

# Yahtzee Formulae

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## Abstract

How to determine scores and other values in Yahtzee.  
For all listed values:

number of dice =  $n \geq 2$   
number of sides per die =  $d \geq 2$   
bonus points needed =  $p$   
yahtzee score earned =  $y$   
set of current dice =  $S \subset \mathbb{N} - \{0\}$

## 1 Scores

### 1.1 Rolls per turn

$$rollsperturn = \lceil \max(d, n) * 0.5 \rceil \quad (1)$$

### 1.2 Numbers

$a \in \{1, 2 \dots d\}$   
 $c$  = number of occurrences of  $a$  in  $S$

$$numscore_a = c * a \quad (2)$$

### 1.3 Kinds

$K = \{a \dots\} \subseteq S$

$$smallkindscore = \left\{ \begin{array}{ll} 0, & \text{if } |K| < \lceil n * 0.5 \rceil \\ \sum_{i \in S} i, & \text{if } |K| \geq \lceil n * 0.5 \rceil \end{array} \right\} \quad (3)$$

$$largekindscore = \left\{ \begin{array}{ll} 0, & \text{if } |K| < \lceil n * 0.75 \rceil \\ \sum_{i \in S} i, & \text{if } |K| \geq \lceil n * 0.75 \rceil \end{array} \right\} \quad (4)$$

## 1.4 Full House

$$\begin{aligned} K &= \{a \dots\} \subset S \mid |K| = \lfloor n * 0.5 \rfloor \\ L &= \{b \dots\} \subset S \mid |L| = \lceil n * 0.5 \rceil \\ K \cap L &= \emptyset \end{aligned}$$

$$fullhousescore = \begin{cases} 0, & \text{if } K \cup L \neq S \\ \lceil d * n * 0.83 \rceil, & \text{if } K \cup L = S \end{cases} \quad (5)$$

## 1.5 Straights

Duplicates in set of straights are removed and not considered for this formula  
 $K = \{a, a + 1 \dots\} \subseteq S$

$$smallstraightscore = \begin{cases} 0, & \text{if } |K| < \lceil n * 0.75 \rceil \\ d * n, & \text{if } |K| \geq \lceil n * 0.75 \rceil \end{cases} \quad (6)$$

$$largestraightscore = \begin{cases} 0, & \text{if } |K| < n \\ \lceil d * n * 1.33 \rceil, & \text{if } |K| = n \end{cases} \quad (7)$$

## 1.6 Yahtzee

$$K = \{a \dots a\} = S$$

$$y = \begin{cases} 0, & \text{if } |K| < n \\ \lceil d * n * 1.66 \rceil, & \text{if } |K| = n \end{cases} \quad (8)$$

## 1.7 Chance

$$K = \{a_0 \dots a_{n-1}\} = S$$

$$chancescore = \sum_{i \in S} i \quad (9)$$

# 2 Bonus Scores

## 2.1 Number Score Bonus

$$p = \lceil n * 0.5 \rceil * \sum_{i=1}^d i \quad (10)$$

## 2.2 Bonus points to add

$$numbonusscore = \begin{cases} 0, & \text{if } \sum_{i=1}^d numscore_i < p \\ \lceil d * n * 1.162 \rceil, & \text{if } \sum_{i=1}^d numscore_i \geq p \end{cases} \quad (11)$$

### 2.3 Yahtzee Bonus

$$yahzteebonuscore = \begin{cases} 0, & \text{if } y = 0 \\ \lceil d * n * 3.32 \rceil, & \text{if } y > 0 \end{cases} \quad (12)$$

## 3 Future Formulae

### 3.1 Multiple Straights

Straights are impossible to achieve in the following situation:

Say we have  $K = \{x, x + 1 \dots x + d\} \subset S$  and  $d < n$

Given the above property, a small straight is possible to get if  $d \geq \lceil n * 0.75 \rceil$

A large straight is impossible to achieve in this scenario

A potential correction to this situation follows where

$s$  = number of straights found and

$d < n$

$$straightscore = \begin{cases} s * d * (\lceil d * 0.75 \rceil), & \text{if } smallstraight \\ s * d * (\lceil d * 0.75 \rceil) * 1.33, & \text{if } largeststraight \end{cases} \quad (13)$$

If we wish to make straights more difficult to score, we can use the below formula

$$straightscore = \begin{cases} 0, & \text{if } s < \lceil n * 0.75 \rceil \\ s * d * n, & \text{if } s \geq \lceil n * 0.75 \rceil \text{ and } s < n \\ s * d * n * 1.33, & \text{if } s = n \end{cases} \quad (14)$$