

# Enabling Multirotors to Perform Construction Tasks Using Swarm Algorithms

Jens-Christian Finnerup



Kongens Lyngby 2016

Technical University of Denmark  
Department of Applied Mathematics and Computer Science  
Richard Petersens Plads, building 324,  
2800 Kongens Lyngby, Denmark  
Phone +45 4525 3031  
[compute@compute.dtu.dk](mailto:compute@compute.dtu.dk)  
[www.compute.dtu.dk](http://www.compute.dtu.dk)

# Summary (English)

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The goal of the thesis is to ...



# Summary (Danish)

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Målet for denne afhandling er at ...



# Preface

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This thesis was prepared at DTU Compute in fulfilment of the requirements for acquiring an M.Sc. in Engineering.

The thesis deals with ...

The thesis consists of ...

Lyngby, 01-August-2016



Not Real

Jens-Christian Finnerup





# Acknowledgements

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I would like to thank my....



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## CHAPTER 1

# Introduction

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In today's world, we increasingly rely on robotics to perform a wide range of tasks, with use cases ranging from complimenting, or even substituting, human labour in factories to more complex tasks such as automated aerial photography. Though technology continues to improve, the use of robotics is often confined to within predictable environments, where machines are told what to do and when to do it. More recently though, as control algorithms improve, autonomous robots are starting to become a practical reality, with increasing ability self-plan and work unsupervised. As such we experience a paradigm shift, where robots are no longer limited to predictable and confined environments, but can act freely and adapt to changing circumstances.

As a consequence of this, new use cases and areas within robotics are starting to gain interest. Specifically the area of autonomous flying vehicles is gaining interest with companies such as amazon, preparing to use flying drones to deliver packages. This requires the drone to be able to plan according to changes in the environment as well as being able to coordinate its movements in relation to other drones around it. At a currently more theoretical scale, using flying drones to perform construction tasks has been subject for testing by universities such as *ETH Zurich*, where micro drones were used to construct a 6 meter tall tower [ALH<sup>+</sup>14].

The task of using flying vehicles to perform construction is especially interesting

because it combines many of the challenges that face robotics today, as agents become more autonomous. A construction task work as a great test bed, for testing flying drones as it involves multiple agents working on the same problem as once and as such they must have the ability to plan according to changes in their individual environment.

One solution to the challenges of enabling drones to collaborate, is to create individual sectors of space in which only a single agent is allowed to move at a certain time. This is a simple way to prevent collisions between the drones, but it also poses some optimization challenges, as the path of the drones cannot intersect. This means that even if a path for a drone towards a goal is optimal (shortest), it cannot be used if it intersects with the path of another agent. Another drawback of this simple solution is that it limits the amount of agents able to act with in a certain space, to a small number, as reach has to have its own designated area. As such there is great motivation to design control algorithms, which can enable drones to collaborate on tasks, while allowing them to avoid collisions without limiting their flight space.

This thesis focuses on how create and use algorithms from the field of swarm robotics as control for flying drones. The different algorithms will be implemented on a simulation test bed, to compare their complexity and their ability to give optimal movements to the drones within the simulation. For the comparison, different metrics will be used measure effectiveness in allowing drones to solve a collaborative problem. As a basis for the comparison, this thesis will document the implementation of the simulation platform and the control algorithms.

## 1.1 Problem Description

The following will outline the detailed goal of this thesis, as well as the subgoals necessary to achieve it.

### 1.1.1 Main Problem

To create and use swarm algorithms to enable quadcopters to coordinate their movements in a multi-agent environment.

### 1.1.2 Sub Problems

- To design and implement a simulation platform, based on a physical model, within which the algorithms can be used to control simulated agents
- To design a problem for the agents to collaborate on, to use as a standardized test for performance of the algorithms
- To determine the correct metrics for optimizing and comparing the swarm algorithms
- To implement swarm algorithms based on existing concepts, and test them using the metrics and the simulation platform
- To optimize the control algorithms based on pre mentioned tests, and analyze potential areas of improvement

## 1.2 Project plan

We note that the contents of the project plan is also something we would like to see in the introductory chapter of your thesis. In fact, you can reuse your final project plan (possibly extended) as the introduction. If you prefer to write an introduction from scratch, it is, of course, important that it is consistent with the final project plan.





# Methodology

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In order to evaluate the different control algorithms and their performance, the approach towards designing and testing the algorithms must be systematic and concise. The different subproblems specified in 1.1.2, can be said to either relate to either the simulation design or the algorithm design. As such, for the purpose of this thesis, a different approach will be used when dealing with constructing the simulation and when designing and testing the control algorithms. In this chapter, I will outline these approaches and the methodology used. The first three sections of this chapter will deal with the simulation methodology, whereas the latter three will deal with the implementation and testing of the control algorithms.

## 2.1 Control Problem

The main research problem of this thesis involves building and evaluating different control algorithms, and as such each algorithm must be subject to the same evaluation technique. This evaluation technique will throughout the thesis be referenced to as the *Control Problem*, and the purpose of the agents will be to solve this problem collectively. As such the problem chosen must be the same problem throughout every simulation and independent of the control algorithms

themselves. The problem must also be able to be solved collectively, by multiple agents at the same time, while still posing enough challenges to properly test the control algorithms. Posing dangers to the agents, such as the risk of collision.

This control problem will exist within the simulation as a physical task that the agents have to carry out. Chapter 3.3.1 will outline the concrete control problem used, as well a discussion on the specific control problem's advantages and limitations.

## 2.2 Simulation Implementation

The control problem and the simulation are mutually dependent, as the problem has to be able to exist and be solvable within the simulation. As such the simulation has to be designed with the control problem in mind, but the control problem also has to be made with the limitations of the simulation taken into account. The simulation aspect is crucial to the validity of the results expressed in this thesis. For the purpose of solving the problems outlined in this thesis, the simulation will be a virtual environment, in which drones can be deployed. The drones will have to be subject to the same physical laws, as they would in real life such that the findings and test results can be applied to issues and control techniques in the real world.

In order to reduce complexity of the simulation, some physical laws are not taken into account when designing the simulation. This is done based on assumptions on which laws influence the results. An outline of the simulation design, can be found in Chapter 3.

## 2.3 Validation

Validation is a method to ensure that the simulation is mimicking real life physics and not simply animating the desired behavior of the drones. The validation will be carried out iteratively along with the construction of the simulation, to monitor the progress of the simulation construction, and act as a sort of checklist to the accuracy and capabilities of the simulation. The validation phase consists of multiple validation tests, meant to test if the simulation actually simulates the physical mechanics required. These mechanics can range from gravitational pull to accurate impulse and mass on the bodies in the simulation. The validation tests will when range from checking the accurate acceleration of drones in free

fall etc. These validation tests are also important because the simulator must have the predictable behavior across many scenarios, such that they can be compatible. The validation tests will be discussed and outlined in Section 3.5

## 2.4 Test Metrics

Up until now this chapter on methodology has been focused on systematically creating and validating the simulation platform. The following part will be covering my approach to creating and testing the control algorithms.

The comparison of the algorithms tested within this thesis, will be done based on their ability to solve the Control Problem. However the control problem must be designed in such a way, that it can be solved to various degrees. To measure how well the control problem is solved, some metrics must be chosen so that they represent the challenges of the control problem. I.e. if the control problem challenges the agents in collision avoidance, a test metric could be each agent's distance to all other agents over time. Time to solve the problem will also act as a simple test metric. The metrics chosen will be covered in Chapter 3 and will in part be based on the challenges of swarm robotics covered in *Multi-robot navigation in formation via sequential convex programming* [AMBR15].

## 2.5 Control Implementation

The algorithms tested within this thesis and presented as *swarm algorithms* will be covered in depth in Chapter 4. When implementing and testing the algorithms in this paper, the algorithms will be partly implemented through experimentation. This is due to the fact that swarm algorithms such as the *Artificial Bee Colony* (or ABC) [BRG<sup>+</sup>11], cannot directly be mapped to the issue of controlling quadcopters to perform construction tasks. The ABC has a different number of agents and multiple categories. Because of this, mapping some of the algorithms will involve some experimentation and for the sake of methodology it must be stated that algorithms will undergo a level of personalization when implemented. This will be documented along with how much the algorithms ends up differing from its theoretical counterpart.

## 2.6 Optimization

In contrast to the Simulation Implementation, the implementation of the control algorithm will not be followed by a validation step in the same way. This is due to the fact the control algorithms cannot be validated with the same fixed criteria, as their desired behavior deviates for each algorithm. Instead, they will undergo optimization. This refers to the activity of not only mapping the control algorithms to control quadcopters, but also tuning them in an attempt to maximize their performance. This will be benchmarked with the test metrics and the control problem within the simulation. The optimization will only be done on the control algorithms themselves, and not by tuning simulation variables, as all algorithms must be tested on the same simulation. The simulation variables will be predetermined in the *Validation* phase (see Section 3.5) and hereafter remain static.

## CHAPTER 3

# Simulation

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As mentioned previously in this paper, there are many advantages to performing simulation vs. carryings

The simulation environment, hereafter referred to as simple *the simulation*, will be the 3D platform on which the quadcopters and their control algorithm can be tested. The simulation is carried out in continues time, and in this chapter i will outline the design and implementation of the simulation platform. Furthermore also the validation step used to ensure that the simulation follows the required physical mechanics.

### 3.1 Simulation vs. Animation

### 3.2 Software

The software used in this paper to create the simulation platform is Matlab Version 8.7 (R2016a) with Simulink [?]. Simulink was chosen based on its ease of use and ability to perform simulations continuous time. Simulink also has a 3D graphics engine called VR3D[?], which can be used to model 3D animations

from any signal output from the simulation model. I.e. if the simulation models a flying quadcopter, the position values of the quadcopter can be sent as signals to the 3D model. The ability to 3D animate the movements of the quadcopters is important, as *seeing* their actual flight paths can be a simple way to discover errors in either the simulation model or the control algorithm.

### 3.3 Design

This section will outline the specifications of the simulation platform, after which it is designed. Note that some specifications were not intended from the beginning, such as a limitation on global velocity, but are the result of an iterative design process and tuning the simulation.

#### 3.3.1 Control Problem

The goal of the control problem is to challenge the control algorithms such that they can be compared. The control problem chosen for the purpose of this thesis, will be for the agents to collaborate on assembling a structure. The structure will be made of boxes or bricks (hereafter referred to only as boxes), which the agents are able to lift and relocate. The starting position of the boxes will be in one end of the rectangular environment, where the assembled structure will be in the other end. This type of setup requires movement by the agents in close proximity to each other, which introduces the risk of collision. This type of problem must also be solved in a specific order, such that the bottom of the structure is created first etc. The control algorithm will be given the position of boxes as well as the position for the proposed bricks in the completed structure. The measurements used to test the performance of the control algorithm on this problem are outlined in 3.6. Figure 3.1 shows the design of the simulation environment, with the control problem and the agents viewed from the top.

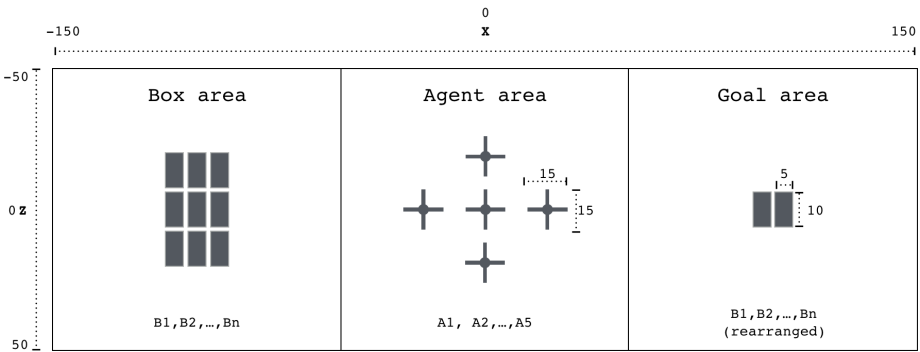


Figure 3.1: Design of simulation environment, as viewed from above

3.3.2 Assumptions on physics

The goal of the simulation is to simulate multiple flying quadcopters, and as such physical mechanics play an important role of the simulation model. This section will list the specifications of the simulation environment as well as some physical parameters. Due to the desire to limit complexity some physical parameters, such as wind, will be assumed to be non-existent in the simulation model. Others such as gravity and impulse must be included in the model, as they play a more vital role in producing accurate test results. The specifications of the physical parameters can be found in Table 3.3, followed by a brief reasoning behind the parameter.

Parameter	Role in simulation
Gravity	Simulated
Mass/Impulse	Simulated
Collisions	Detected, but not simulated
Friction	Not simulated
Wind resistance	Not simulated

Table 3.1: Physical parameters

- **Gravity** is an essential part of the simulation, as the control algorithm has to be tested in an environment where objects behave with close real-life resemblance. Please see 3.4.3 for the implementation of this mechanic
- **Mass** as well as the impulse that an object has when in movement, is an important aspect since it relates to how much force is required to affect

the movement of an object

- **Collisions** are important as well as they are used as a test metric for how well the control algorithms are performing. They are however not important to simulate or animate in 3D, as long as they can be detected. As such they are simply detected, to avoid adding complexity
- **Friction** to objects such as the friction between boxes, is assumed to be non-existent in the simulation. This also applies for the quadcopter's ability to carry the boxes, as it is assumed to always to functioning

### 3.3.3 Agents

The *Agents* within the simulation refer to the drones. The word agent is used as the problem of this thesis, can be mapped as a multi-agent problem with each drone acting as an individual agent. Table 3.2 shows the specifications of the agents in the simulation and is followed by description of, and a reasoning behind each specification.

Parameter	Description	Value
Agent-type	What type of agent to be simulated	<i>Quadcopter</i>
Size	The space occupied by an agent	<i>15x15x2cm</i>
Local Control	The low-level control system which balances and controls the agent position	<i>SimulinkPD</i>
Mass of agent	The number of quadcopters acting to solve the control problem	<i>150g</i>

**Table 3.2:** Agent Specifications

- The **agent-type** is important to not be changed throughout the simulation, as this determines which control surfaces and abilities an agent has. The quadcopter type is chosen because it is most common test platform for micro aerial vehicle (or MAV) control algorithms, and has for many become synonymous with the word *drone* [ALH<sup>+</sup>14]
- **Size** refers to the volume of space taken up by an agent. To reduce complexity an agent is represented by four arms and a center sphere in the simulation. A collision is defined by two or more agent's overlapping each others current space
- **Local Control** does not refer to the control algorithm that the quadcopters use to navigate, but rather the algorithm which stabilizes each



machine individually. This is a fairly standard and well tested part of modern quadcopters, and as such a standard library from Simulink is used for the desired effect. Please see 3.4.2 for the implementation of this

- **Mass of the agent** is implemented through a combination of both the gravitational mechanic and the PD controller library provided by Simulink. 150g is chosen as this is a common weight for MAVs

### 3.3.4 Simulation Environment

This subsection outlines the specifications for the simulation environment. This refers to the specific values of the physical mechanics used to simulate a real world environment, as well as the number of objects in, and the size of the simulated environment. These can be found in Table3.3

Parameter	Description	Value
Gravity	Mechanic to simulate Gravity	$9.8m/s^2$
Dimensionality	The number of space dimensions	3D
Floor size	The floor size relating to the area of the simulation	300x100cm
Number of agents	The number of quadcopters acting to solve the control problem	5
Number of boxes	The number of boxes to be moved to their respective goal position	9
Mass of box	The assumed mass of one box throughout the simulation	massless
Max. velocity	The limit of the velocity of any object on every axis	15cm/s
Max. acceleration	The limit of the acceleration of any object on every axis	$9.8m/s^2$
Attach threshold	The maximum distance from an agent to a box, before the box can be attached	2cm

**Table 3.3:** Environmental Specifications

- **Gravity** as mentioned in Table 3.1 the and is simulated as a force pulling on the Y-axis of the simulation with the normal gravitational acceleration of  $9.8m/s^2$
- **Dimensionality** is set to 3 dimensions. Having a 2-dimensional simulation could have worked for some applications, however one of the challenges

of mapping swarm algorithms to controlling drones, is the 3rd dimension. As such, having the simulation be in 3 dimensions is necessary and cannot be scaled down to reduce complexity without affecting the validity of the test results

- The **floor size** of the simulation platform is chosen to be  $300 \times 100 \text{ cm}$ , where the height is infinite. This is relatively small, but sufficient as the size of the drones are  $15 \times 15 \times 2 \text{ cm}$ , giving them plenty of space to move in
- **Number of agents** and are chosen to be 5. Initially the reasoning behind this was for testing purposes, but when experimentation with the swarm algorithms started, the 5 agents turned out to be posing the same challenges as a higher number due to the size of simulation environment. Therefore a higher number isn't needed
- **Number of boxes** ALRIGHT THIS NEEDS TO BE ADJUSTED
- The **mass of a box** is central to the performance of the control algorithms as it changes the total mass of the drone when carried. To reduce the complexity of the simulation however, these have been assumed to be massless and will as such not affect the drones movement
- **Max. velocity** is a parameter that was decided upon after some trial and error with getting the physical objects in the simulation environment, to behave in a real-life manner
- **Max. acceleration** was as with the limited velocity, inserted to force objects into behaving in a real life manner. This was needed as the Simulink PID component (see Section 3.4.2) had a tendency to overcompensate when accelerating drones to a desired velocity
- **Attach Threshold** is an interesting and quite important parameter. It builds on the assumption that an agent at any given velocity, can grab and carry a box as long as the grabbing action is performed when the distance between the agent and the box is smaller than or equal to this value

### 3.4 Implementation

After assessing the needs of the simulation model, the actual construction in simulink is done by connecting different modules in a circuit like manner. The model consist of a mixture of predefined Simulink blocks and custom Matlab script blocks, for more advanced functionality, such as the control algorithms.

The finished model, which can be seen in Figure 3.2. The modules and sub-modules of the simulation model have been labeled with a title, describing their functionality.

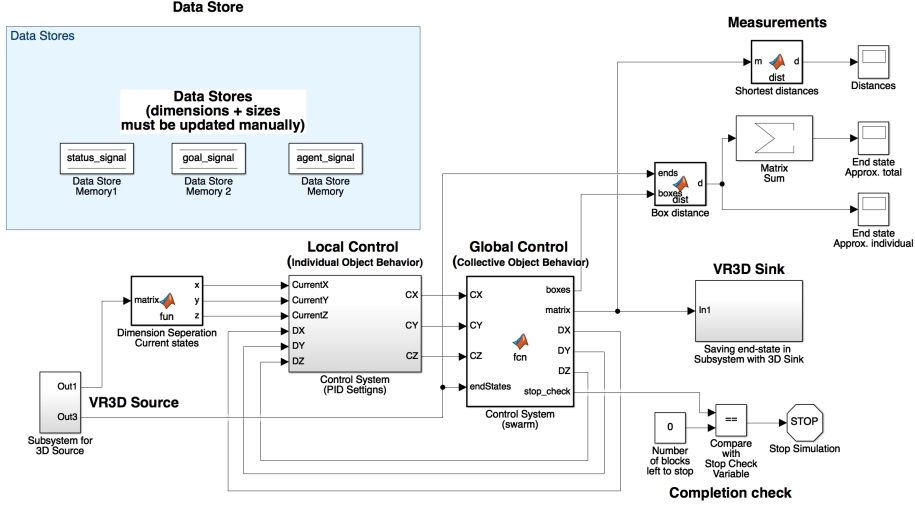
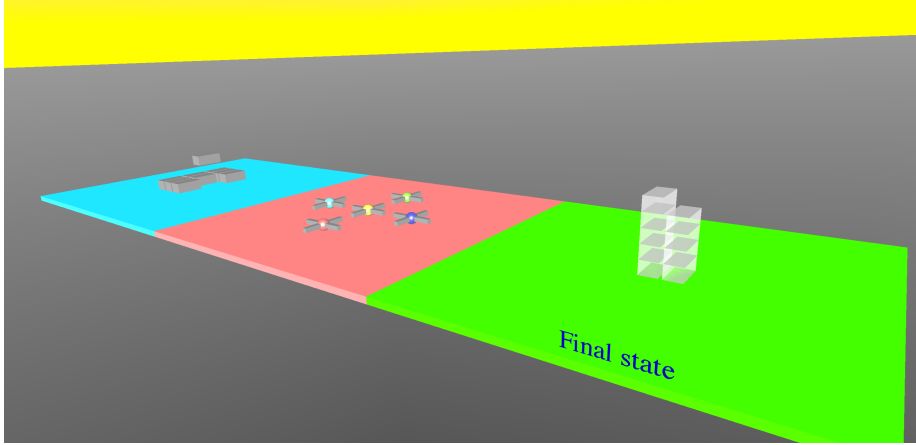


Figure 3.2: Overview of finished model in Simulink

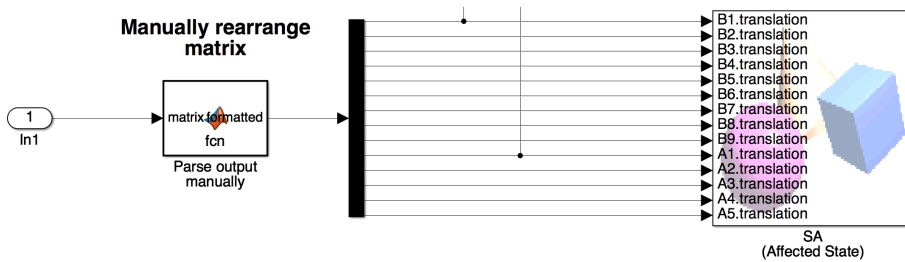
The following subsections will outline how the different model requirements from Section 3.3, were implemented in a step wise manner.

### 3.4.1 VR3D, Sources and Sinks

As shown in Figure 3.1, the simulation environment has certain starting points for the boxes and agents, and a desired endpoint for the boxes. The 3D animation is created with the Simulink plugin VR3D [INSERT REFERENCE], which acts both as a source and a sink. The VR3D editor is used to map the starting points of the objects, as well as the shape, size and all other visual aspects of the 3D environment. The actual 3D visuals can be found in Figure 3.3 where the transparent boxes are not physical objects but simply show the desired structure of the grey boxes. The data from the 3D environment, is then sent as a signal to the simulink model and to the control algorithm, which alters the signal and sends it back into the VR3D block to create an animation. The subsystems of the model which hold the source and the sink can be seen in Figure 3.2 whereas the contents of the sink, with the signal parsing, is shown in Figure 3.4



**Figure 3.3:** Screenshot from the VR3D environment used in the simulation



**Figure 3.4:** Signal from model being parsed to VR3D Sink

### 3.4.2 PID Controller

As mentioned in Section 3.1, it is important the swarm control algorithm cannot alter the position of the agents directly, but instead give instructions to the quadcopters to change their thrust etc. Distribution of control is implemented by having two separate control systems as briefly mentioned in 3.3.3. The two systems are shown in Figure 3.3, as blocks labeled **Local Control** and **Global**.

The **Global Control System**, controls and navigates the agents using the desired swarm algorithm. This Control block is what is referenced to throughout this thesis, as the *Control System*.

The **Local Control** is a subsystem (collection of Simulink blocks) responsible

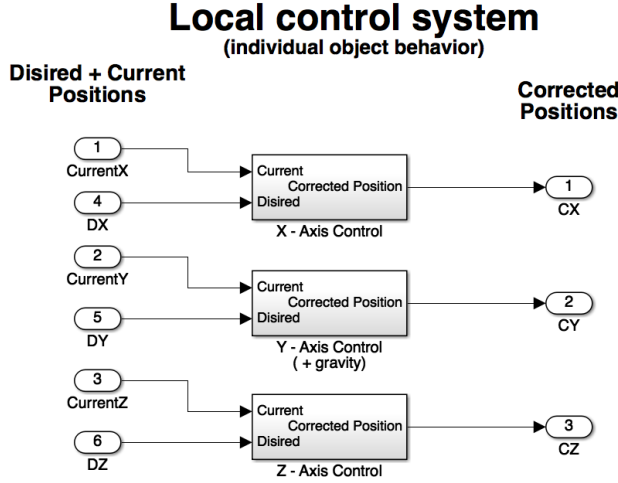
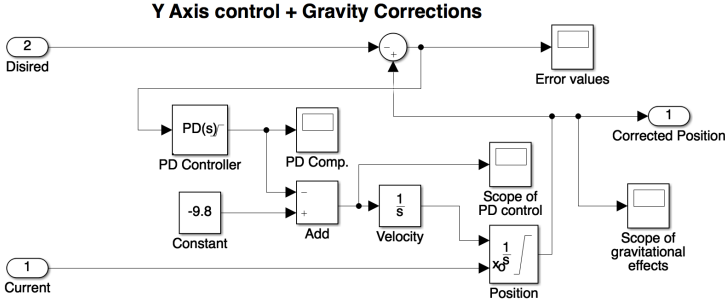


Figure 3.5: Local Control subsystem

for handling the physical mechanics of the individual objects within the simulation. It uses a Simulink PID plugin, to enable the quadcopters to balance and move around in a real life manner. In practice, the global control system maps the different agents' desired position at a given time, sends this as a signal to the local control system. The local control system then attempts to achieve the results within the physical boundaries of the simulation [INSERT REFERENCE]. Figure 3.5 shows the local control system receiving the current and desired locations from the global control system, and for making the appropriate alterations. For the process of adjusting the PID to mimic real world mechanics, please see Section 3.5.

### 3.4.3 Gravity & Mass

The impulse of moving objects and their mass affected by gravity, is implemented within the Local Control System. This is done with a collection of Simulink blocks, which have been adjusted to enable real life object behavior based on newton mechanics [INSERT REFERENCE]. Figure 3.6 shows the model used to control behavior on the Y-Axis of the simulation (vertical), which includes the gravitational acceleration constant of  $9.8m/s^2$ . The models for the X+Z Axis are similar, with the difference of not having a constant acceleration.



**Figure 3.6:** Simulink model to implement physics mechanics on vertical axis

### 3.4.4 Control Loop

The Control Loop is the part of the model labeled as **Global Control** in Figure 3.2. This Simulink block consists of a Matlab function and within this Matlab function, the control loop is implemented, giving actions to each agent based on their sensory inputs. This is where the swarm algorithms, to be outlined in Chapter 4, are implemented based on the agent's sensory inputs. As mentioned in Section 3.4.2 this iteratively communicates with the Local Control block. This block also computes the remaining part of the Control Problem, and sends a signal to the model to perform a simulation stop when the control problem is completed.

### 3.4.5 Data Stores

The Data Stores in Figure 3.2 work in connection with the Global Control Loop of the model, to store the data in between the iterations of the control loop. This is used to save the agent's sensory inputs over time, as well as the positions and other simulation data if required. This is needed due to the fact that Simulink Matlab function blocks, overwrites local variables for each computation of the control loop. As such these data stores are a way to use global variables in simulink.

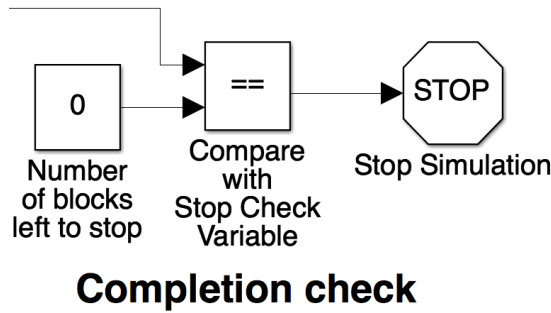
### 3.4.6 Measurements

The measurements blocks in simulation model, are connected to the Global Control Loop, and perform different calculations on the progress of the simula-

tion. The measurements are outlined in Section 3.6, and are exported to graphs such that different control algorithms can be compared. This is done with the Simulink Scope block.

### 3.4.7 Completion Check

Figure 3.7 shows the part of the simulation model which is responsible for stopping the simulation time when the control problem is solved completely or when the time limit of 500 seconds is reached. The control problem is solved once the blocks left to be moved correctly are equal to zero.



**Figure 3.7:** Completion check of the model

## 3.5 Validation

The validation of the simulation is done to check the it can mimic desired real world behavior. For the purpose of this simulation, the desired behavior is outlined in the physical assumptions of Section 3.3.2. The simulation however cannot be run without a control algorithm to move the agents, and for the purpose of validation, I use a Shortest Path algorithm. This simply directs the agents to move in a straight line from the boxes to their desired location, until all boxes have been placed correctly. This can be predicted to cause collisions, as the straight lines will be closer to each other, than the agent's width. For validation purposes this is desired, as it will test the simulation's ability to detect collisions.

3.5.1 Gravity

3.5.2 Measurements

3.5.3 Adjusting for desired behavior

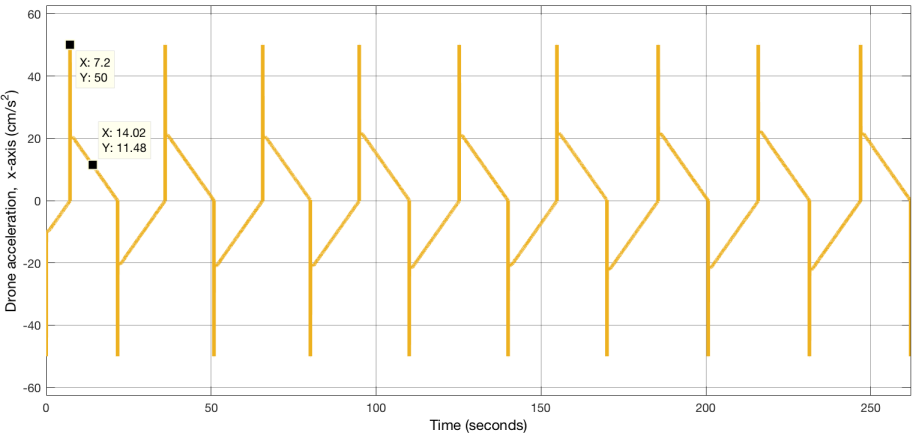


Figure 3.8: Agent acceleration before adjustment

Stable but too tall

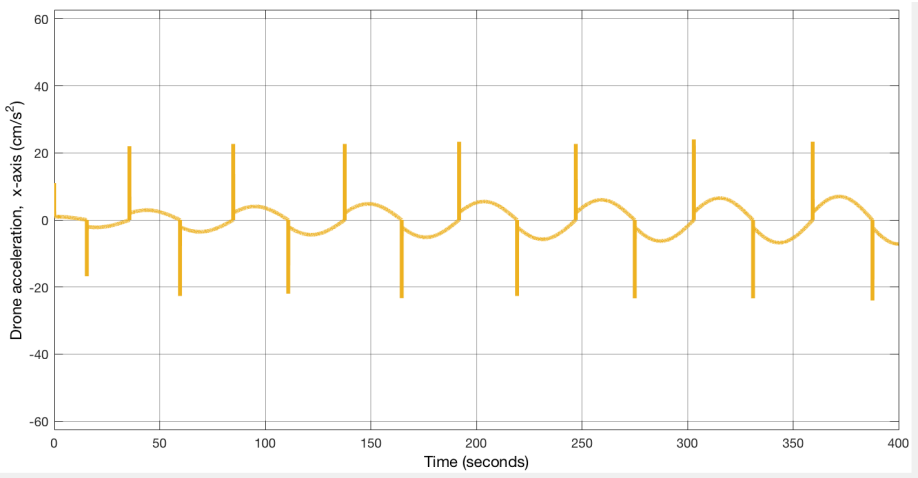


Figure 3.9: Agent acceleration after adjustment of PD gains



short but unstable

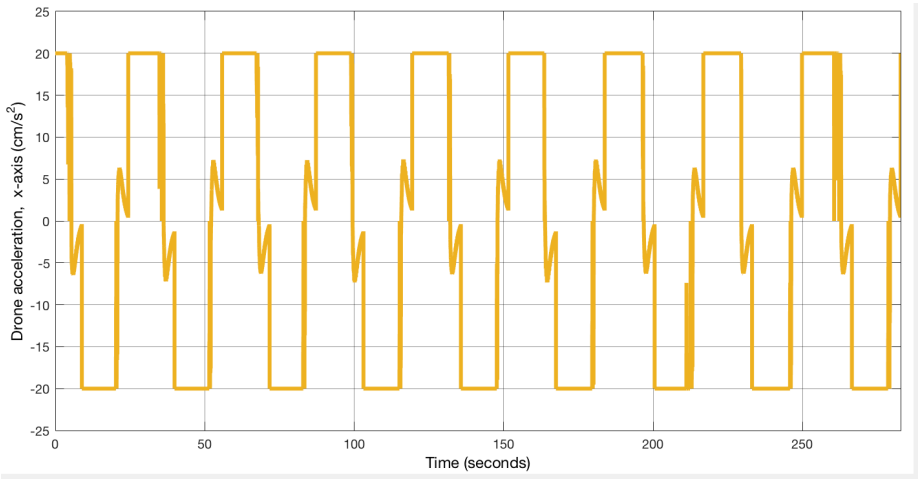


Figure 3.10: Agent acceleration with acceleration

Shorter and wider is stables

3.6 Test Metrics

3.6.1 Testing on shortest path



## CHAPTER 4

# Swarm Logic & Swarm Algorithms

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### 4.1 Multi-body vs. Multi-agent path planning



## CHAPTER 5

# Design

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