NTIN071 A&G: Tutorial 4 – More on closure properties, regular expressions

Solve 1, 2a-f, 3a-e (the rest is for practice).

Problem 1 (Delete). Let L be a regular language over the alphabet $\Sigma = a, b$. Describe the following languages in set notation. Are these languages (necessarily) also regular? Prove or disprove.

Language consisting of all words obtained from words of the language L by...

- (a) ... deleting all occurrences of the letter a.
- (b) ... deleting the initial letter and writing this letter at the end of the word.
- (c) ... deleting the longest contiguous sequence of a's from the beginning of the word.

Problem 2 (Constructing regular expressions). Find regular expressions representing the following languages over $\Sigma = \{a, b\}$ consisting of words that:

- (a) start with 'abba',
- (b) end with 'abba',
- (c) start with 'ab' and end with 'ba',
- (d) contain 'abba' or 'bab' as a subword,
- (e) do not contain 'aa' as a subword,
- (f) contain an even number of a's,
- (g) have at least 2 letters and the first letter is the same as the last letter,
- (h) the first two letters are the same as the last two letters.

Problem 3 (Regex to automaton). Construct finite automata accepting languages described by the following regular expressions:

(a)
$$ab + ba$$

(e)
$$((ab+c)+a(bc)^*+b)^*$$

(b)
$$a^2 + b^2 + ab$$

(f)
$$((ab+c)^*a(bc)^*+b)^*$$

(c)
$$a + b^*$$

(g)
$$(01^* + 101)^*0^*1$$

(d)
$$(ab + c)^*$$

(h)
$$(01)*11(01)*(0+1)*00$$