

# A Study of Intonation in SATB Ensembles

Johanna Devaney

Jonathan Wild

Peter Schubert

Ichiro Fujinaga



Schulich School of Music  
École de musique Schulich



McGill

CIR  
MMT

Centre for Interdisciplinary Research  
in Music Media and Technology



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## Introduction

## Prior Work on Intonation

## Tools for Automatically Extracting Performance Parameters

## Intonation Experiment

## Conclusions/Future Work

# Introduction

- Study of the influence of musical context on SATB ensembles intonation
- Background in Music Technology
  - Automatic extraction of intonation-related data
- Background in Music Theory
  - Use of specially designed exercises designed for this experiment and music theoretical analysis of existing music

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# Prior Work on Intonation

- Schoen (1922) studied 5 performances of Gounod's "Ave Maria"
  - accompanied singers were sharper than equal temperament
    - intervals tended to be flatter when descending and sharper when ascending
- Prame (1997) studied 10 performances of Schubert's "Ave Maria"
  - accompanied singers deviated from equal temperament
    - range of the average deviation was -12 to +20 cents
- Jers and Terström (2005) examined intonation in 1 fast and 1 slow performance by a 16 voice a cappella ensemble
  - a greater amount of intonation dispersion at the faster tempo
    - descending intervals were closer to equal temperament while ascending intervals were sharper

# Prior Work on Intonation

- Vurma and Ross (2006) studied 13 professional singers performing a melodic intonation in a short exercises
  - ascending and descending semitones were smaller than EQT
  - ascending and descending fifths were larger than than EQT
- Howard (2007) studied 2 *a cappella* SATB quartets
  - the ensembles used non-equal temperament with a tendency toward, though not full compliance with, Just-Intonation
- Vurma (2010) studied 15 professional singers' intonation in 2-part 6-note exercises with a synthesized lower voice
  - singers' intonation did not change significantly when the synthesized voice was detuned

# Our Work on Solo Intonation

- Subjects
  - 6 undergraduate vocal majors
  - 6 professional singers
- Experimental Material: Schubert's "Ave Maria" performed
  - 3 times *a cappella*
  - 3 times with accompaniment
- Data Analysis
  - *a cappella* vs. accompanied
  - ascending vs. descending
  - various semitone and whole tone intervallic conditions
  - singer and group identity

# Our Work on Solo Intonation

- Findings (Devaney, Wild, and Fujinaga 2011)
  - Ascending semitones and whole tones tended to be larger than descending ones
  - Non-professional singers tended to compress ascending semitones with a leading tone function
  - Professional singers' intonation was more consistent between *a cappella* and accompanied performances than non-professionals
  - Professional singers' intonation was more consistent with one another than non-professionals

Introduction

Prior Work on Intonation

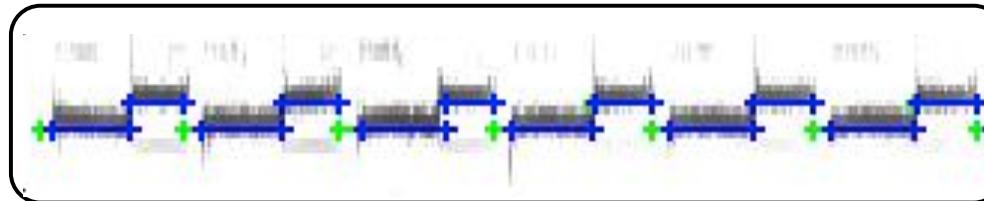
## Tools for Automatically Extracting Performance Parameters

Intonation Experiment

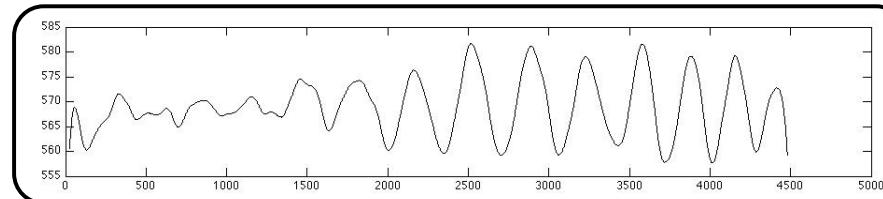
Conclusions/Future Work

# Extracting Performance Parameters

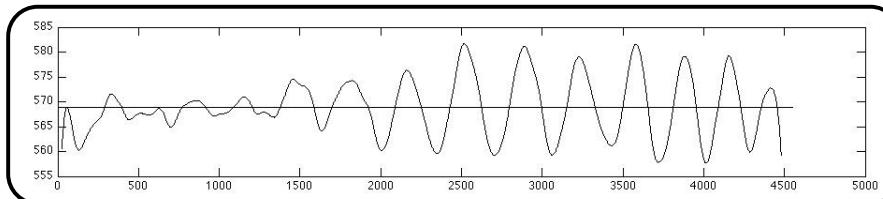
Identify Note Onsets and Offsets



Fundamental Frequency (F0) Estimation

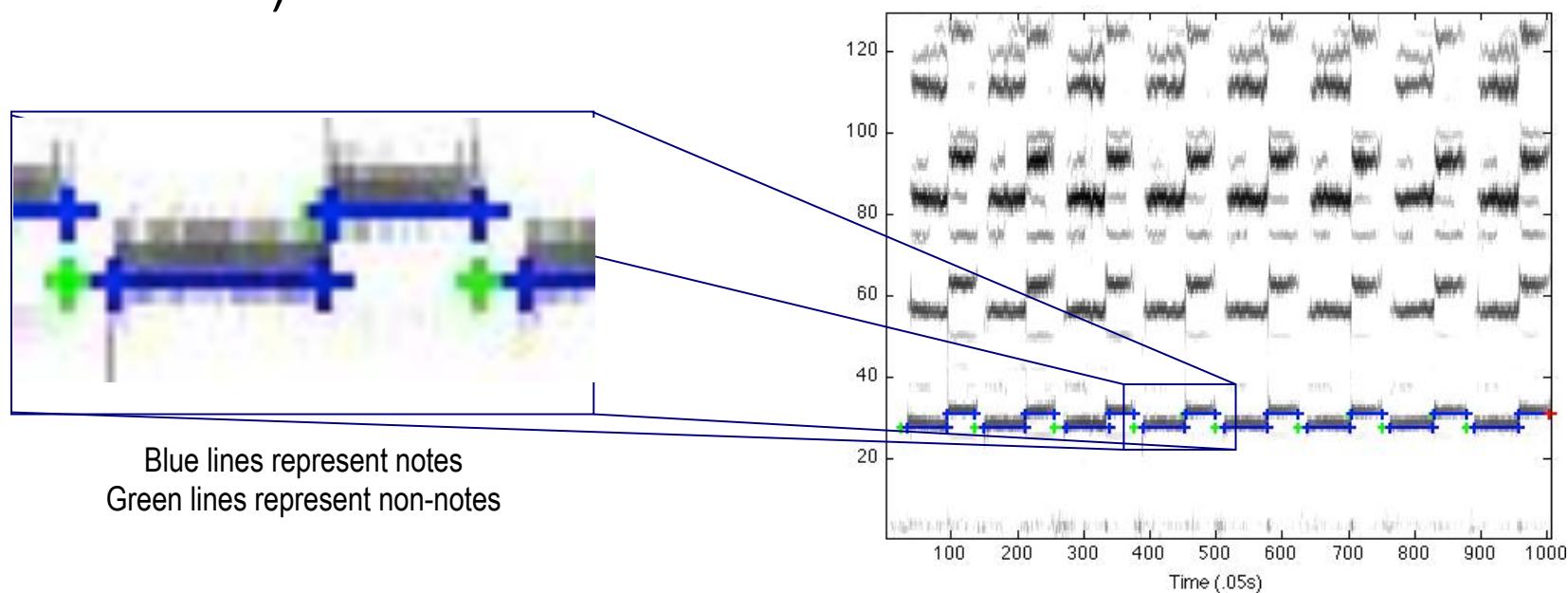


Perceived Pitch

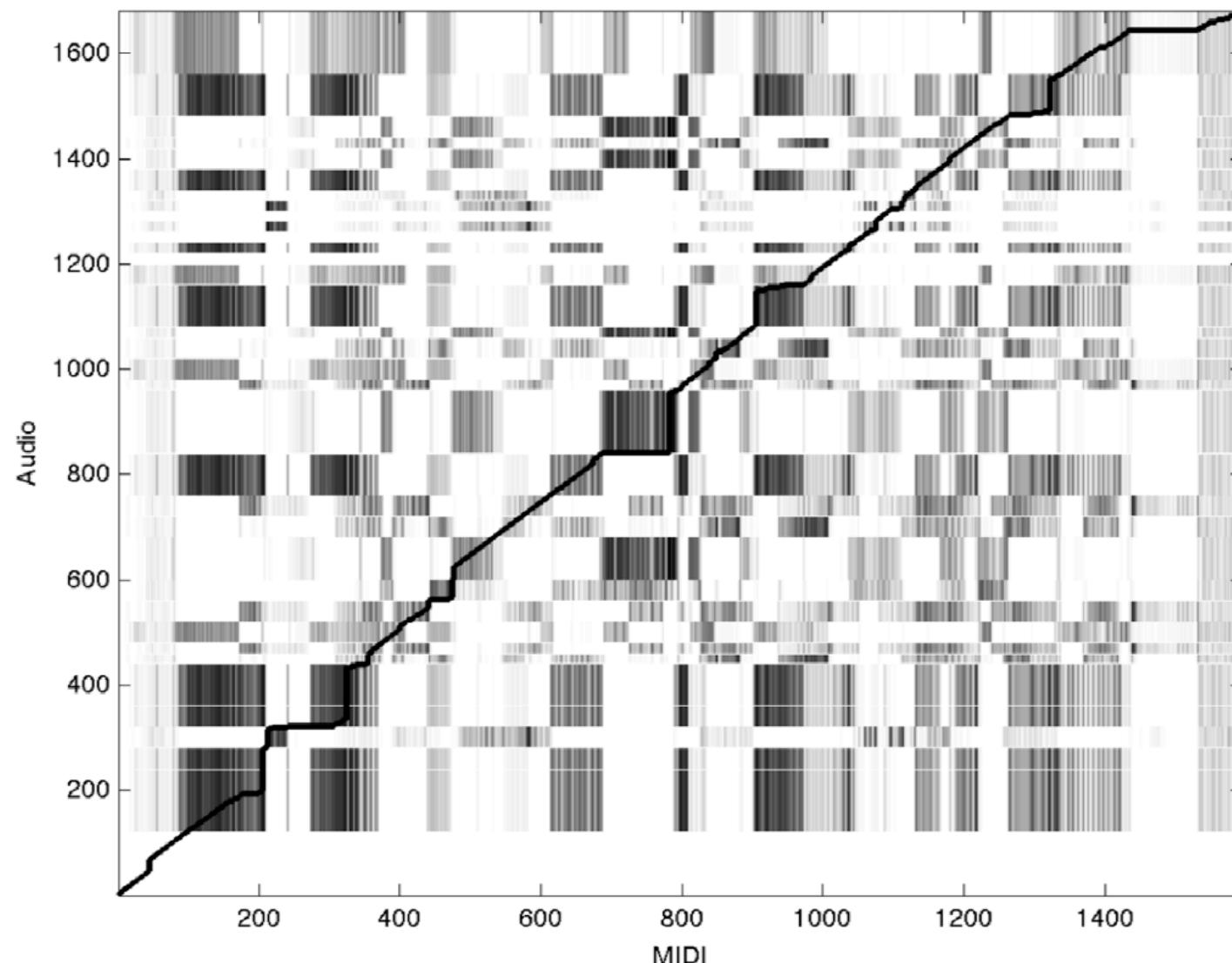


# Identifying Note Onset and Offset

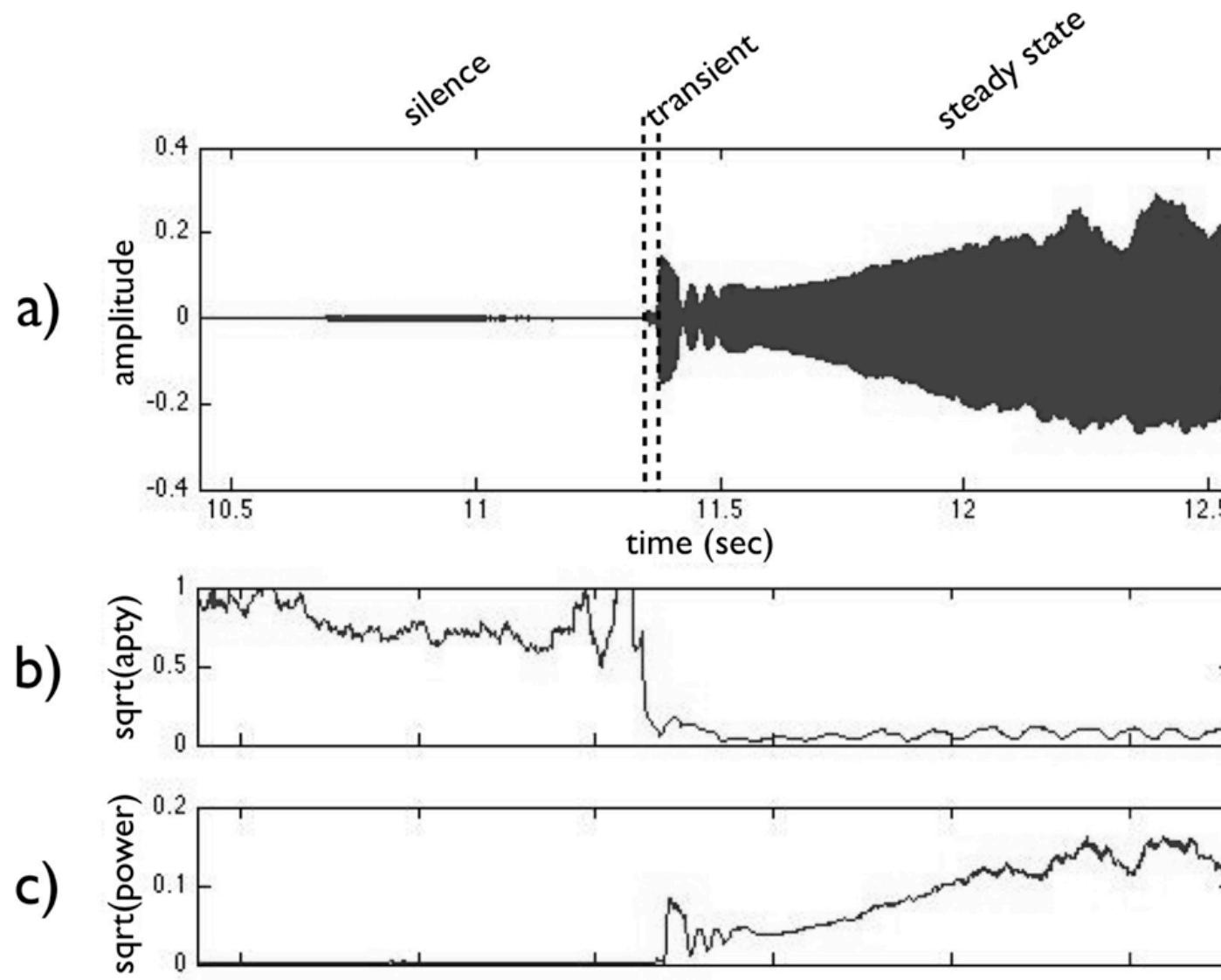
- Note onsets and offsets in the recordings were identified through MIDI-audio alignment
- The method used in this dissertation is a two-step dynamic time warping (Orio and Schwarz)/hidden Markov model alignment algorithm optimized for the singing voice (Devaney, Mandel, & Ellis 2009)



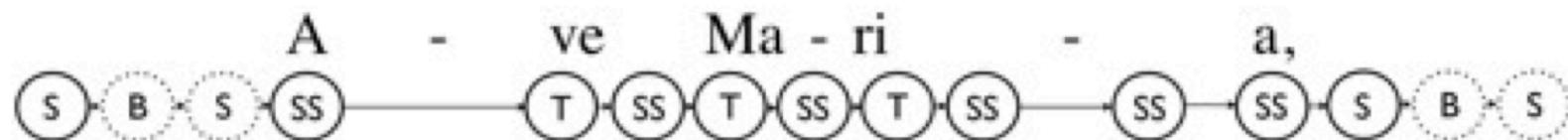
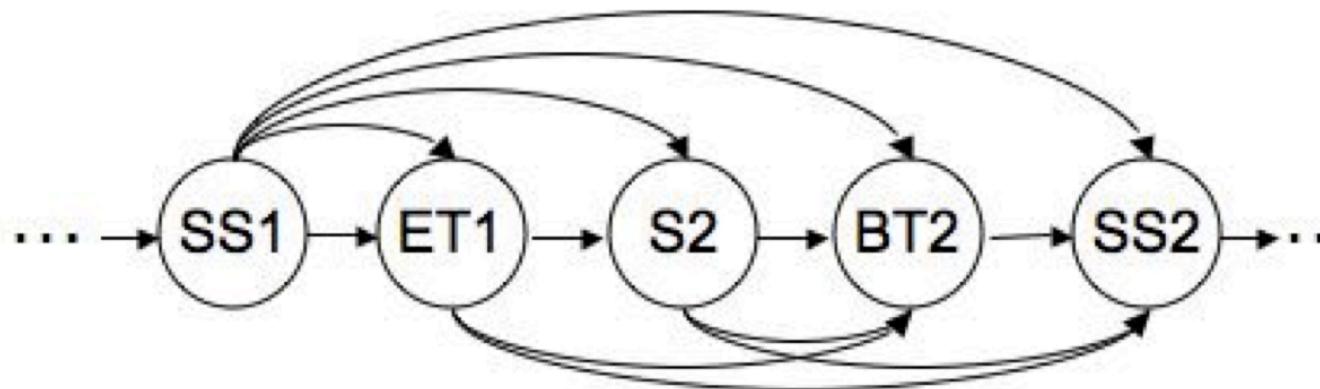
# Dynamic Time Warping Matrix



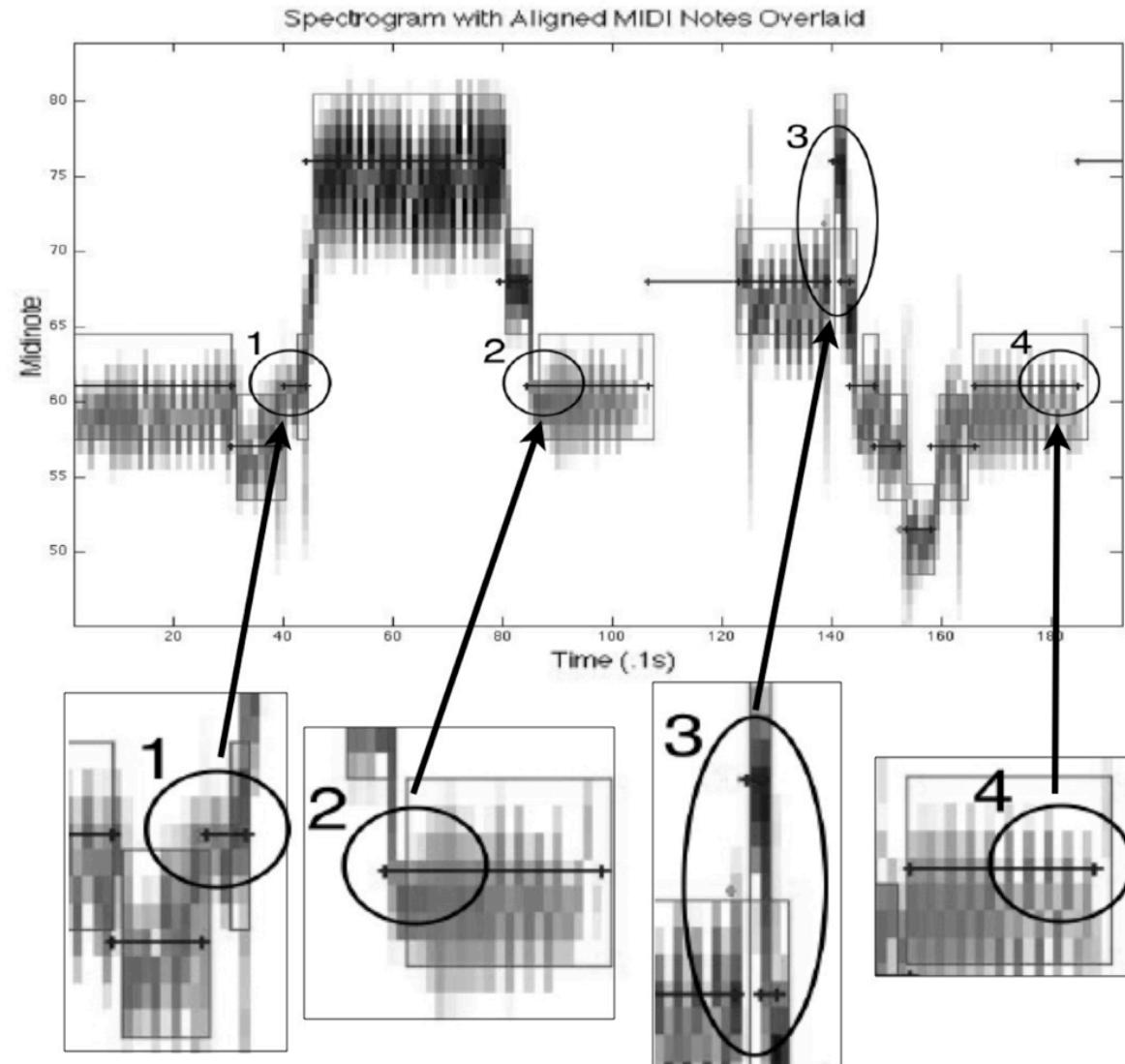
# Acoustic Properties of the Singing Voice



# HMM States

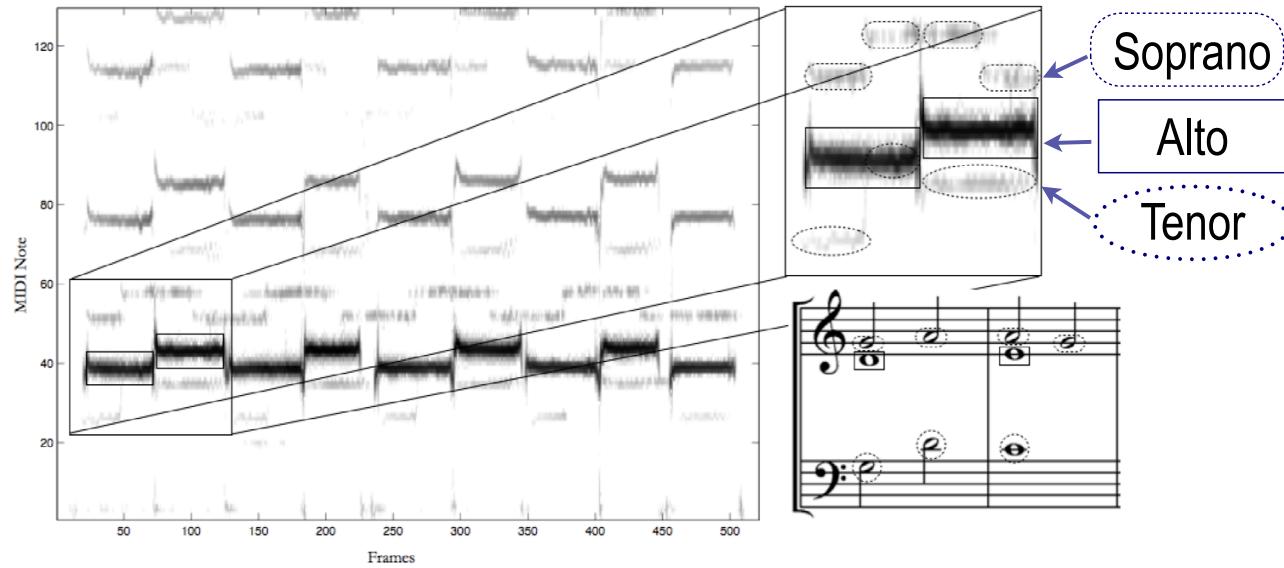


# Alignment Improvements



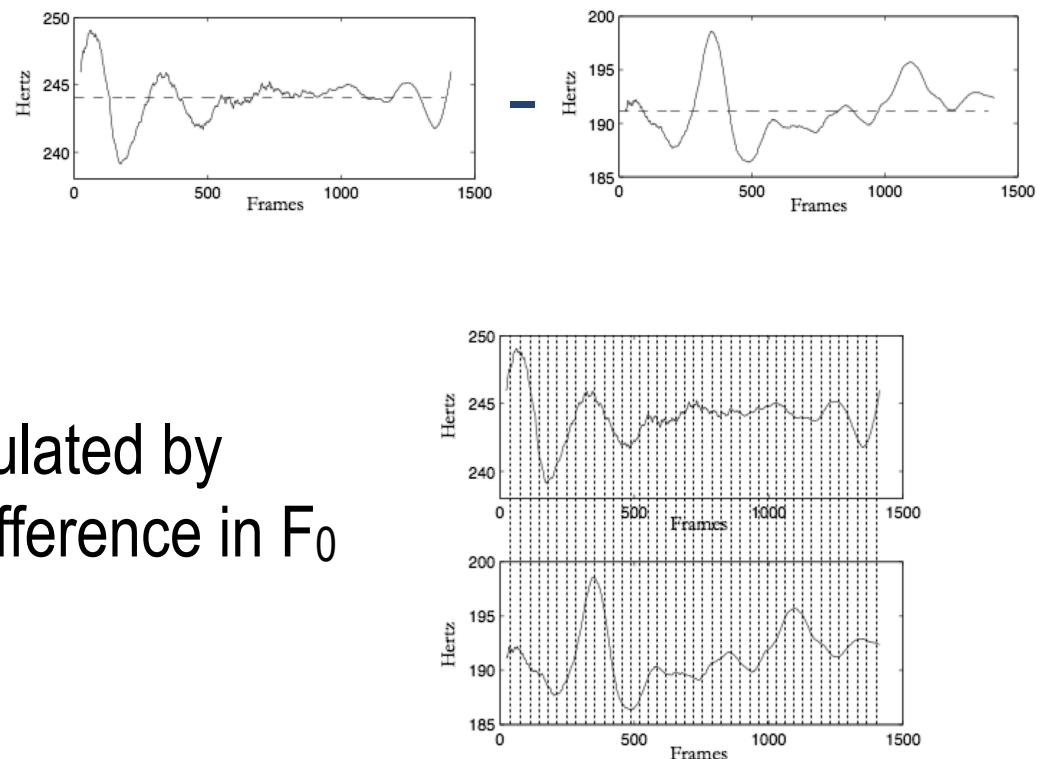
# Fundamental Frequency ( $F_0$ ) Estimation

- The YIN algorithm was used for  $F_0$  estimation (de Cheveigné and Kawahara 2002)
  - A single  $F_0$  estimate is calculated for each frame of audio
  - YIN was designed for monophonic  $F_0$  estimation
  - The ability to specify the minimum and maximum expected  $F_0$  allows YIN to work more robustly for quasi-polyphonic signals



# Calculating Interval Size

- Perceived pitch was calculated by taking a weighted mean based on the  $F_0$ 's rate of change, with higher weightings for frames that had a slower rate of change (Gockel et al. 2001)
- Horizontal interval size was calculated as the difference between two perceived pitch calculations
- Vertical interval size was calculated by taking the mean across the difference in  $F_0$  estimates for each frame



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# Intonation Experiment

- Subjects
  - 1 semi-professional quartet (pilot)
  - 2 professional quartets (lab and church)
- Experimental Material
  - Exercises composed by Jonathan Wild and Peter Schubert, where semitones and whole tones occur in different contexts
  - Chord progression by Giambattista Benedetti
  - Michael Praetorius' "Lo how a rose e'er blooming"

# Semitone Exercises (Wild)



	Chromatic semitones	$\hat{7}-\hat{8}$	$\hat{2}-\hat{3}$	$\hat{3}-\hat{4}$	$\hat{5}-\hat{6}$
Soprano	1–5	6	7	8	9
Alto	10–14	15	16	17	18
Tenor	19–23	24	25	26	27

# Whole tone Exercises (Schubert)

S 1 2 3 4 5 6

The soprano vocal line consists of six measures of whole notes. Measure 1 starts on C. Measures 2-5 each start on a different sharp note (D, E, F#, G#). Measure 6 starts on A.

A

The alto vocal line consists of a single measure of whole notes starting on D.

T

The tenor vocal line consists of a single measure of whole notes starting on E.

B

The bass vocal line consists of a single measure of whole notes starting on F#.

S 7 8 9 10 11 12

The soprano vocal line consists of six measures of whole notes. Measures 7-10 start on C, while measures 11-12 start on D.

A

The alto vocal line consists of a single measure of whole notes starting on D.

T

The tenor vocal line consists of a single measure of whole notes starting on E.

B

The bass vocal line consists of a single measure of whole notes starting on F#.

S 13 14 15 16 17 18

The soprano vocal line consists of six measures of whole notes. Measures 13-16 start on C, while measures 17-18 start on D.

A

The alto vocal line consists of a single measure of whole notes starting on D.

T

The tenor vocal line consists of a single measure of whole notes starting on E.

B

The bass vocal line consists of a single measure of whole notes starting on F#.

	$\hat{2}-\hat{3}$	$\hat{5}-\hat{6}$	$\hat{4}-\hat{5}$	$\hat{3}-\hat{4}$	$\hat{1}-\hat{2}$	$\hat{6}-\hat{7}$
<b>Soprano</b>	1	2	3	4	5	6
<b>Alto</b>	7	8	9	10	11	12
<b>Tenor</b>	13	14	15	16	17	18

# Benedetti Progression



# Praetorius - Semitones/Whole Tones

Musical score for Praetorius' Semitones/Whole Tones, showing four voices (Soprano, Alto, Tenor, Bass) in common time, treble clef, and B-flat key signature. The score consists of three systems of music. Circles and dashed ovals highlight specific notes across the systems, with 'LT' indicating a leap to the next note.

System 1 (Measures 1-6):  
Soprano (S): Notes highlighted by dashed ovals at measures 2-3 and 4-5.  
Alto (A): Notes highlighted by dashed ovals at measures 2-3 and 4-5.  
Tenor (T): Notes highlighted by circles at measures 1-2 and 4-5, and dashed ovals at measures 2-3 and 4-5.  
Bass (B): Notes highlighted by circles at measures 1-2 and 4-5, and dashed ovals at measures 2-3 and 4-5.

System 2 (Measures 7-12):  
Soprano (S): Notes highlighted by dashed ovals at measures 7-8 and 9-10.  
Alto (A): Notes highlighted by dashed ovals at measures 7-8 and 9-10.  
Tenor (T): Notes highlighted by circles at measures 7-8 and 9-10, and dashed ovals at measures 7-8 and 9-10.  
Bass (B): Notes highlighted by circles at measures 7-8 and 9-10, and dashed ovals at measures 7-8 and 9-10.

System 3 (Measures 13-18):  
Soprano (S): Notes highlighted by dashed ovals at measures 13-14 and 15-16.  
Alto (A): Notes highlighted by circles at measures 13-14 and 15-16, and dashed ovals at measures 13-14 and 15-16.  
Tenor (T): Notes highlighted by circles at measures 13-14 and 15-16, and dashed ovals at measures 13-14 and 15-16.  
Bass (B): Notes highlighted by circles at measures 13-14 and 15-16, and dashed ovals at measures 13-14 and 15-16.

Musical score for Praetorius' Semitones/Whole Tones, showing four voices (Soprano, Alto, Tenor, Bass) in common time, treble clef, and B-flat key signature. The score consists of three systems of music. Boxes highlight specific groups of notes across the systems.

System 1 (Measures 1-6):  
Soprano (S): Notes highlighted by boxes at measures 2-3 and 4-5.  
Alto (A): Notes highlighted by boxes at measures 2-3 and 4-5.  
Tenor (T): Notes highlighted by boxes at measures 1-2 and 4-5.  
Bass (B): Notes highlighted by boxes at measures 1-2 and 4-5.

System 2 (Measures 7-12):  
Soprano (S): Notes highlighted by boxes at measures 7-8 and 9-10.  
Alto (A): Notes highlighted by boxes at measures 7-8 and 9-10.  
Tenor (T): Notes highlighted by boxes at measures 7-8 and 9-10.  
Bass (B): Notes highlighted by boxes at measures 7-8 and 9-10.

System 3 (Measures 13-18):  
Soprano (S): Notes highlighted by boxes at measures 13-14 and 15-16.  
Alto (A): Notes highlighted by boxes at measures 13-14 and 15-16.  
Tenor (T): Notes highlighted by boxes at measures 13-14 and 15-16.  
Bass (B): Notes highlighted by boxes at measures 13-14 and 15-16.

# Praetorius - Vertical Intervals

The image displays three staves of musical notation for four voices: Soprano (S), Alto (A), Tenor (T), and Bass (B). The music is in common time. The notation uses treble and bass clefs. Measure numbers 7, 13, and Roman numerals V, vi, I are indicated. Vertical intervals are highlighted by dashed boxes and brackets.

**Measure 7:** The first measure shows vertical intervals between voices. A dashed box highlights a V-vi progression between the Bass and Tenor voices. Another dashed box highlights a V-I progression between the Bass and Soprano voices. The Tenor voice has a 16th-note pattern.

**Measure 13:** The second measure shows vertical intervals. A dashed box highlights a V-vi progression between the Bass and Tenor voices. Another dashed box highlights a V-I progression between the Bass and Soprano voices. The Tenor voice has a 16th-note pattern.

**Measure 13 (continued):** The third measure shows vertical intervals. A dashed box highlights a V-vi progression between the Bass and Tenor voices. Another dashed box highlights a V-I progression between the Bass and Soprano voices. The Tenor voice has a 16th-note pattern.

# Experimental Method

- Recording set-up (Lab Ensemble)
  - Room – Critical Listening Lab in CIRMMT
  - The whole ensemble was recorded with a pair of cardioid microphone
  - Each ensemble singer was also miked with a cardioid headband mic
  - Recording was done a Mac Pro
- Recording set-up (Church Ensemble)
  - Room – St Mathias Church, Westmount
  - Same mics as the lab recordings
  - Recording was done on a portable 16-track recorder

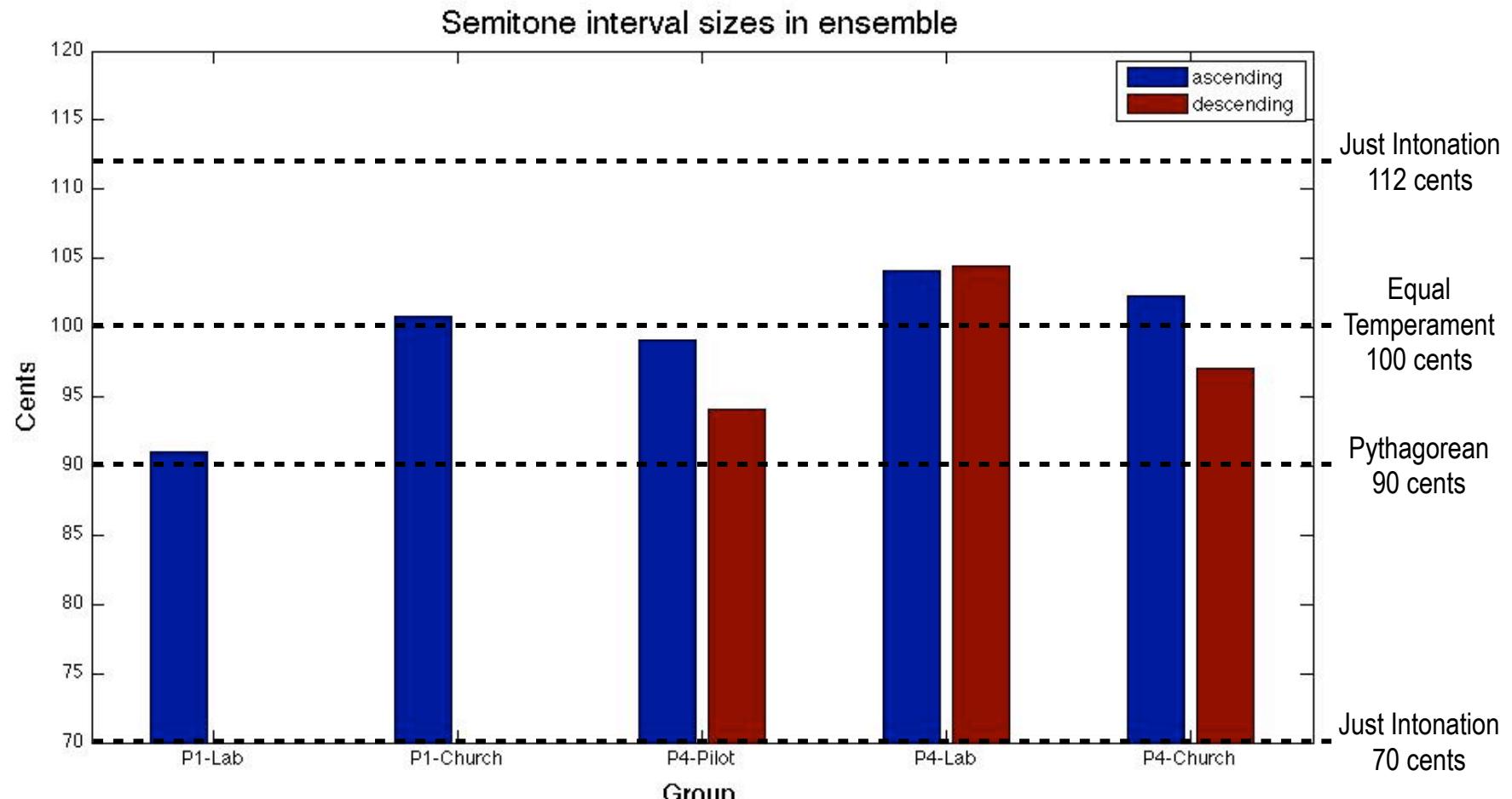




# Regression Analysis

- Linear regression analysis used to determine effects (including size and direction)
  - ascending vs. descending
  - semitone intervallic conditions (part one and four)
  - whole tone intervallic conditions (part two)
  - singer and group identity

# Melodic Interval Size: Semitones



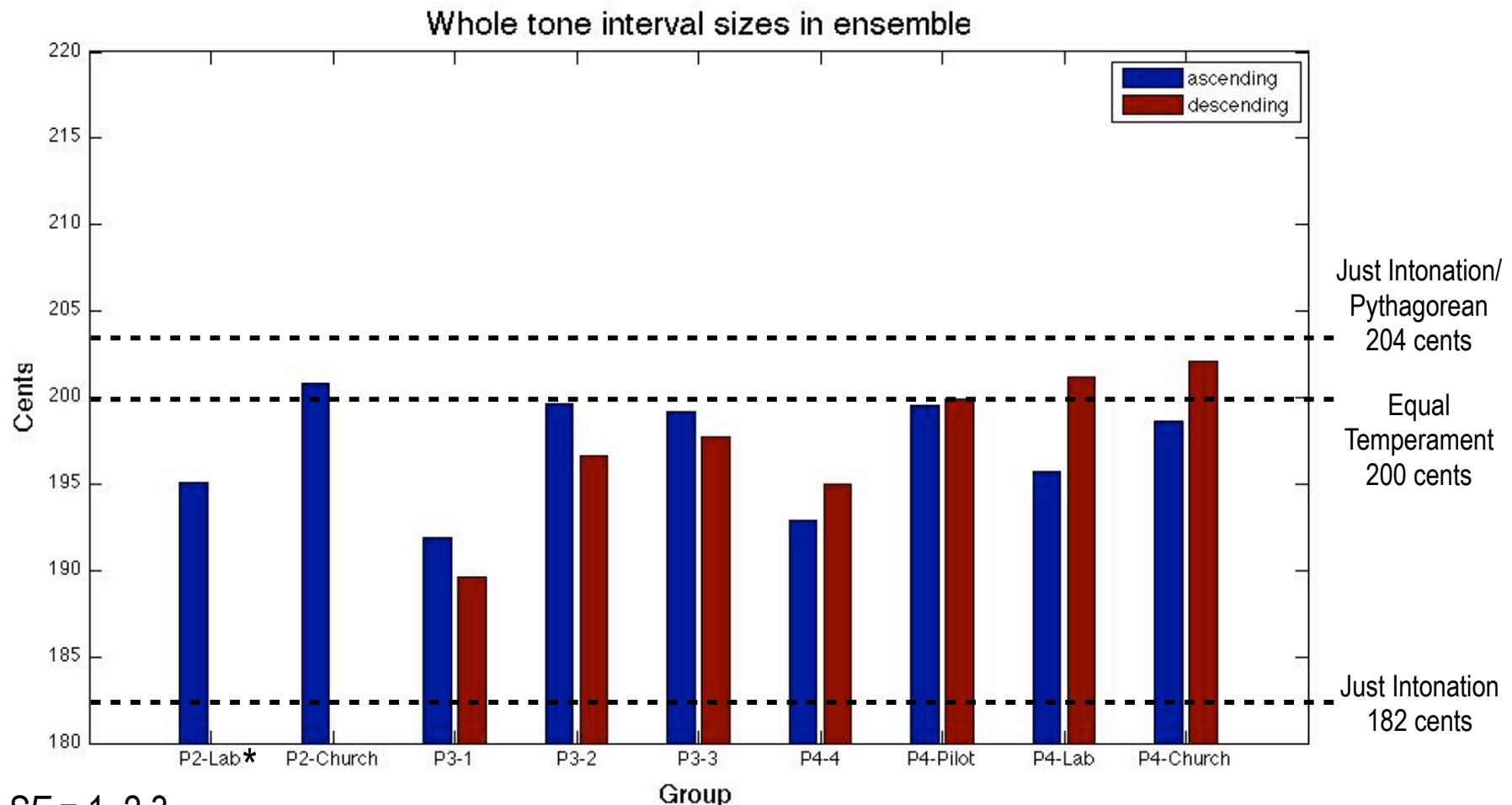
# Melodic Interval Size: Semitones

- Only one semitone category for each of the Lab and Church ensembles showed a significant effect
- The Church ensemble's ascending semitones were on average 8 cents larger than their descending semitones

# Melodic Interval Size: Semitones

	Pilot	Lab	Church
<b>Overall size (all)</b>	closest to equal temperament (except for P4 descending)	closest to equal temperament (except for P1 ascending)	closest to equal temperament
<b>Direction (P4)</b>	<i>P4 - Not Significant</i>	<i>P4 - Not Significant</i>	P4 - ascending semitones 8 cents larger on average
<b>Intervalic Conditions (P1, P4)</b>	N/A	P1 - diatonic vs chromatic was significantly different P1 - 1 condition significantly different from leading tone <i>P4 - Not Significant</i>	<i>P1 - diatonic vs chromatic not significant</i> P1 - 1 condition significantly different from leading tone <i>P4 - Not Significant</i>
<b>Singer Identity (P1, P3, P4)</b>	<i>Not Significant</i>	P1 - <i>Not Significant</i> P4 - Bass	P1 - Tenor, Alto P4 - Tenor, Alto, Bass

# Melodic Interval Size: Whole Tones



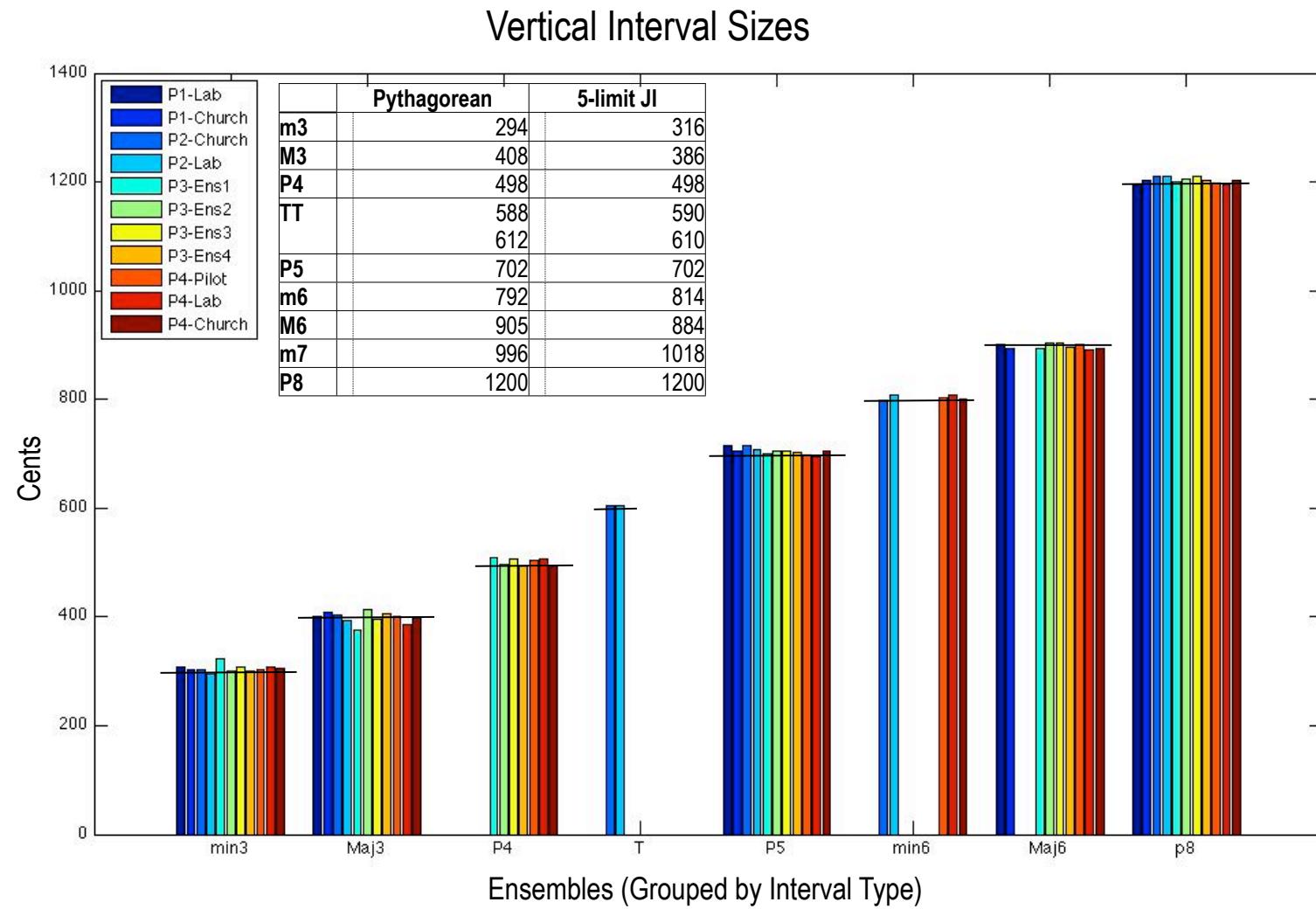
# Melodic Interval Size: *Whole Tones*

- Only one whole tone category for the Lab ensemble showed a significant effect
- The Lab ensemble's ascending whole tones were 4 cents smaller on average than their descending whole tones
- The Church ensemble's ascending whole tones were 5 cents smaller on average than their descending whole tones

# Melodic Interval Size: Whole Tones

	Pilot	Lab	Church
<b>Overall size (all)</b>	closest to equal temperament	closest to equal temperament	closest to equal temperament
<b>Direction (P4)</b>	<i>P3 - Not Significant</i> <i>P4 - Not Significant</i>	<i>P3 - Not Significant</i> P4 - ascending 5 cents smaller	<i>P3 - Not Significant</i> P4 - ascending 5 cents smaller
<b>Intervalic Conditions (P2)</b>	N/A	P2 - effect for 1 condition	<i>P2 - Not Significant</i>
<b>Singer Identity (P2, P3, P4)</b>	P3 - Middle <i>P4 - Not Significant</i>	P2 - Tenor, Alto P3 - Middle <i>P4 - Not Significant</i>	P2 - Alto <i>P3 - Not Significant</i> P4 - Alto

# Vertical Interval Size



# Vertical Interval Size

- Question: Do singers tend towards Just Intonation when tuning vertical intervals?
- If the coincidence of partials encourages Just Intonation tuning, one would expect that Major Thirds would be tuned more justly than intervals with fewer partials in common
  - For most of the ensembles, the Major Thirds were closer to equal temperament (400 cents) than Just Intonation (386 cents)

# Vertical Interval Size

	m3	M3	P4	TT	P5	m6	M6	m7	P8
<b>Equal Temperament</b>	300	400	500	600	700	800	900	1000	1200
<b>5-limit Just Intonation</b>	316	386	498	590 610	702	814	884	1018	1200
<b>Pythagorean</b>	294	408	498	588 612	702	792	905	996	1200

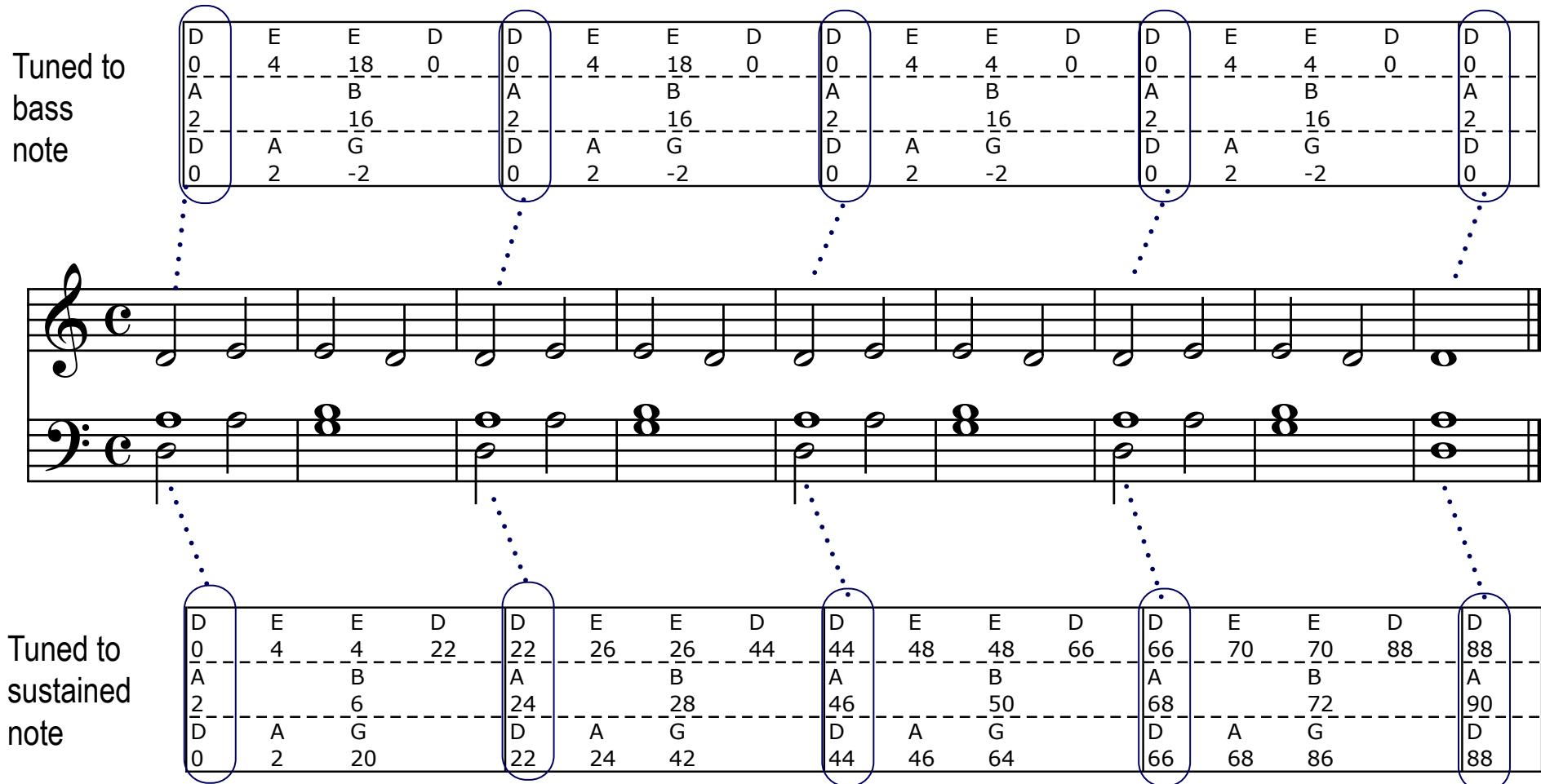
- When cadential context was taken into account in the Praetorius, a *t*-test ( $p = 0.05$ ) revealed that the tuning was closer to Just Intonation in cadential contexts than non-cadential contexts

	Pilot	Lab	Church
<b>Cadence</b>	14.356	14.108	14.261
<b>Non-Cadence</b>	<b>17.027</b>	<b>16.631</b>	<b>17.254</b>

Mean deviation in cents from idealized Just Intonation tunings

# Pitch Drift

Theoretical intonation calculations for the Benedetti chord progression



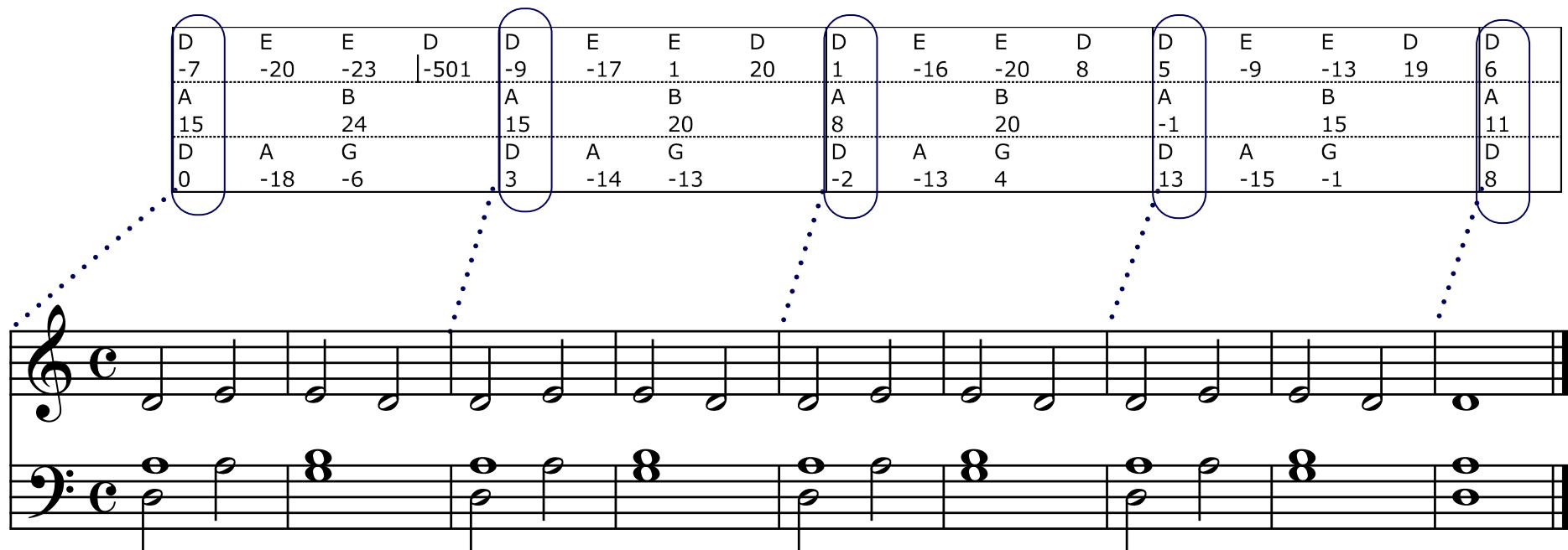
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Many thanks to Gabriel Vigliensoni  
for creating the Vocaloid versions

# Pitch Drift

Example of an actual performance



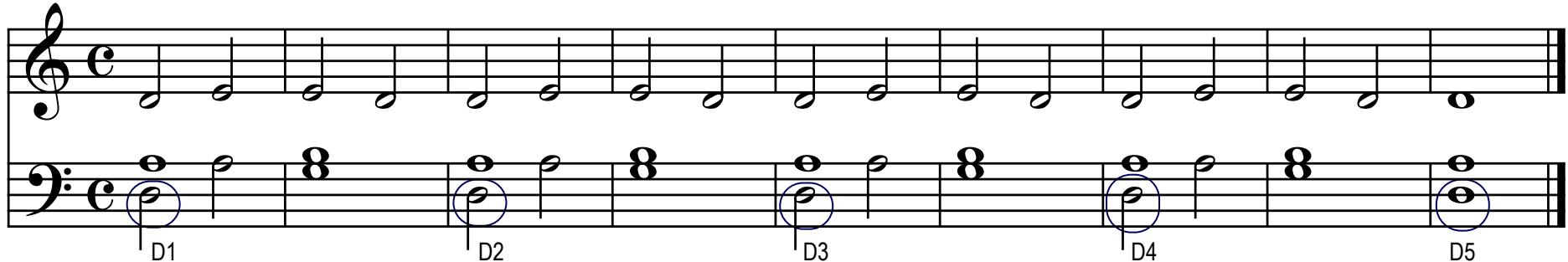
# Pitch Drift

- Ensemble 1 – Semi-professional singers\* (ATB, lab)
- Ensemble 2 – Professional singers\*\* (ATB, lab)
- Ensemble 3 – Professional singers\*\* (SAT, church)
- Ensemble 4 – Professional singers\*\* (ATB, church)

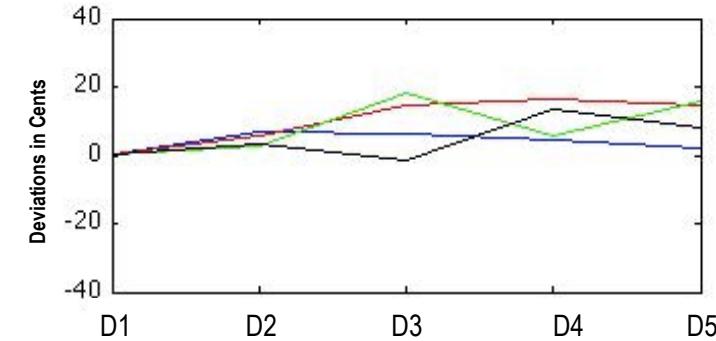
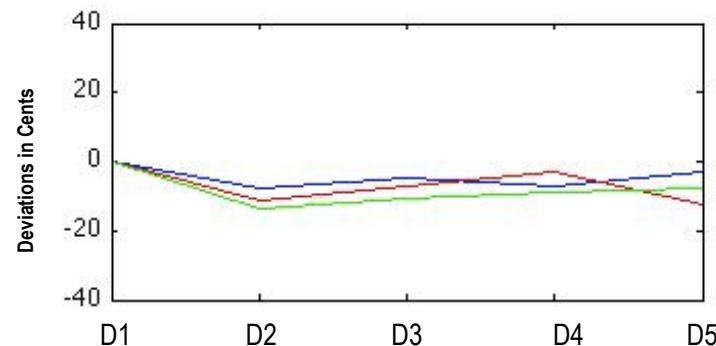
*\*no conductor*

*\*\*conducted by Peter Schubert*

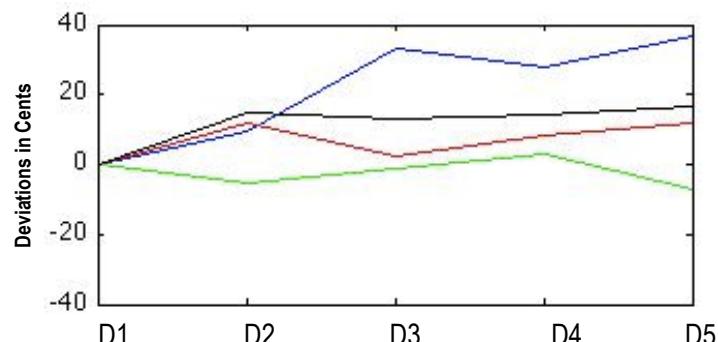
# Pitch Drift



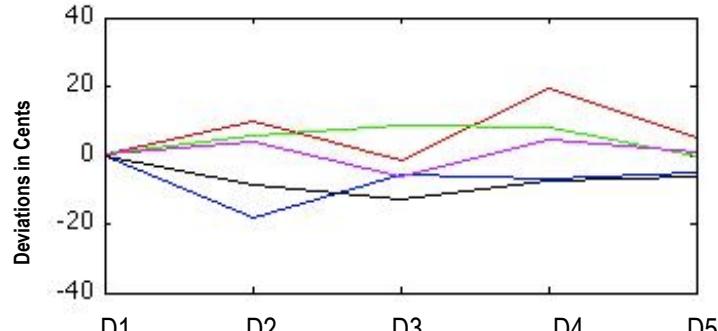
Ensemble 1



Ensemble 3



Ensemble 4



# Impact of Syllable on Intonation

## Benedetti

Ensemble	# takes on 'mi'	# takes on 'ma'
2	2	2
3	2	2
4	3	3

	Melodic ("mi")	Melodic ("ma")	Vertical ("mi")	Vertical ("ma")
Ensemble 2	1.7	-0.1	4.3	8.6
Ensemble 3	2.3	-0.3	<b>5.3</b>	1.0
Ensemble 4	-1.8	0.2	-0.02	<b>4.8</b>

*Bolding indicates significant difference*

## Praetorius

Ensemble	# takes in German	# takes on 'mi'
Lab	4	3
Church	4	4

	Melodic (German)	Melodic ("mi")	Vertical (German)	Vertical ("mi")
Lab	<b>3.180</b>	0.128	<b>0.4284</b>	-4.385
Church	<b>1.971</b>	-1.702	-0.205	1.089

*Bolding indicates significant difference*

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# Conclusions

- Neither horizontal or vertical interval conformed to a fixed system
  - Significant differences between ascending/descending semitones and whole tones
  - Significant difference for Lab ensemble between diatonic/chromatic
  - Vertical intervals were closer to Just Intonation tuning in cadential contexts in all ensembles
- Variable amounts of drift were observed in the ensembles
  - None of the ensembles exhibited sharpening predicted by Benedetti
- There were some significant effects for syllable
  - When the Praetorius was sung with the original german text both horizontal and vertical intervals were larger than when sung on “mi”

# Future Work

- A more controlled experiment
- Same pattern in the upper voice over randomized lower voice

I

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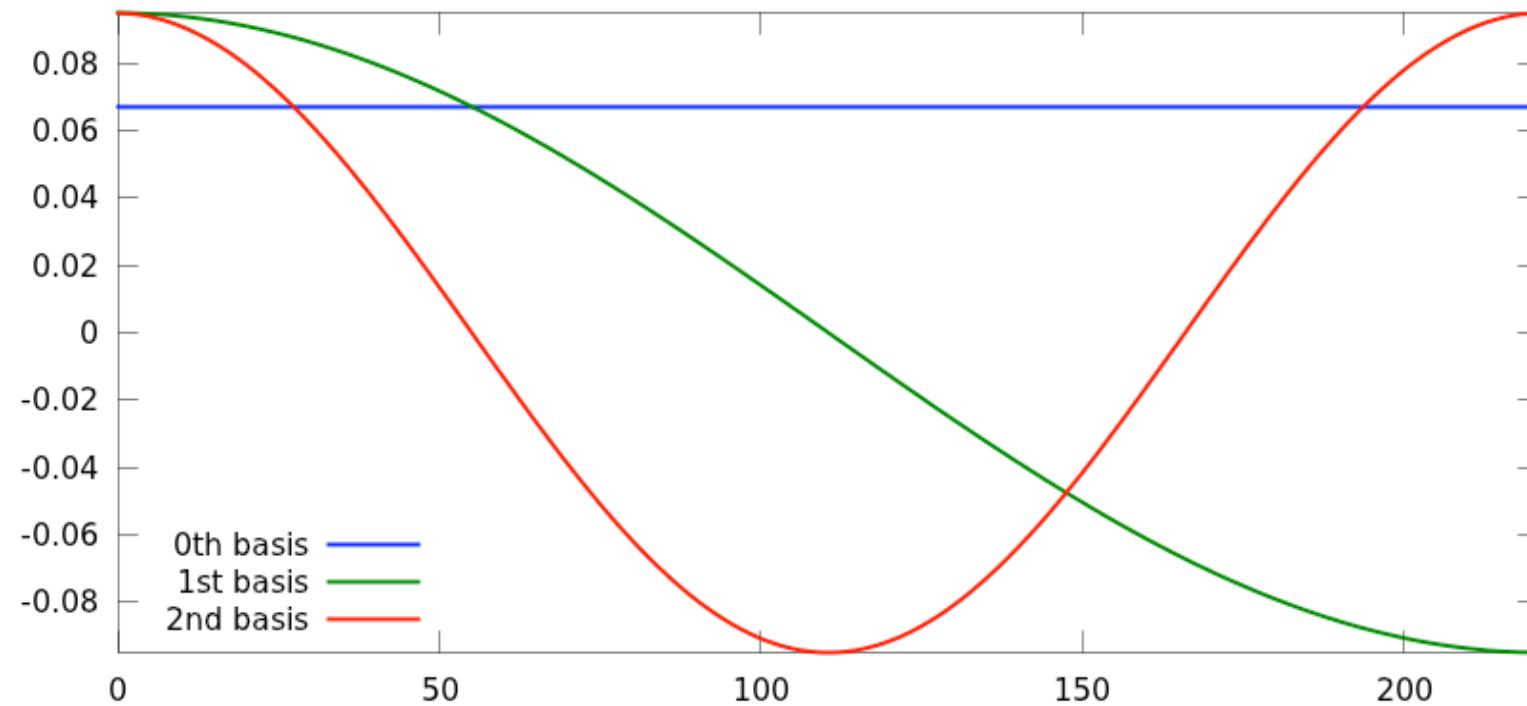
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# Future Work

- Modeling slope and curvature in fundamental frequencies with the first two coefficients of the Discrete Cosine Transform (Devaney, Mandel and Fujinaga 2011)



# Acknowledgements

- Center for Research in Music Media and Technology (CIRMMT)
- Fonds de recherche sur la société et la culture (FQRSC)
- Social Sciences and Humanities Research Council of Canada (SSHRC)
- Advancing Interdisciplinary Research in Singing (AIRS)

Thank you!

# References

- de Cheveigné A. and H. Kawahara. 2002. YIN: A fundamental frequency estimator for speech and music. *Journal of the Acoustical Society of America*. 111: 1917–30.
- Devaney J., M. Mandel, and D. Ellis. 2009. Improving MIDI-audio alignment with acoustic features. In *Proceedings of Workshop on Applications of Signal Processing to Acoustics and Audio*. 45–8.
- Devaney, J., J. Wild, and I. Fujinaga. 2011 Intonation in solo vocal performance: A study of semitone and whole tone tuning in undergraduate and professional sopranos. In *Proceedings of the International Symposium on Performance Science*.
- Devaney, J., M. Mandel, and I. Fujinaga. 2011. Characterizing singing voice fundamental frequency trajectories. in *Proceedings of the Workshop on Applications of Signal Processing to Acoustics and Audio*.
- Gockel H., B. Moore, and R. Carlyon. 2001. Influence of rate of change of frequency on the overall pitch of frequency-modulated tones. *Journal of the Acoustical Society of America*. 109: 701–12.
- Howard, D.M. 2007. Equal or non-equal temperament in a cappella SATB singing. *Logopedics Phoniatrics Vocology*. 32: 87–94.
- Jers, H. and S. Ternström. 2005. Intonation analysis of a multi-channel choir recording. *TMH-Quarterly Progress and Status Report* 47(1): 1–6.
- Orio, N., and D. Schwarz. 2001. Alignment of monophonic and polyphonic music to a score. In *Proceedings of the International Computer Music Conference*, 155–8.
- Prame E. 1997. Vibrato extent and intonation in professional western lyric singing. *Journal of the Acoustical Society of America*, 102: 616–21.
- Sundberg J. 1982. In tune or not? A study of fundamental frequency in music practise. *STL-Quarterly Progress and Status Report*, 23: 49–78.
- Vurma, A and J. Ross. 2006. Production and perception of musical intervals. *Music Perception*. 23(4): 331–44.
- Vurma, A. 2010. Mistuning in two-part singing. *Logopedics Phoniatrics Vocology*. 35: 24–33.