

Summarizing Data

Computational Mathematics and Statistics

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One Minute Paper Results

What was the most important thing you learned during this class?

introduction
course

use
know
dplyr
types
easy base

data
rstudio
install
programming

basics preparation

important learnt time

learned getting

language results

syntax

What important question remains unanswered for you?

first covered confusing
future lateX everything
using think class data syntax
question new know moment
since upcoming language will get
programming session bit getting
nothing week pretty
questions

Data Types / Descriptives / Visualizations

Data Type	Descriptive Stats	Visualization
Continuous	mean, median, mode, standard deviation, IQR	histogram, density, box plot
Discrete	contingency table, proportional table, median	bar plot
Categorical	contingency table, proportional table	bar plot
Ordinal	contingency table, proportional table, median	bar plot
Two quantitative	correlation	scatter plot
Two qualitative	contingency table, chi-squared	mosaic plot, bar plot
Quantitative & Qualitative	grouped summaries, ANOVA, t-test	box plot

Variance

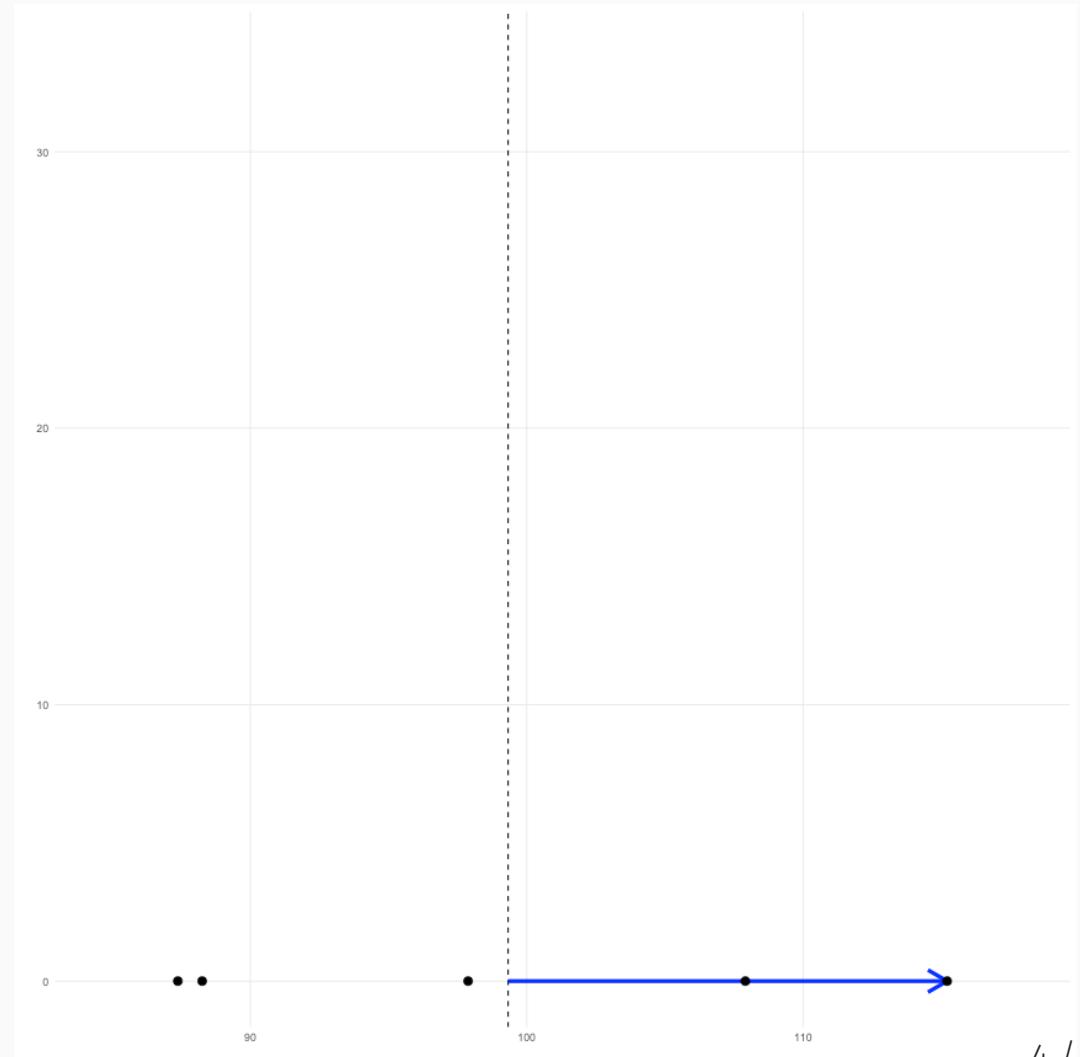
Population Variance:

$$S^2 = \frac{\Sigma(x_i - \bar{x})^2}{N}$$

Consider a dataset with five values (black points in the figure). For the largest value, the deviance is represented by the blue line ($x_i - \bar{x}$).

See also:

<https://shiny.rit.albany.edu/stat/visualizess/>
<https://github.com/jbryer/VisualStats/>

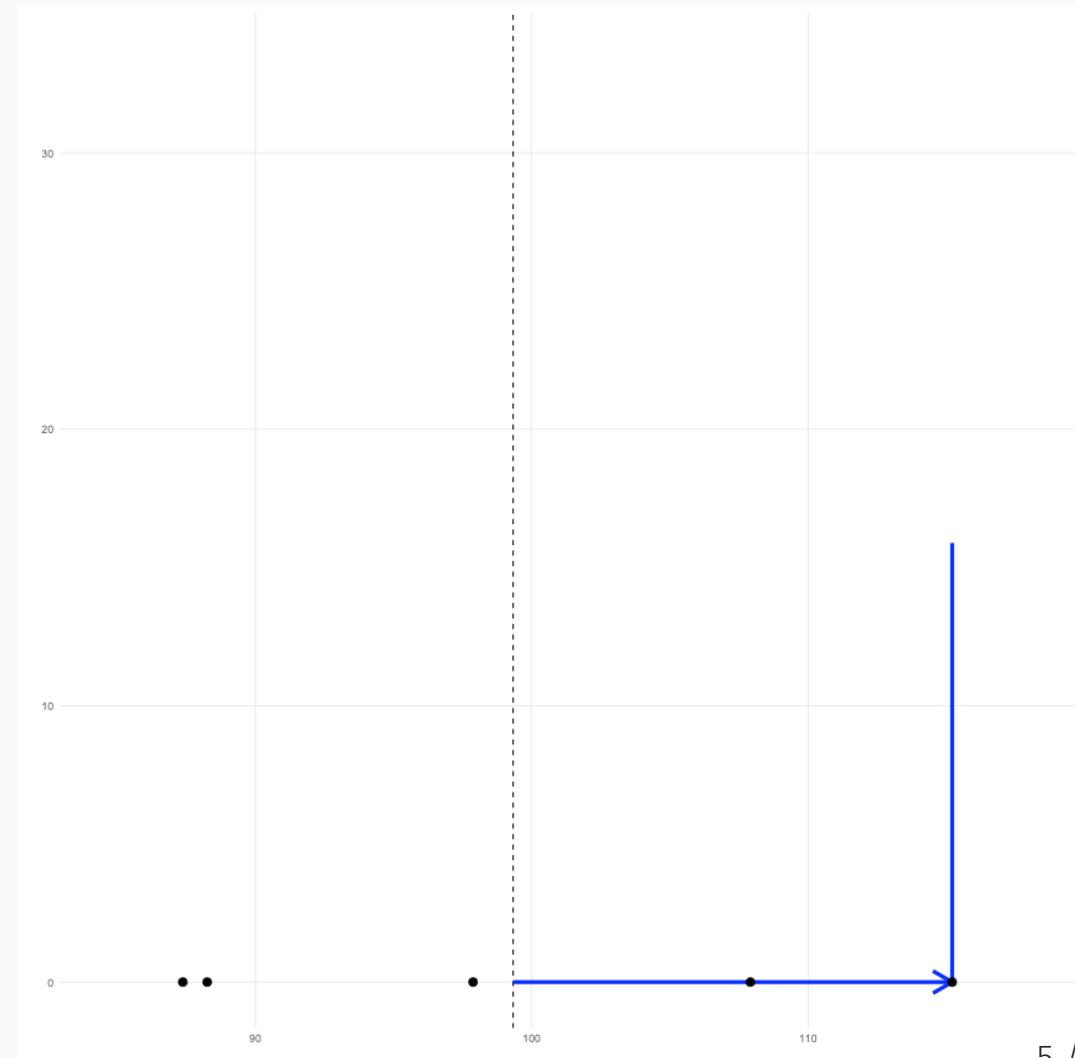


Variance (cont.)

Population Variance:

$$S^2 = \frac{\Sigma(x_i - \bar{x})^2}{N}$$

In the numerator, we square each of these deviances. We can conceptualize this as a square. Here, we add the deviance in the y direction.

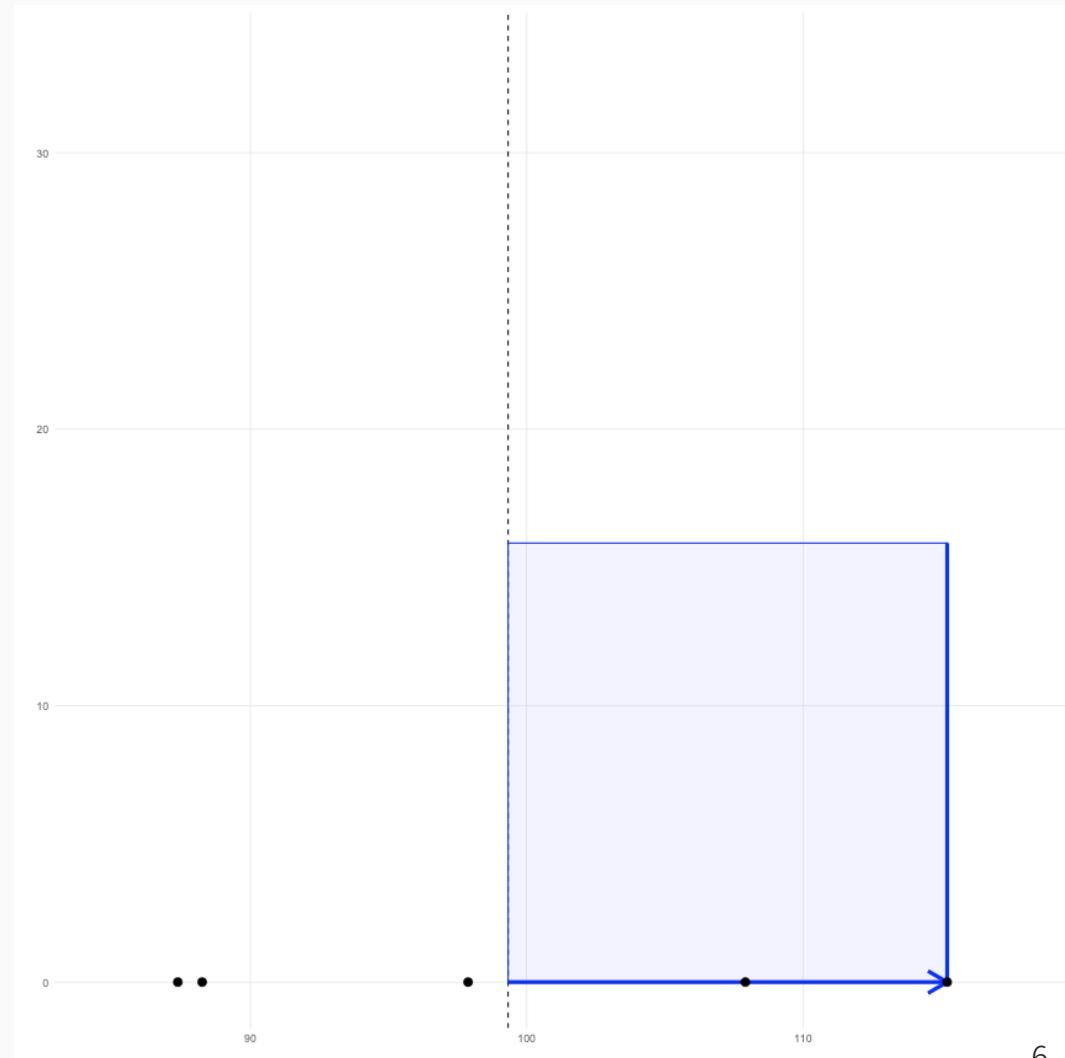


Variance (cont.)

Population Variance:

$$S^2 = \frac{\Sigma(x_i - \bar{x})^2}{N}$$

We end up with a square.

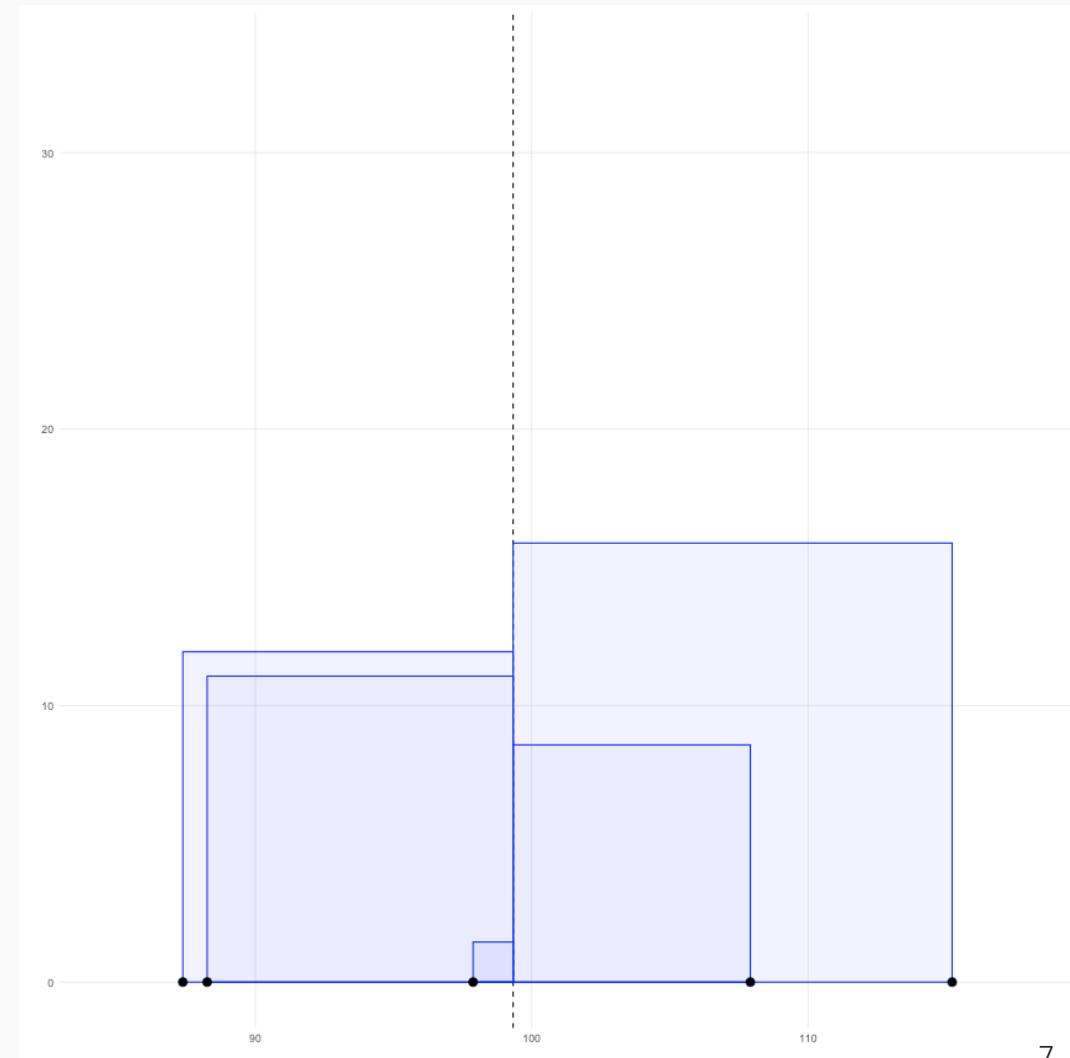


Variance (cont.)

Population Variance:

$$S^2 = \frac{\Sigma(x_i - \bar{x})^2}{N}$$

We can plot the squared deviance for all the data points. That is, each component in the numerator is the area of each of these squares.

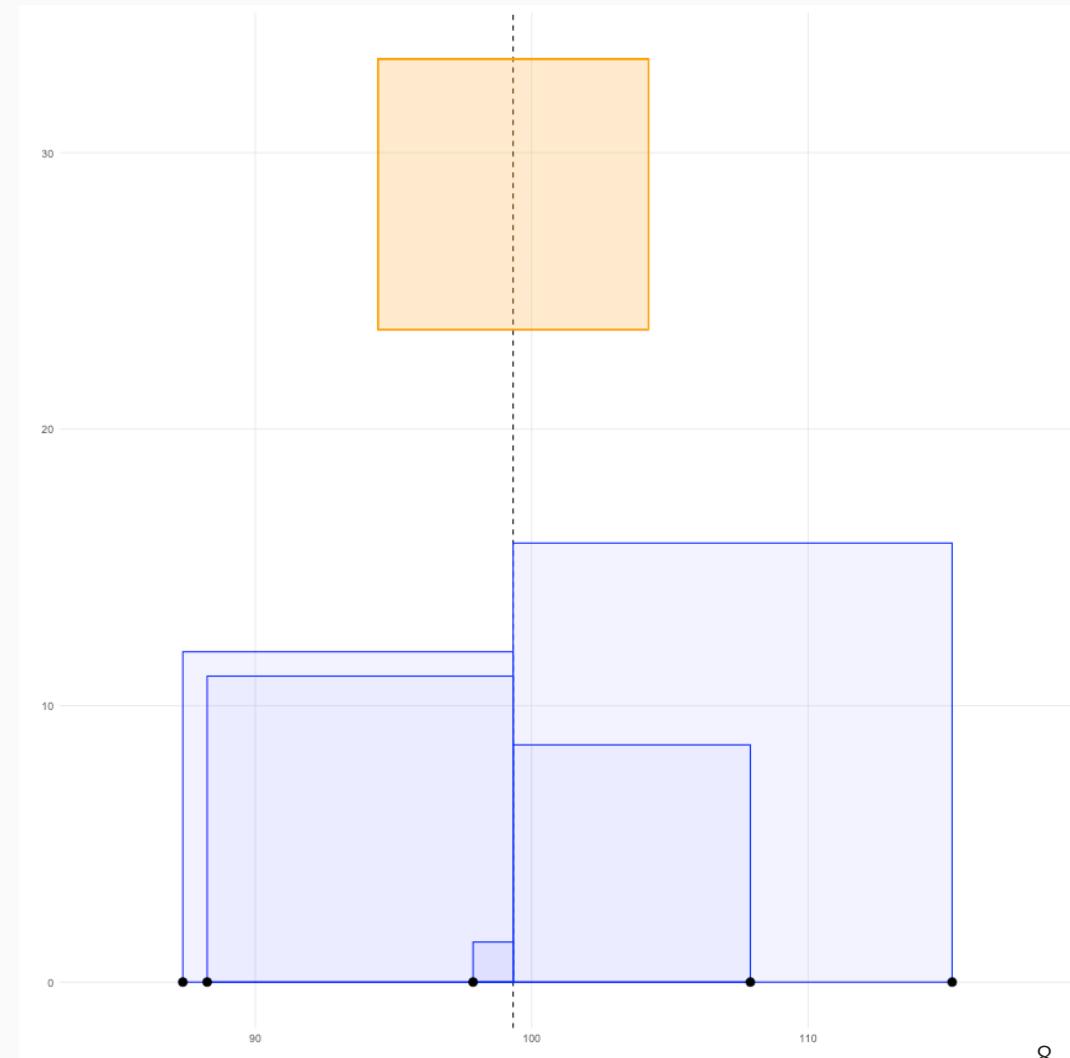


Variance (cont.)

Population Variance:

$$S^2 = \frac{\Sigma(x_i - \bar{x})^2}{N}$$

The variance is therefore the average of the area of all these squares, here represented by the orange square.



Population versus Sample Variance

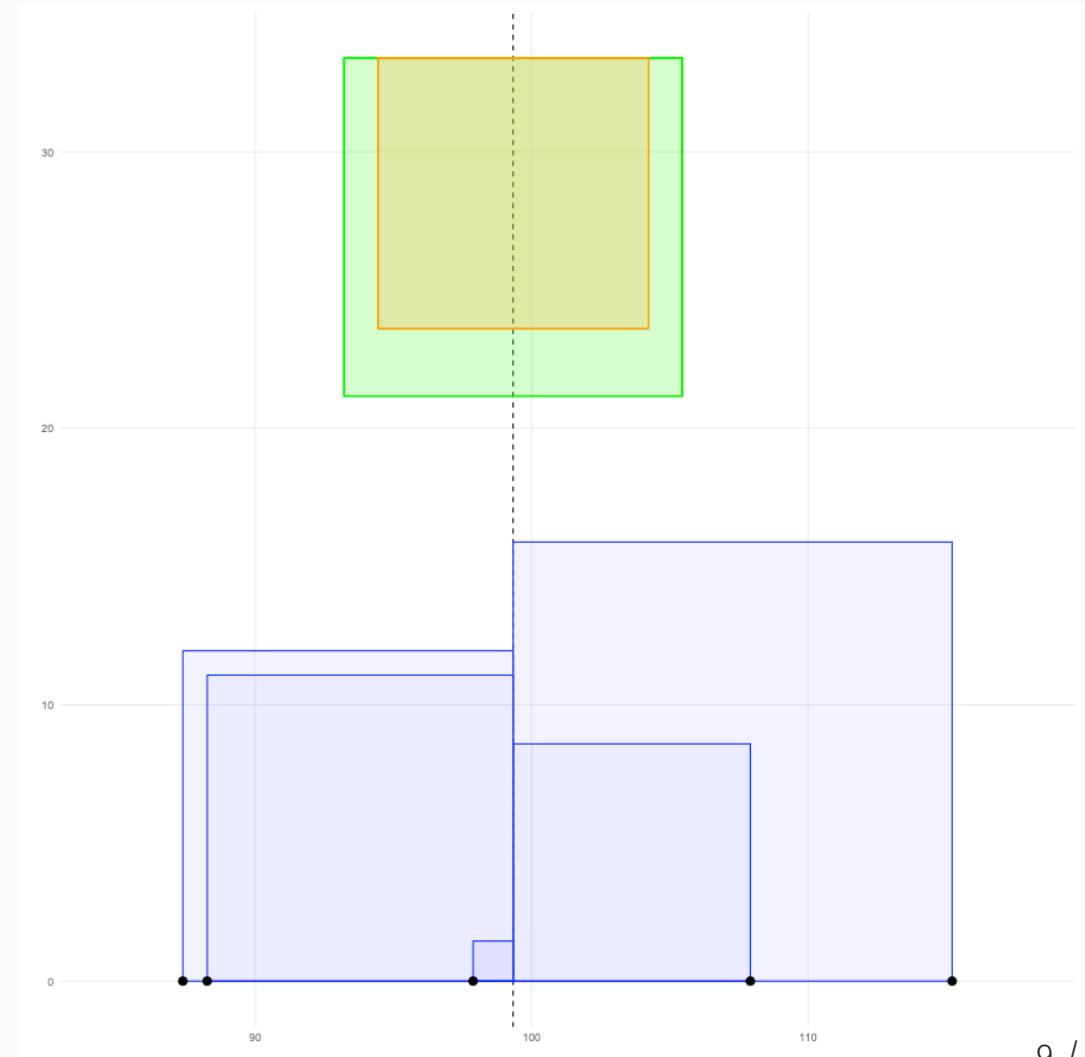
Typically we want the sample variance. The difference is we divide by $n - 1$ to calculate the sample variance. This results in a slightly larger area (variance) then if we divide by n .

Population Variance (yellow):

$$S^2 = \frac{\sum(x_i - \bar{x})^2}{N}$$

Sample Variance (green):

$$s^2 = \frac{\sum(x_i - \bar{x})^2}{n - 1}$$



Robust Statistics

Consider the following data randomly selected from the normal distribution:

```
set.seed(41)
x <- rnorm(30, mean = 100, sd = 15)
mean(x); sd(x)
```

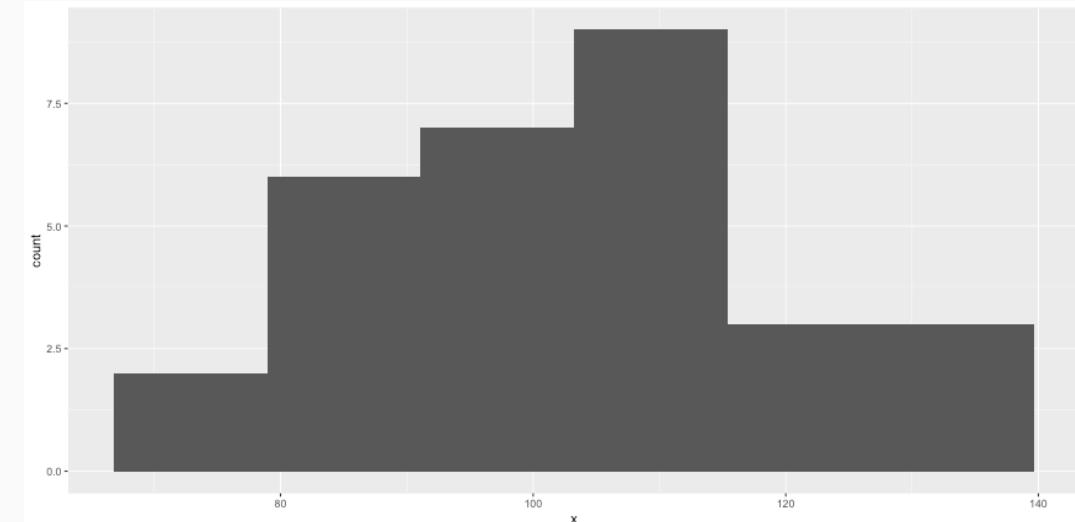
```
## [1] 103.1934
```

```
## [1] 16.8945
```

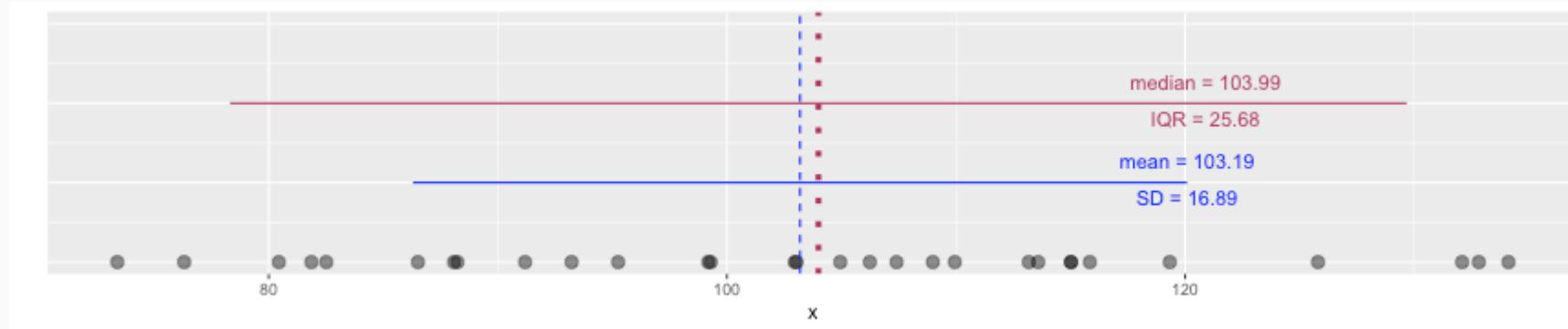
```
median(x); IQR(x)
```

```
## [1] 103.9947
```

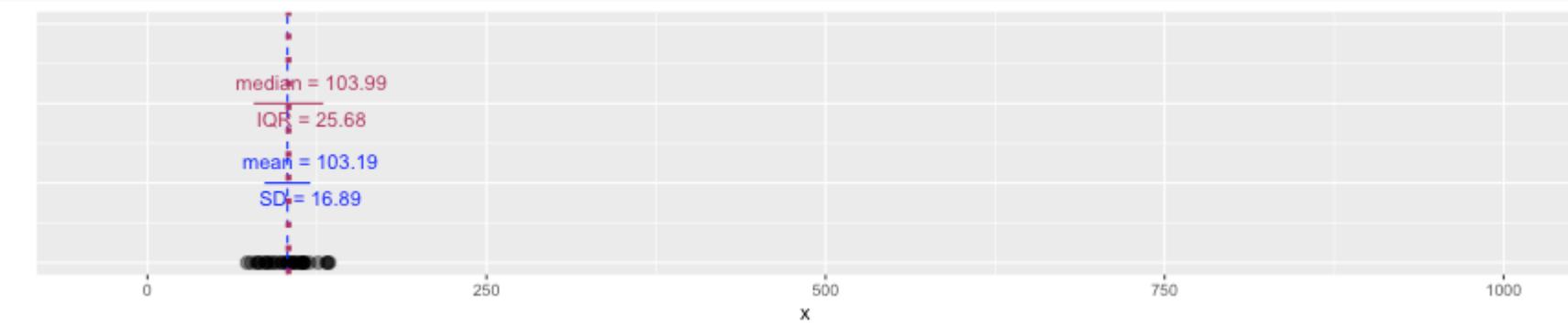
```
## [1] 25.68004
```



Robust Statistics

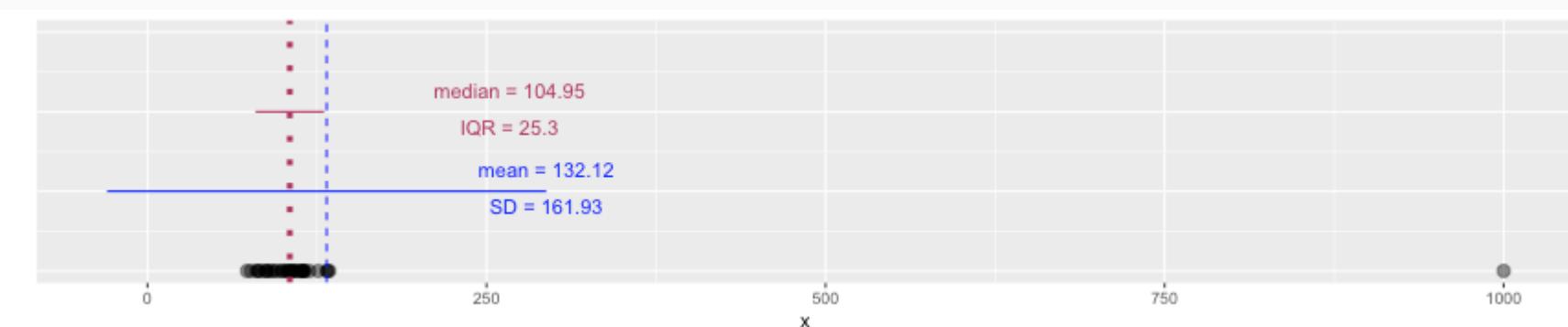


Robust Statistics



Let's add an extreme value:

```
x <- c(x, 1000)
```



Robust Statistics

Median and IQR are more robust to skewness and outliers than mean and SD. Therefore,

- for skewed distributions it is often more helpful to use median and IQR to describe the center and spread
- for symmetric distributions it is often more helpful to use the mean and SD to describe the center and spread

Grammer of Graphics





Data Visualizations with ggplot2

- `ggplot2` is an R package that provides an alternative framework based upon Wilkinson's (2005) Grammar of Graphics.
- `ggplot2` is, in general, more flexible for creating "prettier" and complex plots.
- Works by creating layers of different types of objects/geometries (i.e. bars, points, lines, polygons, etc.) `ggplot2` has at least three ways of creating plots:
 1. `qplot`
 2. `ggplot(...)` + `geom_XXX(...)` + ...
 3. `ggplot(...)` + `layer(...)`
- We will focus only on the second.



Parts of a ggplot2 Statement

- Data

```
ggplot(myDataFrame, aes(x=x, y=y))
```

- Layers

```
geom_point(), geom_histogram()
```

- Facets

```
facet_wrap(~ cut), facet_grid(~ cut)
```

- Scales

```
scale_y_log10()
```

- Other options

```
ggtitle('my title'), ylim(c(0, 10000)), xlab('x-axis label')
```



Lots of geoms

```
ls('package:ggplot2')[grep('^geom_', ls('package:ggplot2'))]
```

```
## [1] "geom_abline"          "geom_area"           "geom_bar"            "geom_blank"          "geom_contour"        "geom_crossbar"       "geom_density_2d"      "geom_hex"            "geom_jitter"         "geom_linerange"      "geom_point"          "geom_raster"         "geom_rug"            "geom_sf_label"       "geom_spoke"          "geom_tile"           "geom_vline"          "geom_bar"            "geom_bin2d"          "geom_col"            "geom_count"          "geom_density"        "geom_errorbar"       "geom_errorbarh"      "geom_function"       "geom_hline"          "geom_line"           "geom_map"            "geom_path"           "geom_polygon"        "geom_point"          "geom_qq"             "geom_rect"           "geom_ribbon"         "geom_sf_label"       "geom_smooth"         "geom_text"           "geom_sf_label"       "geom_step"           "geom_vline"
```



Data Visualization Cheat Sheet

Data Visualization with ggplot2 :: CHEAT SHEET



Basics

ggplot2 is based on the **grammar of graphics**, the idea that you can build every graph from the same components: a **data set**, a **coordinate system**, and **geoms**—visual marks that represent data points.



To display values, map variables in the data to visual properties of the geom (**aesthetics**) like **size**, **color**, and **x** and **y** locations.



Complete the template below to build a graph.

```
ggplot(data = <DATA>) +
  <GEO FUNCTION>(mapping = aes(<POSITION>),
  stat = <STAT>, position = <POSITION>) +
  <COORDINATE FUNCTION> +
  <FACET FUNCTION> +
  <SCALE FUNCTION> +
  <THEME FUNCTION>
```

↑ required
Not required, sensible defaults supplied

`ggplot(data = mpg, aes(x = cyl, y = hwy))` Begins a plot that you finish by adding layers to. Add one geom function per layer.

`aesthetic mappings data geom`

`qplot(x = cyl, y = hwy, data = mpg, geom = "point")` Creates a complete plot with given data, geom, and mappings. Supplies many useful defaults.

`last_plot()` Returns the last plot

`ggsave("plot.png", width = 5, height = 5)` Saves last plot as 5' x 5' file named "plot.png" in working directory. Matches file type to file extension.

Geoms

Use a geom function to represent data points, use the geom's aesthetic properties to represent variables. Each function returns a layer.

GRAPHICAL PRIMITIVES

```
a <- ggplot(economics, aes(date, unemploy))
b <- ggplot(seals, aes(x = long, y = lat))

a + geom_blank()
# (useful for expanding limits)

b + geom_curve(aes(yend = lat + 1,
xend = long + 1, curvature = z)) -> x, yend, y, end,
alpha, angle, color, curvature, linetype, hjust,
vjust

a + geom_path(lineend = "butt", linejoin = "round",
linemtire = 1)
x, y, alpha, color, group, linetype, size

a + geom_polygon(aes(group = group))
x, y, alpha, color, fill, group, linetype, size

b + geom_rect(aes(xmin = long, ymin = lat, xmax =
long + 1, ymax = lat + 1)) -> xmin, ymin, ymax,
ymin, alpha, color, fill, linetype, size

a + geom_ribbon(aes(ymin = unemploy - 900,
ymax = unemploy + 900)) -> y, ymax, ymin,
alpha, color, fill, group, linetype, size
```

LINE SEGMENTS

```
common aesthetics: x, y, alpha, color, linetype, size
b + geom_abline(aes(intercept = 0, slope = 1))
b + geom_hline(aes(yintercept = lat))
b + geom_vline(aes(xintercept = long))
b + geom_spoke(aes(angle = 1:115, radius = 1))
```

ONE VARIABLE continuous

```
c <- ggplot(mpg, aes(hwy)); c2 <- ggplot(mpg)

c + geom_area(stat = "bin")
x, y, alpha, color, fill, linetype, size

c + geom_density(kernel = "gaussian")
x, y, alpha, color, fill, group, linetype, size, weight

c + geom_dotplot()
x, y, alpha, color, fill

c + geom_freqpoly()
x, y, alpha, color, group, linetype, size

c + geom_histogram(binwidth = 5)
x, y, alpha, color, fill, linetype, size, weight

c2 + geom_qq(aes(sample = hwy)) -> x, y, alpha,
color, fill, linetype, size, weight
```

discrete

```
d <- ggplot(mpg, aes(f))
d + geom_bar()
x, alpha, color, fill, linetype, size, weight
```

TWO VARIABLES

continuous x , continuous y

```
e <- ggplot(mpg, aes(cty, hwy))

e + geom_label(aes(label = cty), nudge_x = 1,
nudge_y = 1, check_overlap = TRUE)x, y, label,
alpha, angle, color, family, fontface, hjust,
vjust

e + geom_jitter(height = 2, width = 2)
x, y, alpha, color, fill, shape, size

e + geom_point(), x, y, alpha, color, fill, shape,
size, stroke

e + geom_quartile(), x, y, alpha, color, group,
linetype, size, weight
```

```
e + geom_rug(sides = "bl")
x, y, alpha, color, linetype, size

e + geom_smooth(method = lm)
x, y, alpha, color, fill, group, linetype, size, weight

e + geom_text(aes(label = cty), nudge_x = 1,
nudge_y = 1, check_overlap = TRUE)x, y, label,
alpha, angle, color, family, fontface, hjust,
lineheight, size, vjust
```

discrete x , continuous y

```
f <- ggplot(mpg, aes(class, hwy))

f + geom_col()
x, y, alpha, color, fill, group, linetype, size

f + geom_boxplot()
x, y, lower, middle, upper,
ymin, ymax, alpha, color, fill, group, linetype,
shape, size, weight

f + geom_dotplot(binaxis = "y", stackdir =
"center")
x, y, alpha, color, fill, group

f + geom_violin(scale = "area")
x, y, alpha, color, fill, group, linetype, size, weight
```

discrete x , discrete y

```
g <- ggplot(diamonds, aes(cut, color))

g + geom_count(), x, y, alpha, color, fill, shape,
size, stroke
```

THREE VARIABLES

```
seals$z <- with(seals, sqrt(delta_long^2 + delta_lat^2))l <- ggplot(seals, aes(long, lat))
```

```
l + geom_contour(aes(z = z))
x, y, z, alpha, colour, group, linetype, size, weight
```

continuous bivariate distribution

```
h <- ggplot(diamonds, aes(carat, price))

h + geom_binned(binwidth = c(0.25, 500))
x, y, alpha, color, fill, linetype, size, weight

h + geom_hex()
x, y, alpha, colour, fill, size
```

continuous function

```
i <- ggplot(economics, aes(date, unemploy))

i + geom_area()
x, y, alpha, color, fill, linetype, size

i + geom_line()
x, y, alpha, color, group, linetype, size

i + geom_step(direction = "hv")
x, y, alpha, color, group, linetype, size
```

visualizing error

```
df <- data.frame(grp = c("A", "B"), fit = 4:5, se = 1:2)
j <- ggplot(df, aes(grp, fit, ymin = fit - se, ymax = fit + se))

j + geom_crossbar(fatten = 2)
x, y, ymax, ymin, alpha, color, fill, group, linetype,
size

j + geom_errorbar()
x, y, max, ymin, alpha, color, group, linetype, size, width (also
geom_errorbarh())

j + geom_linerange()
x, ymin, ymax, alpha, color, group, linetype, size

j + geom_pointrange()
x, y, ymin, ymax, alpha, color, fill, group, linetype,
shape, size
```

maps

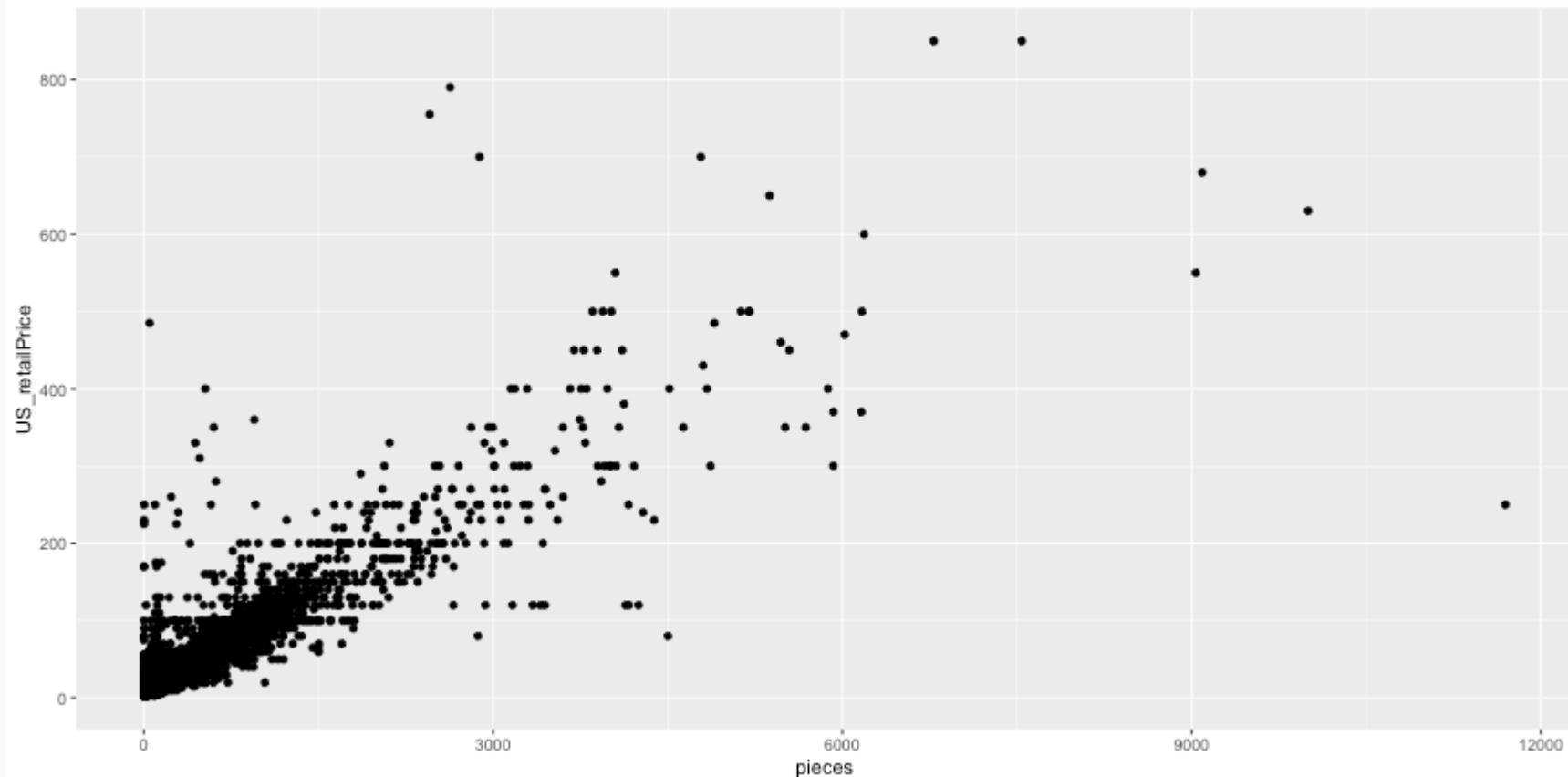
```
data <- data.frame(murder = USArrests$Murder,
state = tolower(rownames(USArrests)))
map <- map_data("state")
k <- ggplot(data, aes(fill = murder))

k + geom_map(aes(map_id = state), map = map)
+ expand_limits(x = map$long, y = map$lat),
map_id, alpha, color, fill, linetype, size
```



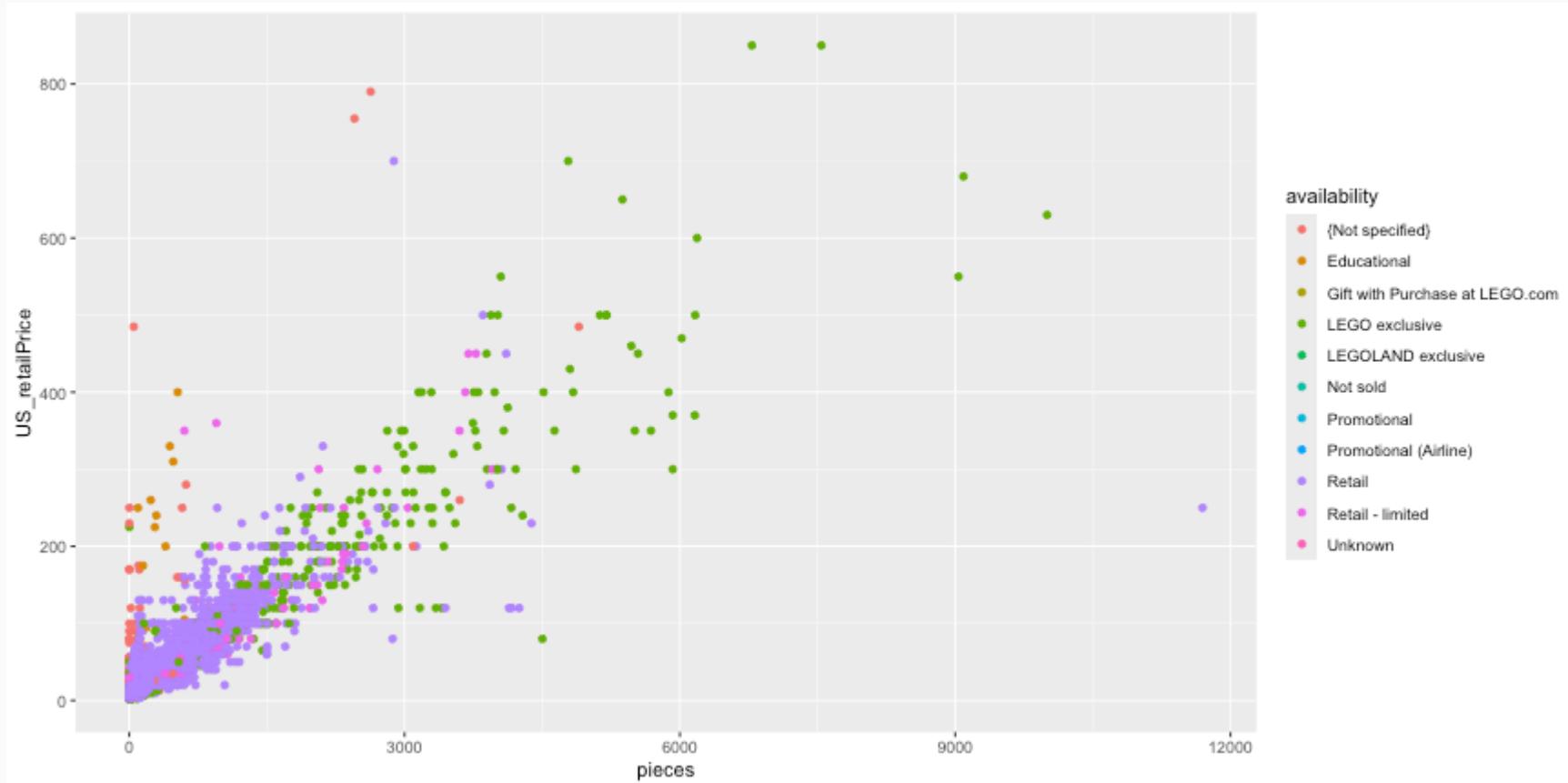
Scatterplot

```
ggplot(legosets, aes(x=pieces, y=US_retailPrice)) + geom_point()
```



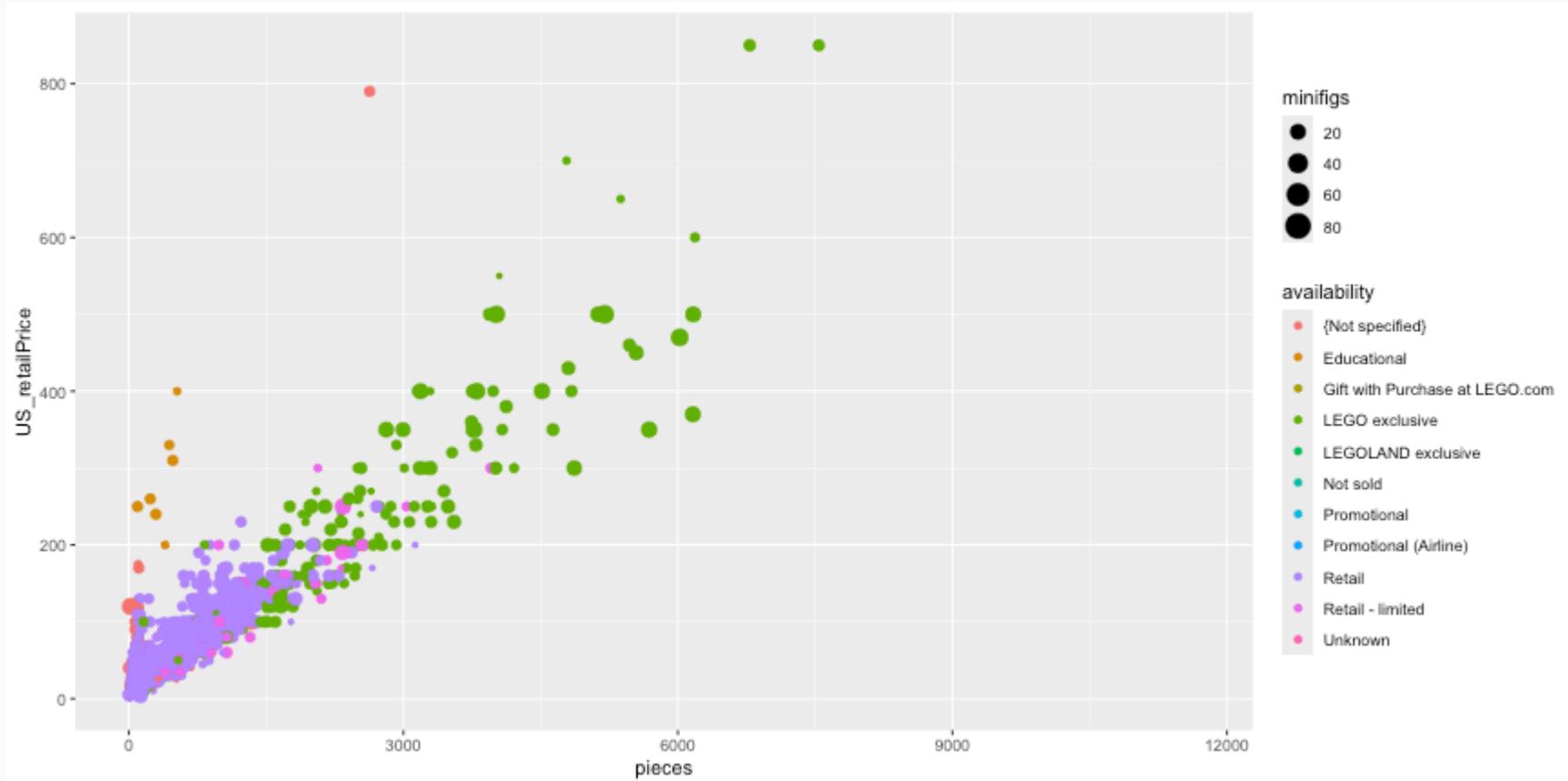
Scatterplot (cont.)

```
ggplot(legosets, aes(x=pieces, y=US_retailPrice, color=availability)) + geom_point()
```



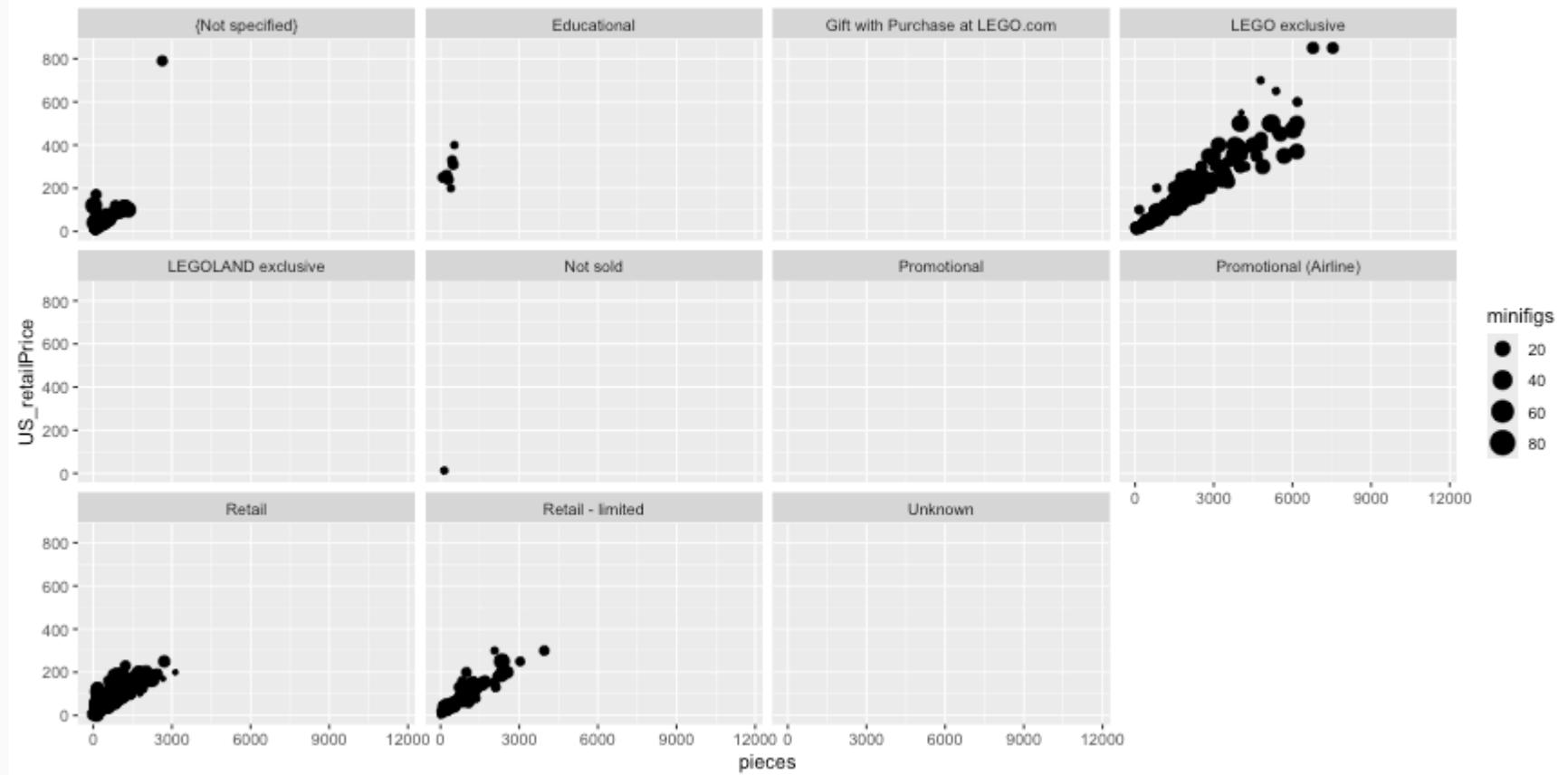
Scatterplot (cont.)

```
ggplot(legosets, aes(x=pieces, y=US_retailPrice, size=minifigs, color=availability)) + geom_point()
```



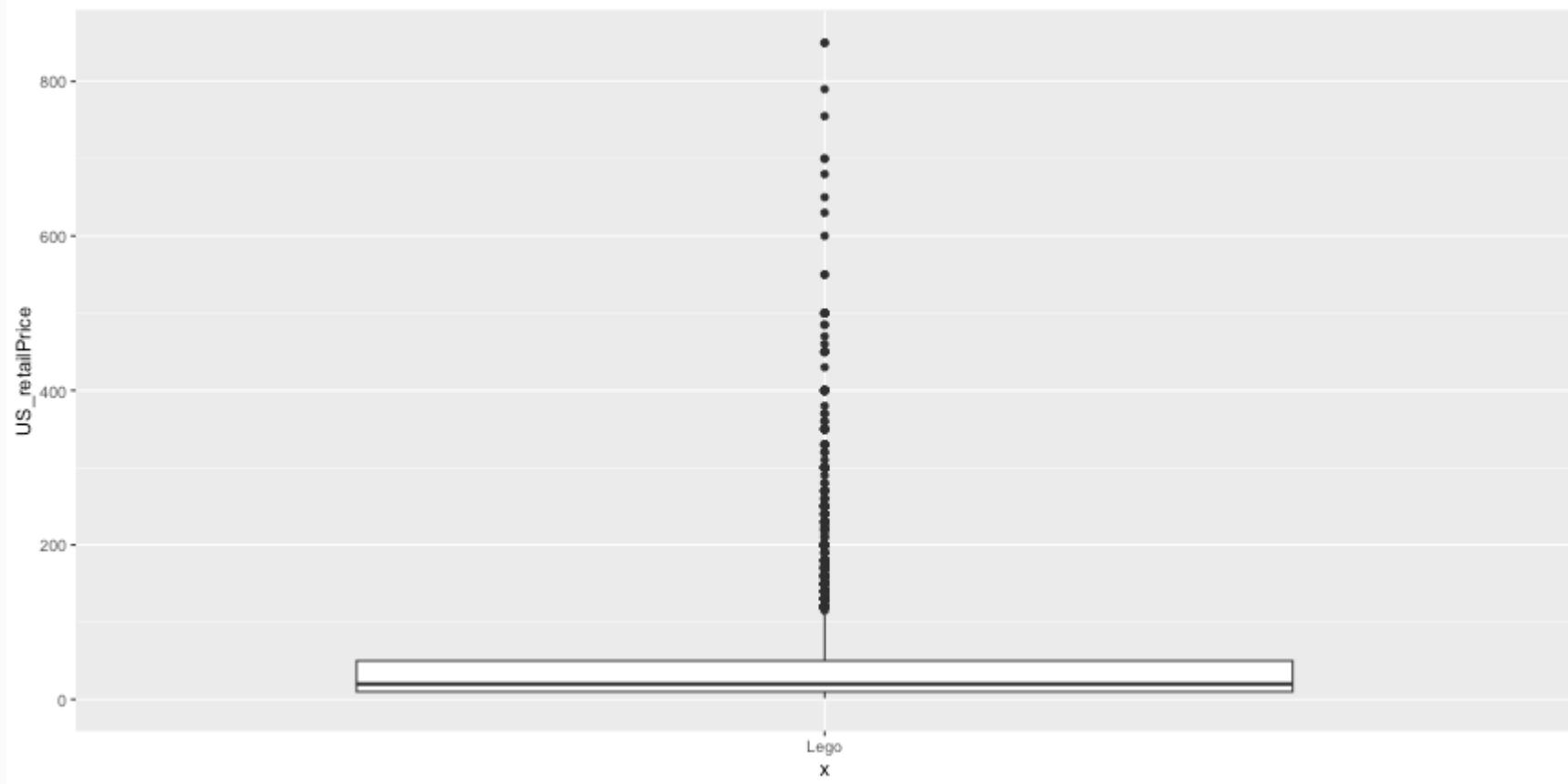
Scatterplot (cont.)

```
ggplot(legosets, aes(x=pieces, y=US_retailPrice, size=minifigs)) + geom_point() + facet_wrap(~ availability)
```



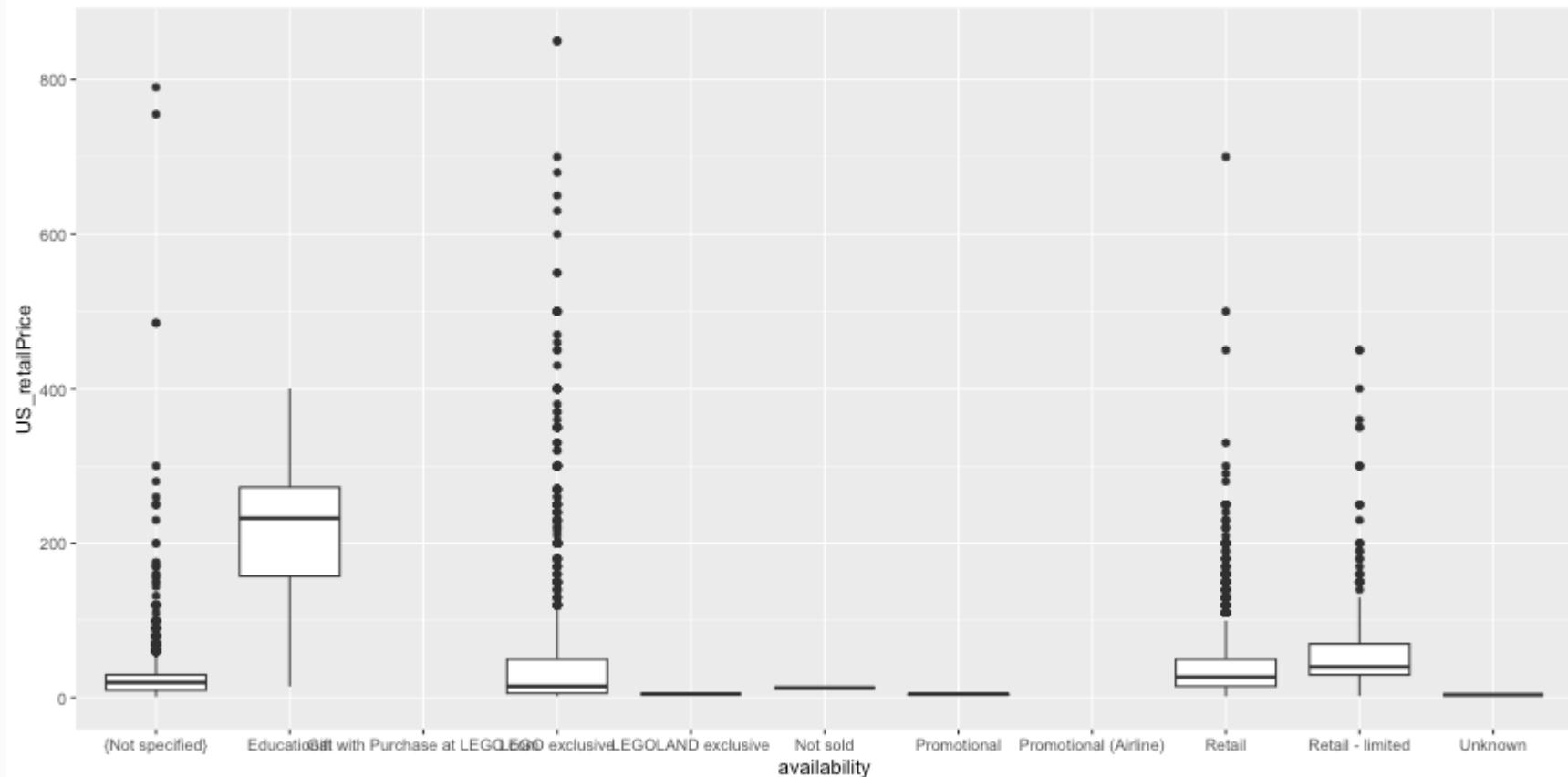
Boxplots

```
ggplot(legosets, aes(x='Lego', y=US_retailPrice)) + geom_boxplot()
```



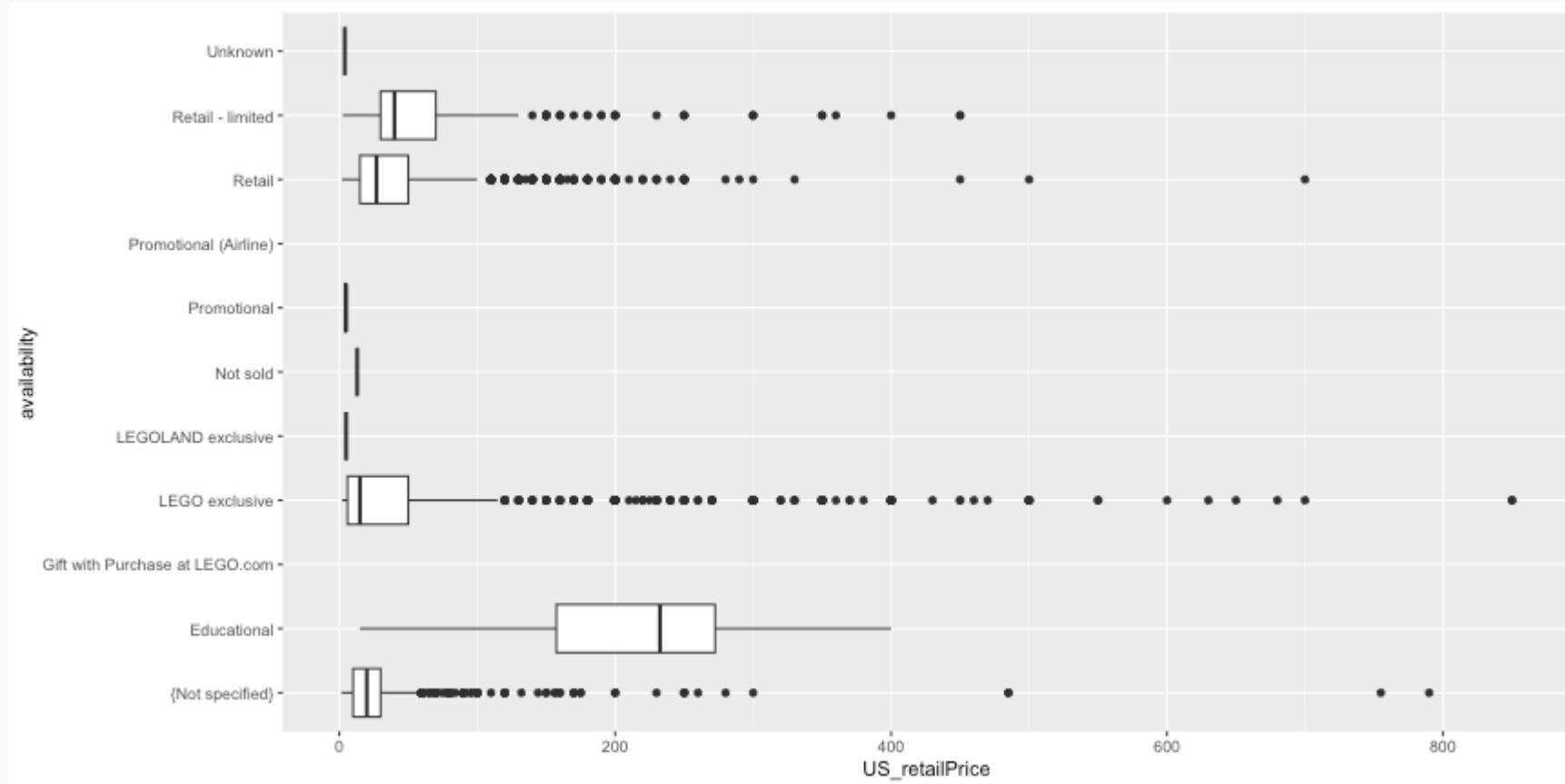
Boxplots (cont.)

```
ggplot(legosets, aes(x=availability, y=US_retailPrice)) + geom_boxplot()
```



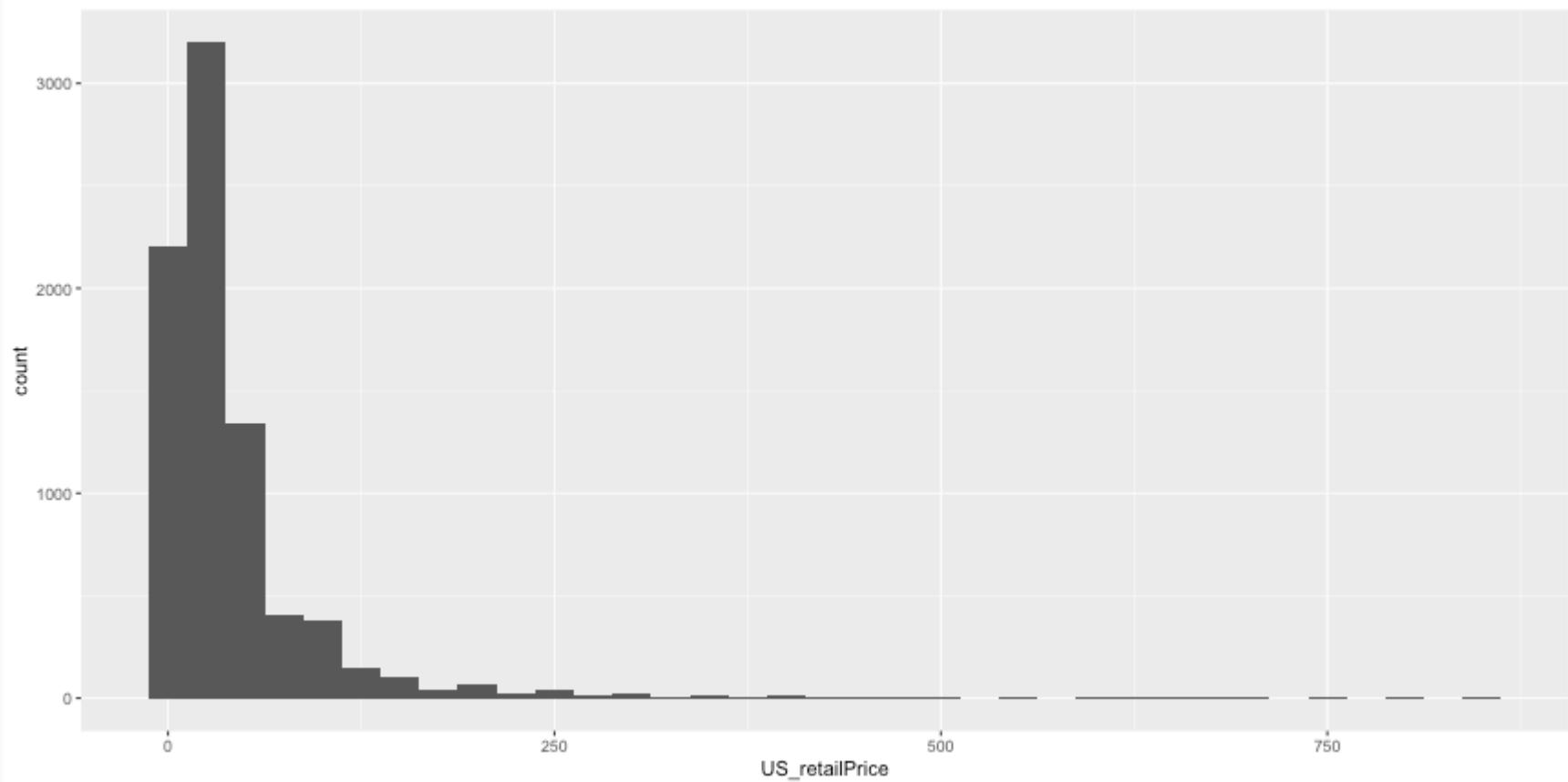
Boxplot (cont.)

```
ggplot(legosets, aes(x=availability, y=US_retailPrice)) + geom_boxplot() + coord_flip()
```



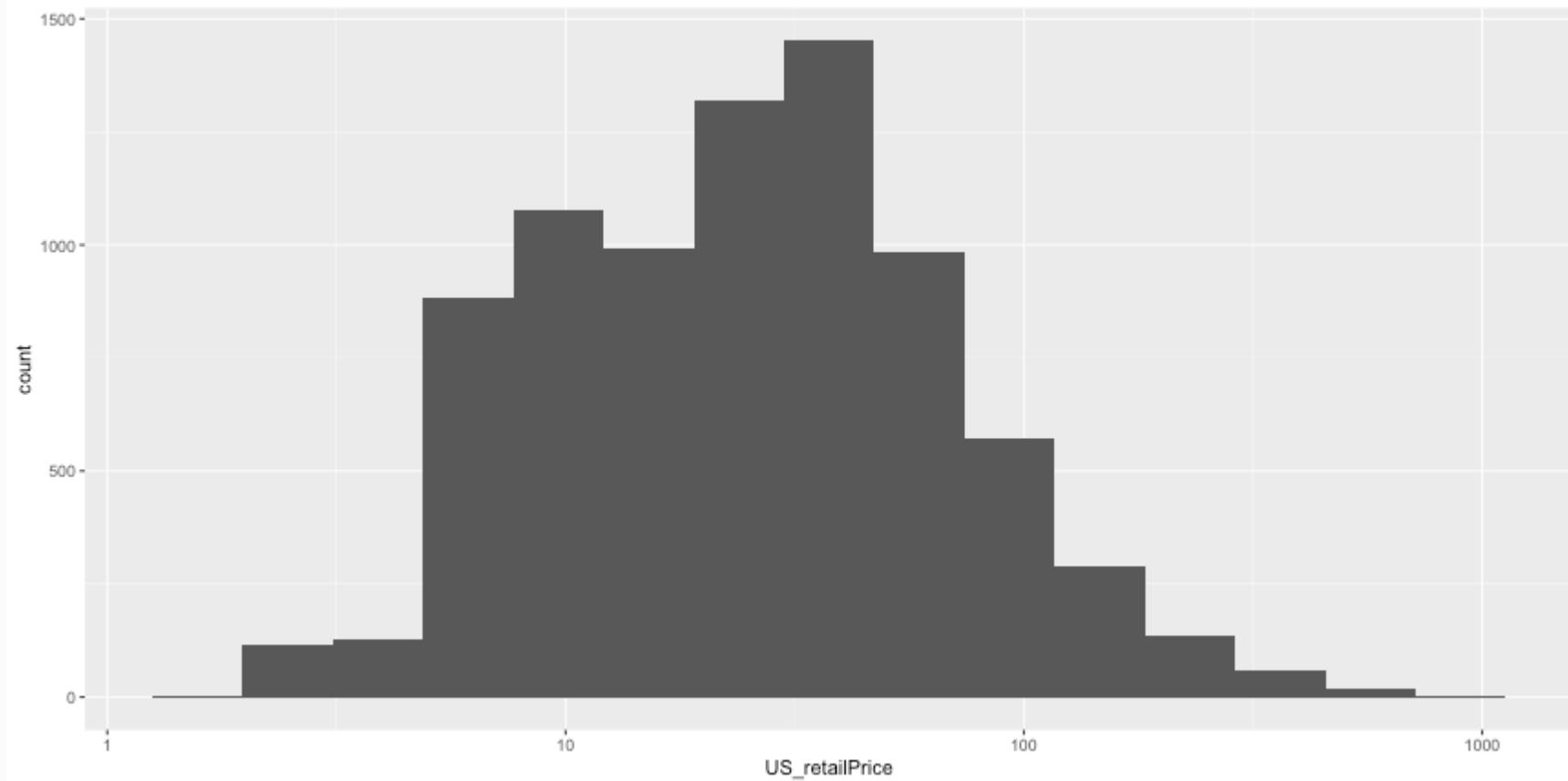
Histograms

```
ggplot(legosets, aes(x = US_retailPrice)) + geom_histogram(binwidth = 25)
```



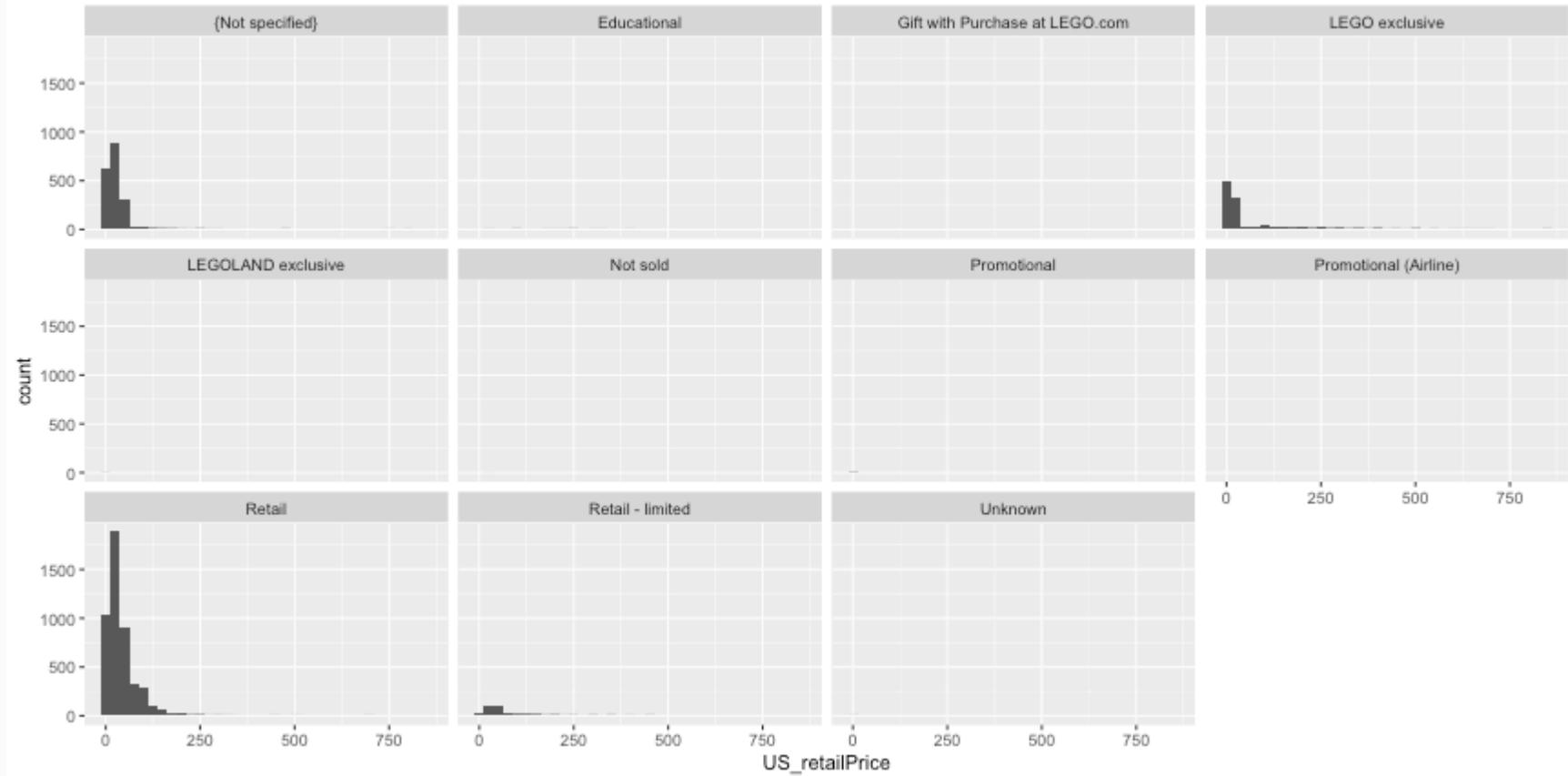
Histograms (cont.)

```
ggplot(legosets, aes(x = US_retailPrice)) + geom_histogram(bins = 15) + scale_x_log10()
```



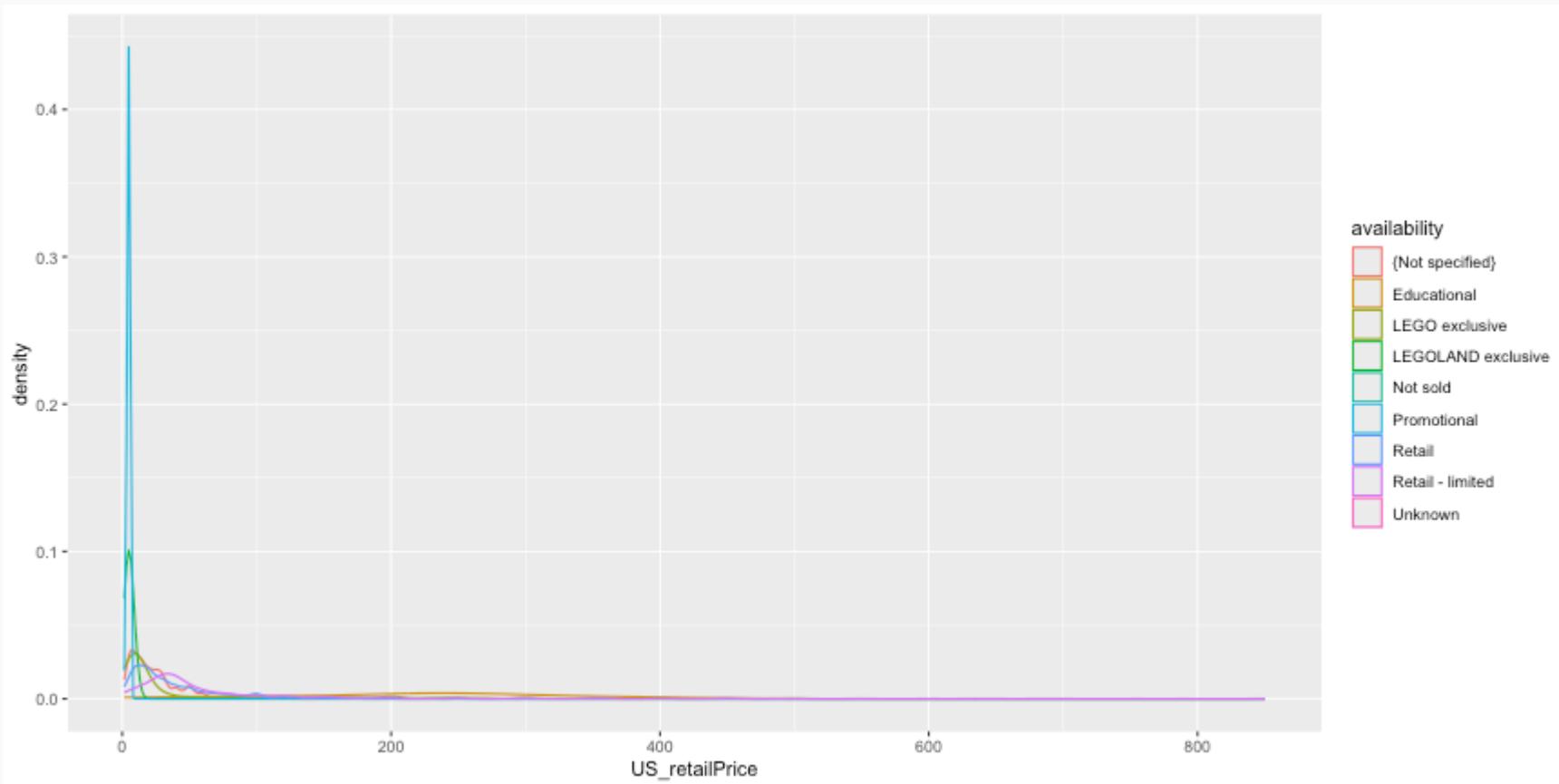
Histograms (cont.)

```
ggplot(legosets, aes(x = US_retailPrice)) + geom_histogram(binwidth = 25) + facet_wrap(~ availability)
```



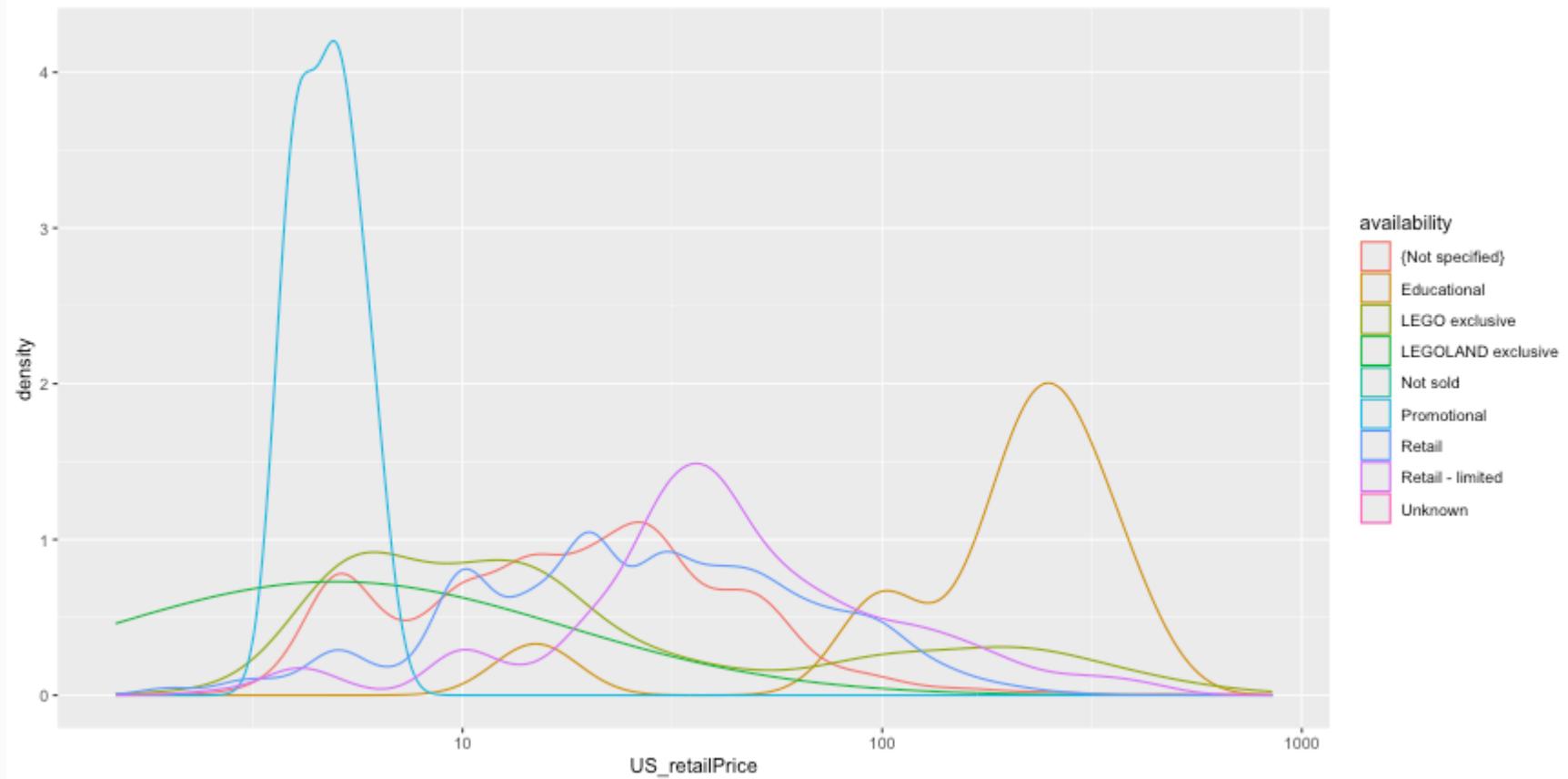
Density Plots

```
ggplot(legosets, aes(x = US_retailPrice, color = availability)) + geom_density()
```

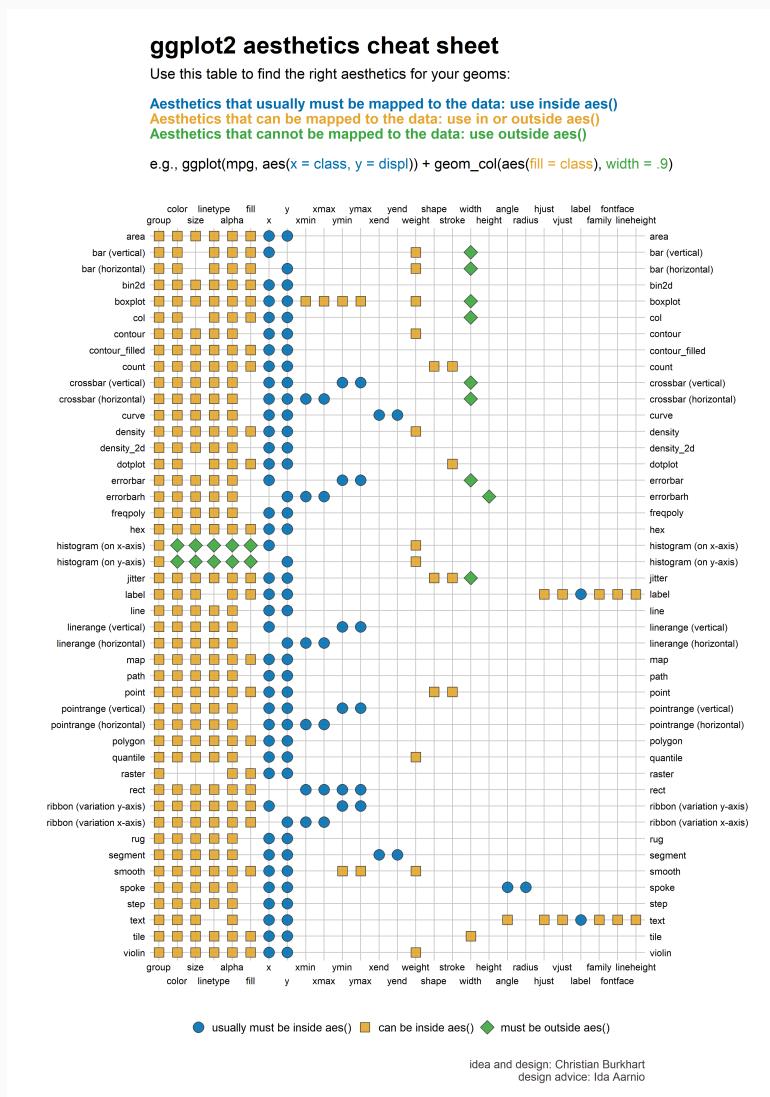


Density Plots (cont.)

```
ggplot(legosets, aes(x = US_retailPrice, color = availability)) + geom_density() + scale_x_log10()
```



ggplot2 aesthetics





Likert Scales

Likert scales are a type of questionnaire where respondents are asked to rate items on scales usually ranging from four to seven levels (e.g. strongly disagree to strongly agree).

```
library(likert)
library(reshape)
data(pisaitems)
items24 <- pisaitems[,substr(names(pisaitems), 1,5) == 'ST24Q']
items24 <- rename(items24, c(
  ST24Q01="I read only if I have to.",
  ST24Q02="Reading is one of my favorite hobbies.",
  ST24Q03="I like talking about books with other people.",
  ST24Q04="I find it hard to finish books.",
  ST24Q05="I feel happy if I receive a book as a present.",
  ST24Q06="For me, reading is a waste of time.",
  ST24Q07="I enjoy going to a bookstore or a library.",
  ST24Q08="I read only to get information that I need.",
  ST24Q09="I cannot sit still and read for more than a few minutes.",
  ST24Q10="I like to express my opinions about books I have read.",
  ST24Q11="I like to exchange books with my friends."))
```



likert R Package

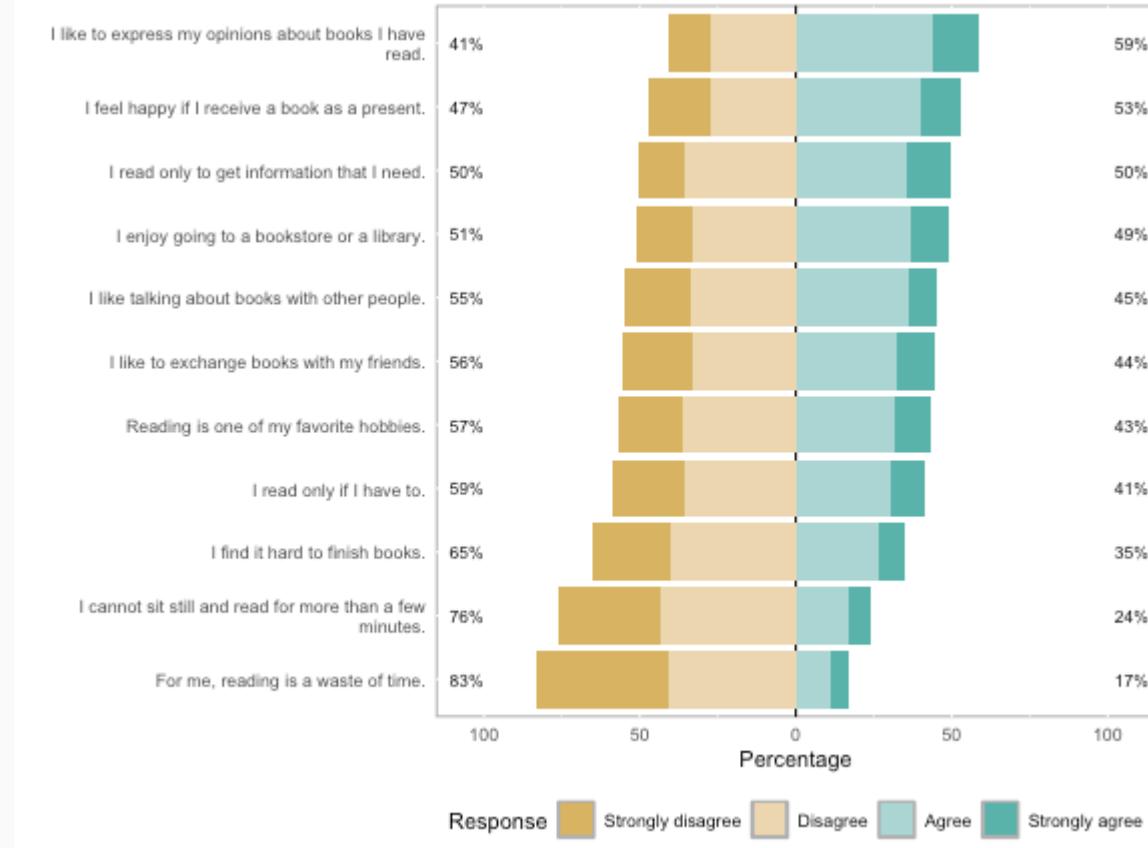
```
l24 <- likert(items24)
summary(l24)
```

```
##                                     Item    low  neutral
## 10   I like to express my opinions about books I have read. 41.07516      0
## 5     I feel happy if I receive a book as a present. 46.93475      0
## 8     I read only to get information that I need. 50.39874      0
## 7     I enjoy going to a bookstore or a library. 51.21231      0
## 3     I like talking about books with other people. 54.99129      0
## 11    I like to exchange books with my friends. 55.54115      0
## 2     Reading is one of my favorite hobbies. 56.64470      0
## 1     I read only if I have to. 58.72868      0
## 4     I find it hard to finish books. 65.35125      0
## 9   I cannot sit still and read for more than a few minutes. 76.24524      0
## 6     For me, reading is a waste of time. 82.88729      0
##          high    mean      sd
## 10 58.92484 2.604913 0.9009968
## 5  53.06525 2.466751 0.9446590
## 8  49.60126 2.484616 0.9089688
## 7  48.78769 2.428508 0.9164136
## 3  45.00871 2.328049 0.9090326
## 11 44.45885 2.343193 0.9609234
## 2  43.35530 2.344530 0.9277495
```



likert Plots

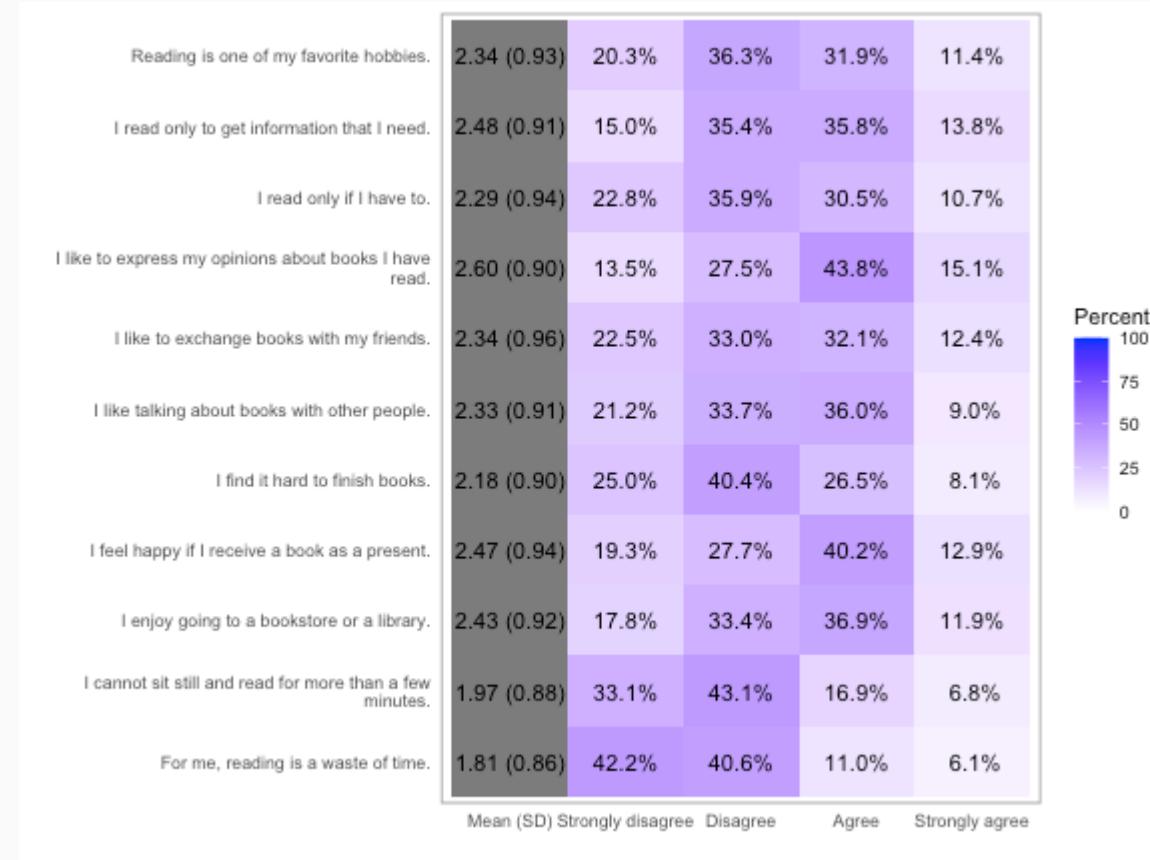
```
plot(l24)
```





likert Plots

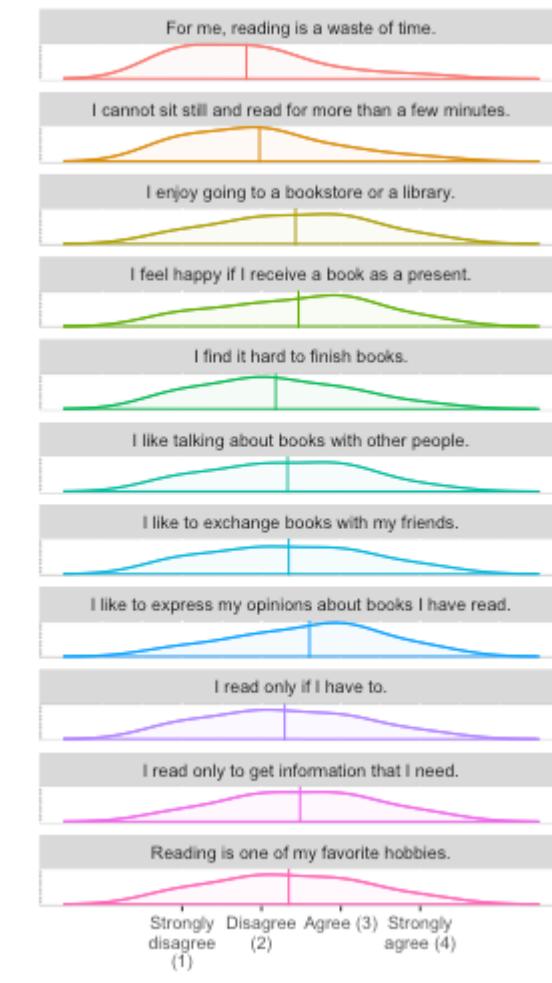
```
plot(l24, type='heat')
```





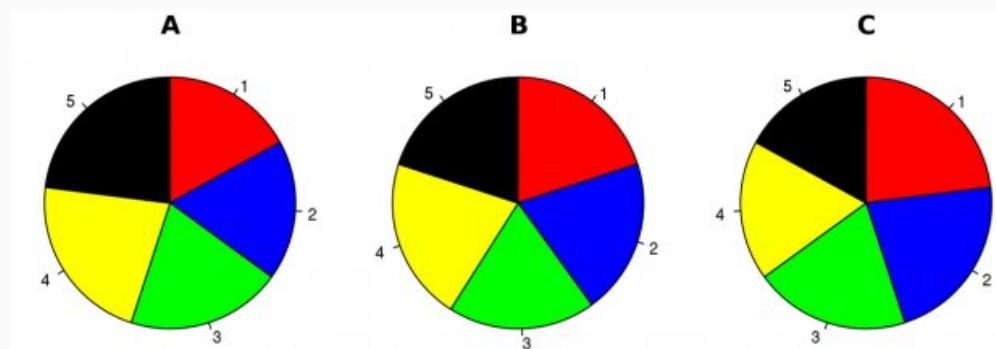
likert Plots

```
plot(l24, type='density')
```



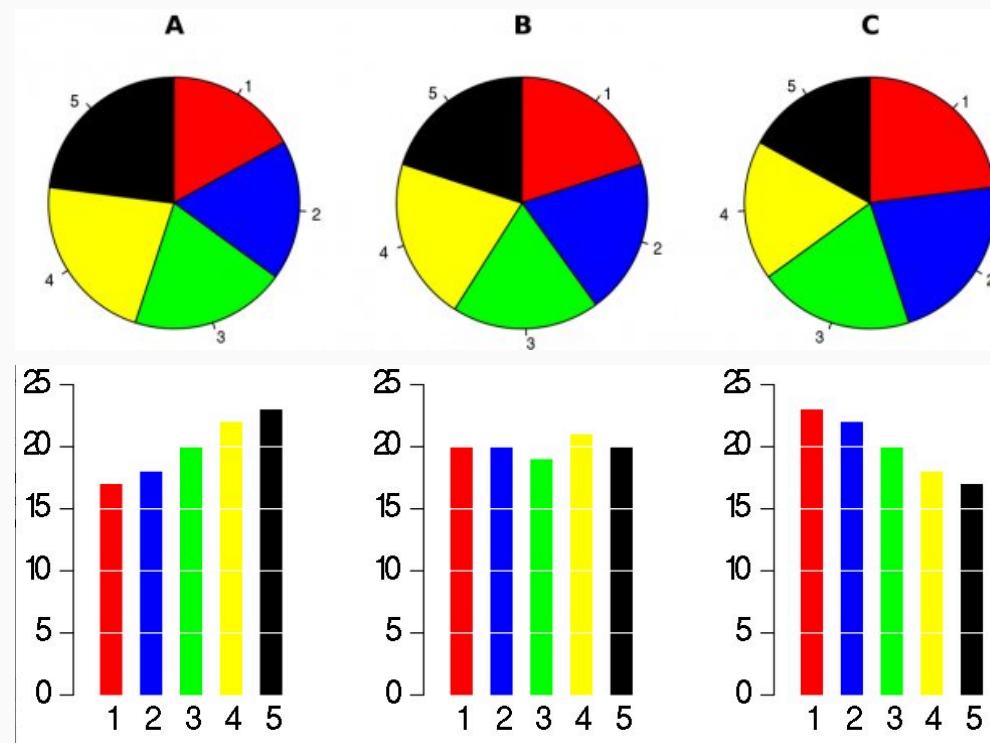
Pie Charts

There is only one pie chart in *OpenIntro Statistics* (Diez, Barr, & Çetinkaya-Rundel, 2015, p. 48). Consider the following three pie charts that represent the preference of five different colors. Is there a difference between the three pie charts? This is probably a difficult to answer.



Pie Charts

There is only one pie chart in *OpenIntro Statistics* (Diez, Barr, & Çetinkaya-Rundel, 2015, p. 48). Consider the following three pie charts that represent the preference of five different colors. Is there a difference between the three pie charts? This is probably a difficult to answer.



"There is no data that can be displayed in a pie chart that cannot better be displayed in some other type of chart"

John Tukey

Additional Resources

For data visualization:

- `ggplot2` website: <https://ggplot2.tidyverse.org>
- R for Data Science book: <https://r4ds.had.co.nz/data-visualisation.html>
- R Graphics Cookbook: <https://r-graphics.org>
- Data visualization cheat sheet: <https://github.com/rstudio/cheatsheets/raw/master/data-visualization-2.1.pdf>

One Minute Paper

1. What was the most important thing you learned during this class?
2. What important question remains unanswered for you?



<https://forms.gle/sTwKB3HivjtbafBb7>