Multivariate Analysis

Regression

```
import pandas as pd
In [1]:
         import numpy as np
         data = pd.read csv('star dataset.csv')
In [2]:
         data.rename(columns={'Temperature (K)': 'temperature', 'Luminosity(L/Lo)': 'luminosity',
         data.head()
                        luminosity radius absolute_magnitude
Out[2]:
            temperature
                                                               star_type star_color
                                                                                   spectral class
         0
                   3068
                          0.002400 0.1700
                                                               Red Dwarf
                                                         16.12
                                                                              Red
                                                                                             Μ
                   3042
                          0.000500 0.1542
                                                              Red Dwarf
                                                         16.60
                                                                              Red
                                                                                             Μ
         2
                   2600
                          0.000300 0.1020
                                                         18.70
                                                              Red Dwarf
                                                                              Red
                                                                                             Μ
         3
                   2800
                          0.000200 0.1600
                                                         16.65 Red Dwarf
                                                                              Red
                                                                                             Μ
                          0.000138 0.1030
                                                        20.06 Red Dwarf
                   1939
                                                                              Red
                                                                                             Μ
         data.corr().style.background gradient(cmap="coolwarm").format(precision=2)
Out[3]:
                             temperature luminosity radius absolute_magnitude
                temperature
                                    1.00
                                               0.39
                                                      0.06
                  luminosity
                                    0.39
                                               1.00
                                                      0.53
                                                                         -0.69
                                    0.06
                                                       1.00
                      radius
                                               0.53
                                                                         -0.61
                                               -0.69
                                                      -0.61
         absolute_magnitude
                                    -0.42
                                                                          1.00
```

Absolute magnitude

We hebben eerder al gezien dat luminosity en absolute magnitude van elkaar afhankelijk zijn, en met een berekening zie je dit ook terug in de correlaties.

```
data['l to m'] = 4.74 - 2.5*np.log10(data['luminosity'])
In [4]:
         data.drop('luminosity', axis=1).corr().style.background gradient(cmap="coolwarm").format
In [5]:
Out[5]:
                            temperature radius absolute_magnitude l_to_m
                                           0.06
                temperature
                                    1.00
                                                                     -0.44
                     radius
                                    0.06
                                           1.00
                                                              -0.61
                                                                     -0.55
         absolute_magnitude
                                   -0.42
                                           -0.61
                                                               1.00
                                                                      0.98
                                   -0.44
                                          -0.55
                                                              0.98
                                                                      1.00
                     I_to_m
```

Het is nu interessant om te kijken of de omgerekende waarde ook een beter resultaat geeft, of dat de decision tree regressor dit verband kan vinden.

In [6]: from sklearn.model_selection import train_test_split

```
In [7]: data train, data test = train test split(data, test size=0.3, random state=42)
In [8]: from sklearn.tree import DecisionTreeRegressor
        def calculate rmse(predictions, actuals):
            if(len(predictions) != len(actuals)):
                raise Exception ("The amount of predictions did not equal the amount of actuals")
            return (((predictions - actuals) ** 2).sum() / len(actuals)) ** (1/2)
In [9]: properties_L = ['luminosity']
         dt regression L = DecisionTreeRegressor(max depth = 3)
         dt regression L.fit(data train[properties L], data train['absolute magnitude'])
        predictionsOnTrainset L = dt regression L.predict(data train[properties L])
        predictionsOnTestset L = dt regression L.predict(data test[properties L])
         rmseTrain L = calculate rmse(predictionsOnTrainset L, data train.absolute magnitude)
         rmseTest L = calculate rmse(predictionsOnTestset L, data test.absolute magnitude)
        print('Using only luminosity: ')
        print("Normalised RMSE on training set: " + str(rmseTrain L / data train.absolute magnit
        print("Normalised RMSE on test set: " + str(rmseTest L / data test.absolute magnitude.st
        Using only luminosity:
        Normalised RMSE on training set: 0.19472536146522196
        Normalised RMSE on test set: 0.19868238845693342
In [10]: properties_LM = ['l_to_m']
         dt regression LM = DecisionTreeRegressor(max depth = 3)
        dt regression LM.fit(data train[properties LM], data train['absolute magnitude'])
        predictionsOnTrainset LM = dt regression LM.predict(data train[properties LM])
        predictionsOnTestset LM = dt regression LM.predict(data test[properties LM])
         rmseTrain LM = calculate rmse(predictionsOnTrainset LM, data train.absolute magnitude)
         rmseTest LM = calculate rmse(predictionsOnTestset LM, data test.absolute magnitude)
        print('Using only converted luminosity: ')
        print("Normalised RMSE of converted luminosity on training set: " + str(rmseTrain LM / d
        print("Normalised RMSE of converted luminosity on test set: " + str(rmseTest LM / data t
        Using only converted luminosity:
        Normalised RMSE of converted luminosity on training set: 0.19472536146522196
        Normalised RMSE of converted luminosity on test set: 0.19799701347652227
```

De genormaliseerde RMSE's van beide zijn inderdaad bijna hetzelfde, wat betekent dat het model een vergelijkbare fit heeft gevonden als de formule voor de magnitude van de luminosity.

Zoals eerder genoemd (in assignment 17) zegt RMSE op zichzelf niet erg veel, vandaar dat we hem normaliseren met de standaard deviatie.

```
In [11]: properties = ['luminosity', 'radius']
    dt_regression = DecisionTreeRegressor(max_depth = 5)
    dt_regression.fit(data_train[properties], data_train['absolute_magnitude'])

predictionsOnTrainset = dt_regression.predict(data_train[properties])

predictionsOnTestset = dt_regression.predict(data_test[properties])

rmseTrain = calculate_rmse(predictionsOnTrainset, data_train.absolute_magnitude)

rmseTest = calculate_rmse(predictionsOnTestset, data_test.absolute_magnitude)

print("RMSE on training set: " + str(rmseTrain))

print("RMSE on test set: " + str(rmseTest))
```

```
print("Normalised RMSE on training set: " + str(rmseTrain/ data_train.absolute_magnitude print("Normalised RMSE on test set: " + str(rmseTest/ data_test.absolute_magnitude.std())

RMSE on training set: 1.1167338365774018

RMSE on test set: 1.3474524463722073

Normalised RMSE on training set: 0.10764998816076433

Normalised RMSE on test set: 0.12296637763790473
```

Met radius erbij kunnen we een nog iets preciezere fit vinden, waar een diepte van 5 het beste resultaat geeft.

Temperatuur toevoegen geeft meestal een net iets hogere RMSE.

properties with T = ['luminosity', 'radius', 'temperature']

```
dt regression with T = DecisionTreeRegressor(max depth = 5)
         dt regression with T.fit(data train[properties with T], data train['absolute magnitude']
         predictionsOnTrainset = dt regression with T.predict(data train[properties with T])
         predictionsOnTestset = dt regression with T.predict(data test[properties with T])
         rmseTrain = calculate rmse(predictionsOnTrainset, data train.absolute magnitude)
         rmseTest = calculate rmse(predictionsOnTestset, data test.absolute magnitude)
         print("Normalised RMSE on training set: " + str(rmseTrain/ data train.absolute magnitude
         print("Normalised RMSE on test set: " + str(rmseTest/ data test.absolute magnitude.std()
        Normalised RMSE on training set: 0.11198109768617558
        Normalised RMSE on test set: 0.12265000749732216
        from sklearn import tree
In [13]:
         import graphviz
         def plot tree regression(model, features):
             # Generate plot data
             dot data = tree.export graphviz (model, out file=None,
                                   feature names=features,
                                   filled=True, rounded=True,
                                   special characters=True)
             # Turn into graph using graphviz
             graph = graphviz.Source(dot data)
             # Write out a pdf
             graph.render("Trees/decision tree 18")
             # Display in the notebook
             return graph
```

```
In [14]: plot_tree_regression(dt_regression, properties)
Out[14]:
```

Radius

In [12]:

Aangezien we van absolute magnitude en luminosity al weten dat ze van elkaar afhankelijk zijn, is het misschien interessanter of er ook een fit gevonden kan worden voor radius.

```
In [15]: properties_for_R = ['luminosity', 'absolute_magnitude', 'temperature']
```

```
dt_regression_for_R = DecisionTreeRegressor(max_depth = 4)
dt_regression_for_R.fit(data_train[properties_for_R], data_train['radius'])

predictionsOnTrainset_for_R = dt_regression_for_R.predict(data_train[properties_for_R])

predictionsOnTestset_for_R = dt_regression_for_R.predict(data_test[properties_for_R])

rmseTrain_for_R = calculate_rmse(predictionsOnTrainset_for_R, data_train.radius)

rmseTest_for_R = calculate_rmse(predictionsOnTestset_for_R, data_test.radius)

print("Normalised RMSE on training set: " + str(rmseTrain_for_R / data_train.radius.std(
    print("Normalised RMSE on test set: " + str(rmseTest_for_R / data_test.radius.std()))
```

Normalised RMSE on training set: 0.11934442157518672 Normalised RMSE on test set: 0.2118431212783145

Hier heeft temperatuur wel een positieve invloed op de uitkomst.

Temperature

```
In [16]: properties_for_T = ['luminosity', 'absolute_magnitude', 'radius']
    dt_regression_for_T = DecisionTreeRegressor(max_depth = 4)
    dt_regression_for_T.fit(data_train[properties_for_T], data_train['temperature'])

predictionsOnTrainset_for_T = dt_regression_for_T.predict(data_train[properties_for_T])
    predictionsOnTestset_for_T = dt_regression_for_T.predict(data_test[properties_for_T])

rmseTrain_for_T = calculate_rmse(predictionsOnTrainset_for_T, data_train.temperature)
    rmseTest_for_T = calculate_rmse(predictionsOnTestset_for_T, data_test.temperature)

print("Normalised RMSE on training set: " + str(rmseTrain_for_T / data_train.temperature
    print("Normalised RMSE on test set: " + str(rmseTest_for_T / data_test.temperature.std())

Normalised RMSE on training set: 0.5234653553680353
```

Voor temperatuur is er echter geen goede fit te vinden met de andere kolommen.

Normalised RMSE on test set: 0.6914738357428835