

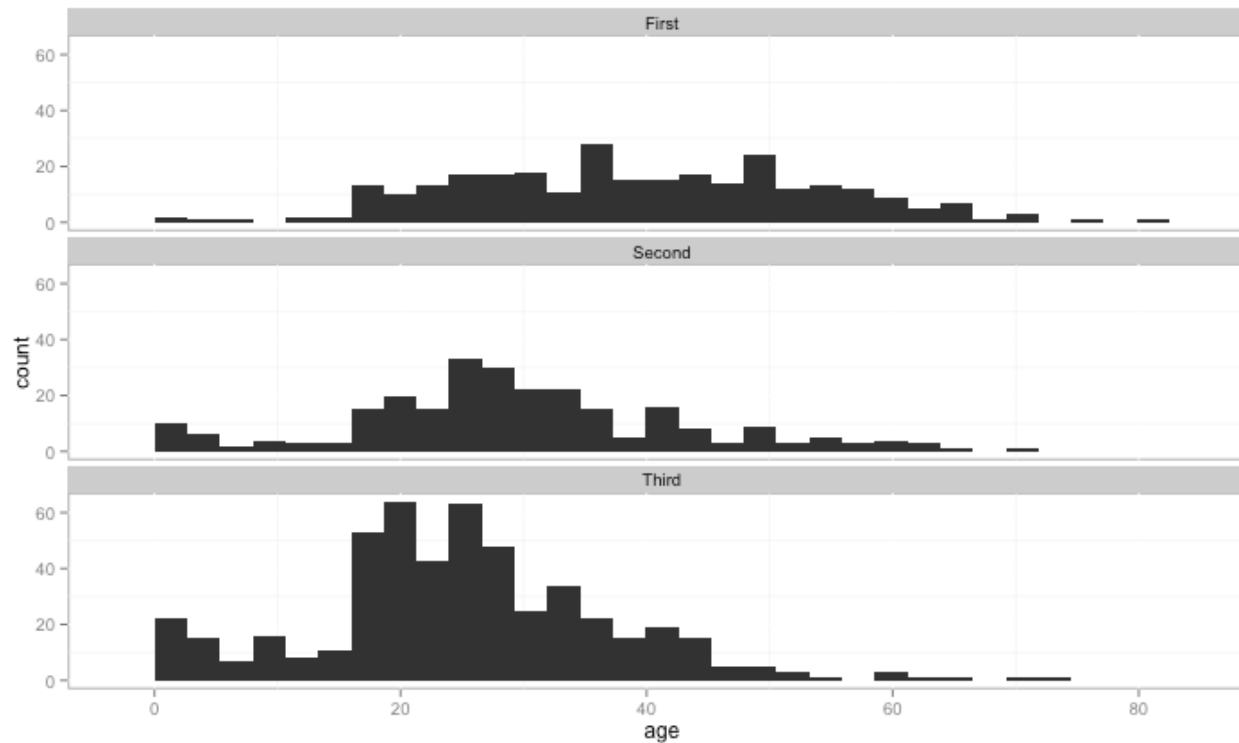
# Distributions

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# Comparing Histograms

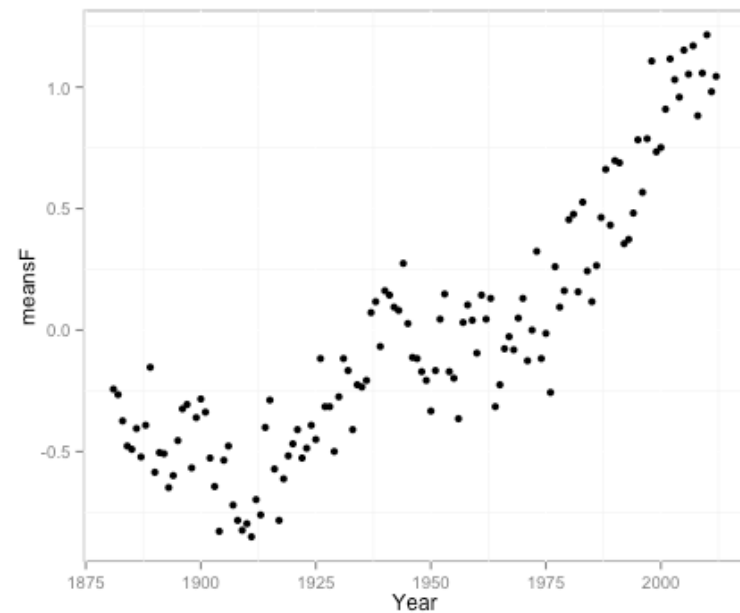
```
ggplot(titanic, aes(x=age)) + geom_histogram() + facet_wrap(~ pclass, ncol=1)
```



# Timeplots

- Timeplots display every data value on a timeline.
- Great for spotting trends

```
ggplot(temp, aes(x=Year, y=meansF)) +  
  geom_point()
```



# Connecting the Dots

- Connecting the dots of a timeplot can sometimes better illustrate the trends.
- This example has so many dots that this graph is busy and not that illustrative.
- Connecting the dots is better for either fewer data values or data with less variation.

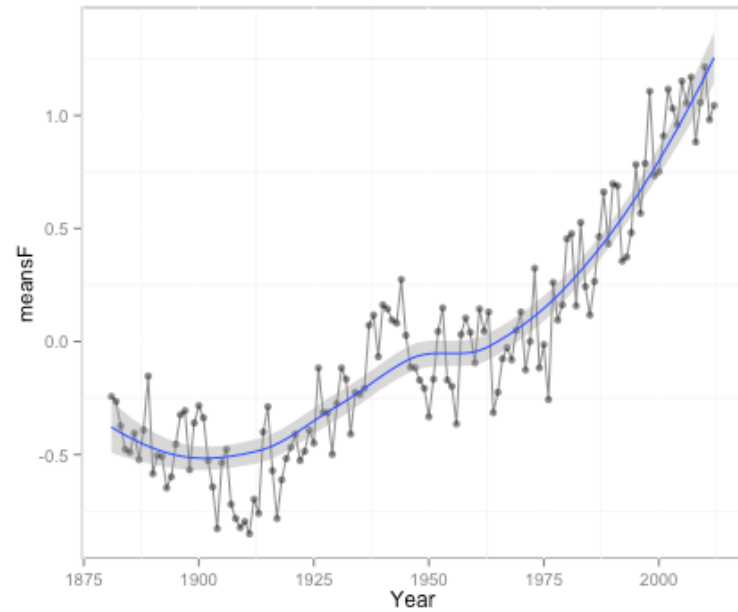
```
ggplot(temp, aes(x=Year, y=meansF)) +  
  geom_point(alpha=.5) +  
  geom_line()
```



# Smoothing the Data

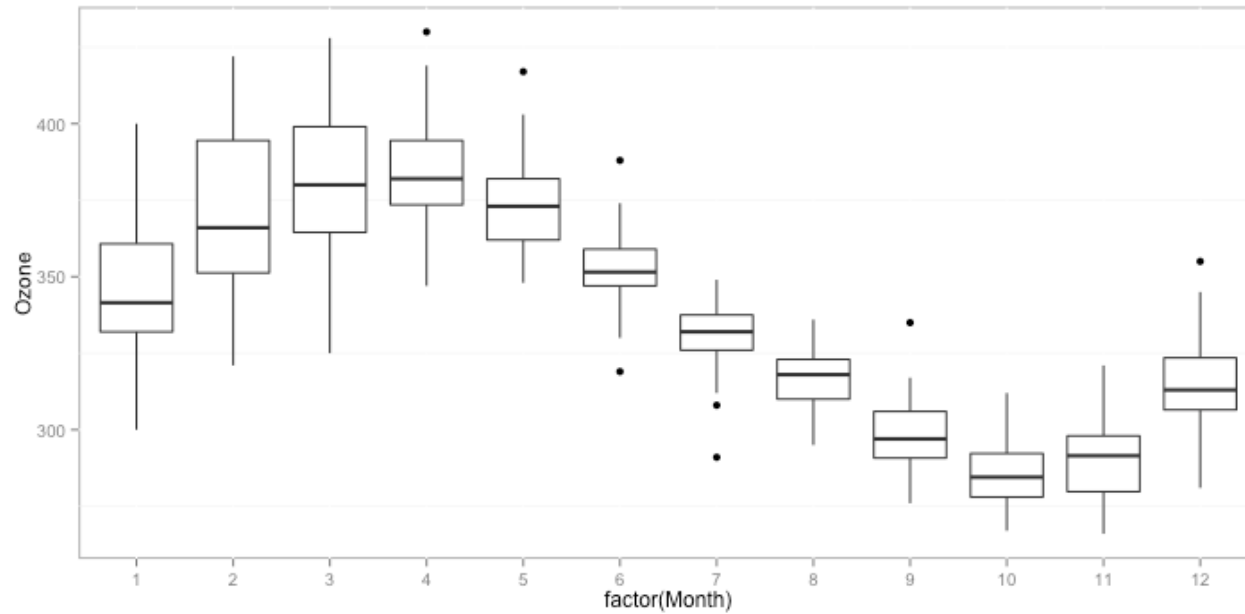
- Drawing a curve of typical values in the neighborhood can sometimes tell the story better.
- There are many ways of doing this and a computer can be used to create this curve.
- The curve, called the lowess (or loess) curve, helps the eye follow the main trend and spot the outliers.

```
ggplot(temp, aes(x=Year, y=meansF)) +  
  geom_point(alpha=.5) +  
  geom_line(alpha=.5) +  
  geom_smooth()
```



# Boxplots

```
ggplot(ozone, aes(x = factor(Month), y = Ozone)) + geom_boxplot()
```



# Outliers

## How to Approach Outliers

- Check to see if there may have been an error in the data collection or data input.
  - If the reported heights of students includes a student that is 170 inches tall (14 feet), maybe that student was measured in centimeters.
- Check to see if there was an extraordinary outcome.
  - The median number of daily customers at the Punxsutawney, PA, gift store may be 42 with an IQR of 12, but on February 2, there were 831 customers.

## Common Errors Causing an Outlier

- Transposing the digits
- A respondent not understanding the survey question
- Misreading results
- Confusion about units
- Cheating

# However, Outliers Can be the Most Interesting Data Values

- Income Data: The CEO
- Student Height: The basketball team's center
- Snowfall: The great blizzard of '98
- Exam Score: The curve breaker
- Milk Purchased: Octomom!

Always comment on the outliers.



# Transforming Data

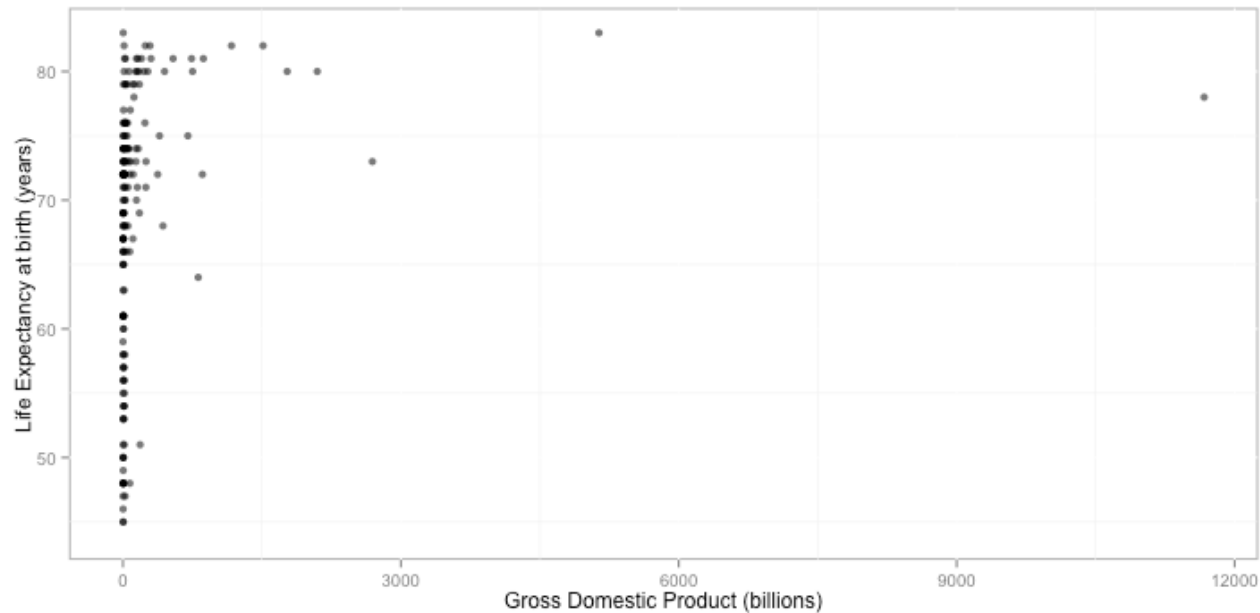
- When data is skewed it becomes difficult to interpret measures of center and spread.
- Transforming data is an approach to make skewed data more symmetric.

## Common Transformations

- Skewed Right: Use log, ln, or  $\frac{1}{x}$
- Skewed Left: Use  $x^2$

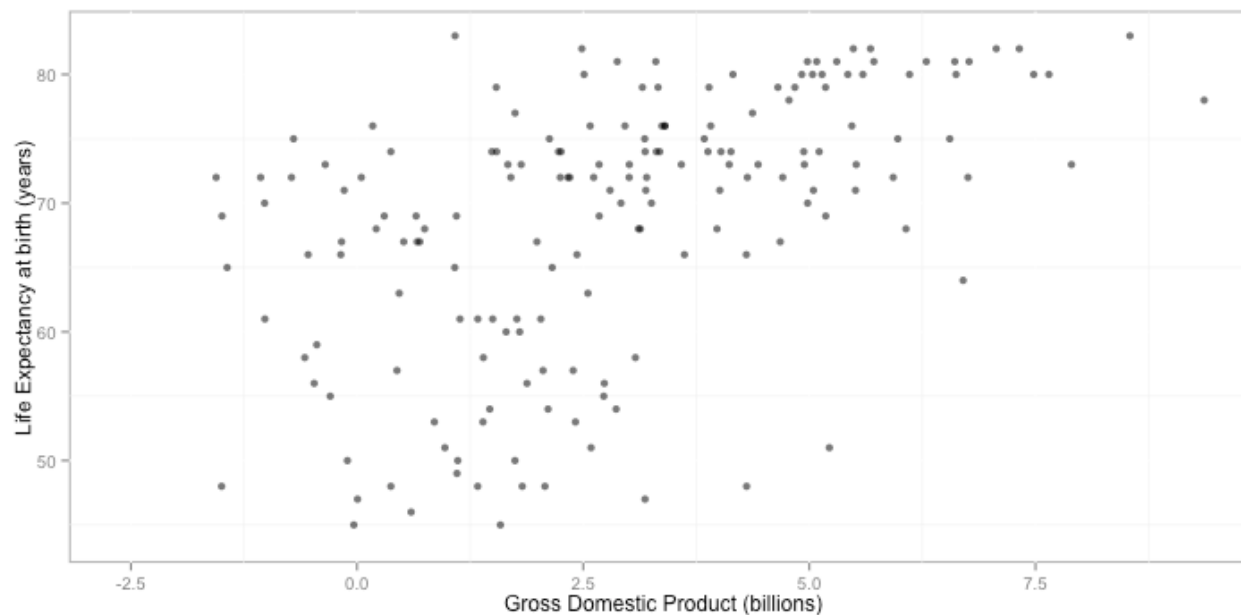
# Example: World GDP and Life Expectancy

```
ggplot(worldData3, aes(x=GDP, y=Life.Expectancy)) +  
  geom_point(stat='identity', alpha=.6) +  
  xlab('Gross Domestic Product (billions)') +  
  ylab('Life Expectancy at birth (years)')
```



# Example: (log of) World GDP and Life Expectancy

```
ggplot(worldData3, aes(x=log(GDP), y=Life.Expectancy)) +  
  geom_point(stat='identity', alpha=.6) +  
  xlab('Gross Domestic Product (billions)') +  
  ylab('Life Expectancy at birth (years)')
```



# On Comparing Distributions

Choose the right tool.

- Use histograms to compare two or three groups.
- Use boxplots to compare many groups.

Treat outliers with attention and care.

- Local or global, especially in a time series
- Investigate if the outliers are errors or remarkable.
- Use a timeplot to track trends over time.

Re-express or transform data for better understanding.

- Can transform skewed distributions to symmetric ones
- Can help to compare spreads of different groups