# Week 8: Logistic Regression

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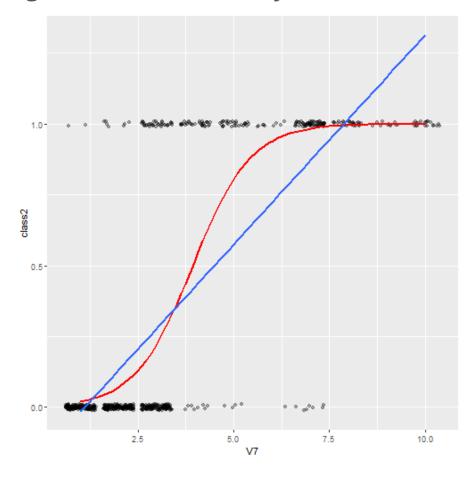
#### Moving On From Linear Problems

- · Up to now, we've only looked at modeling continuous response variables
  - Miles per gallon, rate of crime, etc.
- · There are several problems where we need to model a categorical response
  - Does a team win a game?; Does a student accept an offer of admission?
- · These problems involving categorical response variables are classification problems

### Issues With Modeling This Problem Linearly

- · Let's say we were trying to model a yes/no problem
- · We can treat all yes as 1 and no as 0 and predict the probability of either a 1 or 0
- · A simple linear line isn't really flexible to this scenario
- · Predictions can go above and beyond or 100% probability

# Issues With Modeling This Problem Linearly



#### **Logistic Regression**

- · We can deal with binary classification using the logistic function
  - Can take any input and return a value between 0 and 1

$$P = rac{e^{(B_0 + B_x)}}{1 + e^{(B_0 + B_x)}}$$

- By using some simple math, we can edit the logistic function to get something similar to the linear regression equation
  - Instead of predicting y, we are predicting the log odds of y

$$log(\frac{P}{1-P}) = B_0 + B_x$$

#### **Odds and Probability**

- We aren't predicting probability in logistic regression, we are predicting the log of the odds ratio
- · Probability can be easily changed to odds and vice versa
- The odds ratio is simply the odds of event A happening in the numerator and the odds of it not happening in the denominator
- For example, if a football team had an 80% chance of winning, their odds of winning would be .8 / 1 - .8 or 4 / 1
  - The team has 4 to 1 odds of winning; if the game was played 5 times, the team would win 4 times

## Logistic Regression in R

- We will use glm() or generalized linear model to fit logistic regression models
- glm can fit several non-linear functions
- Specify the argument family = "binomial" to perform logistic regression
- summary() can be used similarly to how we use it for lm() models

### **Logistic Regression Output**

- · Like in our 1m output, we get coefficient estimates and p-values.
- $\cdot$  Coefficient estimates are the increase in the log odds of y for a one unit increase in x
- · Deviance is a measure of model fit
  - The lower the better
- · Residual deviance is the model's deviance, while null deviance is the deviance with only an intercept
  - Similar to F-test in 1m output

#### **Interpreting Logistic Regression Coefficients**

- · Remember that we are predicting the log odds of event y occurring
  - A one unit increase in x, leads to an increase in the log odds of event y occurring by its coefficient estimate
- We can take the exponential of our coefficient estimates to convert them to odds

```
exp(coef(tumor.glm))

## (Intercept) V1 V3 V4 V5

## 0.0000411763 1.7067054139 1.3745942848 1.3908643372 1.1008866850

## V6 V7 V8 V9

## 1.4667887059 1.5628015794 1.2368248052 1.7058506868
```

• For example, a one-unit increase in **V1** would up the odds of the tumor being malignant by about **70**%

# **Logistic Regression Assumptions**

- · Response is binary (two classes)
- · Independent observations
- · No multicollinearity issues
- · Large sample sizes
  - Logistic regression fit by maximum likelihood which requires larger sample sizes

# The Role of Polynomials

- · We don't expect variables to have a linear relation with the response; we do expect variables to have a linear relation with the log odds
- $\cdot$  The log odds of a model can be plotted against an independent variable
- · Relationships that don't appear linear might be improved with the use of polynomials

#### **Measuring Accuracy**

- We can make class probability predictions using predict() and specifying type = "response"
- · Without specifying type, we get log odds predictions
- We can round the predicted probabilities to the nearest whole number and measure how accurate our model is
- · Straightforward method of determining how good our model is