

Q1.

The example in 6.2.1 has $P(\text{cancer} \mid \oplus) = 0.21$

Because $\frac{P(\text{cancer} \mid \oplus) P(\text{cancer})}{P(\text{cancer} \mid \oplus) P(\text{cancer}) + P(\text{cancer} \mid \oplus) P(\oplus \mid \neg \text{cancer})} = 0.21$

$$P(\text{cancer} \mid \oplus \oplus) = \frac{P(\text{cancer} \mid \oplus) P(\oplus \mid \text{cancer})}{P(\oplus \mid \text{cancer}) P(\text{cancer} \mid \oplus) + P(\oplus \mid \neg \text{cancer}) \times P(\neg \text{cancer} \mid \oplus)}$$

And $P(\neg \text{cancer} \mid \oplus)$ and $P(\text{cancer} \mid \oplus)$ must sum to 1
so $P(\neg \text{cancer} \mid \oplus) = 1 - P(\text{cancer} \mid \oplus) = 0.79$

$$P(\text{cancer} \mid \oplus \oplus) = \frac{0.98 \times 0.21}{0.98 \times 0.21 + 0.03 \times 0.79} = 0.91$$

Q2.

Outlook (sunny - yes) => 2/9

Outlook(sunny - no) => 3/5

Outlook (Rainy - yes) = 3/9

Outlook (Rainy - no) = 2/5

Outlook (Overcast - yes) => 4/9

Outlook (Overcast - no) = 0/5

Temperature (hot - yes) => 2/9

Temperature (hot - no) => 2/5

Temperature(cool - yes) => 3/9

Temperature(cool - no) => 1/5

Temperature (mild - yes) => 4/9

Temperature(mild - no) => 2/5

Humidity (high - yes) => 3/9

Humidity (high - no) => 4/5

Humidity (normal - yes) => 6/9

Humidity (normal - no) => 1/5

Wind (strong - yes) => 3/9

Wind (strong - no) => 3/5

Wind (weak - yes) => 6/9

Wind (weak - no) => 2/5

New instance: <Outlook=sun, Temperature=cool, Humidity=high, Wind=strong>

$P(\text{yes}) = (2/9) * (3/9) * (3/9) * (3/9) * (9/14) = 0.0053$

Q3.

First training iteration:

$$b = 0$$

$$a = 1$$

$$\begin{aligned}\text{weights (c)} &= w_{c0} + a * w_{ca} + b * w_{cb} \\ &= 0.1 + (1) * 0.1 + 0 = 0.2\end{aligned}$$

$$O_c = 0.55$$

$$\begin{aligned}\text{weights (d)} &= w_{d0} + O_c * w_{dc} \\ &= 0.1 + 0.55 * 0.1 = 0.155\end{aligned}$$

Errors when $d=1$:

$$\text{error (c)} = 0.55 * (1 - 0.55) * (1 - 0.55) = 0.111375$$

$$\text{error (d)} = 0.55(1 - 0.55) * 0.1 * 0.111375 = 0.00275653125$$

$$a = 1$$

$$b = 0$$

$$\text{Learning rate} = 0.3$$

$$\Delta w_{d0} = 0.3 * 0.111375 * 1 = 0.0334125$$

$$\Delta w_{dc} = 0.3 * 0.111375 * 0.55 = 0.018376875$$

$$\Delta w_{c0} = 0.3 * 0.00275653125 * 1 = 0.00082695937$$

$$\Delta w_{ca} = 0.3 * 0.00275653125 * 1 = 0.00082695937$$

$$\Delta w_{cb} = 0$$

First iteration:

$$w_{d0} = 0.1 + 0.0334125 = 0.1334125$$

$$w_{dc} = 0.1 + 0.018376875 = 0.118376875$$

$$w_{c0} = 0.1 + 0.00082695937 = 0.10082695937$$

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$$w_{ca} = 0.1 + 0.00082695937 = 0.10082695937$$

$$w_{cb} = 0.1 + 0 = 0.1$$

Training example 2:

Errors when $d=0$:

$$\text{error}(c) = 0.55 * (1 - 0.55) * (0 - 0.55) = -0.136125$$

$$\text{error}(d) = 0.55(1 - 0.55) * 0.1 * 0.136125 = 0.00336909375$$

$$a=0$$

$$b=1$$

$$\text{Learning rate} = 0.3$$

$$\text{momentum} = 0.9$$

$$\Delta w_{d0} = 0.3 * (0.136125) * 1 + 0.9 * 0.0334125 = 0.07090875$$

$$\Delta w_{dc} = 0.3 * (0.136125) * 0.55 + 0.9 * 0.018376875 = 0.0389998125$$

$$\Delta w_{c0} = 0.3 * (-0.0389998125) * 1 + 0.9 * 0.00082695937 = -0.01095568031$$

$$\Delta w_{ca} = 0.3 * (-0.0389998125) * 0 + 0.9 * 0.00082695937 = 0.00074426343$$

$$\Delta w_{cb} = 0.3 * (-0.0389998125) * 1 + 0.9 * 0 = -0.01169994375$$

Second iteration :

$$w_{d0} = 0.2 + 0.07090875 = 0.27$$

$$w_{dc} = 0.2 + 0.0389998125 = 0.24$$

$$w_{c0} = 0.2 + (-0.01095568031) = 0.19$$

$$w_{ca} = 0.2 + 0.00074426343 = 0.20$$

$$w_{cb} = 0.2 + (-0.01169994375) = 0.19$$