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Homework 10 – due April 16, 2021

**Problem 1:** On the previous homework, we looked at a zero-padding transformation in Fourier space. Here we will investigate the impact of re-sampling.

As with last time, consider a signal  $h(t_n)$  sampled at N values, and a corresponding Fourier transform  $H(\nu_m)$ .

a) Up-sampling: Suppose we construct a new signal from  $H(\nu_m)$  by doubling the number of points as follows. Let m' = 0, 1, ..., 2N - 1 and

$$G(\nu_{m'}) = \begin{cases} H(\nu_{m'/2}), & m' \text{ even} \\ 0 & m' \text{ odd.} \end{cases}$$

Show that

$$g(t_{n'}) = \begin{cases} h(t_{n'}), & 0 \le n' < N \\ h(t_{n'-N}), & N \le n' < 2N \end{cases}.$$

**b)** Down-sampling: Suppose we construct a new signal from  $H(\nu_m)$  by removing the frequencies with odd m, that is for m' = 0, 1, ..., N/2 - 1 we let  $G(\nu_{m'}) = H(\nu_{2m'})$ . Show that

$$g(t_{n'}) = \frac{1}{2} \left( h(t_{n'}) + h(t_{n'+N/2}) \right).$$

**Problem 2:** In place of a final exam, we will have a final project. Your goal for this week will be to develop a project topic. Make sure to choose something you think you can complete with a reasonable amount of work—this should be roughly 3 homework assignments worth of effort. To get a sense for the scope of a project idea, here is a list of project topics from a similar course:

https://www.asc.ohio-state.edu/physics/ntg/780/project\_list.php

- a) Read through the project guidelines (available on Canvas).
- b) Provide a short written description of your chosen topic, a few sentences and/or bullet points. Outline what steps you will need to take to complete the project.
- c) Sign up for an individual meeting time on Friday to discuss your chosen topic, https://www.signupgenius.com/go/904044EA5A82EA5FE3-p427

**Optional midterm review:** Review your exam, and correct any incorrect or missing work. For a fully corrected exam, you can collect up to half of the grade you missed (eg.  $C \to B$ ).