## Variable Selection for BART: An Application to Gene Regulation Supplementary Materials

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## 1 RMSE Results for Gene Regulatory Network Data

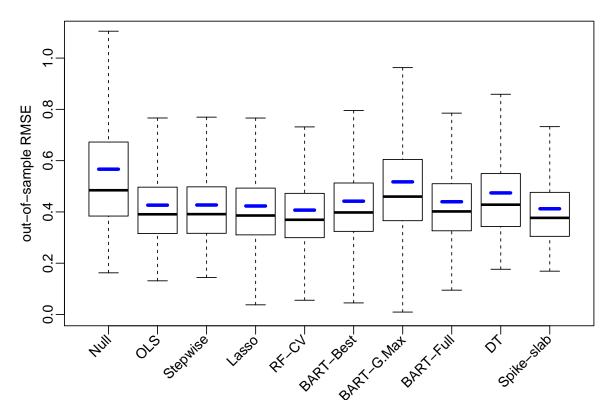


Figure 1: Distributions of out-of-sample RMSEs for each method across the 6026 genes. Blue bars represent the average RMSE across the 6026 genes for each method. Points beyond the whiskers are omitted.

## 2 Linear Model Simulation Results

	Precision	Recall	F1
BART_CV	0.88	0.84	0.83
BART_pointwise	0.21	1.00	0.34
$BART\_simul\_max$	0.97	0.89	0.92
$BART\_simul\_se$	0.93	0.90	0.90
$BART_CV_good_prior$	0.97	0.97	0.96
BART_pointwise_good_prior	0.23	1.00	0.37
BART_simul_max_good_prior	1.00	0.98	0.99
$BART\_simul\_se\_good\_prior$	0.93	1.00	0.96
BART_CV_bad_prior	0.95	0.91	0.92
$BART_pointwise_bad_prior$	0.23	1.00	0.37
BART_simul_max_bad_prior	0.98	0.84	0.89
$BART\_simul\_se\_bad\_prior$	0.95	0.93	0.93
$stepwise\_backward$	0.02	0.98	0.03
$stepwise\_forward$	0.01	1.00	0.02
lasso	0.86	0.95	0.88
$RF_CV$	0.40	0.99	0.49
$RF_{-point}$	0.14	1.00	0.24
RF_simul	0.81	0.99	0.88
dynaTree	0.78	0.65	0.68
spikeSlab	0.51	0.99	0.64

Table 1: Results for  $p=200,\,p_0=2,\,\sigma^2=5$ 

	Precision	Recall	F1
BART_CV	0.23	0.25	0.22
$BART_pointwise$	0.20	0.88	0.32
$BART\_simul\_max$	0.20	0.10	0.13
$BART\_simul\_se$	0.40	0.30	0.33
$BART_CV_good_prior$	0.57	0.43	0.45
$BART_pointwise_good_prior$	0.20	0.97	0.33
BART_simul_max_good_prior	0.52	0.31	0.38
$BART\_simul\_se\_good\_prior$	0.71	0.51	0.57
BART_CV_bad_prior	0.25	0.19	0.20
BART_pointwise_bad_prior	0.19	0.90	0.31
BART_simul_max_bad_prior	0.14	0.07	0.09
$BART\_simul\_se\_bad\_prior$	0.40	0.24	0.29
$stepwise\_backward$	0.02	0.89	0.03
$stepwise\_forward$	0.01	1.00	0.02
lasso	0.22	0.23	0.20
$RF_CV$	0.13	0.75	0.20
$RF_{-point}$	0.12	0.73	0.20
$RF_{simul}$	0.51	0.47	0.47
dynaTree	0.12	0.11	0.11
spikeSlab	0.54	0.78	0.56

Table 2: Results for  $p = 200, p_0 = 2, \sigma^2 = 20$ 

	Precision	Recall	F1
BART_CV	0.86	0.86	0.86
$BART_{-}pointwise$	0.91	0.88	0.89
$BART\_simul\_max$	0.26	0.02	0.03
$BART\_simul\_se$	0.98	0.22	0.35
$BART_CV_good_prior$	0.91	0.95	0.93
BART_pointwise_good_prior	0.95	0.95	0.95
BART_simul_max_good_prior	0.76	0.08	0.14
$BART\_simul\_se\_good\_prior$	1.00	0.35	0.51
$BART_CV_bad_prior$	0.83	0.83	0.83
$BART_pointwise_bad_prior$	0.88	0.85	0.86
BART_simul_max_bad_prior	0.18	0.02	0.03
$BART\_simul\_se\_bad\_prior$	0.99	0.20	0.32
$stepwise\_backward$	0.16	1.00	0.28
$stepwise\_forward$	0.10	1.00	0.18
lasso	0.54	1.00	0.69
$RF_CV$	0.55	0.63	0.58
$RF_{-point}$	0.55	0.66	0.59
$RF\_simul$	0.95	0.30	0.45
dynaTree	0.56	0.07	0.12
spikeSlab	0.55	1.00	0.69

Table 3: Results for  $p=200,\,p_0=20,\,\sigma^2=5$ 

	Precision	Recall	F1
BART_CV	0.60	0.41	0.46
$BART_{-}pointwise$	0.74	0.56	0.63
$BART\_simul\_max$	0.20	0.01	0.02
$BART\_simul\_se$	0.77	0.08	0.14
$BART_CV_good_prior$	0.80	0.71	0.75
BART_pointwise_good_prior	0.86	0.74	0.79
BART_simul_max_good_prior	0.40	0.04	0.06
$BART\_simul\_se\_good\_prior$	0.94	0.15	0.26
BART_CV_bad_prior	0.47	0.34	0.37
BART_pointwise_bad_prior	0.69	0.55	0.61
BART_simul_max_bad_prior	0.10	0.00	0.01
$BART\_simul\_se\_bad\_prior$	0.86	0.08	0.14
$stepwise\_backward$	0.14	0.87	0.25
$stepwise\_forward$	0.10	1.00	0.18
lasso	0.68	0.78	0.70
$RF_{-}CV$	0.44	0.43	0.43
$RF_{-point}$	0.44	0.42	0.43
$RF\_simul$	0.88	0.14	0.24
dynaTree	0.43	0.05	0.08
spikeSlab	0.58	0.93	0.70

Table 4: Results for  $p = 200, p_0 = 20, \sigma^2 = 20$ 

	Precision	Recall	F1
BART_CV	0.57	0.82	0.67
$BART_{-}pointwise$	0.69	0.86	0.77
$BART\_simul\_max$	0.18	0.01	0.02
$BART\_simul\_se$	0.99	0.26	0.41
$BART_CV_good_prior$	0.67	0.94	0.78
$BART\_pointwise\_good\_prior$	0.80	0.95	0.87
BART_simul_max_good_prior	0.54	0.04	0.07
$BART\_simul\_se\_good\_prior$	1.00	0.42	0.58
BART_CV_bad_prior	0.56	0.82	0.67
$BART_pointwise_bad_prior$	0.67	0.83	0.74
$BART\_simul\_max\_bad\_prior$	0.24	0.01	0.02
$BART\_simul\_se\_bad\_prior$	0.98	0.26	0.41
$stepwise\_backward$			
$stepwise\_forward$			
lasso	0.41	1.00	0.58
$RF_{-}CV$	0.33	0.48	0.39
$RF_{-point}$	0.33	0.49	0.39
RF_simul	0.97	0.16	0.27
dynaTree	0.40	0.03	0.05
spikeSlab	0.53	0.96	0.68

Table 5: Results for p = 500,  $p_0 = 25$ ,  $\sigma^2 = 1$ 

	Precision	Recall	F1
BART_CV	0.54	0.69	0.58
$BART_{-}pointwise$	0.60	0.74	0.66
$BART\_simul\_max$	0.18	0.01	0.02
$BART\_simul\_se$	0.94	0.20	0.32
$BART_CV_good_prior$	0.63	0.85	0.70
$BART_pointwise_good_prior$	0.73	0.87	0.79
BART_simul_max_good_prior	0.54	0.03	0.06
$BART\_simul\_se\_good\_prior$	0.99	0.33	0.49
$BART_CV_bad_prior$	0.54	0.67	0.57
BART_pointwise_bad_prior	0.59	0.73	0.65
BART_simul_max_bad_prior	0.14	0.01	0.01
$BART\_simul\_se\_bad\_prior$	0.97	0.20	0.33
$stepwise\_backward$			
$stepwise\_forward$			
lasso	0.42	1.00	0.59
$RF_{-}CV$	0.30	0.44	0.35
$RF_{-point}$	0.28	0.41	0.33
$RF\_simul$	0.92	0.12	0.21
dynaTree	0.28	0.03	0.05
spikeSlab	0.47	0.93	0.62

Table 6: Results for  $p = 500, p_0 = 25, \sigma^2 = 5$ 

Precision	Recall	F1
0.53	0.31	0.37
0.66	0.43	0.52
0.06	0.00	0.00
0.95	0.07	0.13
0.70	0.57	0.63
0.79	0.60	0.68
0.08	0.00	0.00
0.98	0.12	0.21
0.43	0.26	0.30
0.62	0.41	0.49
0.04	0.00	0.00
0.93	0.07	0.12
0.38	1.00	0.55
0.34	0.25	0.28
0.35	0.25	0.29
0.92	0.04	0.08
0.22	0.01	0.02
0.64	0.77	0.70
	0.53 0.66 0.06 0.95 0.70 0.79 0.08 0.98 0.43 0.62 0.04 0.93 0.38 0.34 0.35 0.92 0.22	0.53       0.31         0.66       0.43         0.06       0.00         0.95       0.07         0.70       0.57         0.79       0.60         0.08       0.00         0.98       0.12         0.43       0.26         0.62       0.41         0.04       0.00         0.93       0.07            0.38       1.00         0.34       0.25         0.35       0.25         0.92       0.04         0.22       0.01

Table 7: Results for  $p = 500, p_0 = 50, \sigma^2 = 1$ 

	Precision	Recall	F1
BART_CV	0.36	0.18	0.22
$BART_pointwise$	0.62	0.40	0.48
$BART\_simul\_max$	0.00	0.00	0.00
$BART\_simul\_se$	0.87	0.05	0.10
$BART_CV_good_prior$	0.63	0.48	0.54
BART_pointwise_good_prior	0.78	0.58	0.66
BART_simul_max_good_prior	0.12	0.00	0.01
$BART\_simul\_se\_good\_prior$	0.97	0.10	0.17
BART_CV_bad_prior	0.28	0.13	0.15
BART_pointwise_bad_prior	0.56	0.38	0.45
BART_simul_max_bad_prior	0.00	0.00	0.00
$BART\_simul\_se\_bad\_prior$	0.81	0.05	0.09
$stepwise\_backward$			
$stepwise\_forward$			
lasso	0.44	0.97	0.61
$RF_{-}CV$	0.32	0.21	0.25
$RF_{-point}$	0.33	0.22	0.26
$RF_{simul}$	0.81	0.03	0.06
dynaTree	0.29	0.02	0.03
spikeSlab	0.62	0.74	0.67

Table 8: Results for  $p = 500, p_0 = 50, \sigma^2 = 5$ 

## 3 Friedman Simulation Results

	Precision	Recall	F1
BART_CV	0.98	1.00	0.99
$BART_pointwise$	0.34	1.00	0.50
BART_simul_max	1.00	1.00	1.00
$BART\_simul\_se$	1.00	1.00	1.00
$BART_CV_good_prior$	0.99	1.00	0.99
$BART_pointwise_good_prior$	0.37	1.00	0.53
BART_simul_max_good_prior	1.00	1.00	1.00
$BART\_simul\_se\_good\_prior$	0.99	1.00	0.99
$BART_CV_bad_prior$	0.99	1.00	0.99
BART_pointwise_bad_prior	0.33	1.00	0.49
BART_simul_max_bad_prior	1.00	1.00	1.00
$BART\_simul\_se\_bad\_prior$	0.98	1.00	0.99
$stepwise\_backward$			
$stepwise\_forward$			
lasso	0.85	0.80	0.81
$RF_{-}CV$	0.98	0.84	0.90
$RF_{-}point$	0.15	0.98	0.26
$RF\_simul$	0.99	0.80	0.88
dynaTree	0.82	0.52	0.62
spikeSlab	0.16	0.81	0.26

Table 9: Results for  $p = 500, \, \sigma^2 = 1$ 

	Precision	Recall	F1
BART_CV	0.83	0.65	0.69
$BART_{pointwise}$	0.21	0.93	0.34
BART_simul_max	0.96	0.35	0.50
$BART\_simul\_se$	0.91	0.65	0.75
$BART_{-}CV_{-}good_{-}prior$	0.90	0.73	0.78
BART_pointwise_good_prior	0.23	0.98	0.37
BART_simul_max_good_prior	1.00	0.54	0.69
$BART\_simul\_se\_good\_prior$	0.90	0.74	0.80
BART_CV_bad_prior	0.85	0.71	0.74
BART_pointwise_bad_prior	0.21	0.92	0.34
BART_simul_max_bad_prior	0.96	0.37	0.52
$BART\_simul\_se\_bad\_prior$	0.89	0.64	0.72
$stepwise\_backward$			
$stepwise\_forward$			
lasso	0.85	0.69	0.73
$RF_{-}CV$	0.63	0.70	0.57
$RF_{-}point$	0.13	0.79	0.22
$RF\_simul$	0.93	0.62	0.73
dynaTree	0.54	0.20	0.27
spikeSlab	0.11	0.82	0.19

Table 10: Results for p = 500,  $\sigma^2 = 25$ 

	Precision	Recall	F1
BART_CV	0.89	1.00	0.93
$BART_{-}pointwise$	0.13	1.00	0.23
BART_simul_max	1.00	0.99	1.00
BART_simul_se	0.96	1.00	0.97
$BART_CV_good_prior$	0.95	1.00	0.97
BART_pointwise_good_prior	0.14	1.00	0.25
$BART\_simul\_max\_good\_prior$	1.00	1.00	1.00
$BART\_simul\_se\_good\_prior$	0.97	1.00	0.98
$BART_CV_bad_prior$	0.91	0.99	0.94
$BART\_pointwise\_bad\_prior$	0.13	1.00	0.23
BART_simul_max_bad_prior	1.00	1.00	1.00
$BART\_simul\_se\_bad\_prior$	0.95	1.00	0.97
$stepwise\_backward$			
$stepwise\_forward$			
lasso	0.83	0.80	0.80
$RF_{-}CV$	0.98	0.77	0.86
$RF_{-point}$	0.09	0.92	0.16
$RF\_simul$	0.98	0.78	0.87
dynaTree	0.79	0.44	0.54
spikeSlab	0.12	0.80	0.21

Table 11: Results for p = 1000,  $\sigma^2 = 1$ 

	Precision	Recall	F1
BART_CV	0.70	0.66	0.65
$BART_pointwise$	0.11	0.88	0.19
$BART\_simul\_max$	0.94	0.28	0.42
$BART\_simul\_se$	0.79	0.69	0.72
$BART_CV_good_prior$	0.71	0.71	0.66
BART_pointwise_good_prior	0.12	0.96	0.21
BART_simul_max_good_prior	1.00	0.43	0.59
$BART\_simul\_se\_good\_prior$	0.79	0.75	0.75
BART_CV_bad_prior	0.69	0.69	0.65
BART_pointwise_bad_prior	0.10	0.87	0.18
BART_simul_max_bad_prior	0.98	0.32	0.47
$BART\_simul\_se\_bad\_prior$	0.77	0.69	0.72
$stepwise\_backward$			
$stepwise\_forward$			
lasso	0.77	0.70	0.69
$RF_{-}CV$	0.47	0.66	0.41
$RF_{-point}$	0.07	0.73	0.13
$RF_simul$	0.97	0.57	0.71
dynaTree	0.39	0.17	0.22
spikeSlab	0.09	0.78	0.16

Table 12: Results for p = 1000,  $\sigma^2 = 25$