DELTA Testing Services

go.ncsu.edu/testing

Campus Box 7555 1730 Varsity Dr. Venture IV, Suite 236 Raleigh, NC 27695-7113

919.515.1560 phone 919.515.7180 fax

delta-testing@ncsu.edu

MRe job Matthier! You've really
got the concepts down

NC STATE
UNIVERSITY

(M the Hlrs) is going

DELTA Testing Services equally as well!

| Student Name: <u>Matthieu Cayton</u> | Date: 2/7/25 | | | | | |
|---|--------------|--|--|--|--|--|
| Student's NCSU Email Address: Mccartm@ncsu.edu | | | | | | |
| Course: 5T 563 601 | Exam #: | | | | | |
| Start Time: 1002 am | _ End Time: | | | | | |
| Proctor's Name (Print): Bilha Lucero | | | | | | |
| Proctor's Signature: Bilha Guceno | | | | | | |
| Institution: Univ. of New Mexic Testing + Training Ctr. | | | | | | |

PLEASE SIGN & DATE THIS SHEET AND RETURN ALONG WITH THE EXAM

Proctoring Guidelines

If you are unable to comply with the following, please destroy the exam and have the student submit the name of another proctor for approval.

- 1. Please ask student for their photo ID.
- 2. Have the student put their name on the exam and exam answer sheet.
- 3. The test should be conducted in an atmosphere conducive to good concentration (quiet, good lighting, etc.).
- 4. The student must take the exam without outside help. Have the students leave all materials (except blank paper, pen or pencil, or calculator, as needed) outside the testing room. This includes notes, books, calculators, phones, etc. (excluding materials required for the exam).
- 5. Close and constant supervision must be provided.
- 6. Please scan and email the proctoring form, completed exam, and any formula sheets permitted for the assessment to delta-testing@ncsu.edu or fax to 919-515-7180.
- 7. Not including exams that permit all notes or textbooks, students should not be permitted to leave the testing room with formula sheets or scrap paper unless explicitly stated.
- 8. DO NOT GIVE THE EXAM TO THE STUDENT TO MAIL BACK

If you have any questions, please contact DELTA Testing Services at our main Venture IV location via phone: (919)-515-1560 or e-mail: delta-testing@ncsu.edu.

Thank you for assisting our students. **DELTA Testing Services** NC State University

Exam 1

Please write your answers below each question. You should not have access nor use any materials during this exam.

A reminder that, by taking this exam, you are required to uphold the NC State honor pledge:

"I have neither given nor received unauthorized aid on this test or assignment."

1. In the statistical learning paradigm, we discussed three major goals: statistical inference, predictive modeling, and pattern finding.

Give a brief real world example for each of these goals. Specify a possible model or method we discussed in class that would help answer the question from each real world example.

Statistical Inference (4 pts) Multiple linear regression model in which we aim to prodel income as a tinction of education, age, and IQ. Here we are looking to examine if any of these covariates are meaningful in our model. We want to answer guestions like Is age related to income?

• Predictive Modeling (4 pts) (soccer reference)

KNN model in which we aim to model the # of goals scored by a team in a given game as a function of passed completed, experted goals (xy), and possession. We are looking to try and make accurate predictions regarding the number of goals scored (as accurate as possible) games that have not yet been played! We are not so interested in in games that have

· Pattern Finding (4 pts) which covariates are statistically significant.

Principle components analysis to try and group U.S States that have similar subscriber attrition at two time intervals (unsupervised learning method). We want to see : Four PCA finds patterns via grouping - perhaps some states share similar addition rates Warroughd loube these metrics. -) PCA doesn't really do grapmy but that doesn't come to be described

- 2. Consider having models characterized by flexibility with the scale going from not very flexible to very flexible.
 - a. What type of relationship between flexibilty and squared bias would we expect?

 Why? (4 pts)

 (inverse relationship)

As flexibility increases, we would expect the squared bies to decrease as the model fits the data more and more closely.

b. What type of relationship between flexibilty and variance would we expect? Why? (4 pts)

As flexibility increases, we would expect variance to increase (and vice-versa) more flexibility means that changing a single observation can have a larger impact on our model fit, and this is what our model variance measures.

c. What type of relationship between flexibilty and training error would we expect? Why? (4 pts)

As flexibility increases, training error decreases because our model more closely fits the training data (brading off a decrease in squared bias for a smaller increase in variance).

d. What type of relationship between flexibility and test error would we expect?

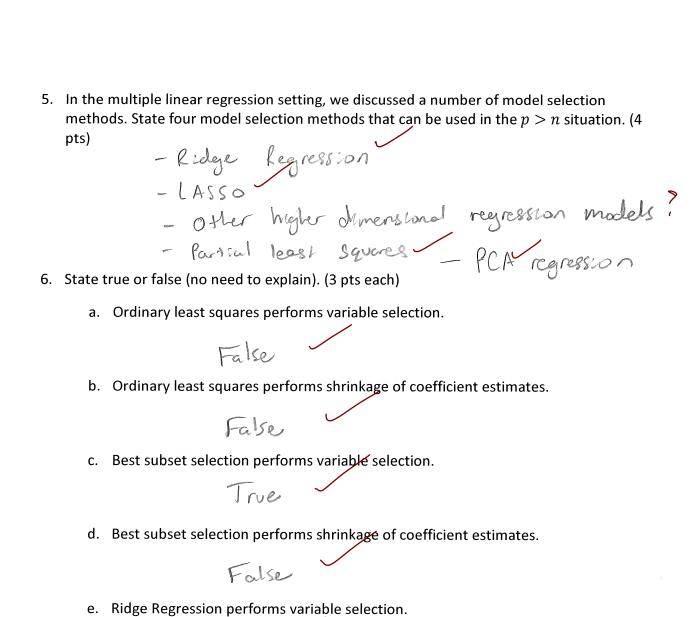
Why? (4 pts)

To our trained model

Leger our test error to increase. As a model becomes more flexible, it begins to overfit to the training data and thus does not generalize as well to the test soft.

3. What is a tuning parameter or hyperparameter? How does this differ from a 'regular' parameter in a parametric model? (4 pts)

A regular parameter in a parametric model is derived via a closed term solution (think OLS), whereas a tuning parameter is not arrived at via closed term solution. It must be "tuned" (a turing parameter will have some kind of Search grid), that is, we must test the performance of our model with a variety of candidate values for our tuning parameter to find the optimal value (think k in a k NN model).



Falso,

h. LASSO performs shrinkage of coefficient estimates.

True

g. LASSO performs variable selection.

True

True

f. Ridge Regression performs shrinkage of coefficient estimates.

7. Suppose we have a large data set where we want to perform a regression task. We want to determine the best overall model between a LASSO model and a kNN regression model. We want to use a train test split and compare the best kNN and LASSO model on the test set. We wish to determine the appropriate tuning parameters on the training set only using cross-validation. Fully outline the process for splitting the data, tuning, comparing, and fitting a final overall best model. (10 pts)

1. Train/Test Split (split date into training and test sets, w/about 70%-80% of date 2. Split Training set into v-folds in the training set). 3. Create a Search grid for each model type 1. For KNN, choose some rector of cardidate values ?. For LASSO, choose some vector of condidate values for A.

4. For each value of the given hyperparameter, for the model on v-1 folds, and evaluate the performance on the - fold that was left out Do this repeatedly until all v folds have been left out once (the left out fold is the internal training validation set for that iteration). Average all v cv errors for that value of UK (or) : I we are turing our LASSO Model).

> 5. Once the above step has been done for each cardidate Value of the hyperparameter, those the hyperparameter that achieved the lowest cu error.

6. Refit both models on the entire training data, each with their respective best choice for k and A.

7. Evaluate the performance of these tried models against the test set. Choose the model with the lowest test set error as the final overall best model fitth to the entire

record

8. Consider the Ridge Regression procedure for fitting a multiple linear regression model. With this model we minimize the following criterion (recall $\lambda \geq 0$):

$$\sum_{i} (Y_i - \beta_0 - X_{i1}\beta_1 - \dots - X_{ip}\beta_p)^2 + \lambda \sum_{j=1}^{p} \beta_j^2$$

a. What are the benefits of fitting a Ridge Regression model as compared to an ordinary least squares model? (4 pts)

Multicollinearity, shrinking correlated variables towards one another (so that their effect is distributed between them and is not silved into only one of them).

- Rielge Regression allows us to tune our model va & so that we may have a better chance of finding the right balance between bus and variance (and thus make better predictions).

b. What happens to our coefficient estimates for a 'large' value of the tuning parameter? What happens for a tuning parameter value near 0? (4 pts)

As λ 1, our & values Shrink depending on their level of importance to the model (though they will not strink to Zero). Correlated variables will have &s that shrink toward one another.

AS λ , our β values grow, and when $\lambda \approx 0$, we effectively have the OLS solution because our penalty is effectively gone.

9. Suppose we fit a multiple linear regression model to data about how much people earn. Our response variable is the wage (in 1000's of dollars) and our predictors are marital_status (married, never_married, or divorced), and age.

We fit a linear and quadratic term for age and include an interaction between marital_status and age and an interaction between marital_status and age squared in the model. Output for the model is given below.

| | Estimate | Std. Error | t value | Pr(> t) |
|--------------------------------------|----------|------------|---------|----------|
| (Intercept) | 25.293 | 38.116 | 0.664 | 0.507 |
| marital_statusmarried | -19.780 | 40.405 | -0.490 | 0.624 |
| marital_statusnever_married | -31.760 | 40.992 | -0.775 | 0.439 |
| age | 2.846 | 1.611 | 1.767 | 0.077 |
| I(age^2) | -0.024 | 0.017 | -1.470 | 0.142 |
| marital_statusmarried:age | 2.024 | 1.716 | 1.179 | 0.238 |
| marital_statusnever_married:age | 2.230 | 1.820 | 1.225 | 0.221 |
| marital_statusmarried:I(age^2) | -0.025 | 0.018 | -1.412 | 0.158 |
| marital_statusnever_married:I(age^2) | -0.032 | 0.020 | -1.607 | 0.108 |

a. Write down the fitted equation for \hat{y} . Define any indicator variables as needed. (4 pts)

$$V_{\text{ungl}} = 25.293 - 19.780 \, \text{X}_1 - 31.700 \, \text{X}_2 + 2.846 \, \text{X}_3 - 0.024 \, \text{X}_3^2 + 2.024 \, \text{X}_1 \, \text{X}_3 + 2.230 \, \text{X}_2 \, \text{X}_3 - 0.025 \, \text{X}_1 \, \text{X}_3^2 - 0.032 \, \text{X}_2 \, \text{X}_3^2 \neq \text{E}$$

b. One column of the output represents the t-value or t-statistic. What is the usefulness of this t-value? (2 pts)

this t-value? (2 pts)

this t-test test the hypothesis that the partial effect of test of the to the the partial effect of the to the test of the total effect of the

c. Write down the form of a predicted value for somone that is married and has an age of 30. No need to simplify. (2 pts)

$$\dot{y} = 25.243 - (19.780 \cdot 1) - (31.760 \cdot 0) + (2.846 \cdot 30) - (0.024 \cdot 30^2) + (2.024 \cdot 1.30) + (2.230 \cdot 0.30) - (6.025 \cdot 1.30^2) - (0.032 \cdot 0.30) + (2.0061)$$

| d. Write down the fo | rm of a predicted value for | somone that is divorced ar | nd has an age |
|----------------------|-----------------------------|----------------------------|-----------------|
| of 30. No need to s | simplify. (2 pts) | | <i>_</i> |
| of 30. No need to s | (31.760.0)+(2. | 846 - 30) - (0.024 | .30) |
| + (2.024 0.30) + | (2.230-0-30) | $-(0.025 \cdot 0.30^{2})$ |)-(0.032-0.302) |
| cancels | · connels | Cancels | Cancels |
| f Concentually who | | San baharan 11 7 1 1 | |

f. Conceptually, what does including an interaction between marital_status and age and an interaction between marital_status and age squared do to our model as compared to a model without those interactions (that still includes a main effect for marital_status and a linear and quadratic term for age)? (3 pts)

It allows our model to potentially capture non-additive patterns covariates (non-linear in x's not Bs!) Der example, the effect of age on how much someone earns many depend on that person's marital status. A purely additive model would not account for this. Completely different quadrates are for for each grap —

- g. The F-statistic for the global model test is 46.26 on 8 numerator and 2991 denominator degrees of freedom. The p-value for the test is very close to zero.
 - i. Write down the null and alternative hypotheses for this global test. (3 pts)

Ho:
$$\beta_1 = \beta_2 = \dots = \beta_9 = 0$$

HA: At least one of $\beta_1, \beta_2, \dots, \beta_9 \neq 0$

ii. We see a significant global test but none of the coefficient tests are significant. What do you think could be causing this issue? (3 pts)

A number of thirds could be consing this:

- collinearity

- type II error among t-tests

- Overall Significance may be achieved but our coverates

must not be properly specified - we may want to include
must not be properly specified - we may want to include
(i.e. the assumption of equal error variance)? (3 pts)

We would want to look at a Scatterplot of (Standardized) residuals by their fitted values to assess homogeneity of variance.