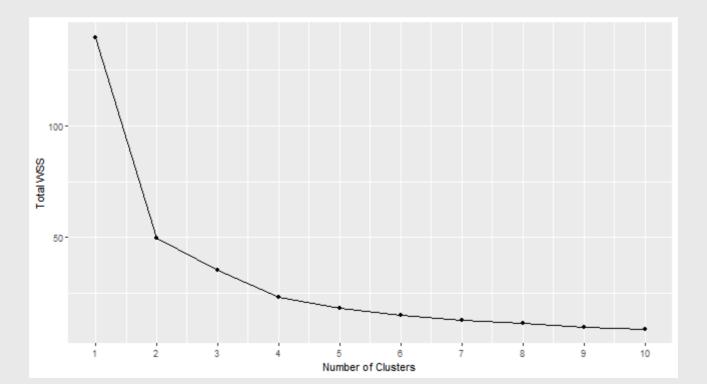
Compare 97th Congress (1981-1983) to 117th Congress (2021-2023)

Check for the "elbow"

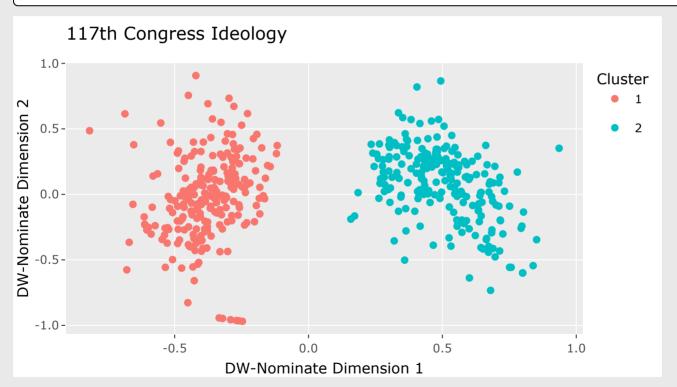
```
totWSS <- NULL
for(k in 1:10) {
    m.cluster <- datClust %>%
        select(-nameParty) %>% kmeans(centers = k,nstart = 25)
    totWSS <- data.frame(totWSS = m.cluster$tot.withinss,k = k) %>%
        bind_rows(totWSS)
}
```

Check for the "elbow"

```
totWSS %>%
  ggplot(aes(x = k,y = totWSS)) +
  geom_line() + geom_point() +
  labs(x = 'Number of Clusters',y = 'Total WSS') +
  scale_x_continuous(breaks = 1:10)
```



Growing polarization?



Conclusion

- Clustering is part of a third camp of data science
 - 1. Theory Testing
 - 2. Prediction
 - 3. Learning
- Next lecture: clustering applied to **TEXT**