$$\begin{split} \mu_1 & \quad \mu_2 & \quad \mu_D \\ \bar{Y_1} - \bar{Y_2} \\ E\left(\bar{Y_1} - \bar{Y_2}\right) = E\left(\bar{Y_1}\right) - E\left(\bar{Y_2}\right) = \mu_1 - \mu_2 = \mu_D \\ & \quad Var\left(\bar{Y_1} - \bar{Y_2}\right) = \sigma_1^2/n + \sigma_2^2/n \\ \bar{D} = \frac{1}{n} \sum_{i=1}^n D_i = \frac{1}{n} \sum_{i=1}^n (Y_{1i} - Y_{2i}) \\ E\left(\bar{D}\right) = E\left(\frac{1}{n} \sum_{i=1}^n (Y_{1i} - Y_{2i})\right) = \frac{1}{n} \sum_{i=1}^n (E\left(Y_{1i}\right) - E\left(Y_{2i}\right)) = \frac{1}{n} \sum_{i=1}^n (\mu_1 - \mu_2) = \mu_D \\ E\left(\bar{Y_1}\right) = E\left(\frac{1}{n} \sum_{i=1}^n Y_{1i}\right) = \frac{1}{n} \sum_{i=1}^n E(Y_{1i}) = \frac{1}{n} \sum_{i=1}^n \mu_1 = \mu_1 \\ & \quad Var\left(\bar{Y_1}\right) = Var\left(\frac{1}{n} \sum_{i=1}^n Y_{1i}\right) = \frac{1}{n^2} Var\left(\sum_{i=1}^n Y_{1i}\right) \\ = \frac{1}{n^2} \left(\sum_{i=1}^n Var(Y_{1i}) + \sum_{i \neq j} Cov(Y_{1i}, Y_{1j})\right) = \frac{1}{n^2} \sum_{i=1}^n \sigma_1^2 = \sigma_1^2/n \\ & \quad Var(aX) = a^2 Var(X) \\ & \quad Var(X - Y) = Var(X) + Var(Y) - 2Cov(X, Y) \\ & \quad Var\left(\bar{Y_1} - \bar{Y_2}\right) = Var\left(\bar{Y_1}\right) + Var\left(\bar{Y_2}\right) \\ & \quad Var\left(\bar{D}\right) = Var\left(\frac{1}{n} \sum_{i=1}^n D_i\right) + \frac{1}{n^2} Var\left(\sum_{i=1}^n D_i\right) = \frac{1}{n^2} \sum_{i=1}^n Var(D_i) \\ = \frac{1}{n} Var(D_1) = \frac{1}{n} Var(Y_{11} - Y_{21}) = \frac{1}{n} \left(Var(Y_{11}) + Var(Y_{21}) - 2Cov(Y_{11}, Y_{21})\right) \\ = \sigma_1^2/n + \sigma_2^2/n - 2Cov(Y_{11}, Y_{21})/n = \sigma_D^2/n \\ & \quad Var\left(\bar{D}\right) = \sigma_1^2/n + \sigma_2^2/n - 2Cov(Y_{11}, Y_{21}) \\ E\left(\bar{D}\right) = \mu_D \\ E\left(\bar{Y_1} - \bar{Y_2}\right) = \mu_D \\ & \quad E\left(\bar{D}\right) = \mu_D \\ & \quad Z = \frac{\bar{Y} - \mu}{\sigma/\sqrt{n}} \xrightarrow{d} N(0, 1) \\ & \quad \bar{Y} \sim N(\mu, \sigma^2/n) \\ & \quad \bar{\sigma}_D^2 \\ & \quad \bar{D} \sim N(\mu_D, \sigma_D^2/n) \\ \end{split}$$