Week 7: Linear Regression Pt 2

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Expanding on Simple Linear Regression

- · A lot of the time you'll have access to several variables you can use to develop a model
- · Adding additional variables can have a positive on a regression model to a degree
- · Adding too many can cause our model to overfit the data
- There are additional assumptions and things to take into account when dealing with multiple independent variables

Developing a Linear Model with Multiple Variables

- · Like in simple linear regression, we use lm() and R's formula interface to develop a linear model
- \cdot To add additional independent variables to the formula interface, we use a +
- Think about variables that you are putting in the model... does their relationship with the response make sense?
 - Adding too many independent variables to our model can cause it to overfit our data, creating issues in predicting future values

What Does our Output Mean?

- · Our summary output is very similar to the output in simple linear regression
- \cdot Coefficient estimates are the change in \mathbf{y} with each additional unit of \mathbf{x} WITH all other independent variables held constant
- · R squared never decreases with each additional variable
 - Adding variables of little to no importance can inflate our R squared value
 - Adjusted R squared takes into account the number of variables in the model and penalizes additional variables that don't improve the model

Model Assumptions

- \cdot The assumptions from simple linear regression apply to multiple regression
- · In addition, we have to think about multi-collinearity
 - This is when our independent variables are highly correlated amongst each other
 - Doesn't necessarily cause issues with predictions or adjusted R squared
 - Does mess with our coefficients, making relationships difficult to interpret

Detecting and Dealing with Multicollinearity

$$VIF_k = \frac{1}{1 - R_k^2}$$

- The variance inflation factor can detect high collinearity
 - Use the vif() function from the car library
- VIF values above 10 indicate a variable with strong collinearity; above 5 could also signal problems
- · Essentially the VIF is looking at how well the independent variables can be used to predict each other
- Adjust for multi-collinearity by combining correlated variables or removing them from the model altogether

Comparing Nested Models

- We can use a partial F-test to see if a complex model is significantly better than a simple model that uses a subset of the variables in the complex model
- · Is the improvement created by developing a more complex model actually substantial enough to warrant making the model more complex?
- · Run anova() using both models as your arguments
- · A p-value less than alpha .05 indicates that our full, complex model significantly improves on the reduced model

Okay, So Now What?

- · Linear regression is a good introduction to the modeling process, but it has issues
 - There are a lot of things that we want to model that aren't linear
 - Being a parametric model, linear regression has a lot of assumptions
- · What can we do to make linear models more flexible and address assumption issues?

Words of Caution

- · When relationships between variables start becoming much more advanced than a linear model can determine, might be easier to go non-parametric route
 - Ensemble tree models: boosting, random forest
- · These non-parametric approaches don't need to meet a laundry list of assumptions
- · They can better identify non-linear patterns and complex interactions
- · Their main con: difficult to explain results to others

Transforming the Response

- · Sometimes the response isn't normally distributed
 - This can lead to issues in residual normality
 - Can lead to non-constant variance
 - Common issue when predicting monetary values

Box-Cox Transformation

- · Searches all possible values of lambda for the one that maximizes the likelihood that **y** comes from a normal distribution
- · Instead of looking at the lambda that produces the most normal y, look at the range to see if it includes a more common value
 - Using a specific lambda can make our results more confusing

Common Box-Cox Transformations

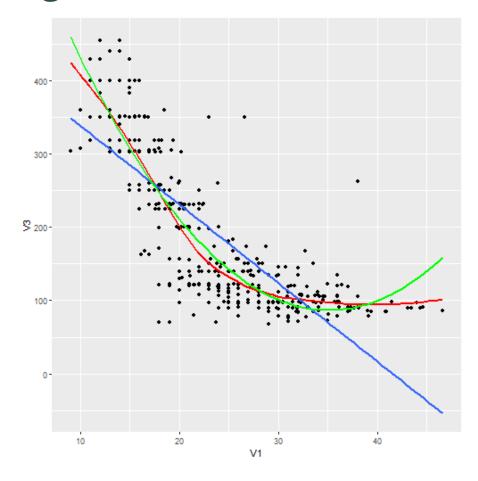
Maybe Your Data Isn't Linear

- · Linear regression is fitting a straight line relationship through your data
- · Maybe your data has a curved relationship
 - Polynomial Regression
- · Maybe your data has a complicated, hard to determine relationship (maybe a sin wave)
 - Splines
- Maybe your data is categorical
 - Logistic Regression

Polynomial Regression

- · If we see a curved relationship between our predictor and response we can use polynomial regression to get a better fit
- If we miss the curved relationship in the initial graphs, we can also identify it in the residuals vs. fitted plot

Polynomial Regression



Polynomial Regression

- Polynomial regression can take on different degrees
 - 2 is quadratic, 3 is cubic; not suggested going beyond cubic to avoid overfit
- Each coefficient is an additional degree; for example, consider a model predicting salary by age to the second degree.
 - $PredictedSalary = B_0 + B_1(age) + B_2(age^2)$
- · poly() can be used to take the polynomial in R
 - Specify degree=x to set degree
 - Orthogonal or raw return... What's the difference?