

MATH 131 Homework 3  
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1. **Let  $a, b \in \mathbb{R}$ . Show if  $a \leq b_1$  for every  $b_1 > b$ , then  $a \leq b$ .**
2. **Prove that for any  $A, B \subset \mathbb{R} : \sup(A \cup B) = \max\{\sup(A), \sup(B)\}$ .**  
Note that  $\sup(A) \leq \sup(A \cup B)$  and  $\sup(B) \leq \sup(A \cup B)$ .  
WLOG Suppose  $\sup(A) > \sup(B)$  and  $\sup(A \cup B) \neq \sup(A)$  then
3. **Determine if  $\lim_{n \rightarrow \infty} \inf$**