

Google JAX

Prepared for the Bank of Portugal Computational Economics
Course

John Stachurski

October 2025

Topics

- What's JAX?
- JIT compilation
- Autodiff
- Array operations
- Functional programming



<https://jax.readthedocs.io/en/latest/>

A high-performance numerical computing library

- Developed by [Google Research](#)
- Conforms to NumPy API for array operations
- GPU/TPU acceleration
- Automatic differentiation
- Math-centric library semantics

“The JAX compiler aims to enable researchers to write Python programs...that are **automatically** compiled and scaled to leverage accelerators and supercomputers”

Example. AlphaFold3 is built with Google JAX

google-deepmind / alphafold3

<> Code Issues 18 Pull requests Actions Projects Security Insights

alphafold3 Public Watch 65

main 1 Branch 2 Tags Go to file Add file >> Code

Author	Commit Message	Timestamp
Augustin-Zidek and copybara-github	Validate bonded atoms against th...	6207434 - 13 hours ago 156 Commits
	.github/workflows	Do not test ref_pos which depends on a specific RDKit ve... 4 months ago
	docker	Do not limit parallelism of make when building HMMER 4 days ago
	docs	Save embeddings as float16 instead of float32 to make t... last week
	legal	Add translations of legal terms 3 months ago
	src/alphafold3	Validate bonded atoms against the CCD 13 hours ago
	CMakeLists.txt	Initial release of AlphaFold 3 6 months ago
	LICENSE	Initial release of AlphaFold 3 6 months ago

Highly accurate protein structure prediction with AlphaFold

John Jumper, Richard Evans, Alexander Pritzel, Tim Green,
Michael Figurnov, Olaf Ronneberger, Kathryn Tunyasuvunakool,...

Nature Vol. 596 (2021)

- Citation count = 35K
- Nobel Prize in Chemistry 2024

“The acronym JAX stands for **Just After eXecution**”

- monitor function execution once and then compile

Another acronym:

- **J**ust-in-time compilation
- **A**utomatic differentiation
- **X**LA (accelerated linear algebra)

Familiar NumPy-style array API

```
import jax.numpy as jnp

A = ((2.0, -1.0),
      (5.0, -0.5))

b = (0.5, 1.0)

A, b = jnp.array(A), jnp.array(b)

x = jnp.inv(A) @ b
```


Implicit JIT via the XLA pipeline

The sequence of actions for performing `jnp.inv(A)` are as follows:

1. JAX identifies that it needs to invert a matrix `A` of specific data type and shape
2. JAX passes this information to XLA in an intermediate representation
3. XLA generates compiled code specialized to your hardware, the data type and shape of the array
4. The code is executed on the device and the result is returned to the user
5. The code is cached in memory for future use (when called again with the same specific dtype and shape)

Explicit just-in-time compilation

We can also explicitly JIT compile JAX functions

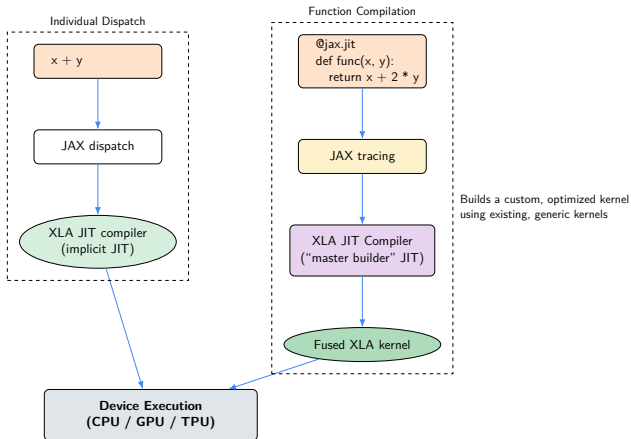
```
@jax.jit
def f(x):
    term1 = 2 * jnp.sin(3 * x) * jnp.cos(x/2)
    term2 = 0.5 * x**2 * jnp.cos(5*x) / (1 + 0.1 * x**2)
    term3 = 3 * jnp.exp(-0.2 * (x - 4)**2) * jnp.sin(10*x)
    return term1 + term2 + term3
```

- Compiles at first call (e.g., `result = f(x)`)
- Compiler specializes on **both** shape and data type

Compiler tools for optimizing function operations:

- Operations combined into fused kernels for GPU/TPU
- Eliminate intermediate buffers / memory writes and reads
- Loop unrolling
- Specialized algorithms
- Memory layout optimization for multi-dimensional arrays

Implicit and explicit JIT



Automatic differentiation

```
import jax.numpy as jnp
from jax import grad, jit

def f( $\theta$ , x):
    for W, b in  $\theta$ :
        w = x @ W + b
        x = jnp.tanh(w)
    return x

def loss( $\theta$ , x, y):
    return jnp.sum((y - f( $\theta$ , x))**2)

grad_loss = jit(grad(loss))  # Now use gradient descent
```

More features of JAX

Let's review some other features

- Functional programming
- PyTrees

Functional Programming

JAX adopts a functional programming style

⇒ Functions are **pure**

```
def f(θ, x):  
    for W, b in θ:  
        w = W @ x + b  
        x = jnp.tanh(w)  
    return x  
  
def loss(θ, x, y):  
    return jnp.sum((y - f(θ, x))**2)
```

Pure functions:

1. Deterministic
2. No side effects

Deterministic means

- Same input \implies same output
- Outputs do not depend on global state

No side effects

- Won't change global state
- Won't modify data passed to the function (immutable data)

A non-pure function

```
tax_rate = 0.1
prices = [10.0, 20.0]

def add_tax(prices):
    for i, price in enumerate(prices):
        prices[i] = price * (1 + tax_rate)
    print('Modified prices: ', prices)
    return prices
```

Why is this not pure?

A **pure** function

```
tax_rate = 0.1
prices = (10.0, 20.0)

def add_tax_pure(prices, tax_rate):
    return [price * (1 + tax_rate) for price in prices]
```

General advantages:

- Helps testing: each function can operate in isolation
- Promotes deterministic behavior and hence reproducibility
- Prevents bugs that arise from mutating shared state

Advantages for JAX:

- Data dependencies are explicit, which helps with optimizing complex computations
- Pure functions are easier to differentiate (autodiff)
- Pure functions are easier to parallelize and optimize (don't depend on shared mutable state)

In summary, functional programming is good for

- JIT, autodiff, & parallelization

JAX PyTrees

Consider a function of the form

$$f_{\theta} = G_m \circ G_{m-1} \circ \dots \circ G_2 \circ G_1$$

where

- $G_{\ell}x = \sigma_{\ell}(xW_{\ell} + b_{\ell})$ for $\ell = 1, \dots, m$
- θ represents the “vector” of all parameters
- σ_{ℓ} is a given function

The idea that the vector θ contains all parameters is conceptually useful but awkward within code...

To handle these kinds of situations we can use PyTrees

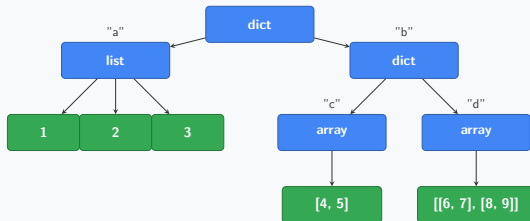
- A tree-like data structure built from Python containers
- A concept, not a data type
- Used to store parameters


Examples.

- A list of dictionaries, each dictionary contains parameters
- A dictionary of lists
- A dictionary of lists of dictionaries
- etc.

JAX PyTree Structure

```
pytree = {  
  "a": [1, 2, 3],  
  "b": {"c": jnp.array([4, 5]), "d": jnp.array([[6, 7], [8, 9]])}  
}
```



 Container nodes (dict, list, tuple)

 Leaf nodes (arrays, scalars)

JAX can

- apply functions to all leaves in a PyTree structure
- differentiate functions with respect to the leaves of PyTrees
- etc.

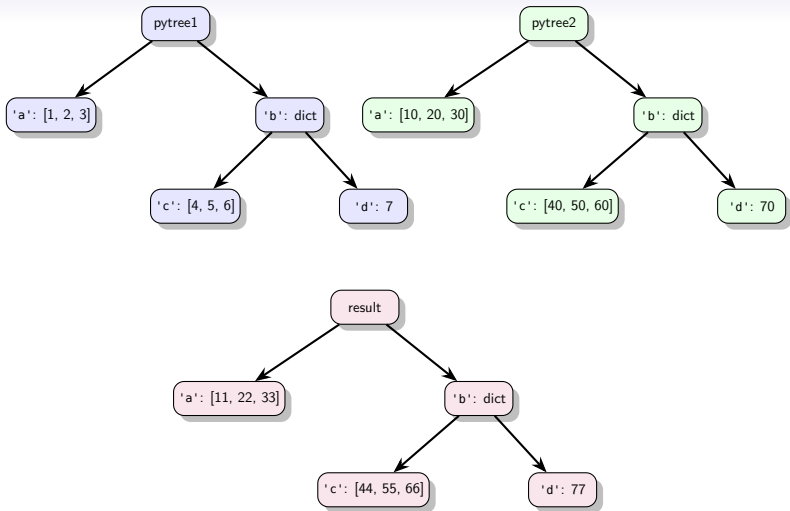


Figure: `jax.tree.map(lambda x, y: x + y, pytree1, pytree2)`

Apply gradient updates to all parameters

```
def sgd_update(params, grads, learning_rate):
```

```
    return jax.tree.map(  
        lambda p, g: p - learning_rate * g,  
        params,  
        grads  
    )
```

Calculate gradients (PyTree with same structure as params)

```
loss_grad = jax.grad(loss_fn)
```

```
grads = loss_grad(params, x, y)
```

Update all parameters at once

```
updated_params = sgd_update(params, grads, 0.01)
```

Summary

Advantages over NumPy / MATLAB

- Machine code specialized to data types, shapes and devices!
- Automatically matches tasks with accelerators
- Same code, multiple backends (CPUs, GPUs, TPUs)
- Can fuse array operations for speed and memory efficiency
- Elegant functional style
- Integrated efficient autodiff

Advantages of JAX (vs PyTorch / Tensorflow / etc.) for economists:

- elegant functional programming style – close to maths
- elegant autodiff tools
- array operations follow standard NumPy API

Exposes low level functions