Part 3

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Agenda

- 1. Recap of Movie Analysis
- 2. Multiple Regression
- 3. Categorical Predictors

Recap of Movie Analysis

```
require(tidyverse)
mv <-
read_rds('https://github.com/jbisbee1/ISP_Data_Science_2024/raw/main/da</pre>
```

- Theory: the more a movie costs, the more it should make
 - If not, Hollywood would go out of business!
- X: budget
- \bullet Y: gross

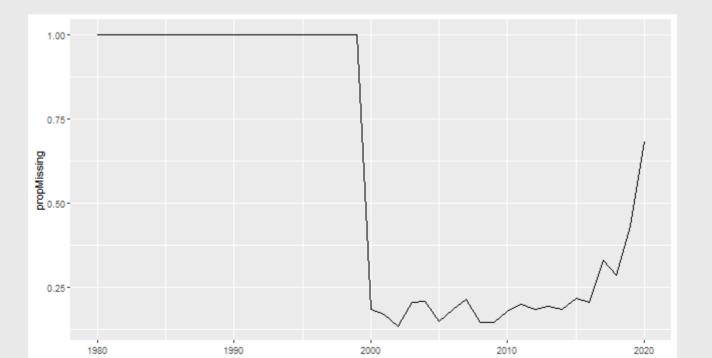
Step 1: Look

```
summary(mv %>% select(gross,budget))
```

```
budget
##
       gross
##
   Min.
          :7.140e+02
                      Min.
                                   5172
##
   1st Qu.:1.121e+07
                      1st Qu.: 16865322
##
   Median :5.178e+07
                     Median : 37212044
                    Mean : 57420173
##
   Mean :1.402e+08
                    3rd Qu.: 77844746
##
   3rd Qu.:1.562e+08
##
   Max. :3.553e+09
                     Max. :387367903
##
   NA's :3668
                      NA's :4482
```

Step 1: Look

```
mv %>%
  mutate(missing = ifelse(is.na(gross) | is.na(budget),1,0)) %>%
  group_by(year) %>%
  summarise(propMissing = mean(missing)) %>%
  ggplot(aes(x = year,y = propMissing)) +
  geom_line()
```



Some quick wrangling

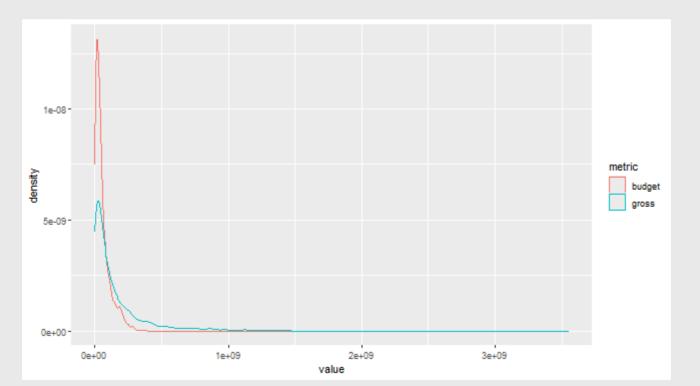
```
mv <- mv %>%
  drop_na(gross,budget)

mv %>%
  select(gross,budget) %>%
  glimpse()
```

```
## Rows: 3,179
## Columns: 2
## $ gross <dbl> 73677478, 53278578, 723586629, 11490339, 62...
## $ budget <dbl> 93289619, 10883789, 160147179, 6996721, 139...
```

Step 2: Univariate Viz

```
mv %>%
  select(title,gross,budget) %>%
  gather(metric,value,-title) %>%
  ggplot(aes(x = value,color = metric)) +
  geom_density()
```

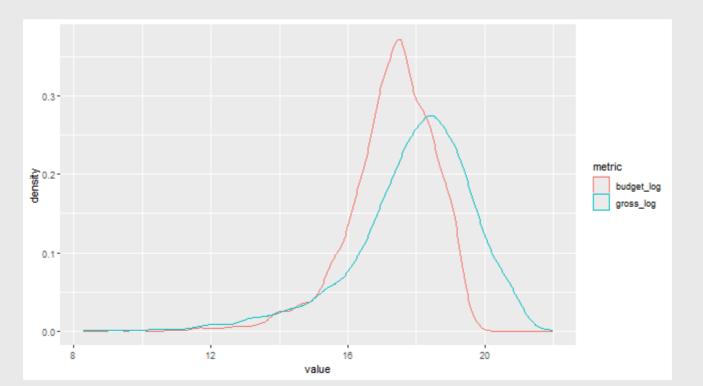


More Wrangling?

- Univariate visualization higlights significant skew in both measures
 - Most movies don't cost a lot and don't make a lot
 - But there are a few blockbusters that pull the density way out
- Let's wrangle two new variables that take the log of these skewed measures
 - Logging transforms skewed measures to more "normal" measures

Step 2: Univariate Viz

```
mv %>%
  select(title,gross_log,budget_log) %>%
  gather(metric,value,-title) %>%
  ggplot(aes(x = value,color = metric)) +
  geom_density()
```

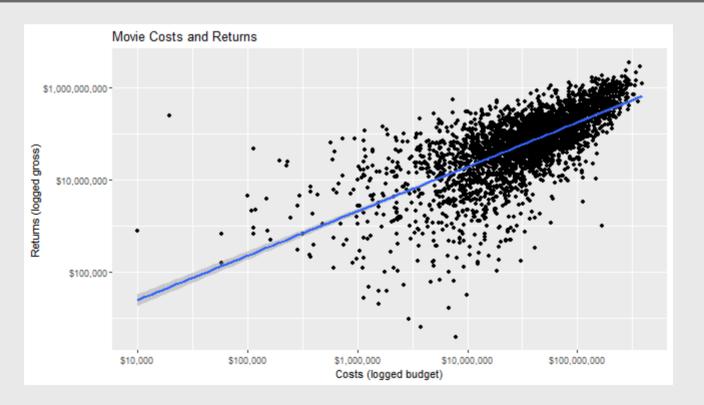


Step 3: Multivariate Viz

Step 3: Multivariate Viz

```
pClean + geom_smooth(method = 'lm')
```

```
## geom_smooth() using formula = 'y ~ x'
```



Step 4: Regression!

Step 5.1: Univariate Viz of Errors

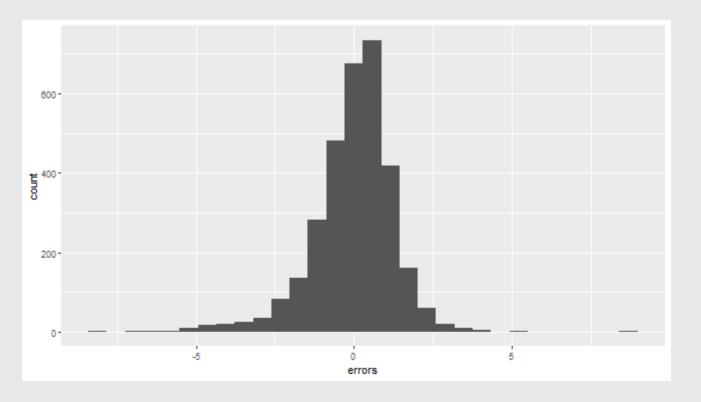
- Errors $\varepsilon = Y \hat{Y}$
 - In R, can also get them via resid() function

```
mv %>%
  mutate(errors_manual = gross_log - predict(m),
        errors_resid = resid(m))
```

```
## # A tibble: 3,179 × 24
     title rating genre year released score votes director
##
   ##
  1 Almost… R Adve… 2000 Septemb… 7.9 2.6 e5 Cameron…
##
  2 Americ… R Come… 2000 April 1… 7.6 5.14e5 Mary Ha…
##
## 3 Gladia... R Acti... 2000 May 5, ... 8.5 1.4 e6 Ridley ...
   4 Requie... Unrat... Drama 2000 Decembe... 8.3 7.86e5 Darren ...
##
## 5 Memento R
               Myst... 2000 May 25,... 8.4 1.20e6 Christo...
  6 Cast A... PG-13 Adve... 2000 Decembe... 7.8 5.42e5 Robert ...
##
##
  7 Scary ... R
              Come... 2000 July 7,... 6.2 2.38e5 Keenen ...
   8 The Pe... PG-13 Acti... 2000 June 30... 6.4 1.6 e5 Wolfgan...
##
   9 Coyote... PG-13 Come... 2000 August ... 5.7 1.08e5 David M...
##
  10 X-Men PG-13 Acti...
                         2000 July 14... 7.4 5.82e5 Bryan S...
## # : 3 169 mara rows
```

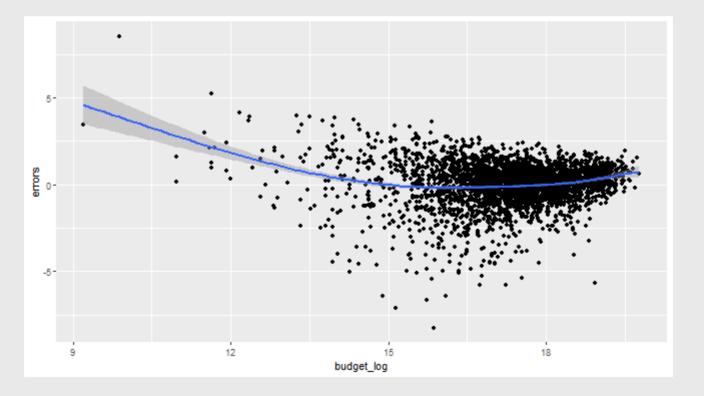
Step 5.1: Univariate Viz of Errors

```
mv %>%
  ggplot(aes(x = errors)) +
  geom_histogram()
```



Step 5.2: Multivariate Viz of Errors

```
mv %>%
  ggplot(aes(x = budget_log,y = errors)) +
  geom_point() +
  geom_smooth()
```



Step 5.3: Cross Validated RMSE

```
set.seed(123)
rmseBudget <- NULL
for(i in 1:100) {
  train <- mv %>%
    sample n(size = round(nrow(mv)*.5),replace = F)
  test <- mv %>% anti join(train)
  mTrain <- lm(gross log ~ budget log,train)</pre>
  test$preds <- predict(mTrain,newdata = test)</pre>
  rmse <- sqrt(mean((test$gross log - test$preds)^2,na.rm=T))</pre>
  rmseBudget <- c(rmseBudget,rmse)</pre>
mean(rmseBudget)
```

```
## [1] 1.279899
```

Thinking like a scientist

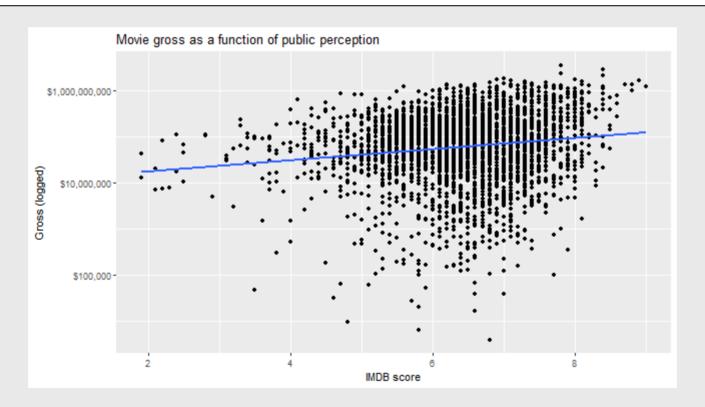
- Our previous model predicted gross as a function of budget
- Theoretically, is this sensible?
 - 1. Bigger budgets → famous actors → mass appeal → more tickets
 - 2. Bigger budgets → advertising money → mass appeal → more tickets
- But what if the movie is just...not good?

Alternative Theory

- Good movies make more money
 - Theory: good movies → recommendations → more tickets
- Predict gross with IMDB rating (score)

Alternative Model

pIMDB



Evaluating the Model

- Let's go straight to RMSE
 - We can have R calculate errors for us with residuals() command

```
m2 <- lm(gross_log ~ score,mv)
error <- residuals(m2)
(rmseScore <- sqrt(mean(error^2)))</pre>
```

[1] 1.753146

• Even worse!

Multivariate Regression

• Recall that we can **model** our outcome with multiple **predictors**

$$Y = \alpha + \beta_1 X_1 + \beta_2 X_2 + \cdots + \varepsilon$$

How much better can we predict gross with BOTH budget and score?

```
m3 <- lm(gross_log ~ budget_log + score,mv)
error <- residuals(m3)
(rmseBudgScore <- sqrt(mean(error^2)))</pre>
```

[1] 1.248817

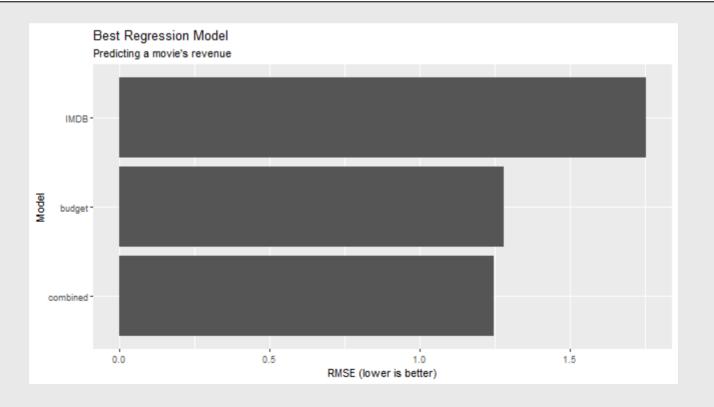
Comparing Models

Which model best predicts movie revenues?

Comparing Models

Which model best predicts movie revenues?

p



Why RMSE?

- Want to understand how good / bad our model is
- Can use it to compare models

Why RMSE?

• Do we improve our model with score?

```
set.seed(123)
bsRes <- NULL
for(i in 1:100) {
  train <- my %>%
    sample n(size = round(nrow(mv)*.8), replace = F)
  test <- mv %>% anti join(train)
  mB <- lm(gross log ~ budget log,train)</pre>
  mS <- lm(gross log ~ score,train)</pre>
  mC <- lm(gross log ~ budget log + score, train)</pre>
  hsRes <- test %>%
    mutate(pB = predict(mB, newdata = test),
           pS = predict(mS, newdata = test),
           pC = predict(mC, newdata = test)) %>%
    summarise(Budget = sqrt(mean((gross log - pB)^2,na.rm=T)),
              Score = sqrt(mean((gross log - pS)^2,na.rm=T)),
              Combined = sqrt(mean((gross log - pC)^2,na.rm=T))) %>%
    bind rows(bsRes)
```

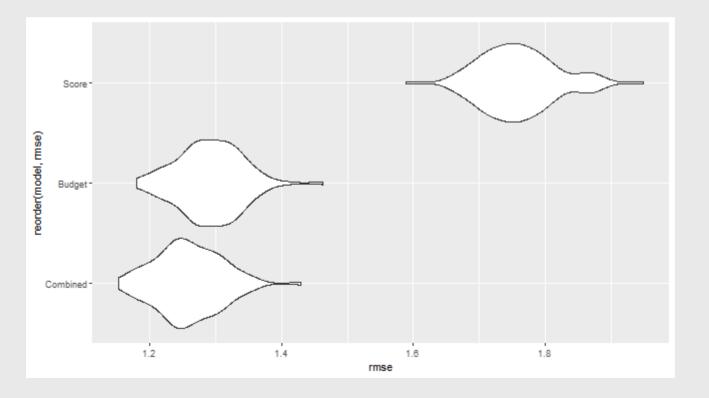
Why RMSE?

```
bsRes %>%
summarise_all(mean,na.rm=T)
```

```
## # A tibble: 1 × 3
## Budget Score Combined
## <dbl> <dbl> <dbl>
## 1 1.29 1.76 1.26
```

Visualizing

```
bsRes %>%
  gather(model,rmse) %>%
  ggplot(aes(x = rmse,y = reorder(model,rmse))) +
  geom_violin()
```



Categorical Data

- Thus far, only using continuous variables
- But we can do regression with categorical data too!
- The Bechdel Test: 3 questions of a movie
 - 1. Does it have two women in it?
 - 2. Who talk to each other?
 - 3. About something other than a man?

```
mv %>%
count(bechdel_score)
```

Research Question

- Do movies that pass the Bechdel Test make more money?
 - Theory: Women are ~50% of the population. Movies that pass the test are more appealing to women.
 - Hypothesis: Movies that pass the test make more money.
- Wrangling: Let's turn the bechdel_score variable into a binary

```
mv <- mv %>%
  mutate(bechdel_bin = ifelse(bechdel_score == 3,"Pass","Fail"))
```

We can add the binary factor to our regression

```
tidy(lm(gross_log ~ bechdel_bin,mv))
```

- Coefficient is negative
- What is the interpretation?
 - Movies that pass make less money...
 - ...than what?
 - Movies that fail the Bechdel Test
- Categorical variables are always interpreted in relation to the hold-out category!

- Movies that fail the test make more money!?
- **REMEMBER**: Correlation ≠ causation
 - What might explain this pattern?
 - Budgets in a sexist Hollywood!
 - Movies that fail the test get larger budgets
 - Budgets are positively associated with gross
- So we want to "control" for budget by adding it to our regression

```
mBechCtrl <- lm(gross_log ~ budget_log + bechdel_bin,mv)</pre>
```

```
tidy(mBechCtrl)
```

```
## # A tibble: 3 × 5
##
                  estimate std.error statistic
                                             p.value
    term
                     <dbl> <dbl> <dbl> <dbl> </dbl>
##
  <chr>
                                                <dbl>
## 1 (Intercept)
                     2.12 0.353 6.01 2.25e- 9
## 2 budget log
                   0.921 0.0199
                                      46.2 3.57e-320
## 3 bechdel binPass
                             0.0525
                     0.188
                                       3.58 3.56e- 4
```

- Our hypothesis is supported!
- What about non-binary categorical variables?

```
mv %>%
count(rating)
```

```
## # A tibble: 9 × 2
   rating
##
    <chr> <int>
##
## 1 G
  2 NC-17
  3 Not Rated
## 4 PG
               434
  5 PG-13
               1249
               1388
  6 R
  7 TV-MA
  8 Unrated
## 9 <NA>
```

Categorical

• Let's first remove rarely-occurring ratings

```
mvAnalysis <- mv %>%
  filter(!rating %in% c('Approved','TV-14','TV-MA','TV-PG','X'))
```

Categorical

```
tidy(lm(gross_log ~ rating,mvAnalysis))
```

```
## # A tibble: 7 × 5
                  estimate std.error statistic
                                            p.value
##
    term
  <chr>
                             <dh1>
                                      <dbl> <dbl>
##
                    <dbl>
## 1 (Intercept)
                   19.2
                             0.218
                                      88.1 0
## 2 ratingNC-17
                   -2.45
                             0.688 -3.56 3.81e- 4
  3 ratingNot Rated
                   -4.43
                             0.350
                                     -12.7 7.62e-36
## 4 ratingPG
                   -0.391
                             0.231
                                      -1.69 9.08e- 2
## 5 ratingPG-13
                   -0.763
                             0.222 -3.43 6.05e- 4
## 6 ratingR
                             0.222 -8.62 1.06e-17
                   -1.91
## 7 ratingUnrated
                   -4.66
                             0.643
                                      -7.25 5.38e-13
```

Categorical

- Everything makes less money than the hold-out category!
 - "G"-rated movies are powered by children
- What if we wanted to compare to a different reference category?

Categorical

```
tidy(mRating2)
```

```
## # A tibble: 5 × 5
##
                  estimate std.error statistic
                                             p.value
    term
   <chr>
                     <dh1>
                              <dbl>
                                       <dh1>
                                               <dbl>
##
## 1 (Intercept)
                     17.3
                             0.0430
                                      402. 0
  2 ratingPG-13
                      1.15
                             0.0624
                                       18.4 5.81e-72
  3 ratingPG
                      1.52
                             0.0880
                                       17.3 4.66e-64
## 4 ratingG
                      1.91
                             0.222
                                       8.61 1.09e-17
## 5 ratingNot Rated
                     -2.52
                             0.278
                                       -9.07 2.04e-19
```

Cross Validation

```
set.seed(123)
rmseRes rating <- NULL
for(i in 1:100) {
  train <- mvAnalysis %>%
    group by(rating) %>%
    sample n(size = round(n()*.8), replace = F)
  test <- mvAnalysis %>% anti_join(train)
  m <- lm(gross_log ~ rating,train)</pre>
  rmseRes rating <- test %>%
    mutate(preds = predict(m,newdata = test)) %>%
    summarise(rmse = sqrt(mean((gross log - preds)^2,na.rm=T))) %>%
    bind rows(rmseRes rating)
rmseRes rating %>%
  summarise(rmse = mean(rmse))
```

```
## # A tibble: 1 × 1
## rmse
## <dbl>
## 1 1.60
```

BREAK

Practice

- How to interpret a regression table:
 - 1. Check if any of the variables are logged
 - 2. Check if the X variable is categorical
 - 3. (Coming soon) Check if the Y variable is binary

Practice: 1, 2, 3 = "No"

- If 1, 2 & 3 are "No", then
 - $\circ \ \alpha$ is the value of Y when X is zero
 - \circ β is the amount Y increases when X increases by 1

Practice: 1, 2, 3 = "No"

RQ: What is the relationship between head shots and eliminations?

```
fn <-
read_rds('https://github.com/jbisbee1/ISP_Data_Science_2024/raw/main/da
tidy(lm(eliminations ~ head_shots,fn))</pre>
```

Practice: 1, 2, 3 = "No"

- ullet **NB**: Pay attention to the units of X and Y!
- RQ: What is the relationship between accuracy and head shots?

```
tidy(lm(head_shots ~ accuracy,fn))
```

• Then need to remember THESE rules:

```
1. \log(Y) \sim X: 1 unit change in X 	o (exp(eta) - 1) * 100 % change in Y
```

- 2. Y $\sim \log(X)$: 1% increase in $X \rightarrow \beta/100$ unit change in Y
- 3. $\log(Y) \sim \log(X)$: 1% increase in $X \to \beta$ % change in Y

- 1. $\log(Y) \sim X$: 1 unit change in $X \rightarrow (exp(\beta) 1) * 100$ % change in Y
- RQ: What is the relationship between movie gross and IMDB score?

```
tidy(lm(gross_log ~ score,mv))
```

```
1. \log(Y) \sim X: 1 unit change in X \rightarrow (exp(\beta) - 1) * 100 % change in Y
```

2. Y $\sim \log(\mathrm{X})$: 1% increase in $X \to eta/100$ unit change in Y

RQ: What is the relationship between IMDB score and budget?

```
tidy(lm(score ~ budget_log,mv))
```

- 1. $\log(\mathsf{Y}) \sim \mathsf{X}$: 1 unit change in $X \to (exp(\beta) 1) * 100$ % change in Y
- 2. Y $\sim \log(\mathrm{X})$: 1% increase in $X \to eta/100$ unit change in Y
- 3. $\log(Y) \sim \log(X)$: 1% increase in $X \rightarrow \beta$ % change in Y

RQ: What is the relationship between gross and budget?

```
tidy(lm(gross_log ~ budget_log,mv))
```

Practice: Categorical X = "Yes"

 RQ: What is the relationship between a movie's PG rating and it's IMBD rating?

```
tidy(lm(score ~ rating,mv))
```

```
## # A tibble: 8 × 5
                   estimate std.error statistic p.value
##
    term
                                       <db1>
                     <dh1>
                              <dbl>
                                              <db1>
##
   <chr>
  1 (Intercept)
                    6.37
                              0.129
                                      49.2
                                              0
  2 ratingNC-17
                    0.431
                              0.409
                                     1.06
                                              0.291
  3 ratingNot Rated
                    0.481
                              0.208
                                              0.0207
                                       2.31
  4 ratingPG
##
                    -0.0775
                              0.137
                                       -0.565
                                              0.572
  5 ratingPG-13
                    -0.0540
                              0.132
                                       -0.409
                                              0.683
## 6 ratingR
                    0.168
                              0.132
                                       1.27
                                              0.204
  7 ratingTV-MA
                    0.481
                              0.684
                                              0.482
                                       0.704
## 8 ratingUnrated
                    0.546
                              0.382
                                       1.43
                                              0.153
```

Practice: Categorical X = "Yes"

RQ: What is the relationship between mental state and accuracy (Fortnite data)?

```
tidy(lm(accuracy ~ mental_state,fn))
```

Aside: scientific notation

- What is 7.47e-4?
 - Decimal, then 4 zeros, then the number
 - 0.0000747
- What is 1.39e-1?
 - 0.0139

Practice: Categorical Y = "Yes"

Next class!