

Uncertainty

How confident are we?

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Agenda

1. Uncertainty
2. More NBA data
3. Bootstrap Sampling

The Missing Ingredient

- Thus far we have:
 1. Tested whether **selective** schools have **higher SAT scores**: Yes
 2. Tested Trump's theory that **polls were biased against him**: No
 3. Tested whether RDD polls **contact more Trump supporters**: No
 4. Tested whether state polls **accurately predicted the president**: No
- We want to do more than say "Yes" or "No" when answering a Research Question or making a Prediction
- We want to express our **confidence**

What is "confidence"?

- In frequentist statistics:
 - How often your conclusion would be correct if you were able to run an "experiment" many times
 - How often your conclusion would be correct if you were able to observe the world many times
- **Research Question**: Are NBA players in their rookie season more prone to turnovers?
 - **Theory**: ??
 - **Hypothesis**: ??
- **Analysis**: compare `tov` by `isRookie`

NBA Example

```
require(tidyverse)
nba <-
read_rds('https://github.com/jbisbee1/DS1000_S2024/raw/main/data/nba_pl
glimpse(nba %>% select(tov,isRookie))
```

```
## Rows: 530
## Columns: 2
## $ tov      <dbl> 144, 4, 135, 14, 121, 8, 33, 6, 28, 2, 72...
## $ isRookie <lgl> FALSE, FALSE, FALSE, FALSE, FALSE, TRUE, ...
```

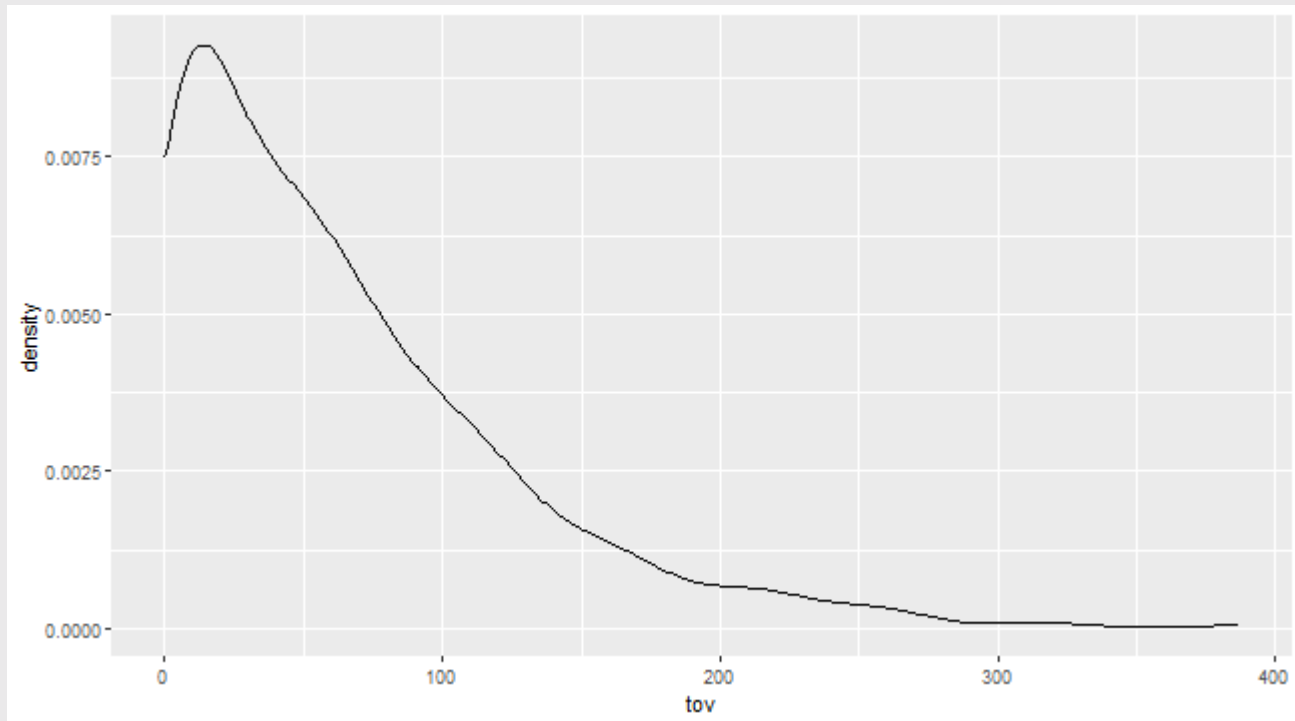
Look

```
summary(nba %>% select(tov,isRookie))
```

```
##      tov      isRookie
##  Min.   : 0.00  Mode :logical
## 1st Qu.: 14.25  FALSE:425
## Median : 47.00  TRUE :105
## Mean   : 62.82
## 3rd Qu.: 91.75
## Max.   :387.00
```

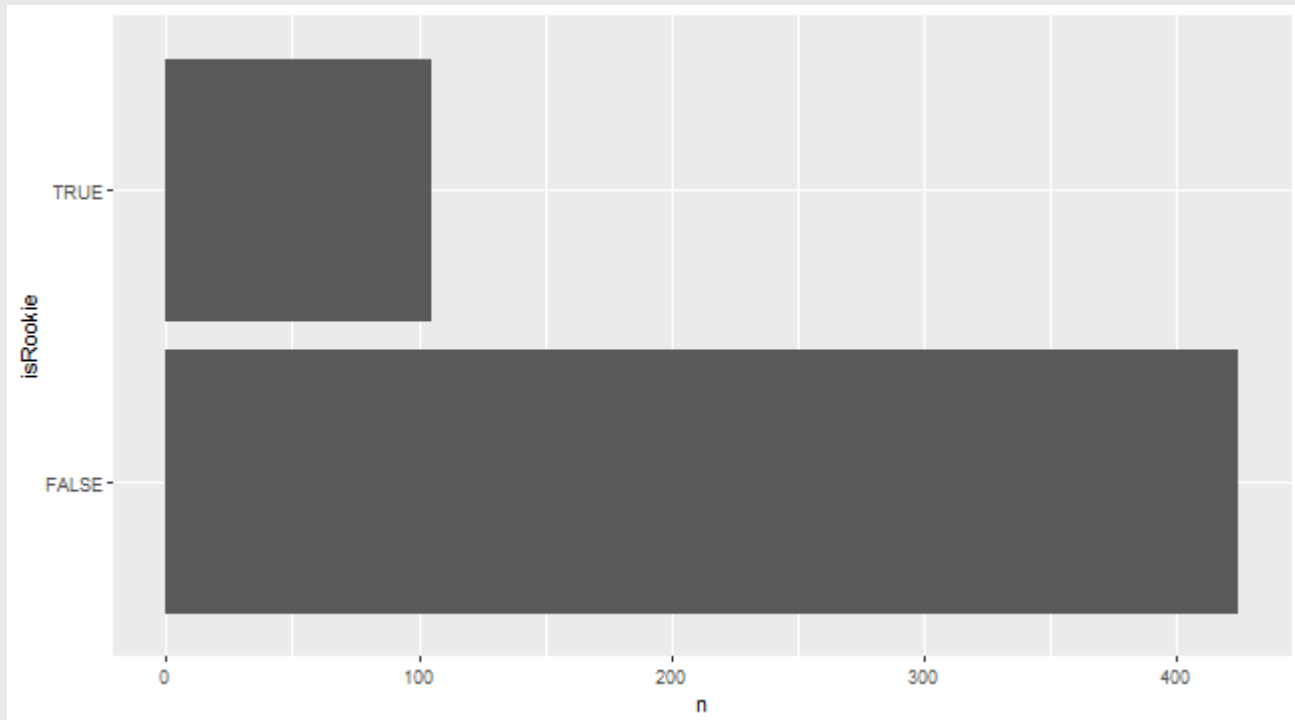
Visualize: Univariate Y

```
nba %>%  
  ggplot(aes(x = tov)) +  
  geom_density()
```



Visualize: Univariate X

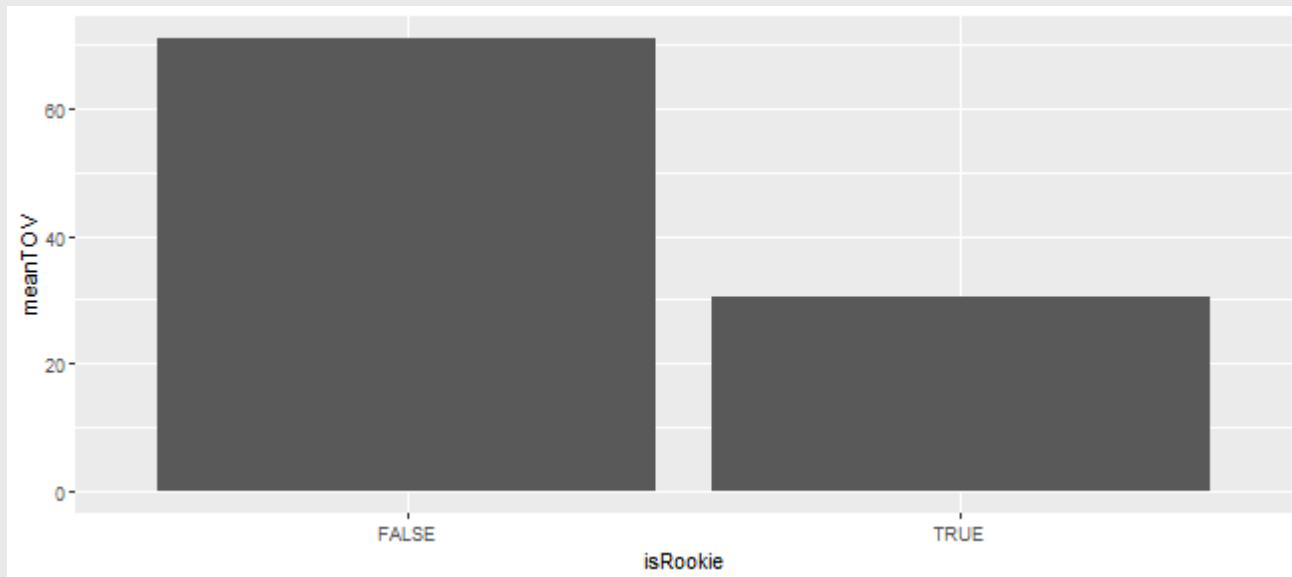
```
nba %>%  
  count(isRookie) %>%  
  ggplot(aes(x = n, y = isRookie)) +  
  geom_bar(stat = 'identity')
```



Visualize: Multivariate

- Option #1: `summarise()` data prior to plotting

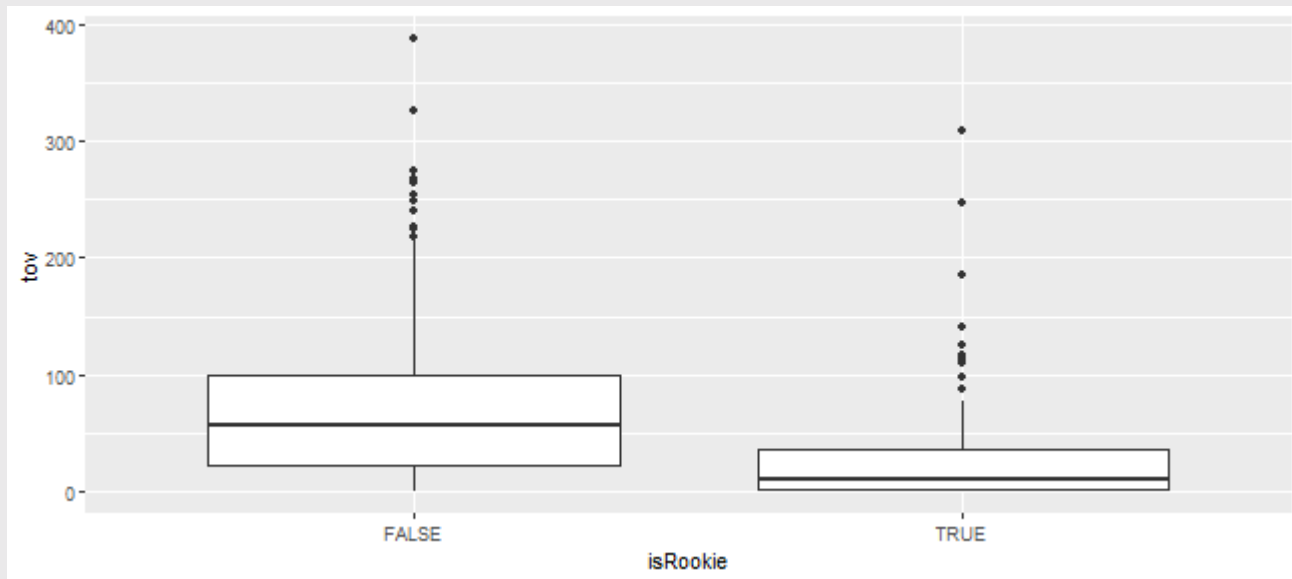
```
nba %>%  
  group_by(isRookie) %>%  
  summarise(meanTOV = mean(tov,na.rm=T)) %>%  
  ggplot(aes(x = isRookie,y = meanTOV)) +  
  geom_bar(stat = 'identity')
```



Visualize: Multivariate

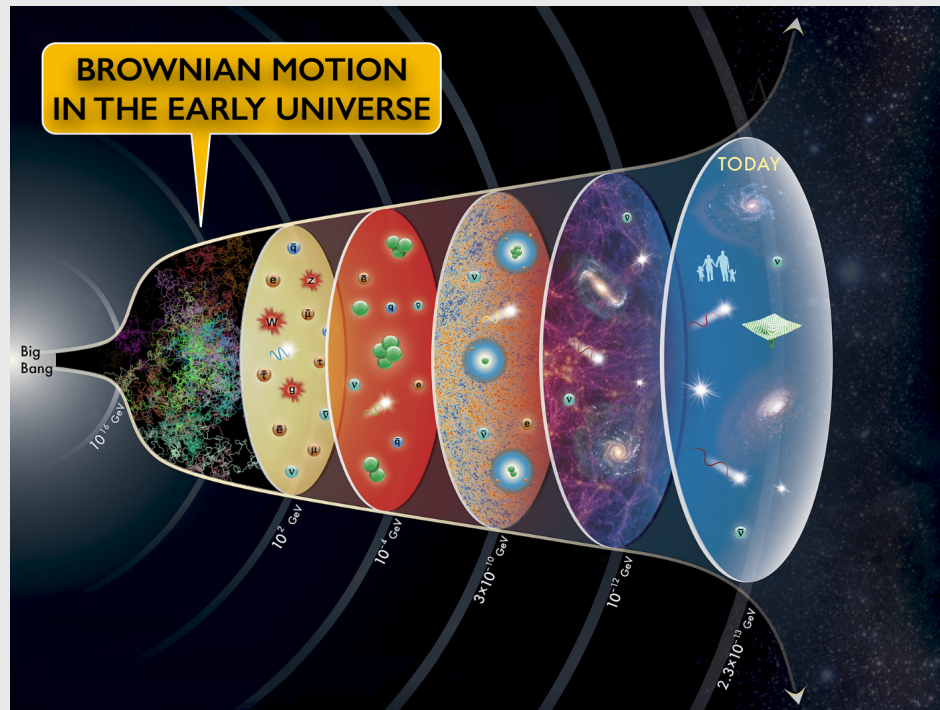
- Option #2: plot raw data

```
nba %>%  
  ggplot(aes(x = isRookie,y = tov)) +  
  geom_boxplot()
```



Uncertainty

- Are rookies **better** than more senior players?
- Big philosophical step back
 - We live in a stochastic universe!



Uncertainty

- Are rookies **better** than more senior players?
- Populations versus samples
 - Intro stats: uncertainty due to **sample**

Uncertainty

- Big philosophical step back
 - We live in a stochastic universe!
- What does **better** mean?
 - **Theory**: An innate quality in greater abundance
 - **Prediction**: If we had to bet on who turns over the ball less, who do we choose?
- How **confident** would we be with this bet?

Uncertainty

- If the universe is inherently stochastic, we are inherently uncertain
 - We THINK rookies are more careful passers, but not 100% certain
- How to measure this?
 - Run 100 experimental seasons
 - Record turnovers for rookies and non-rookies for each season
 - Calculate how many times rookies turned the ball over less than non-rookies
- 90 seasons out of 100 → 90% confident / certainty
- 100 seasons out of 100 → 100%?
- **FUNDAMENTAL STOCHASTIC NATURE OF REALITY (FSNoR)**

Uncertainty

- Running 100 experimental seasons is impossible
 1. We are not Adam Silver
 2. Even if we were Adam Silver, 100 seasons = a century of basketball!



Uncertainty

- Running 100 experimental seasons is impossible
 1. We are not Adam Silver
 2. Even if we were Adam Silver, 100 seasons = a century of basketball!
 3. If we were God? 100 seasons with the same players?
- *STILL wouldn't be 100% certain due to **FSNoR***
 - (**F**undamental **S**tochastic **N**ature **o**f **R**eality)

Uncertainty

- But we are data scientists
- Take 1 season of basketball but sample it randomly
- **Bootstrap sampling**
- **Theory**: By mimicking the sampling process, we can simulate a God experiment
 - (NB: this goes much deeper. Uncertainty from bootstrap combines FSNOR + sampling uncertainty.)
- **Practice**: `sample_n()` + `for()` loops

Bootstrap Demo Step 1

- One randomly sampled player via `sample_n(size,replace)`
 - `size`: how many samples (from 1 to all observations)
 - `replace`: whether to put the sample back (`TRUE` or `FALSE`)

```
set.seed(123) # Ensure we can reproduce results exactly
```

```
nba %>%  
  sample_n(size = 1,replace = T) %>%  
  select(namePlayer,slugSeason,isRookie,tov)
```

```
## # A tibble: 1 × 4  
##   namePlayer    slugSeason isRookie   tov  
##   <chr>        <chr>      <lgl>    <dbl>  
## 1 Moritz Wagner 2018-19    TRUE      39
```

Bootstrap Demo Step 2

- Two randomly sampled players

```
set.seed(123)
nba %>%
  sample_n(size = 1, replace = T) %>%
  select(namePlayer, slugSeason, isRookie, tov)
```

```
## # A tibble: 1 × 4
##   namePlayer    slugSeason isRookie   tov
##   <chr>         <chr>      <lgl>    <dbl>
## 1 Moritz Wagner 2018-19    TRUE      39
```

```
nba %>%
  sample_n(size = 1, replace = T) %>%
  select(namePlayer, slugSeason, isRookie, tov)
```

```
## # A tibble: 1 × 4
##   namePlayer slugSeason isRookie   tov
##   <chr>      <chr>      <lgl>    <dbl>
## 1 Sam Dekker 2018-19    FALSE    24
```

Bootstrap Demo Step 2

- OR two randomly sampled players

```
set.seed(123)

nba %>%
  sample_n(size = 2, replace = T) %>%
  select(namePlayer, slugSeason, isRookie, tov)
```

```
## # A tibble: 2 × 4
##   namePlayer      slugSeason isRookie    tov
##   <chr>          <chr>      <lgl>    <dbl>
## 1 Moritz Wagner  2018-19    TRUE      39
## 2 Sam Dekker     2018-19    FALSE     24
```

Bootstrap Demo Step 3

- Randomly sample all players: `size = nrow(nba)` (or `nrow(.)`)

```
set.seed(123)
```

```
nba %>%
```

```
  sample_n(size = nrow(nba), replace = T) %>% # Same as nrow(.)
```

```
  select(namePlayer, slugSeason, isRookie, tov)
```

```
## # A tibble: 530 × 4
```

```
##   namePlayer      slugSeason isRookie   tov
##   <chr>          <chr>      <lgl>   <dbl>
## 1 Moritz Wagner  2018-19    TRUE     39
## 2 Sam Dekker     2018-19   FALSE    24
## 3 Joe Harris     2018-19   FALSE   121
## 4 Jonas Valanciunas 2018-19   FALSE    90
## 5 John Holland   2018-19   FALSE     0
## 6 Angel Delgado   2018-19    TRUE     0
## 7 Donovan Mitchell 2018-19   FALSE   218
## 8 Damian Jones    2018-19   FALSE    16
## 9 Luke Kornet     2018-19   FALSE    25
## 10 Justin Anderson 2018-19   FALSE    23
## # i 520 more rows
```

Bootstrap Demo Step 4

- Linking to **confidence**: Do we draw the same conclusion twice?

```
set.seed(123)

# Bootstrapped Season #1
bsSeason1 <- nba %>%
  sample_n(size = nrow(.),replace = T) %>%
  select(isRookie,tov) %>%
  mutate(bsSeason = 1)

# Bootstrapped Season #2
bsSeason2 <- nba %>%
  sample_n(size = nrow(.),replace = T) %>%
  select(isRookie,tov) %>%
  mutate(bsSeason = 2)
```

Bootstrap Demo Step 4

- Linking to **confidence**: Do we draw the same conclusion twice?

```
bsSeason1 %>%  
  group_by(isRookie) %>%  
  summarise(mean_tov = mean(tov))
```

```
## # A tibble: 2 × 2  
##   isRookie mean_tov  
##   <lgl>      <dbl>  
## 1 FALSE      68.6  
## 2 TRUE       36.9
```

```
bsSeason2 %>%  
  group_by(isRookie) %>%  
  summarise(mean_tov = mean(tov))
```

```
## # A tibble: 2 × 2  
##   isRookie mean_tov  
##   <lgl>      <dbl>  
## 1 FALSE      65.6  
## 2 TRUE       28.5
```

Bootstrap Demo Step 5

- Want to do this 100 times!
- Use a `for()` loop to make it cleaner
- A `for()` loop repeats the same code multiple times
 - Benefit: don't need to copy and paste a chunk of code 100 times
 - Just put a chunk of code in a loop that repeats 100 times!

```
set.seed(123) # Ensure you'll get the same results each time
bsSeasons <- NULL # Instantiate empty object
for(bsSeason in 1:100) { # Repeat 100 times
  tmpSeason <- nba %>%
    sample_n(size = nrow(.), replace = T) %>% # Sample the data
    select(isRookie, tov) %>% # Select variables of interest
    mutate(bsSeasonNumber = bsSeason) # Save the simulation ID
  bsSeasons <- bind_rows(bsSeasons, tmpSeason) # Append to the empty
object!
}
```


Bootstrap to measure Confidence

- Compare rookie versus non-rookie turnovers each season

```
bsSeasons %>%  
  group_by(bsSeasonNumber, isRookie) %>%  
  summarise(mean_tov = mean(tov), .groups = 'drop')
```

```
## # A tibble: 200 × 3  
##   bsSeasonNumber isRookie mean_tov  
##           <int> <lgl>      <dbl>  
## 1             1 FALSE      68.6  
## 2             1 TRUE       36.9  
## 3             2 FALSE      65.6  
## 4             2 TRUE       28.5  
## 5             3 FALSE      62.5  
## 6             3 TRUE       26.5  
## 7             4 FALSE      67.5  
## 8             4 TRUE       29.9  
## 9             5 FALSE      74.8  
## 10            5 TRUE       31.3  
## # i 190 more rows
```

Bootstrap to measure Confidence

- Compare rookie versus non-rookie turnovers each season

```
bsSeasons %>%  
  group_by(bsSeasonNumber,isRookie) %>%  
  summarise(mean_tov = mean(tov),.groups = 'drop') %>%  
  spread(isRookie,mean_tov)
```

```
## # A tibble: 100 × 3  
##   bsSeasonNumber `FALSE` `TRUE`  
##   <int>      <dbl>  <dbl>  
## 1         1      68.6   36.9  
## 2         2      65.6   28.5  
## 3         3      62.5   26.5  
## 4         4      67.5   29.9  
## 5         5      74.8   31.3  
## 6         6      70.7   31.6  
## 7         7      73.7   19.8  
## 8         8      73.7    33  
## 9         9      65.0   24.3  
## 10        10      72.2   28.0  
## # i 90 more rows
```

Bootstrap to measure Confidence

- Compare rookie versus non-rookie turnovers each season

```
bsSeasons %>%  
  group_by(bsSeasonNumber,isRookie) %>%  
  summarise(mean_tov = mean(tov),.groups = 'drop') %>%  
  spread(isRookie,mean_tov) %>%  
  filter(complete.cases(.)) %>%  
  mutate(rookieBetter = ifelse(`FALSE` > `TRUE`,1,0))
```

```
## # A tibble: 100 × 4  
##   bsSeasonNumber `FALSE` `TRUE` rookieBetter  
##           <int>   <dbl> <dbl>         <dbl>  
## 1             1    68.6   36.9           1  
## 2             2    65.6   28.5           1  
## 3             3    62.5   26.5           1  
## 4             4    67.5   29.9           1  
## 5             5    74.8   31.3           1  
## 6             6    70.7   31.6           1  
## 7             7    73.7   19.8           1  
## 8             8    73.7   33            1  
## 9             9    65.0   24.3           1  
## 10            10    72.2   28.0           1
```

Bootstrap to measure Confidence

- Compare UVA and UT's FT percentages in each season

```
(conf <- bsSeasons %>%  
  group_by(bsSeasonNumber,isRookie) %>%  
  summarise(mean_tov = mean(tov),.groups = 'drop') %>%  
  spread(isRookie,mean_tov) %>%  
  filter(complete.cases(.)) %>%  
  mutate(rookieBetter = ifelse(`FALSE` > `TRUE`,1,0)) %>%  
  summarise(rookieBetter = mean(rookieBetter)))
```

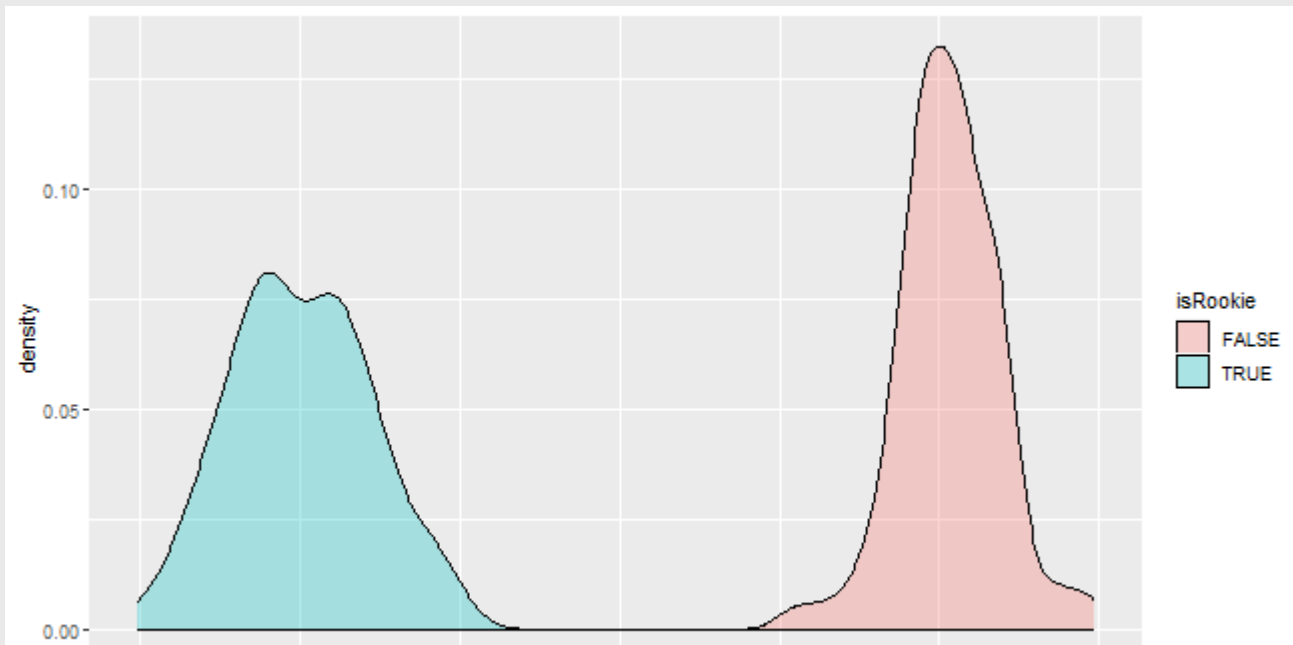
```
## # A tibble: 1 × 1  
##   rookieBetter  
##         <dbl>  
## 1             1
```

- Rookies have fewer turnovers 100% of the time! (How much do you bet on next season?)

Other ways to use bootstraps

- Could plot the **distributions** for each school

```
bsSeasons %>%  
  group_by(bsSeasonNumber,isRookie) %>%  
  summarise(mean_tov = mean(tov),.groups = 'drop') %>%  
  ggplot(aes(x = mean_tov,fill = isRookie)) +  
  geom_density(alpha = .3)
```



Other ways to use bootstraps

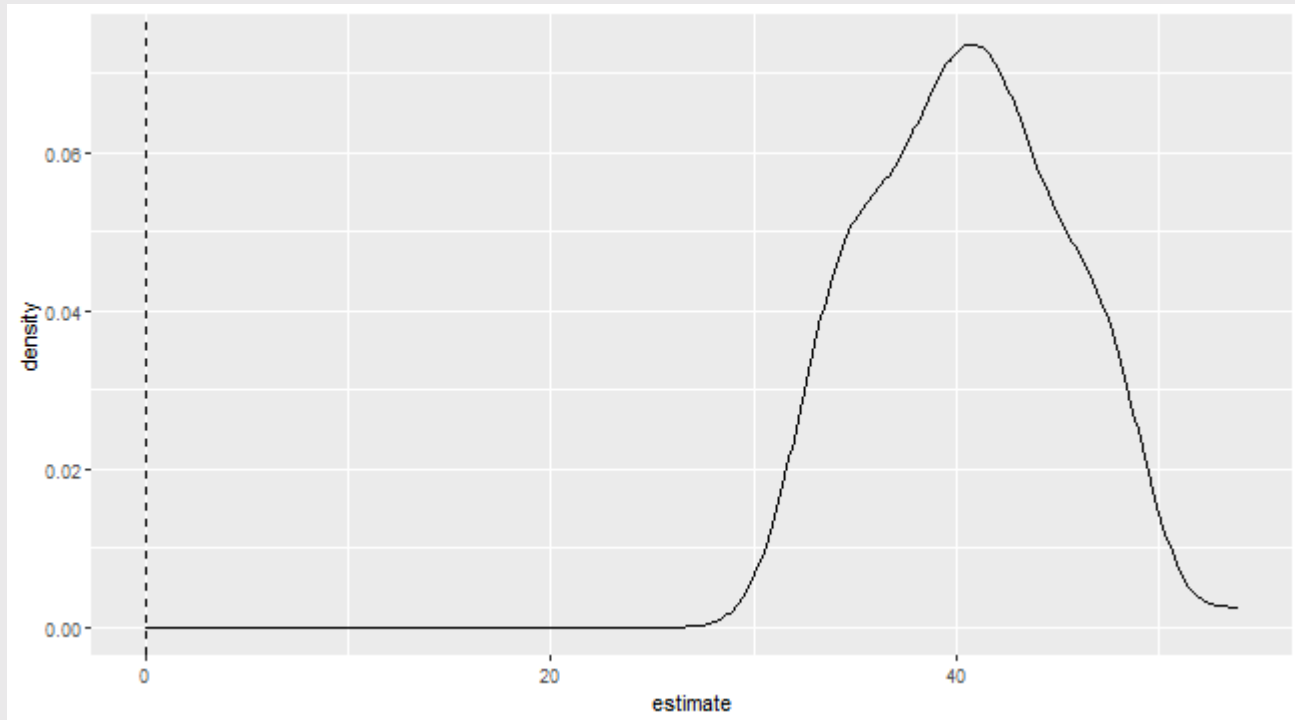
- Could plot the **distributions** of the "estimate"

```
p <- bsSeasons %>%  
  group_by(bsSeasonNumber,isRookie) %>%  
  summarise(mean_tov = mean(tov),.groups = 'drop') %>%  
  spread(isRookie,mean_tov) %>%  
  mutate(estimate = `FALSE` - `TRUE`) %>%  
  ggplot(aes(x = estimate)) +  
  geom_density(alpha = .3) +  
  geom_vline(xintercept = 0,linetype = 'dashed')
```

Other ways to use bootstraps

- Could plot the **distributions** of the "estimate"

p



Where to calculate the "estimate"

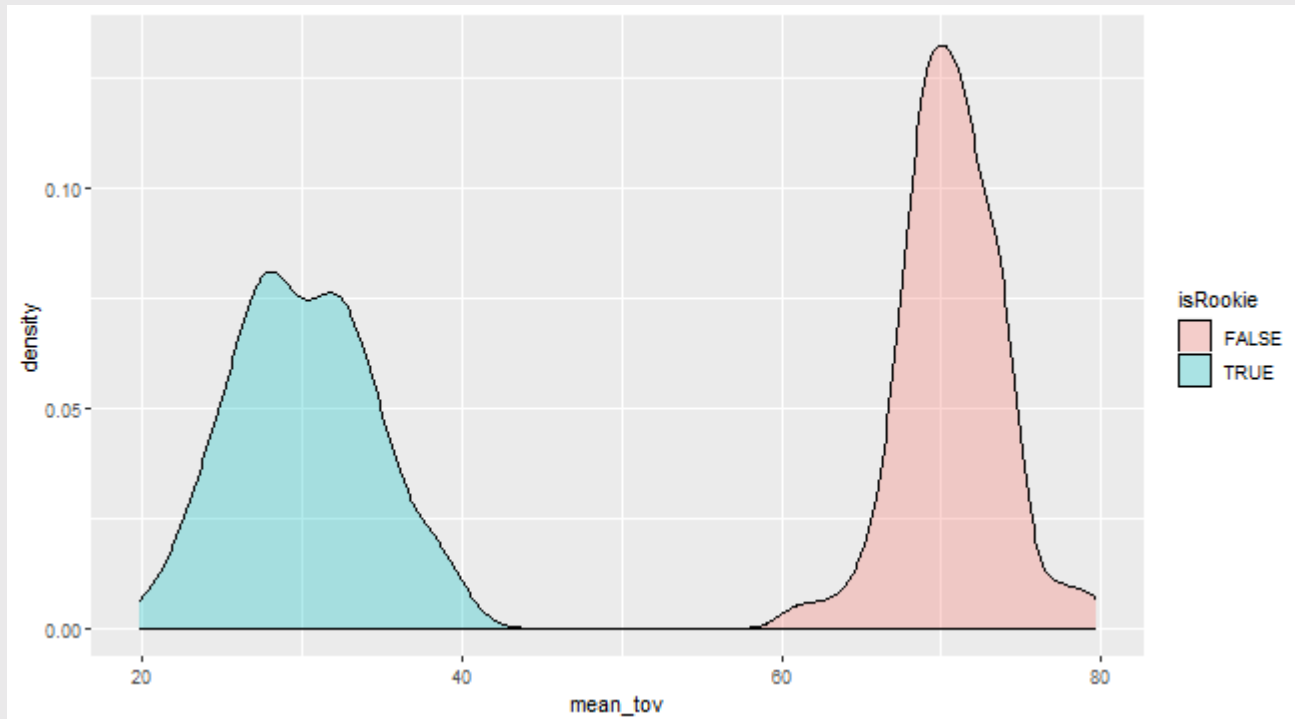
- **First** we created a new dataset of 100 simulated seasons
- **Then** we calculate average FT % for TN and UVA for each simulation
- **Finally** we calculate proportion of times average is higher for TN
- **BUT!** It is equally valid to calculate the "estimate" *within* the `for()` loop

```
set.seed(123)
bsRes <- NULL
for(counter in 1:100) {
  tmpEst <- nba %>%
    sample_n(size = nrow(.), replace = T) %>%
    group_by(isRookie) %>%
    summarise(mean_tov = mean(tov, na.rm=T)) %>%
    mutate(bsSeason = counter)

  bsRes <- bind_rows(bsRes, tmpEst)
}
```

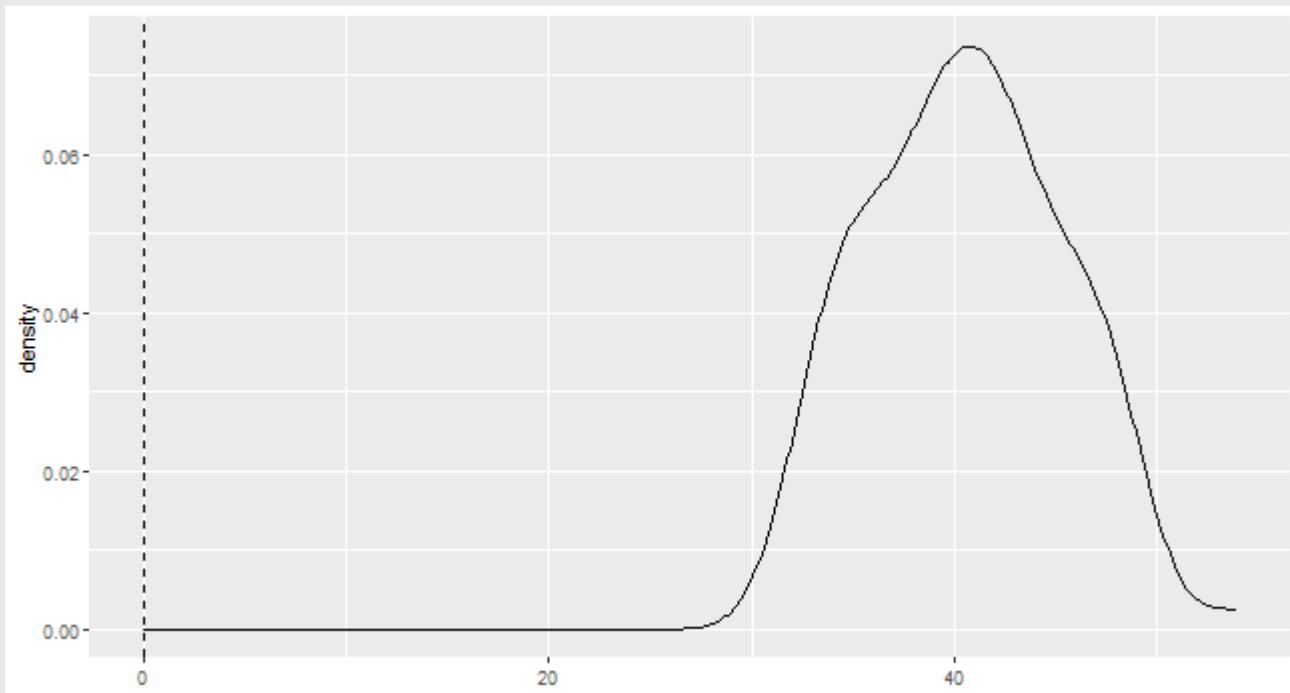

Where to calculate the "estimate"

```
bsRes %>%  
  ggplot(aes(x = mean_tov, fill = isRookie)) +  
  geom_density(alpha = .3)
```



Where to calculate the "estimate"

```
bsRes %>%  
  spread(isRookie,mean_tov) %>%  
  mutate(rookieBetter = `FALSE` - `TRUE`) %>%  
  ggplot(aes(x = rookieBetter)) +  
    geom_density(alpha = .3) +  
    geom_vline(xintercept = 0,linetype = 'dashed')
```



Where to calculate the "estimate"

- Same confidence measure

```
bsRes %>%  
  spread(key = isRookie,value = mean_tov) %>%  
  mutate(rookieBetter = ifelse(`FALSE` > `TRUE`,1,0)) %>%  
  summarise(confidence = mean(rookieBetter,na.rm=T))
```

```
## # A tibble: 1 × 1  
##   confidence  
##   <dbl>  
## 1      1
```

Interpreting Confidence

- **Is this high?**
 - What value reflects the minimum confidence?
 - A coin flip → 50%
- What does a confidence level of 0.1 (or 10%) mean?
 - We are 100% confident?

Do we believe this?

- Why might this conclusion be **spurious**?
- Rookies get less playing time
- Therefore fewer opportunities to turn the ball over
- Solution? Turnovers per minute (or hour)

Re-evaluating

```
nba <- nba %>%  
  mutate(tov_hr = tov*60 / minutes)  
  
nba %>%  
  group_by(isRookie) %>%  
  summarise(tov_hr = mean(tov_hr))
```

```
## # A tibble: 2 × 2  
##   isRookie tov_hr  
##   <lgl>     <dbl>  
## 1 FALSE      3.24  
## 2 TRUE       2.78
```

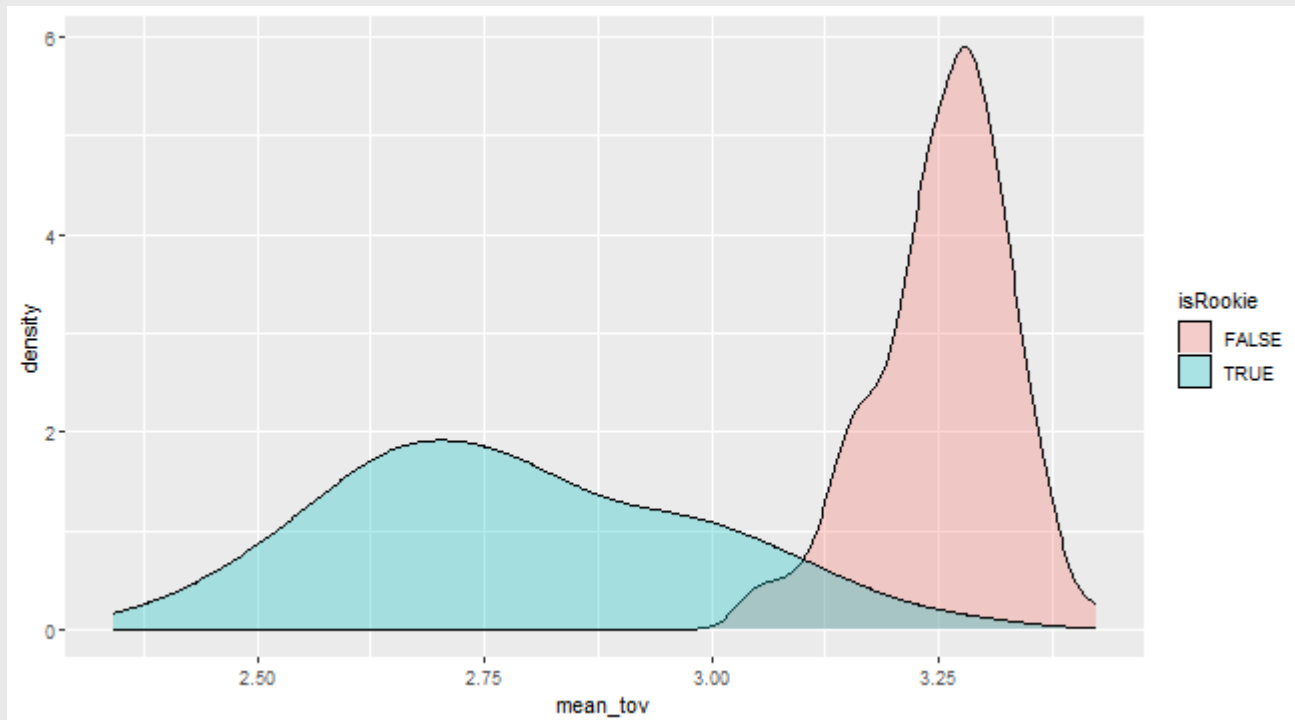
Re-evaluating

```
set.seed(123)
bsRes <- NULL
for(counter in 1:100) {
  tmpEst <- nba %>%
    sample_n(size = nrow(.),replace = T) %>%
    group_by(isRookie) %>%
    summarise(mean_tov = mean(tov_hr,na.rm=T)) %>%
    mutate(bsSeason = counter)

  bsRes <- bind_rows(bsRes,tmpEst)
}
```

Re-evaluating

```
bsRes %>%  
  ggplot(aes(x = mean_tov, fill = isRookie)) +  
  geom_density(alpha = .3)
```



Re-Evaluating

```
bsRes %>%  
  mutate(isRookie = ifelse(isRookie == TRUE, 'Rookie', 'Not Rookie'))  
%>%  
  spread(isRookie, mean_tov) %>%  
  summarise(conf = mean(`Not Rookie` > Rookie))
```

```
## # A tibble: 1 × 1  
##   conf  
##   <dbl>  
## 1  0.99
```

Other Applications

- Could do the same to express **confidence** in conclusions about:
 - The relationship between SAT scores and selective admissions
 - The relationship between MSM polls and anti-Trump bias
 - Whether state polls are good at predicting the 2020 president

Conclusion

- Anyone can spit stats



- Data scientists are comfortable with **uncertainty**

Quiz & Homework

- Go to Brightspace and take the **9th** quiz
 - The password to take the quiz is ####
- **Homework:**
 1. Work through ds1000_hw_10.Rmd (regression!)
 2. Problem Set 6 (on Brightspace)