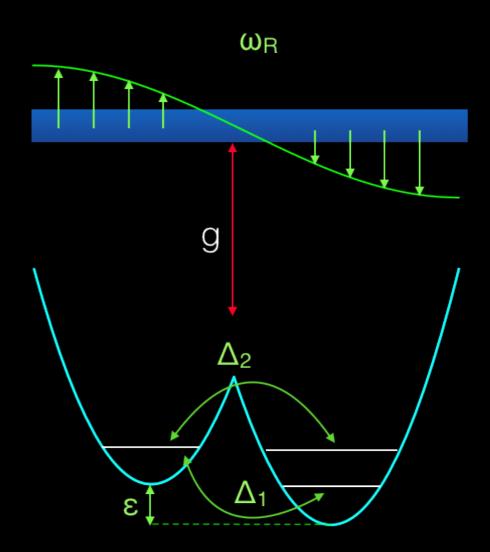
Long-range two-qubit gates: hybrid qubit & quadrupolar

Phys. Rev. A 104, 032612 (2021) Phys. Rev. Research 3 (1), 013171 (2021)

Outline

- -Background and basics
- -Hybrid qubit
 - -HQ basics
 - -HQ sweet spots
 - -Resonant gate
 - -Cavity frequency problem
 - -SB gate
- -Charge-quadrupole qubit
 - -CQ basics
 - -Experiment
 - -Noise characterization
- -Conclusions



Background

Single-qubit gates with 99% fidelities are already achievable

See: Veldhorst et al. Nat. Nano 9, 981-985 (2014)

Kawakami et al. PNAS October 18, 2016 113 (42) 11738-11743

Takeda et al. Science Advances 2, 8, e1600694

Yoneda et al. Nat. Nano **13**, 102-106 (2018)

Two-qubit gates based on exchange have been implemented. >90% achieved

See: Veldhorst et al. Nature **526**, 410-414 (2015)

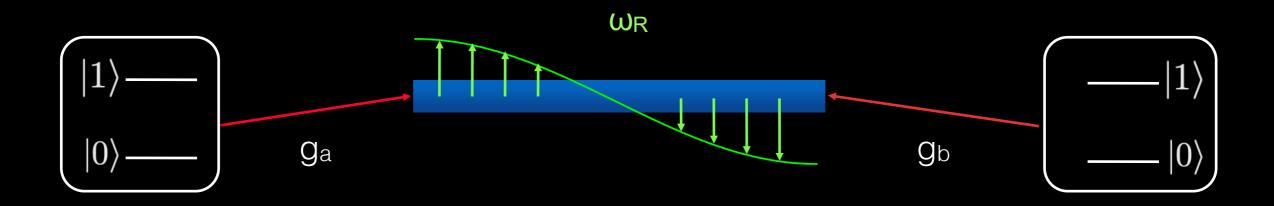
Zajac et al. Science **359**, 6374, 439-442 (2018)

Watson et al. Nature **555**, 633-637 (2018)

Huang et al. Nature **569**, 532-536 (2019)

Xue et al. PRX **9**, 021011 (2019)

On the way towards long-range two-qubit gates



Spin-cQED architectures allow long-range coupling between qubits

Not limited by nearest neighbor interactions

Potential for hybrid quantum systems

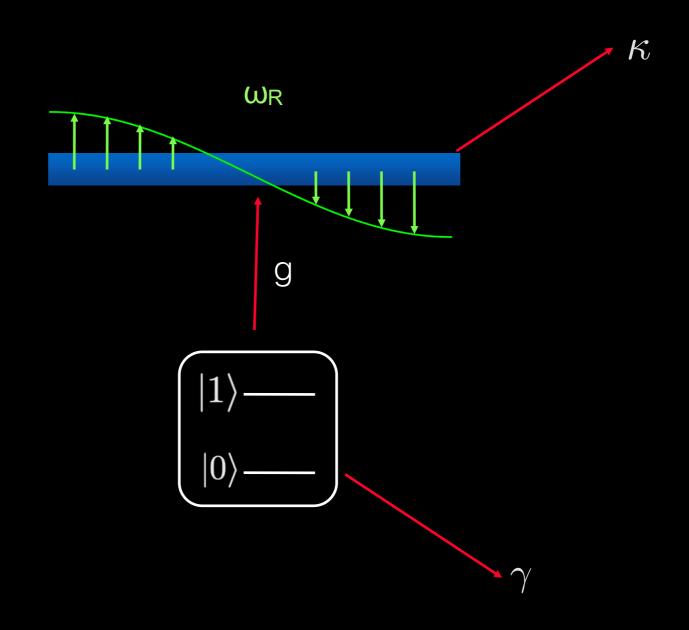
Coupling spin qubits with superconducting resonators

Strong coupling regime achieved with semiconductor qubits

See: Landig et al. Nature 560, 179-184 (2018)

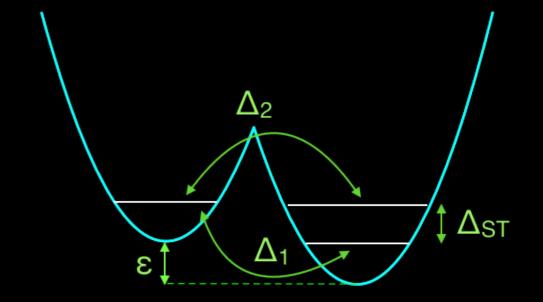
X. Mi et al. Nature **555**, 599-603 (2018)

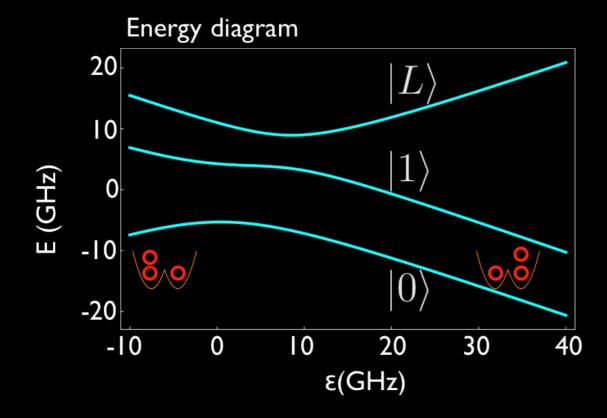
Samkharadze et al. Science 10.1126/science (2018)



Hybrid qubit

$$H = \begin{pmatrix} -\varepsilon/2 & 0 & \Delta_1 \\ 0 & -\varepsilon/2 + \Delta_{ST} & \Delta_2 \\ \Delta_1 & \Delta_2 & \varepsilon/2 \end{pmatrix}$$



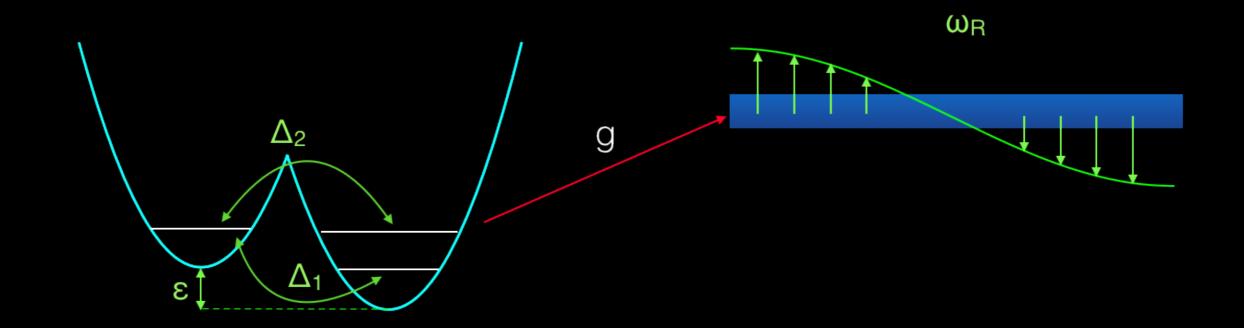


Two anticrossings related to the qubit parameters

Far-detuned regime

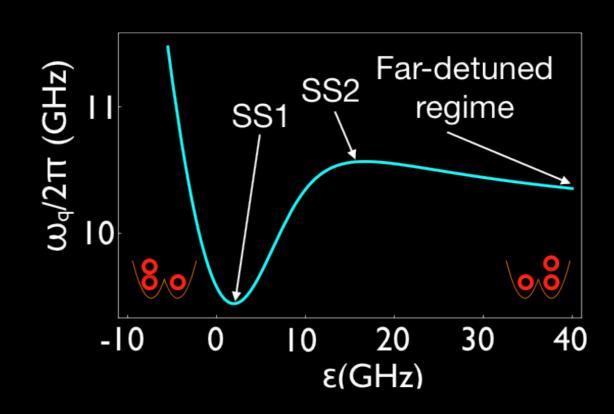
Dipolar coupling maximized near the 1st anticrossing

Strategy: Maximize g/γ

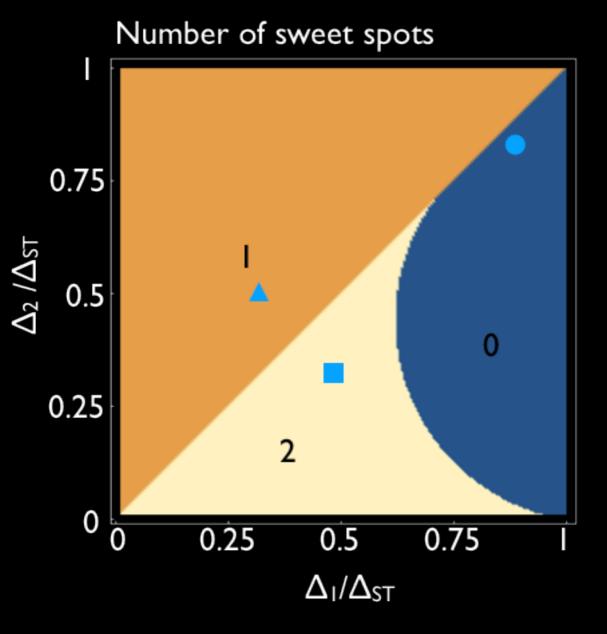


Achieving strong coupling requires $g/\gamma>1$

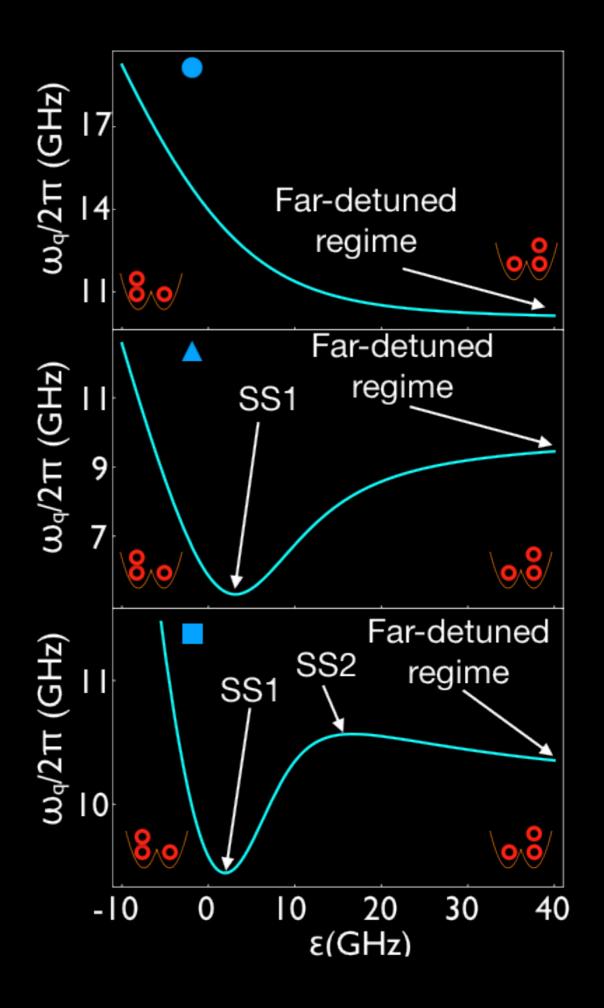
Strong coupling candidates: SSs, fardetuned regime



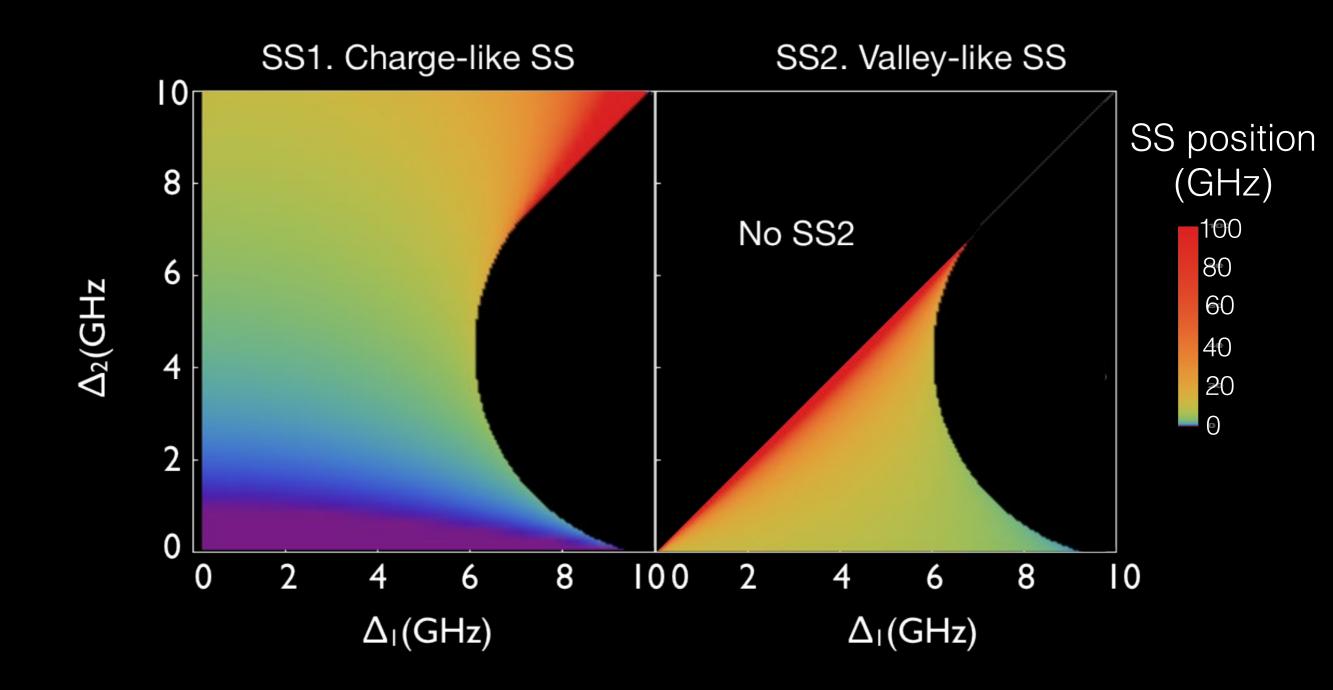
Basic properties of the HQ



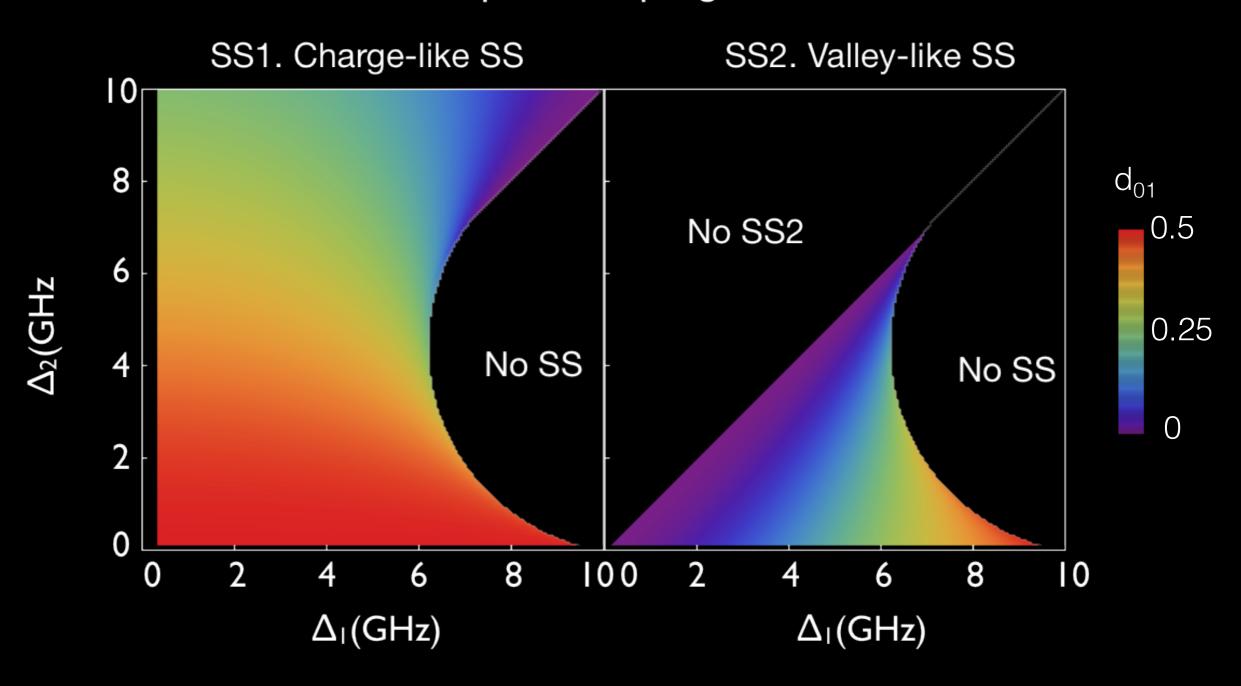
SS1: higher coupling, bad coherence SS2: Smaller coupling with improved coherence Far-detuned regime: Small coupling with good coherence



Sweet spot position.



Dipolar coupling

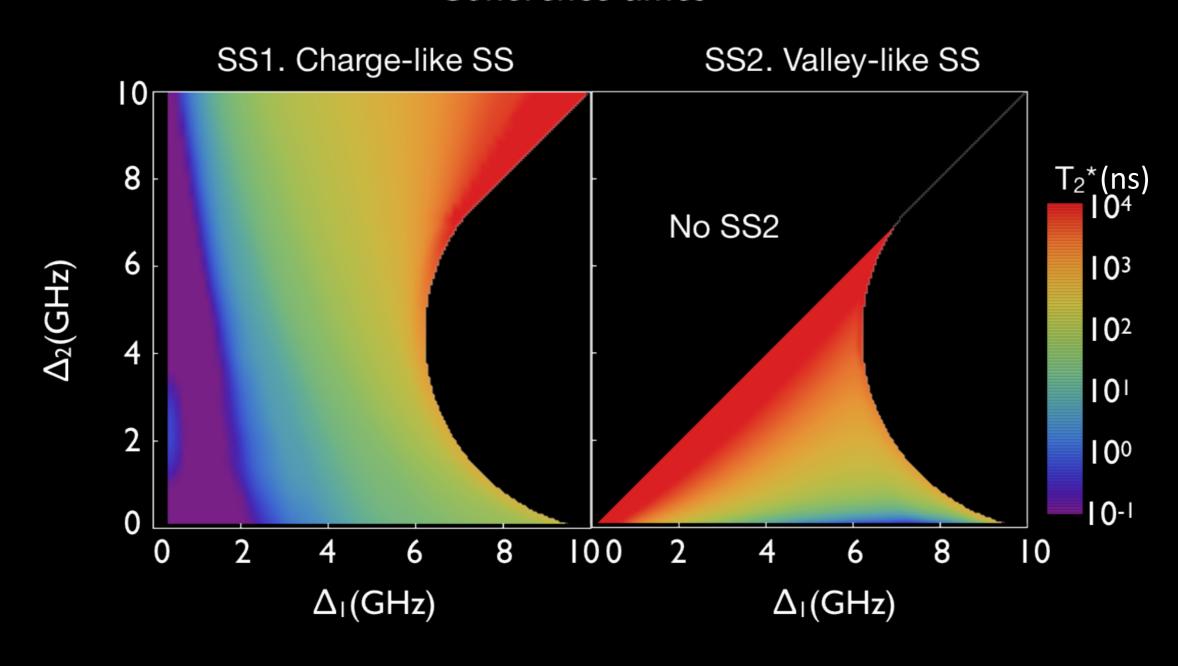


Sweet spot properties. VS=10 GHz

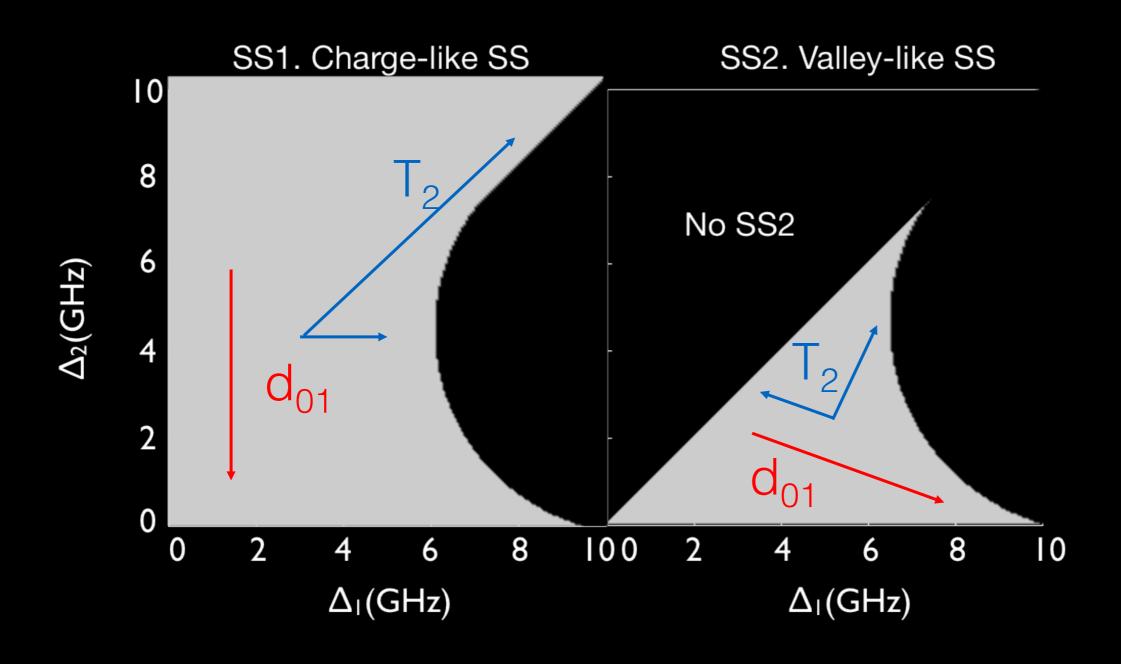
We estimate coherence times by simulating 1/f noise

$$\sigma_{\varepsilon} = 2\mu eV$$

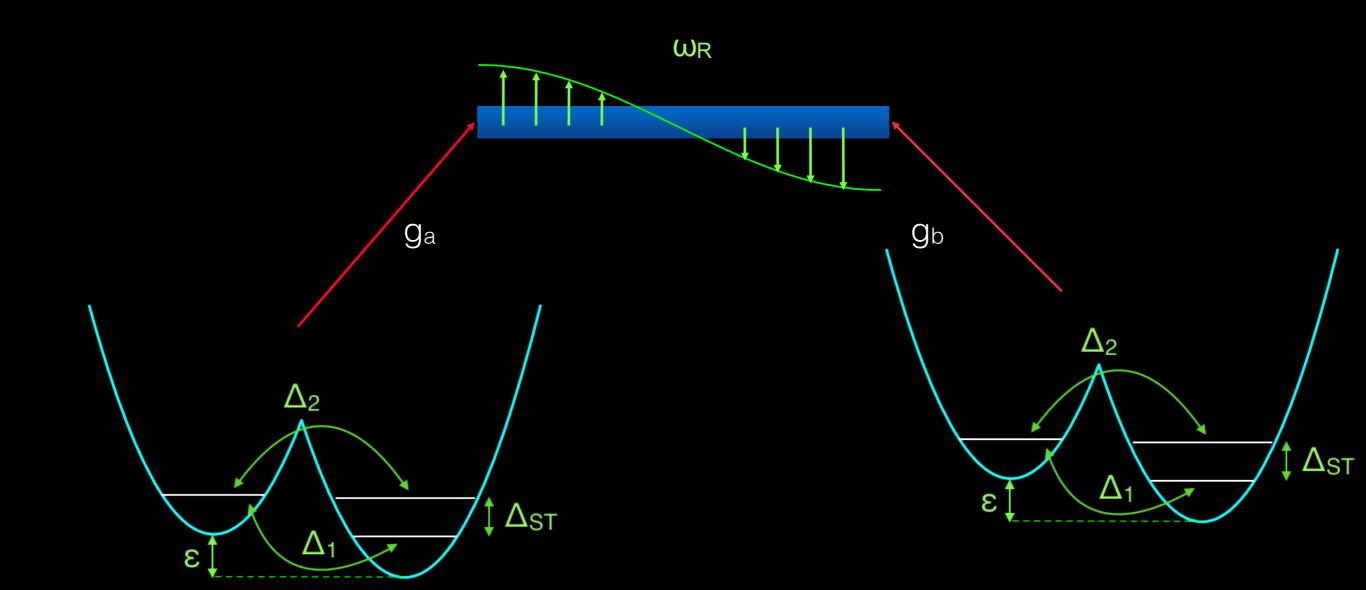
Coherence times



Overview of the sweet spot properties



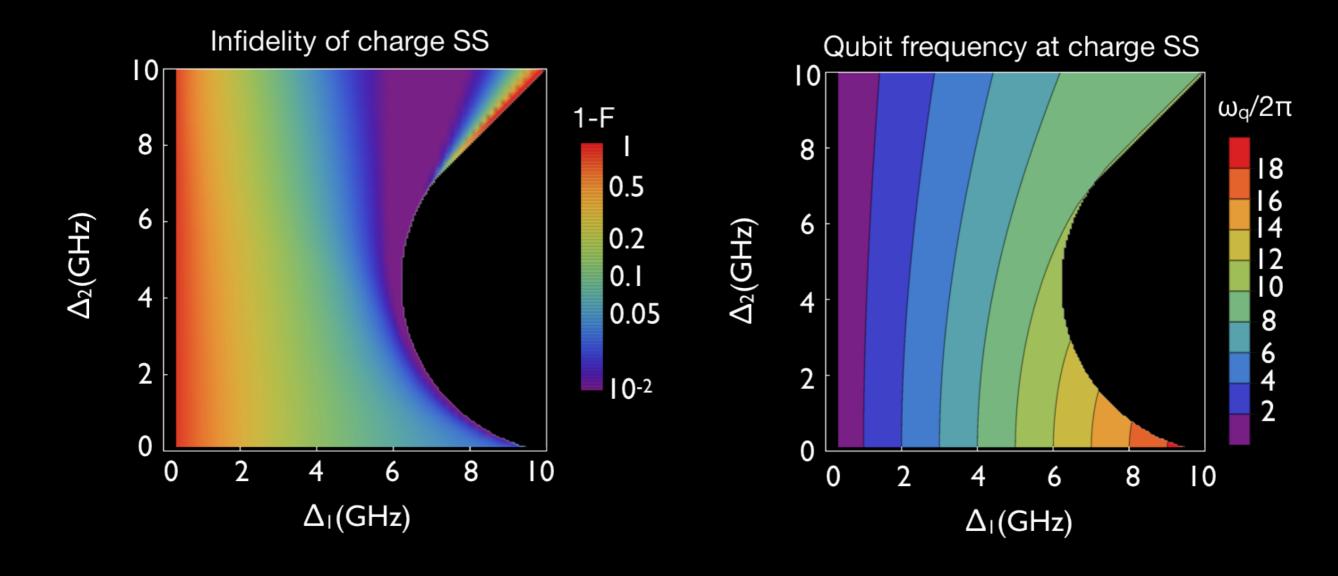
Coupling two hybrid-qubits through a resonator



Upper bound two-qubit gate fidelities. Charge SS

Resonant operation with κ =0 gives the upper bound gate fidelities for a 01 <-> 10 operation

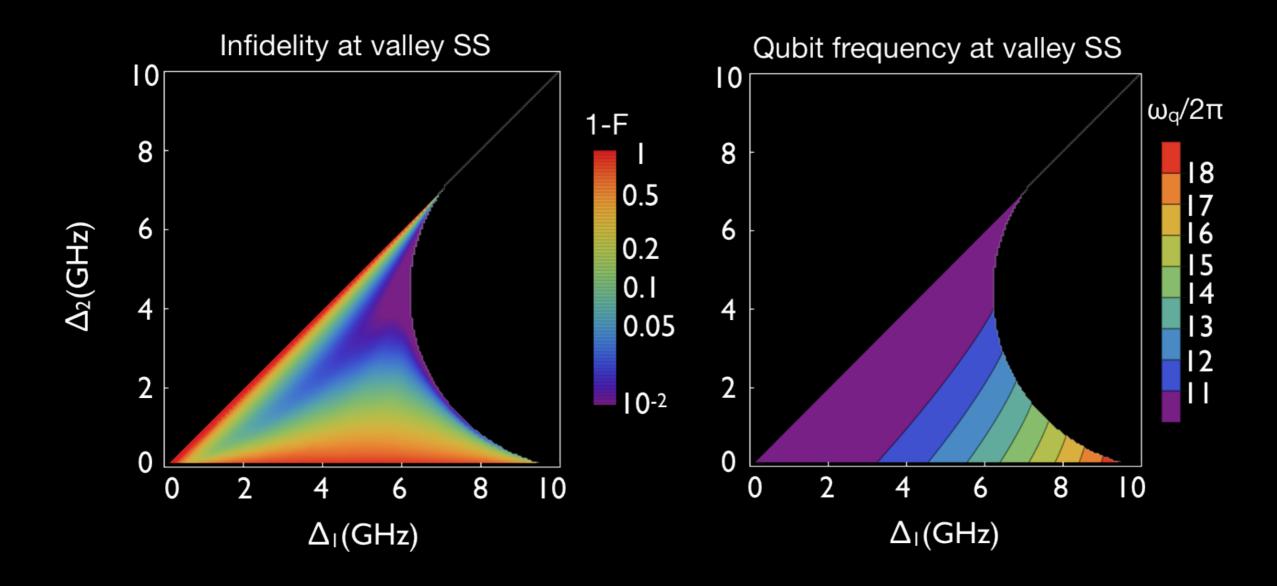
$$H = \omega_c a^{\dagger} a + \sum_{I=1,2} \frac{\omega_{q,i}}{2} \sigma_z^i + g_0 d_{01}^i (a + a^{\dagger}) \sigma_x^i$$



Upper bound two-qubit gate fidelities. Valley SS

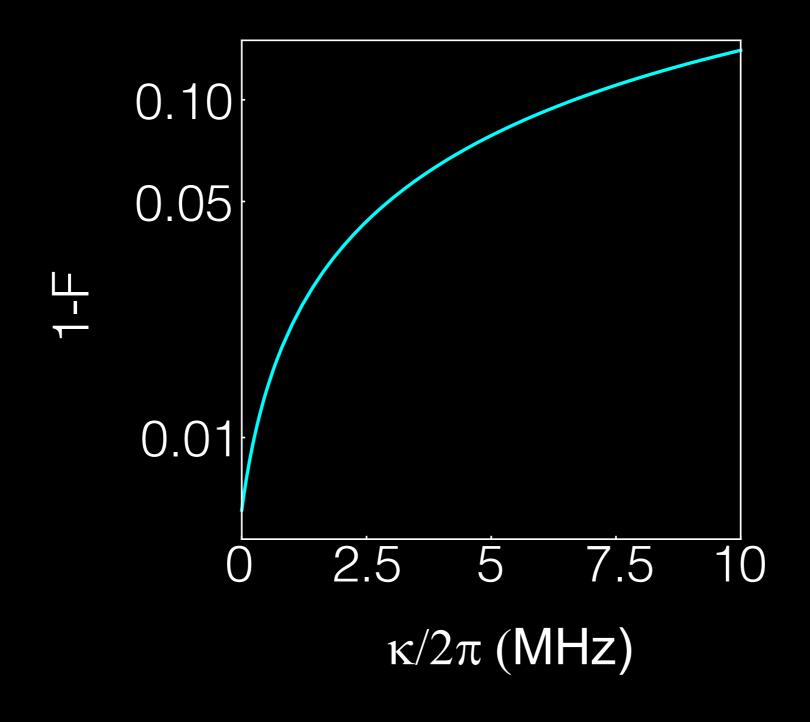
Resonant operation with κ =0 gives the upper bound gate fidelities for a 01 <-> 10 operation

$$H = \omega_c a^{\dagger} a + \sum_{I=1,2} \frac{\omega_{q,i}}{2} \sigma_z^i + g_0 d_{01}^i (a + a^{\dagger}) \sigma_x^i$$



Infidelity due to finite Q

Realistic resonators have finite decay rates (1-10 MHz)



SB transitions mediated by driving detuning and tunnel coupling

$$H = \omega_{c}a^{\dagger}a + \frac{\omega_{q,i}}{2}\sigma_{z}^{i} + g_{0}d_{01}\sigma_{x}^{i}(a + a^{\dagger}) + d_{01}\delta\varepsilon\cos(\omega_{q,i}t + \phi)\sigma_{x}^{i}$$

$$\omega_{c} - \omega_{q} = \pm d_{01}\delta\varepsilon$$

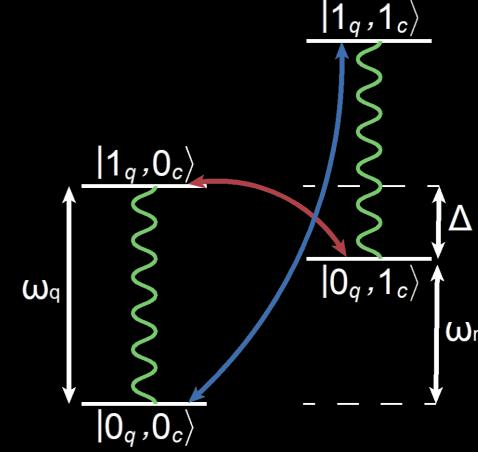
$$H_{S^{+}} = \frac{g}{2}(e^{i\phi}\sigma^{-}a + e^{i\phi}\sigma^{+}a^{\dagger})$$

$$H_{S^{-}} = \frac{g}{2}(e^{i\phi}\sigma^{+}a + e^{i\phi}\sigma^{-}a^{\dagger})$$

$$\omega_{q}$$

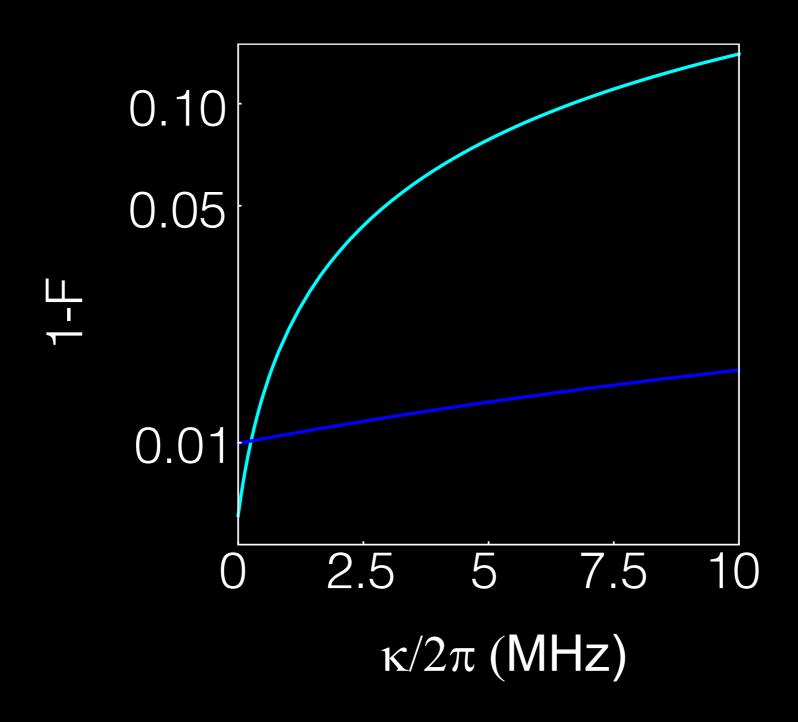
$$\omega_{q}$$

This method allows to work detuned away from resonance while keeping fast gates



$$U_{CZ} = R_{z,a}(\frac{\pi}{\sqrt{2}})S_a^+(\pi,\phi)S_a^-(\pi/2,0)S_a^-(\pi\sqrt{2},\pi/2)S_a^-(-\pi/2,0)R_{z,b}(\pi/\sqrt{2})S_a^+(\pi,\phi)$$

Sideband transition fidelities decay slower



Coupling a Charge quadrupole qubit to a SC resonator

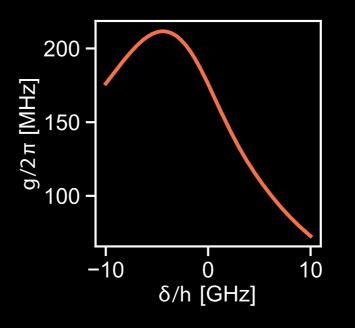
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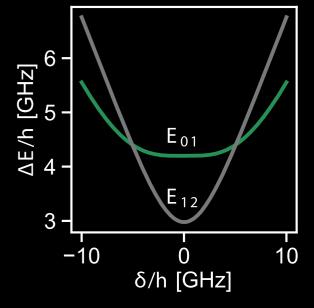
$$H = egin{pmatrix} \delta/2 & t_L & 0 \ t_L & E_M & t_R \ 0 & t_R & -\delta/2 \end{pmatrix}$$

(d)
$$\begin{bmatrix} |L\rangle & |M\rangle & |R\rangle & |S\rangle & |S\rangle$$

$$E_M^{\mathrm{Opt}} \approx -0.493t$$

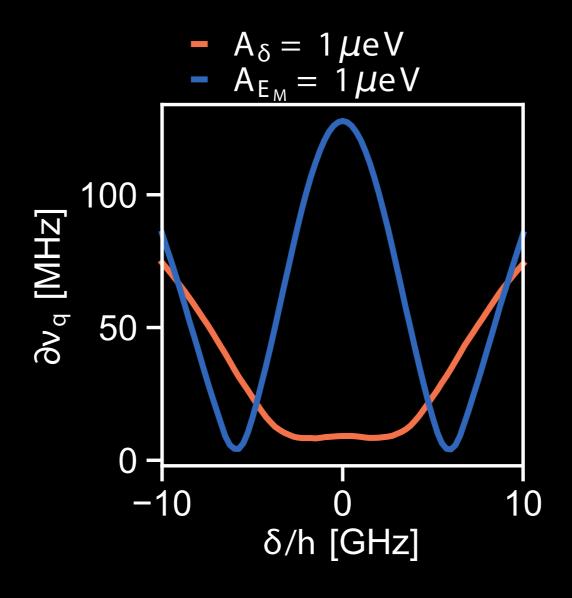
At this optimal point, the qubit is in a 2nd order SS in dipolar detuning





Operating in the quad detuning vs dipolar detuning

If noise is dominated by long-range charged sources dipolar noise dominates



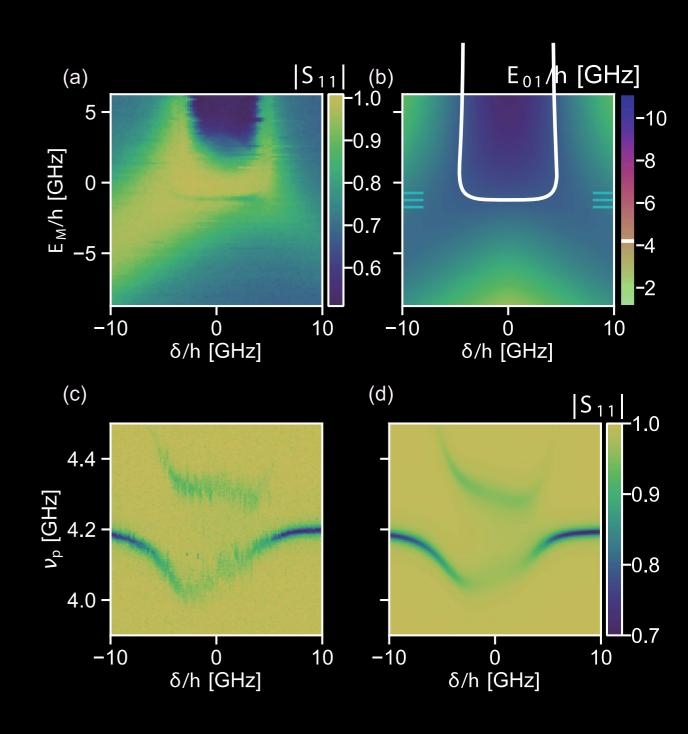
Experimental results and fitting

Fitting to IO theory yields

$$g/2\pi=203 \text{ MHz}$$

$$\kappa_{int}/2\pi = 14 \text{ MHz}$$

$$\kappa_{\text{ext}}/2\pi = 1.3 \text{ MHz}$$



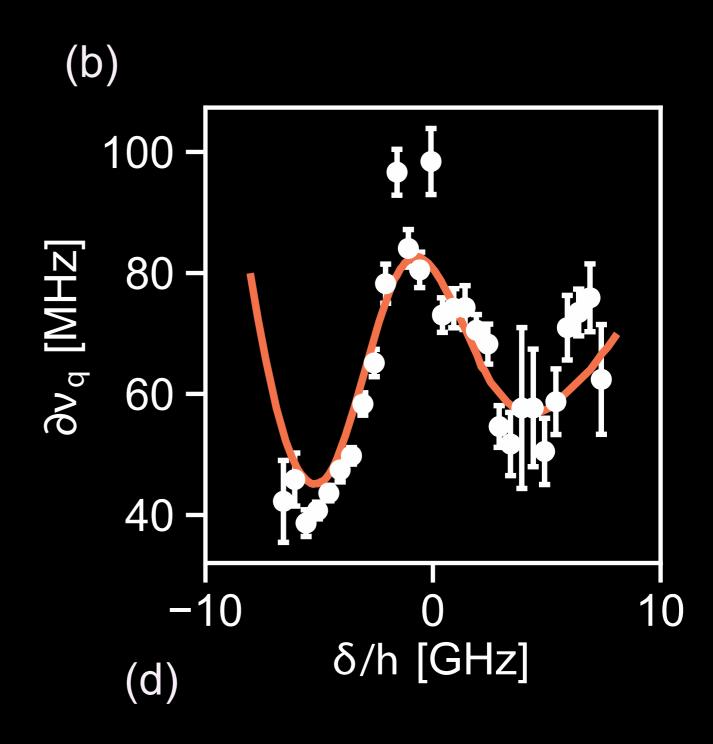
Noise characterization

1/f noise simulations allow to fit the decoherence rate

$$A_{\delta}$$
=1.95 μeV

$$A_{EM}$$
=0.935 μeV

$$\rho = -0.084$$



Conclusion

Superconducting resonators are a promising technology for long-range two-qubit gates

Coupling a HQ to a SCR imposes a frequency constraint. Can be reduced by operating off-resonance

The CQ qubit allows to spatially characterize charge noise. The experimental results seem to point towards close-range noise