

전기회로 (가, 나)

Chapter 6 : Capacitors & Inductors

2017. 1학기

윤영식 교수

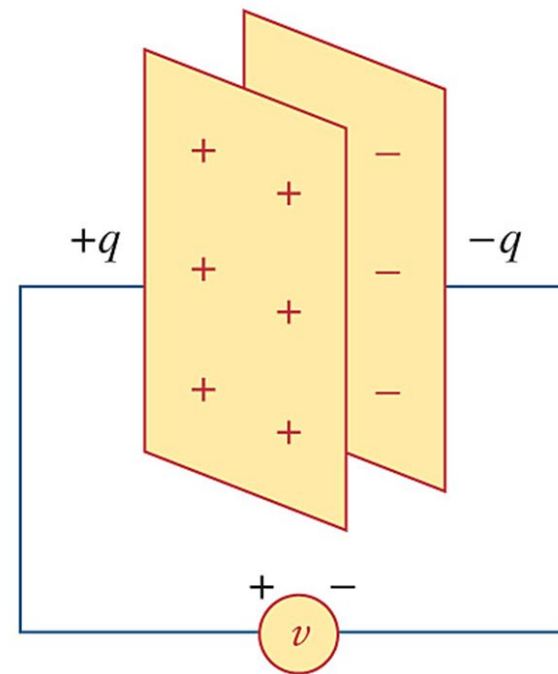
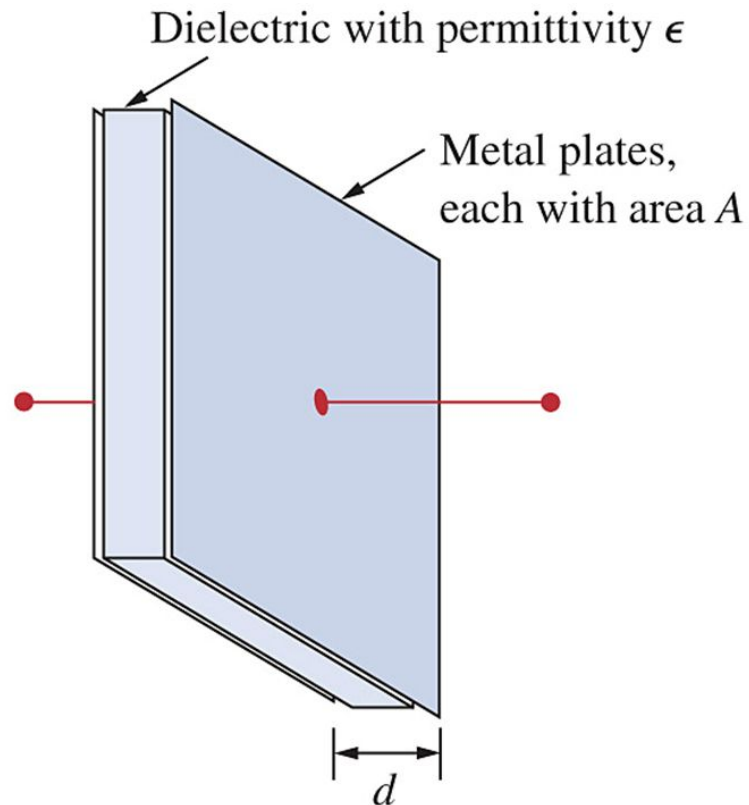
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6.2 Capacitors (캐패시터)

● Capacitor

- 전기장(electric field)에 에너지를 저장하는 수동소자
- 절연체(또는 유전체)를 사이에 두고 2장의 전도판으로 구성



6.2 Capacitor : capacitance

- 전하(electric charge)를 저장 → 충전
- 저장되는 전하의 양은 두 판 사이에 걸리는 전압에 비례

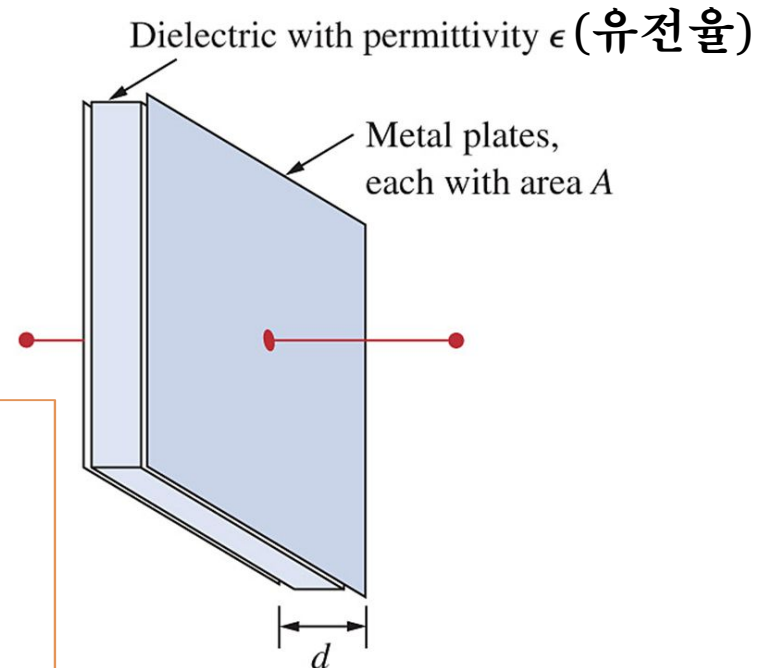
$$q = Cv$$

C : 비례상수 (farad, F) → capacitance

$$C = \frac{\epsilon A}{d}$$

C (capacitance) 증가

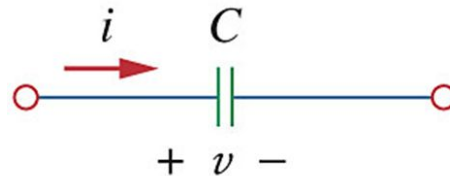
- 판의 표면적이 넓을수록
- 판 사이의 거리가 가까울수록
- 절연체의 유전율이 높아질수록



6.2 Capacitor

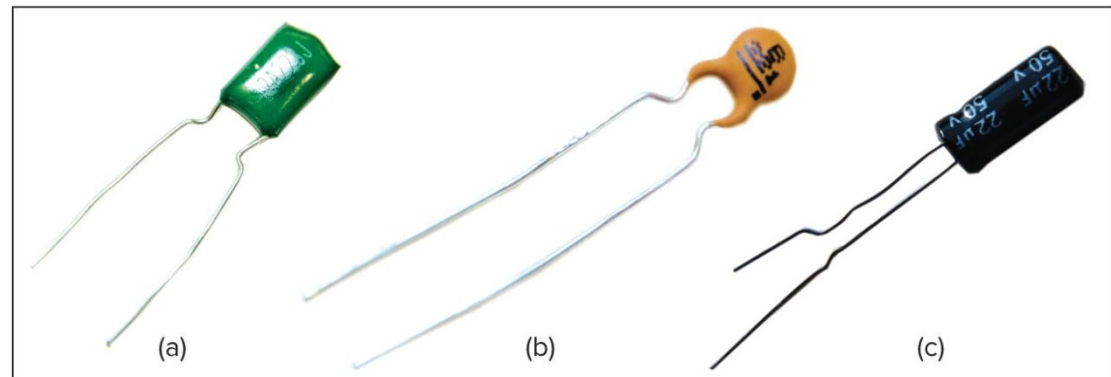
○ 충전과 방전

- 충전(charging) : 전류의 방향과 전압강하의 방향이 일치
- 방전(discharging) : 전류의 방향과 전압강하의 방향이 반대



○ 용도

- DC(직류) 차단
- 위상 변화, 주파수 변화
- 에너지 저장/방전
- 잡음 제거
- 라디오 튜너
- 메모리



6.2 Capacitors : i-v relationship

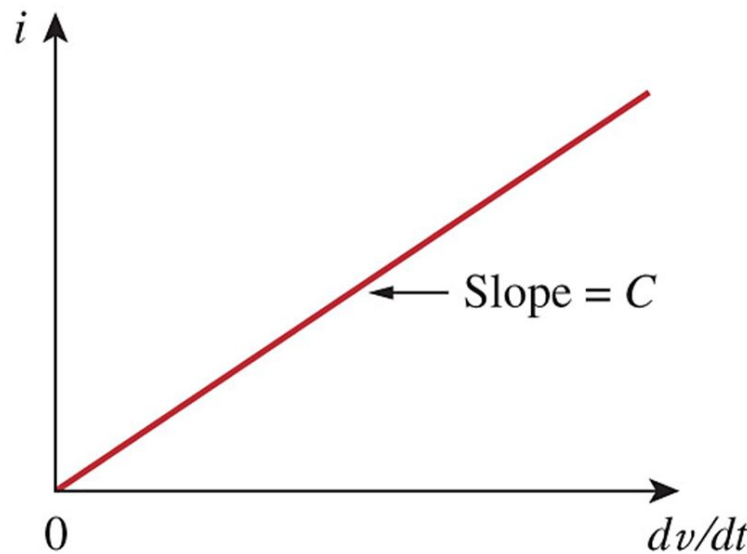
$$q = Cv \quad \& \quad i = \frac{dq}{dt}$$



$$i = C \frac{dv}{dt}$$

$$v = \frac{1}{C} \int_{-\infty}^t i dt \quad \text{or} \quad v = \frac{1}{C} \int_{t_0}^t i dt + v(t_0)$$

$$v(t_0) = q(t_0) / C$$



시간(t)에 따라 변함.

cf) 저항(R) : $v = iR$ $i = \frac{v}{R}$

6.2 Capacitors : Capacitor Energy

- 순간전력 $p(t)$: $p(t) = v(t)i(t) = Cv \frac{dv}{dt}$

- capacitor에 저장된 에너지 w :

$$w(t) = \int_{-\infty}^t p(t) dt = C \int_{-\infty}^t v(t) \frac{dv(t)}{dt} dt = C \int_{v(-\infty)}^{v(t)} v dv = \frac{1}{2} C v^2$$

$$w = \frac{1}{2} C v^2$$

6.2 Capacitors

Capacitor의 주요 성질

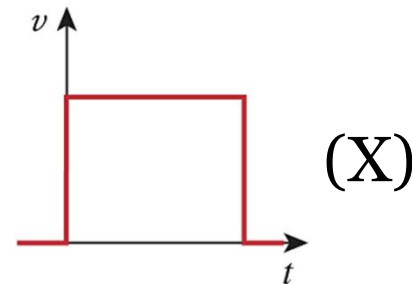
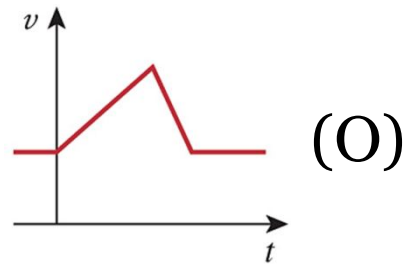
- 직류 차단 (직류 전류는 C 통과 불가)

$$i = C \frac{dv}{dt}$$

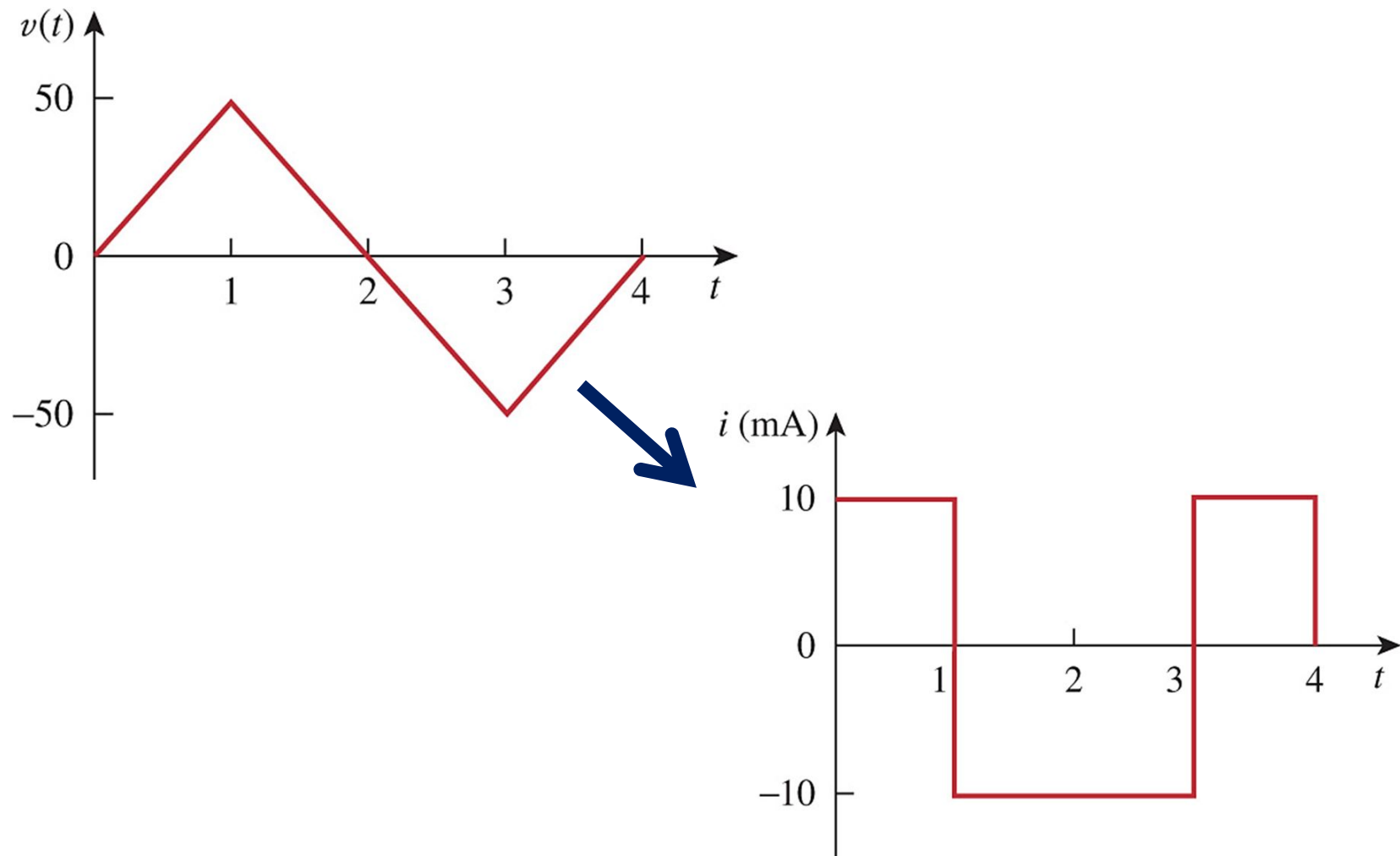
- DC에 대하여 C는 open circuit
- DC 전압에 의하여 충전은 가능

- Capacitor 전압은 급하게 변하지 못한다.

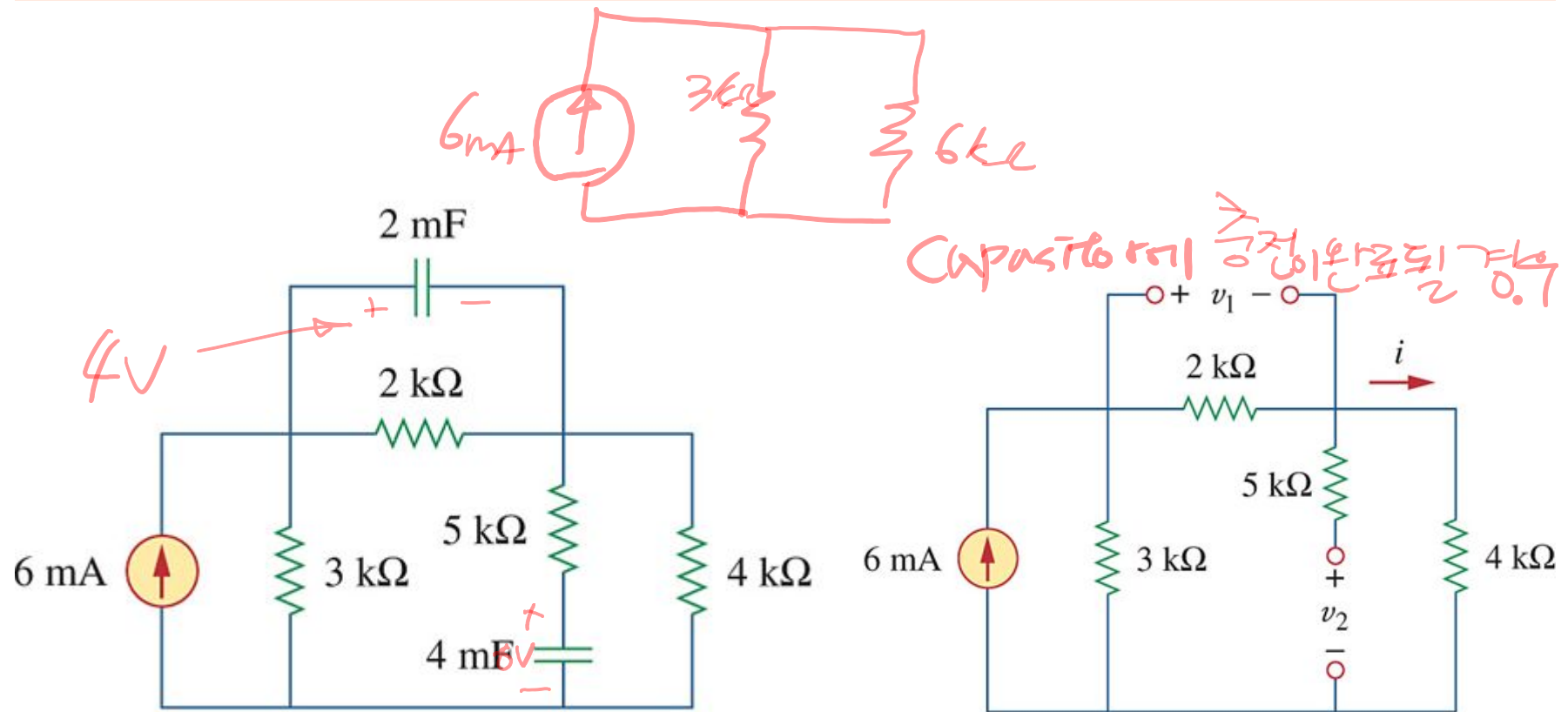
- 전압의 변화를 방해



Example 6.4

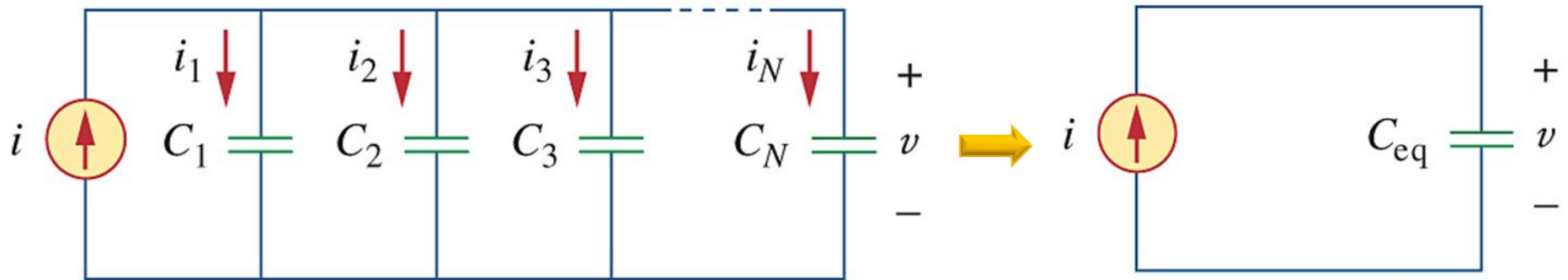


Example 6.5



6.3 Series & Parallel Capacitors

Capacitor의 병렬연결



KCL 적용 :

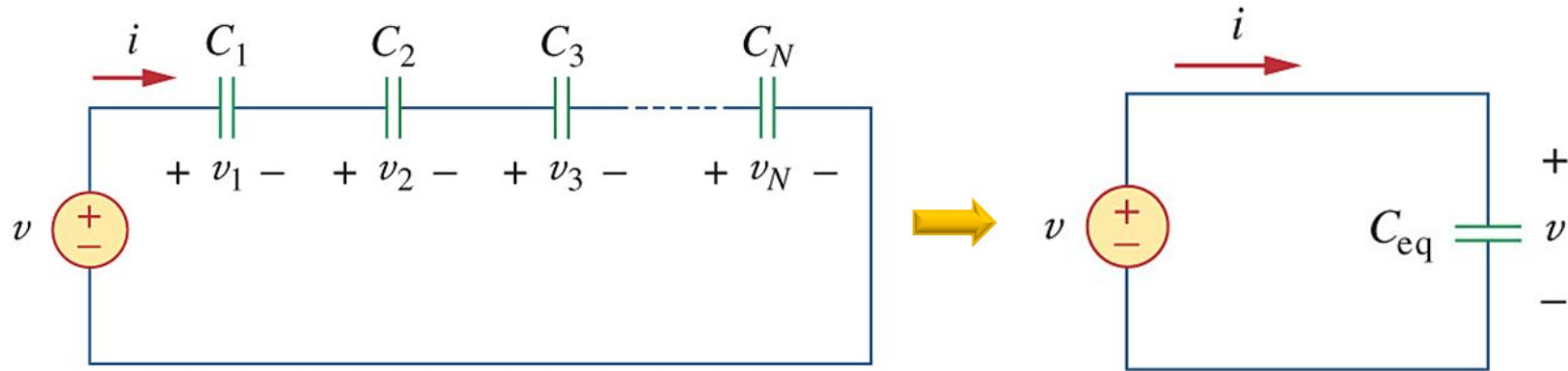
$$i = i_1 + i_2 + i_3 + \dots + i_N$$

$$C_{eq} \frac{dv}{dt} = C_1 \frac{dv}{dt} + C_2 \frac{dv}{dt} + C_3 \frac{dv}{dt} + \dots + C_N \frac{dv}{dt}$$

$$C_{eq} = C_1 + C_2 + C_3 + \dots + C_N$$

6.3 Series & Parallel Capacitors

Capacitor의 직렬연결



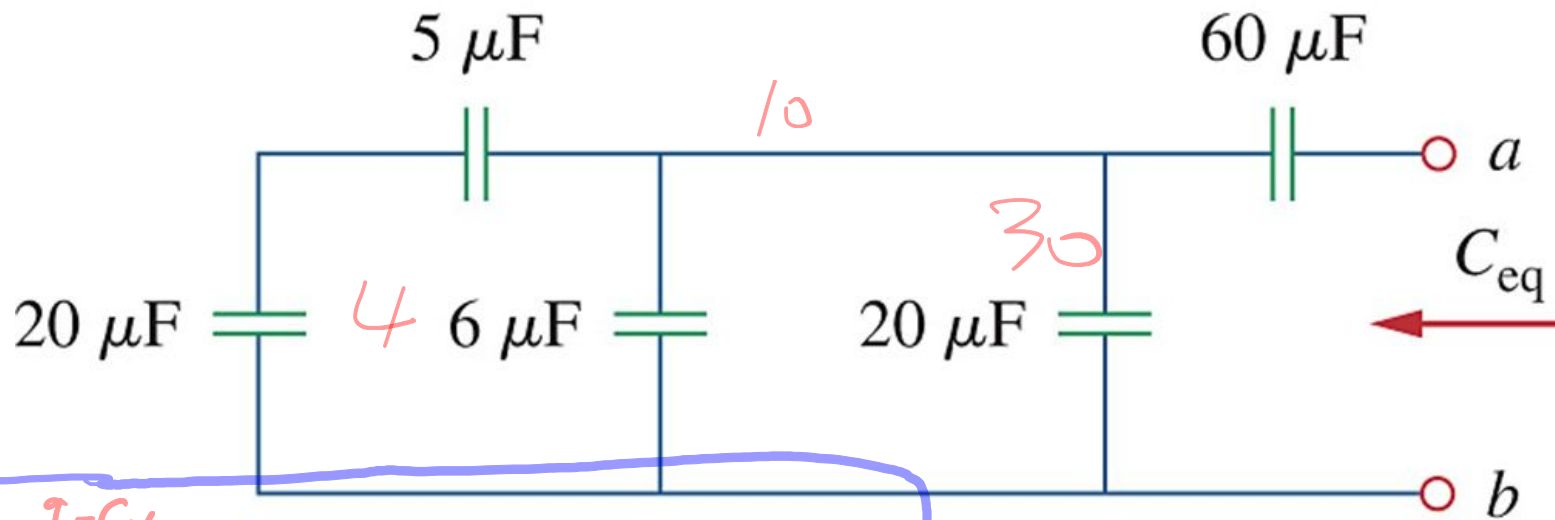
KVL 적용 :

$$v = v_1 + v_2 + v_3 + \dots + v_N$$

$$\frac{1}{C_{eq}} \int_{-\infty}^t i(t) dt = \frac{1}{C_1} \int_{-\infty}^t i(t) dt + \frac{1}{C_2} \int_{-\infty}^t i(t) dt + \frac{1}{C_3} \int_{-\infty}^t i(t) dt + \dots + \frac{1}{C_N} \int_{-\infty}^t i(t) dt$$

$$\boxed{\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots + \frac{1}{C_N}}$$

Example 6.6



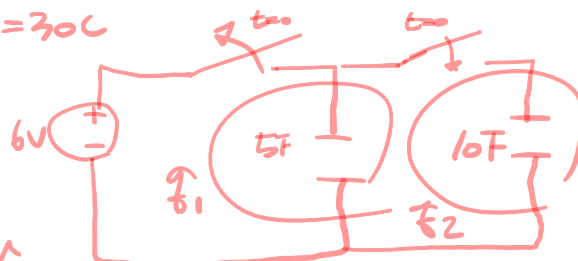
$$Q = CV$$

$$= 5\ \text{F} \times 6\ \text{V} = 30\ \text{C}$$

$$Q_1 = 5\ \text{F} \times 5\ \text{V} = 25\ \text{C}$$

$$Q_2 = 5\ \text{F} \times 5\ \text{V} = 25\ \text{C}$$

$$30 = 25\ \text{V} + 5\ \text{V} = 30\ \text{V} \quad \therefore 2\ \text{V}$$

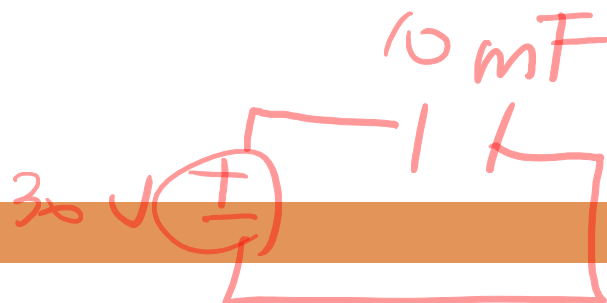
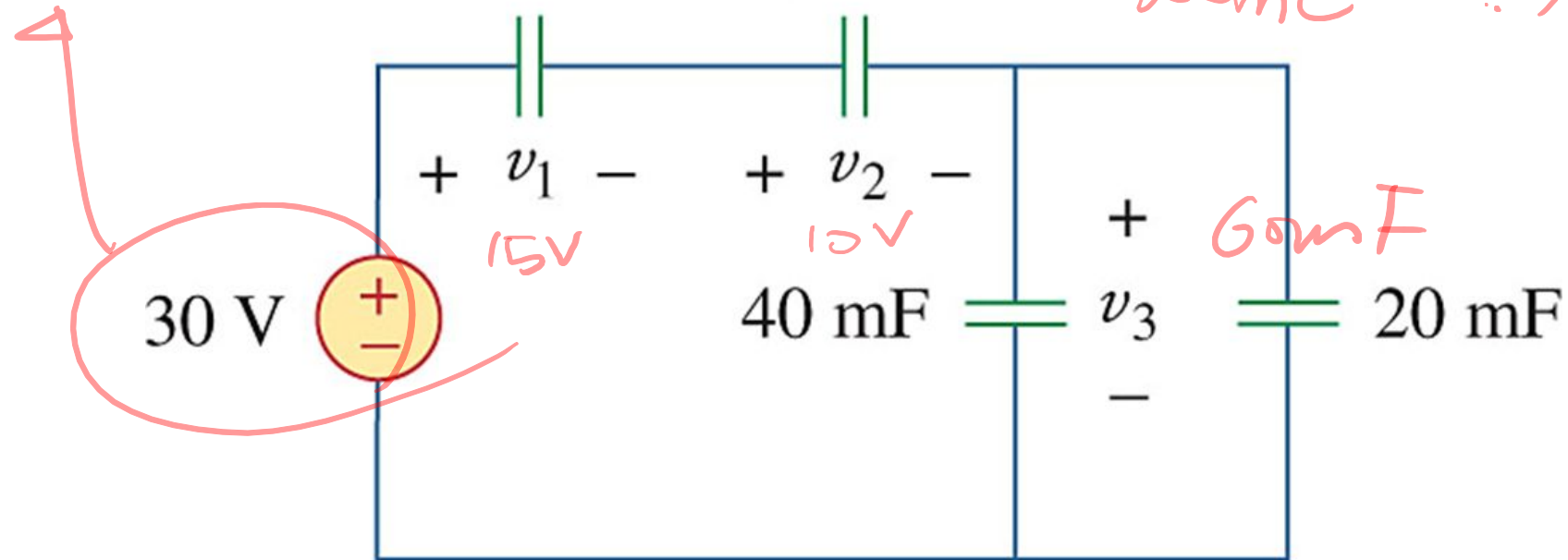


$20\ \mu\text{F}$

Example 6.7

전하가 같은데
충전된 전하량도 같음

$$q = C_V = 10 \text{ mF} \times 30 \text{ V} \\ = 300 \text{ mC} = 0.3 \text{ C}$$



$$q_1 = 300 \text{ mC} = 20 \text{ mF} \times V_1 \\ V_1 = 15 \text{ V}$$

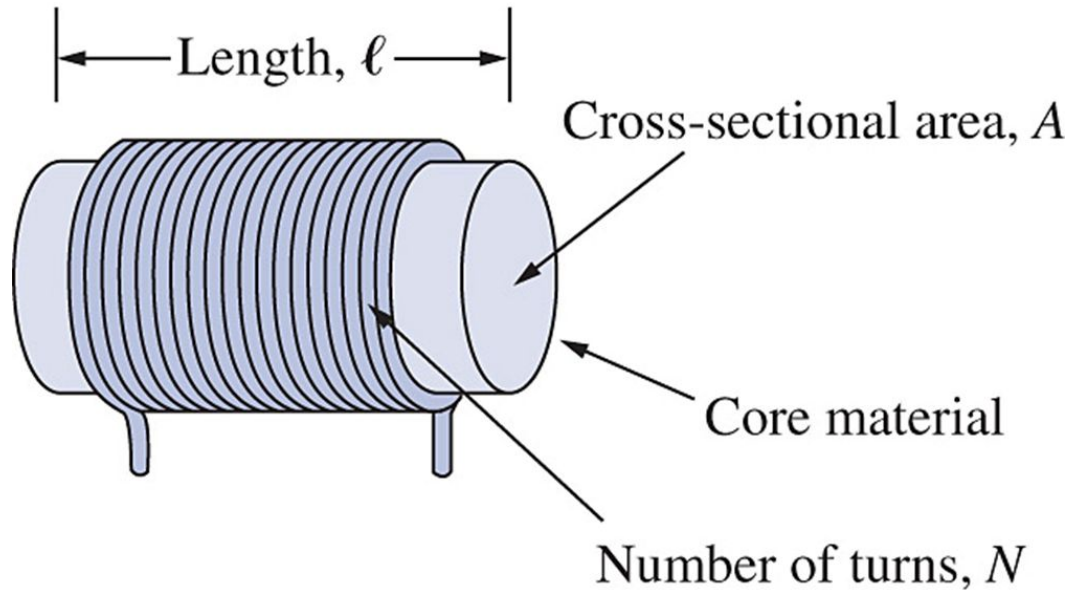
$$q_2 = 300 \text{ mC} = 30 \text{ mF} \times V_2 \\ V_2 = 10 \text{ V}$$

6.4 Inductor

● Inductor란?

$$q = CV, \quad i = C \frac{dv}{dt}$$

- 자기장(Magnetic Field)에 에너지를 저장하는 수동 소자
- 모든 금속은 자체적으로 인덕턴스가 존재 함
- 인덕턴스 값을 증가 시키기 위하여 주로 코일의 형태로 구현



6.4 Inductors : Inductance

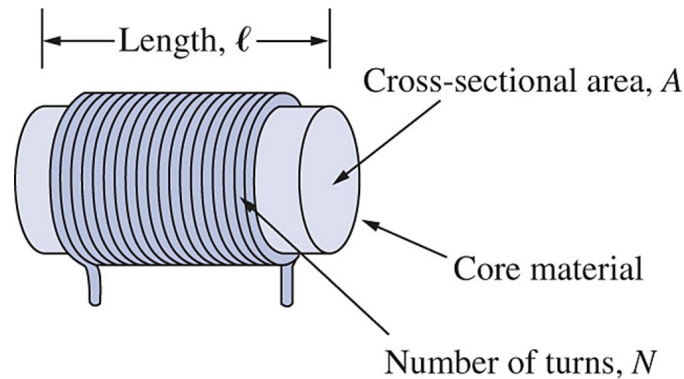
- 인덕터에 걸리는 전압은 전류의 시간적 변화량에 비례

$$v = L \frac{di}{dt}$$

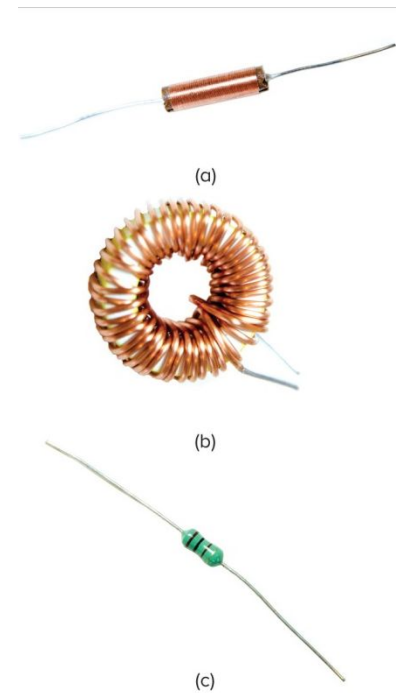
전류 \uparrow : 전류 흐름을 방해

L : 비례상수 (inductance, henry(H))

$$L = \frac{N^2 \mu A}{l}$$



μ : permeability(투자율, 透磁率)



6.4 Inductors : i-v relationship

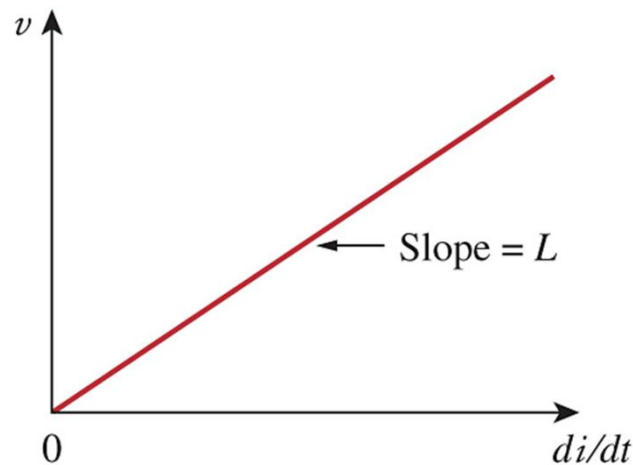
$$v = L \frac{di}{dt}$$



$$i = \frac{1}{L} \int_{-\infty}^t v(t) dt$$

or

$$i = \frac{1}{L} \int_{t_0}^t v(t) dt + i(t_0)$$



6.4 Inductors : Power & Energy

- 인덕터의 전력(power) : $p = vi = \left(L \frac{di}{dt} \right) i$

- 인덕터에 저장되는 에너지 :

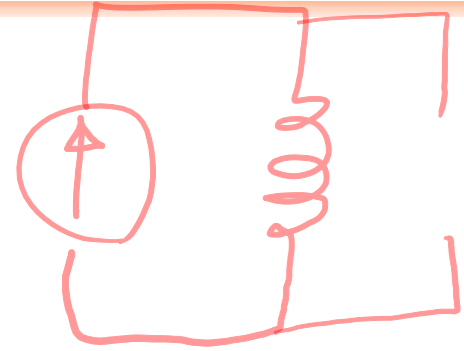
$$w = \int_{-\infty}^t p dt = \int_{-\infty}^t \left(L \frac{di}{dt} \right) i dt = L \int_{-\infty}^t i di = \frac{1}{2} Li^2(t)$$

$$w = \frac{1}{2} Li^2$$

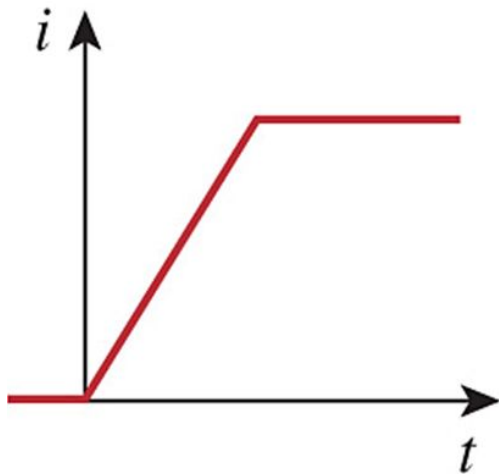
6.4 Inductors

- Inductor의 주요 성질

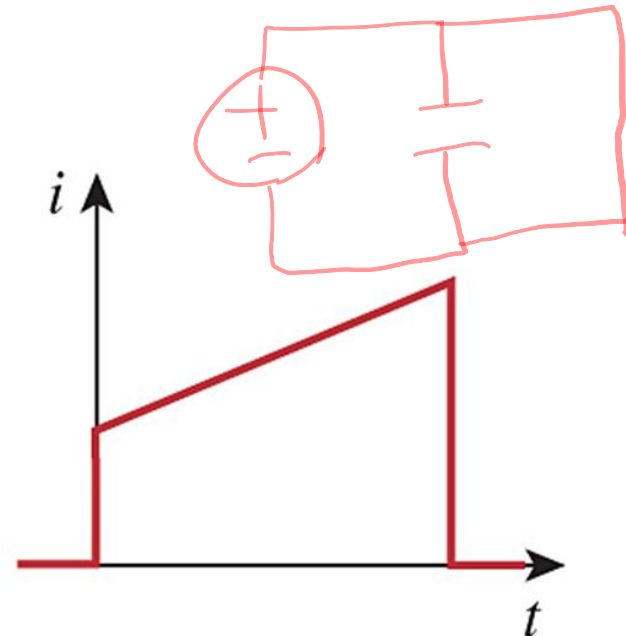
- 직류 전류에 대하여 저항 0 \rightarrow short circuit로 동작
- 인덕터를 통하여 흐르는 전류는 급격하게 변하지 못한다.
 - 전류의 변화를 방해



전압소모 X

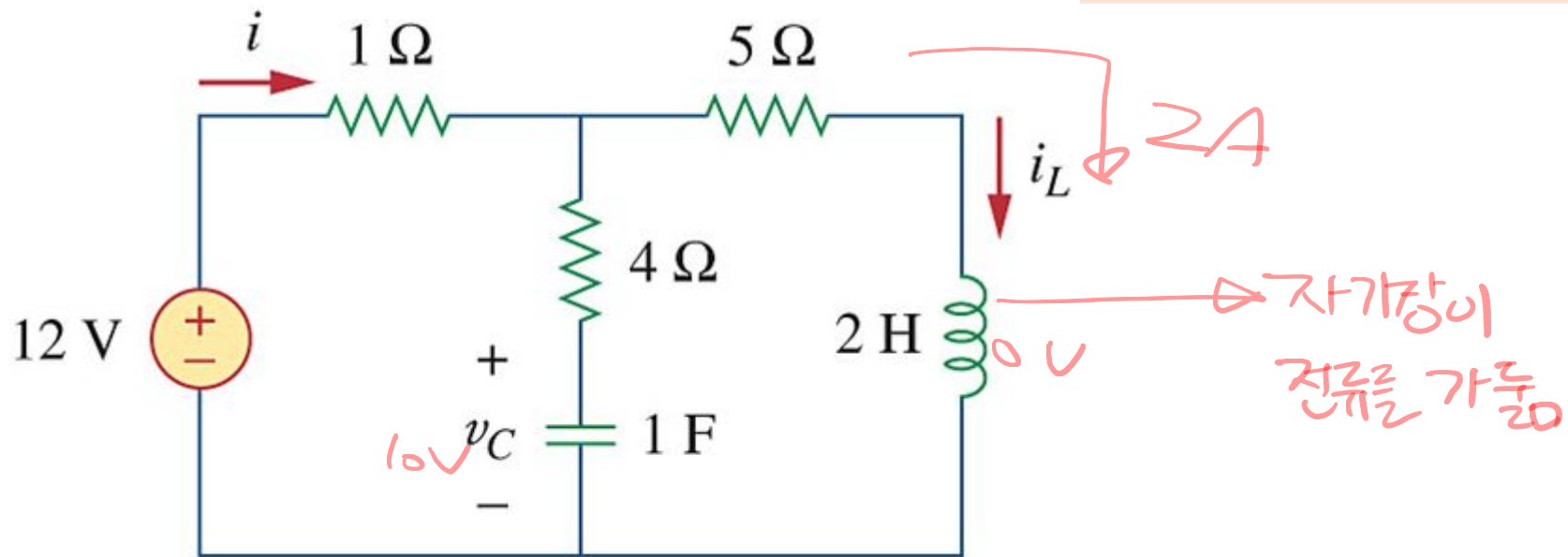


(O)

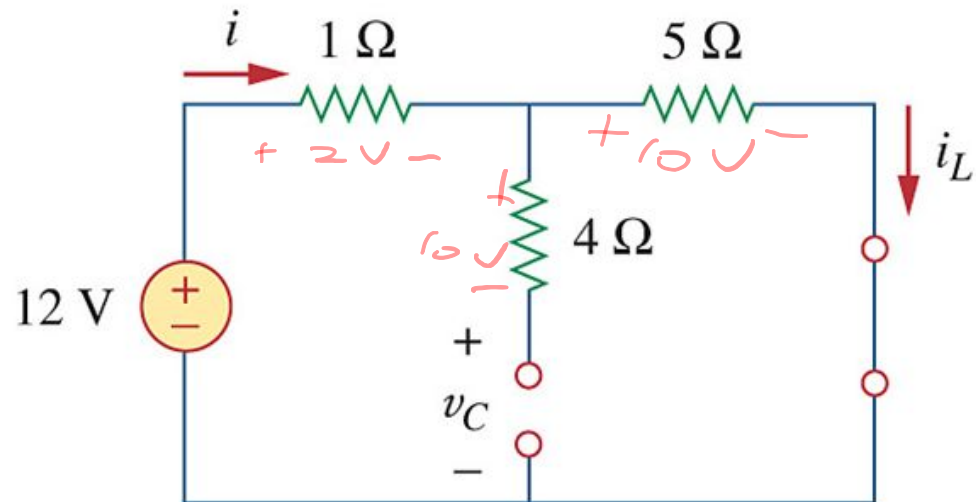


(X)

Example 6.10

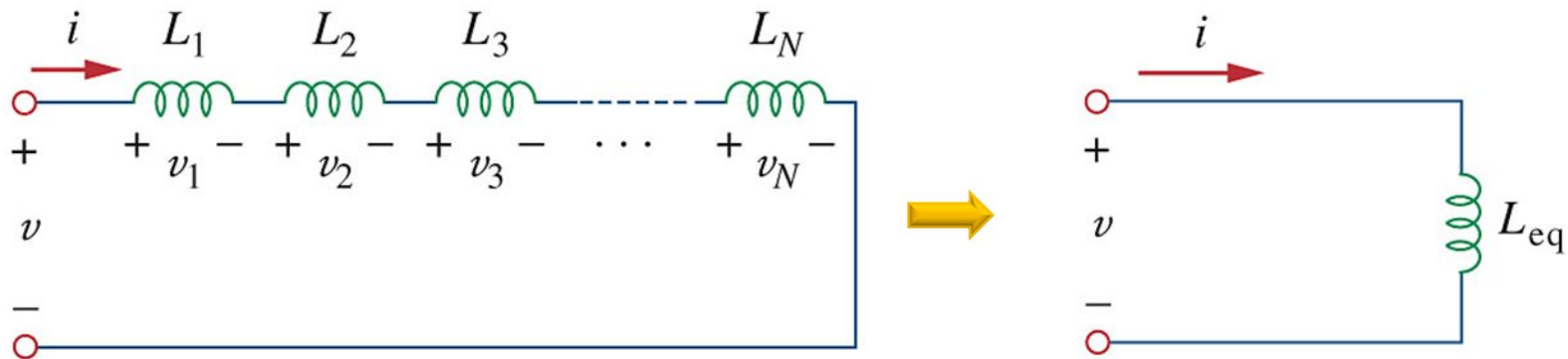


$t = \infty$



6.5 Series & Parallel Inductors

● Inductor의 직렬연결



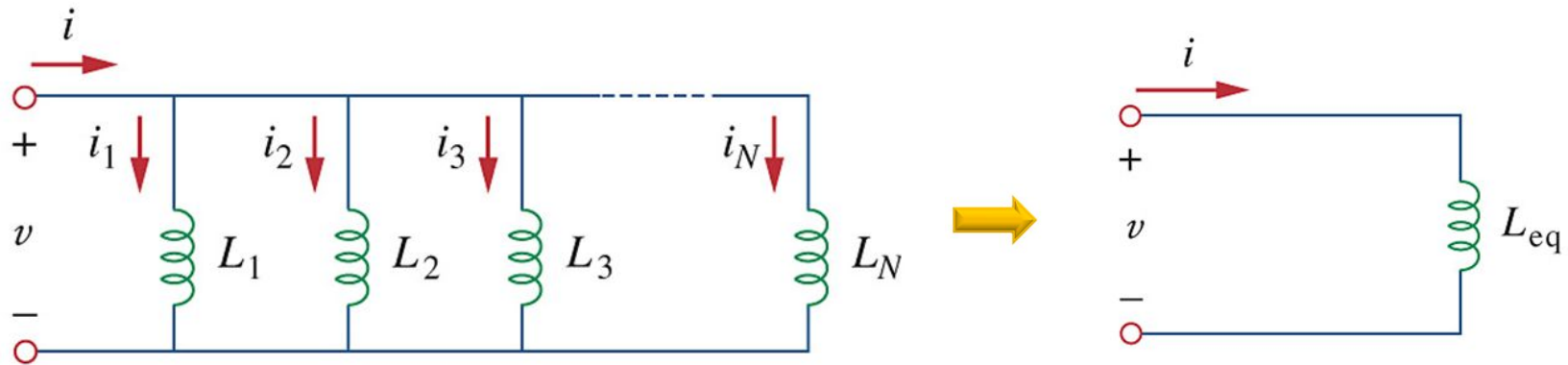
KVL 적용 : $v = v_1 + v_2 + v_3 + \dots + v_N$

$$L_{eq} \frac{di}{dt} = L_1 \frac{di}{dt} + L_2 \frac{di}{dt} + L_3 \frac{di}{dt} + \dots + L_N \frac{di}{dt}$$

$$L_{eq} = L_1 + L_2 + L_3 + \dots + L_N$$

6.5 Series & Parallel Inductors

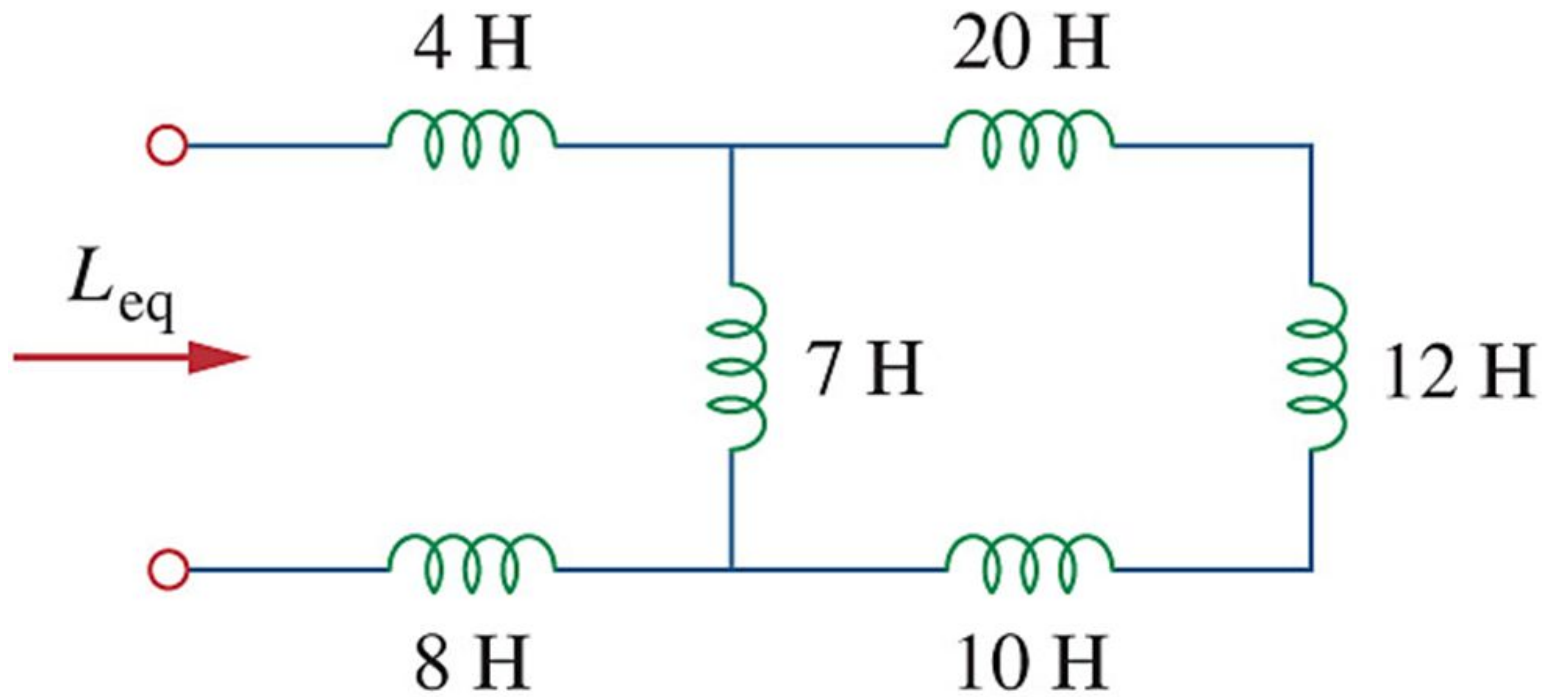
- Inductor의 병렬연결



KCL 적용 :

$$\frac{1}{L_{eq}} = \frac{1}{L_1} + \frac{1}{L_2} + \dots + \frac{1}{L_N}$$

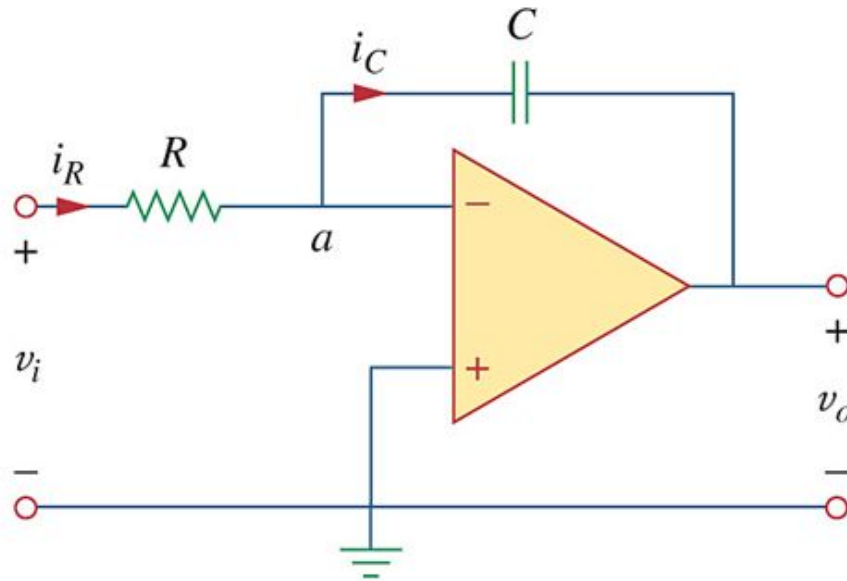
Example 6.11



Summary

Relation	Resistor (R)	Capacitor (C)	Inductor (L)
v-i	$v = iR$	$v = \frac{1}{C} \int i dt$	$v = L \frac{di}{dt}$
i-v	$i = \frac{v}{R}$	$i = C \frac{dv}{dt}$	$i = \frac{1}{L} \int v dt$
전력(p), 에너지(w)	$p = i^2 R = \frac{v^2}{R}$	$w = \frac{1}{2} C v^2$	$w = \frac{1}{2} L i^2$
직렬연결	$R_{eq} = R_1 + R_2$	$C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$	$L_{eq} = L_1 + L_2$
병렬연결	$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$	$C_{eq} = C_1 + C_2$	$L_{eq} = \frac{L_1 L_2}{L_1 + L_2}$
@ 직류	-	open circuit	short circuit
방해 요소	전류의 흐름	전압의 변화	전류의 변화

6.6.1 Integrator (적분기)



Node a에서 KCL 적용 :

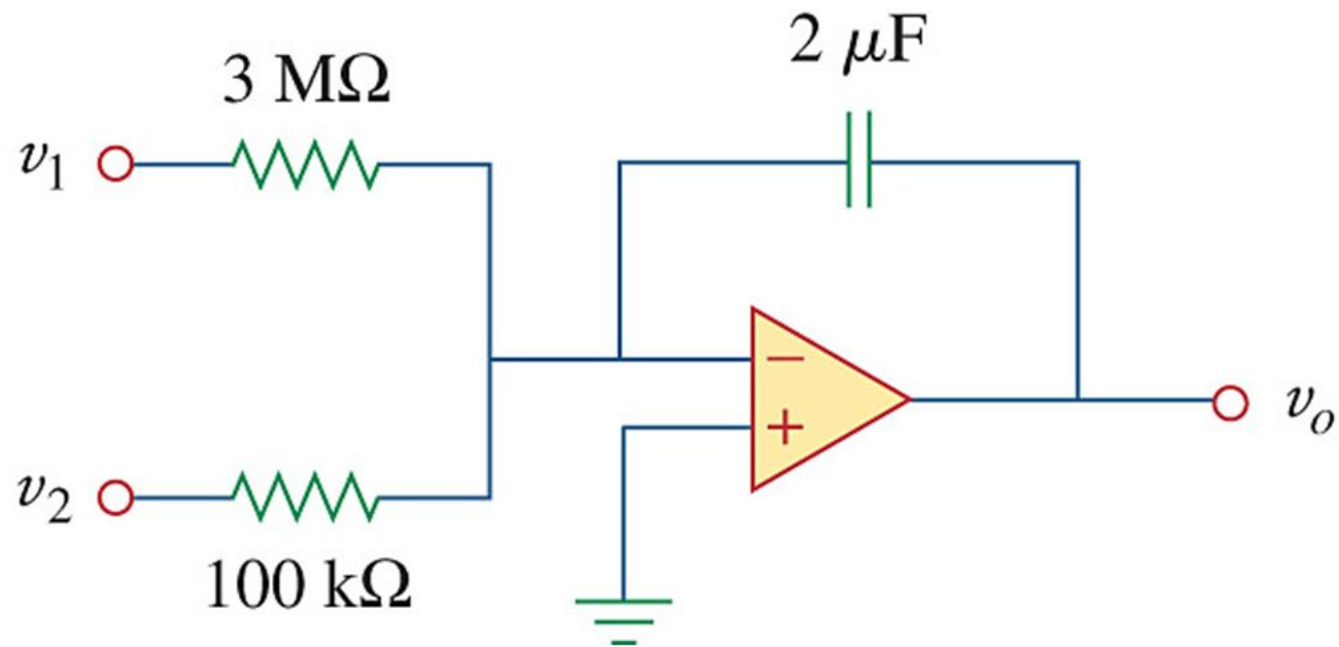
$$i_R = i_C$$

$$\frac{v_i}{R} = -C \frac{dv_o}{dt}$$

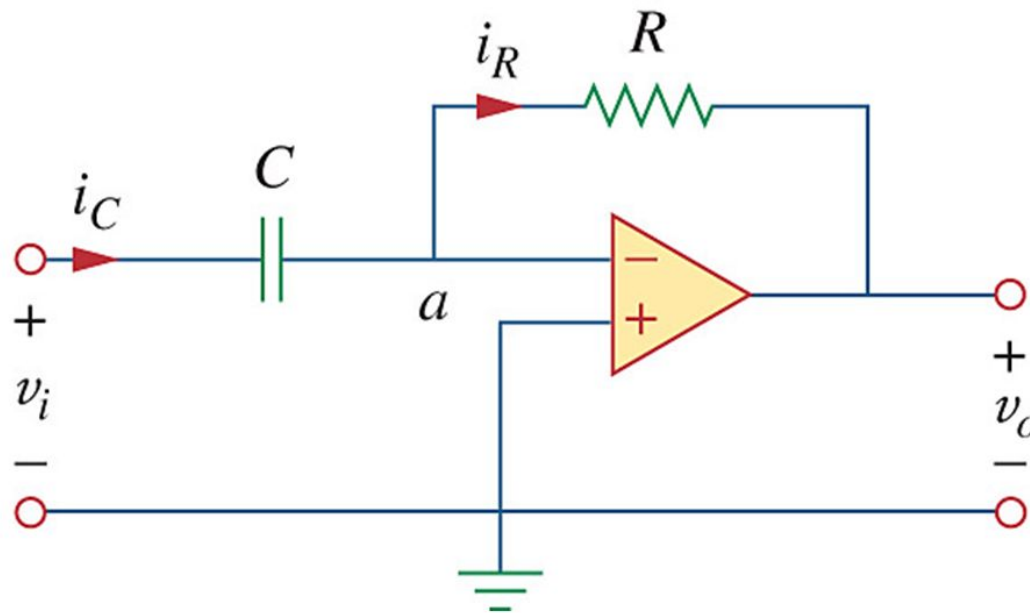
$$v_o = -\frac{1}{RC} \int_0^t v_i(t) dt$$

Example 6.13

- $v_1 = 10\cos 2t$ mV, $v_2 = 0.5t$ mV



6.6.2 Differentiator (미분기)

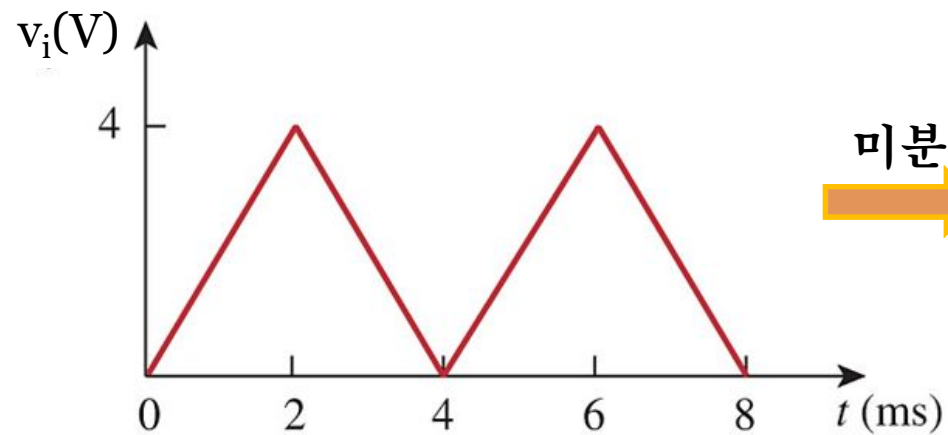
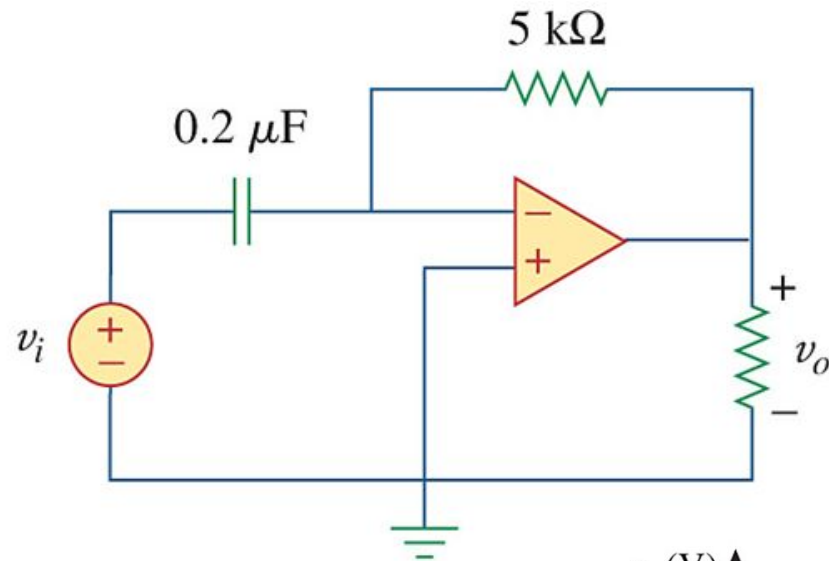


$$i_R = i_C$$

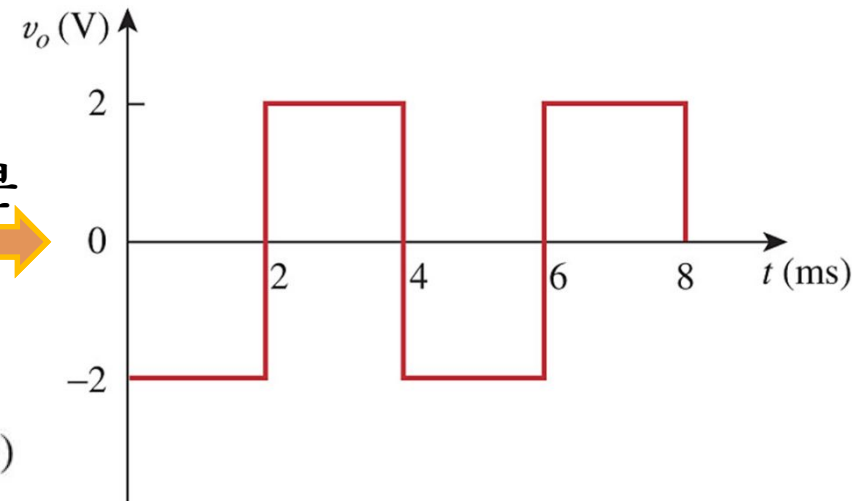
$$-\frac{v_o}{R} = C \frac{dv_i}{dt}$$

$$v_o = -\frac{1}{RC} \frac{dv_i}{dt}$$

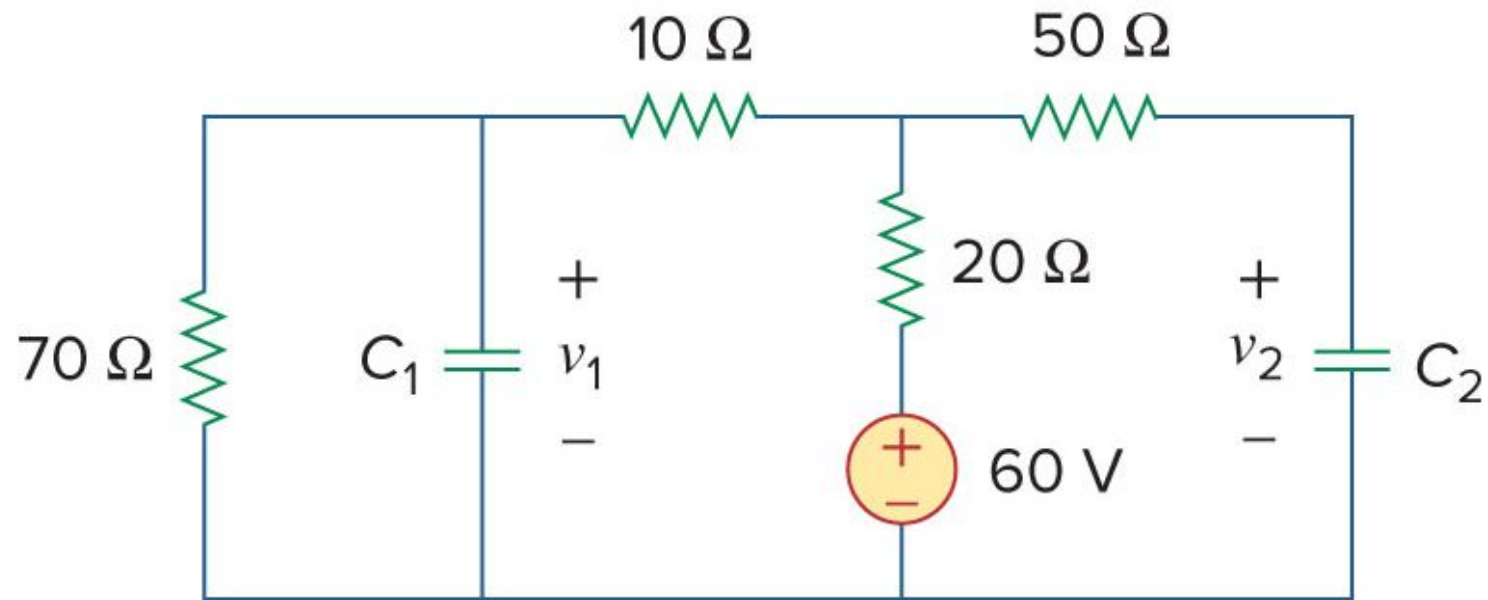
Example 6.14



미분
→

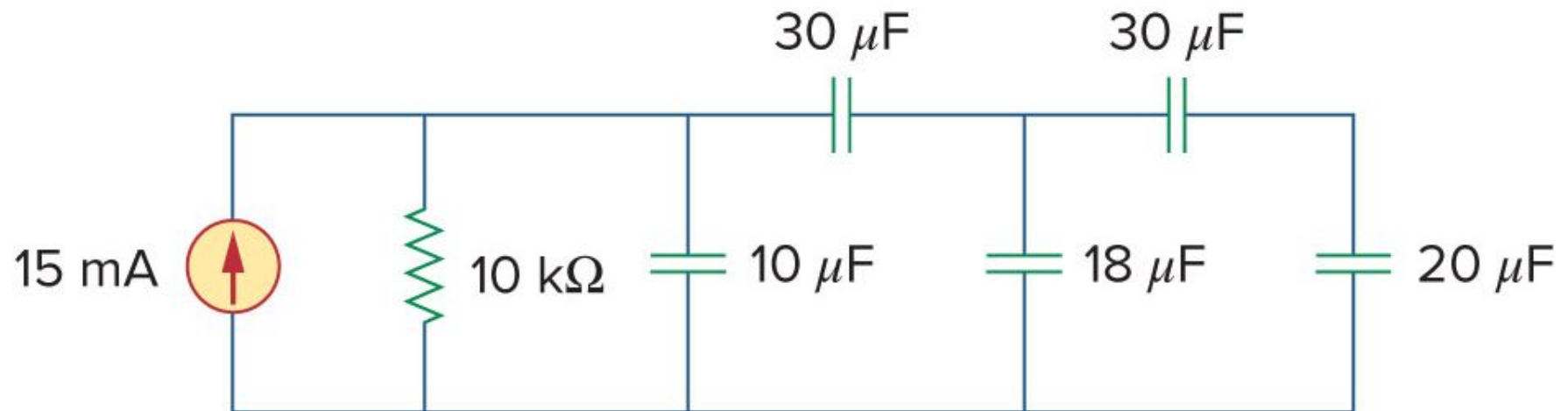


Problem 6.13



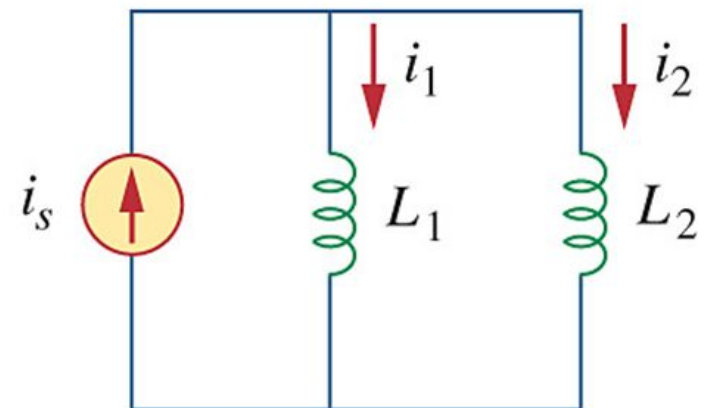
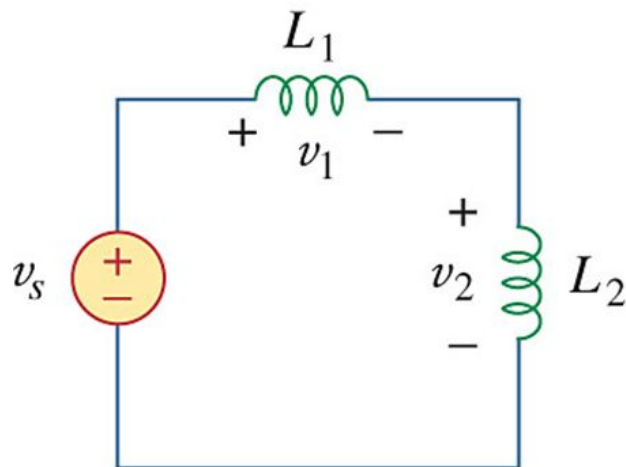
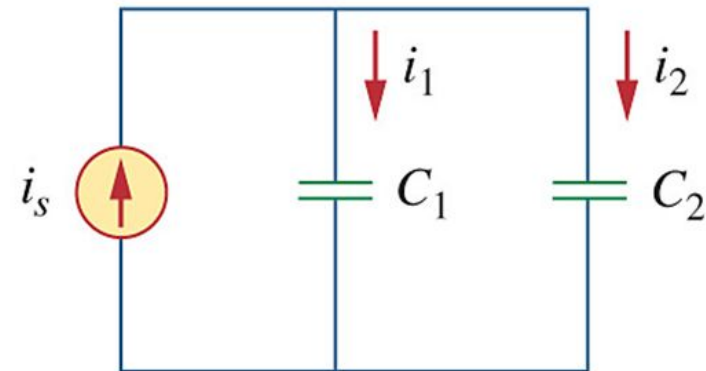
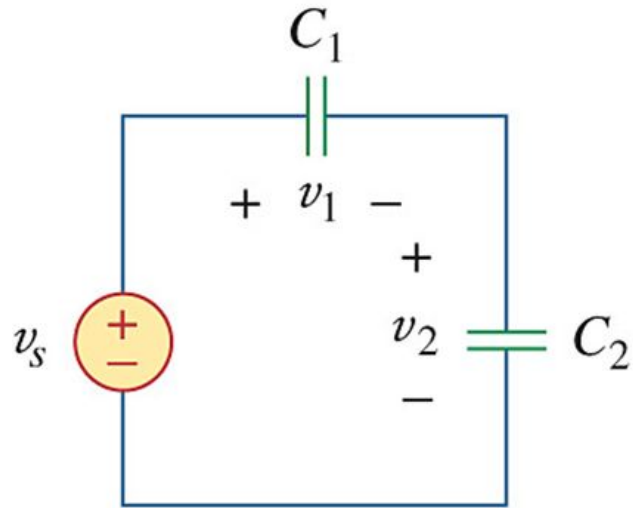
Problem 6.24

- 각 capacitor에 걸리는 전압은?

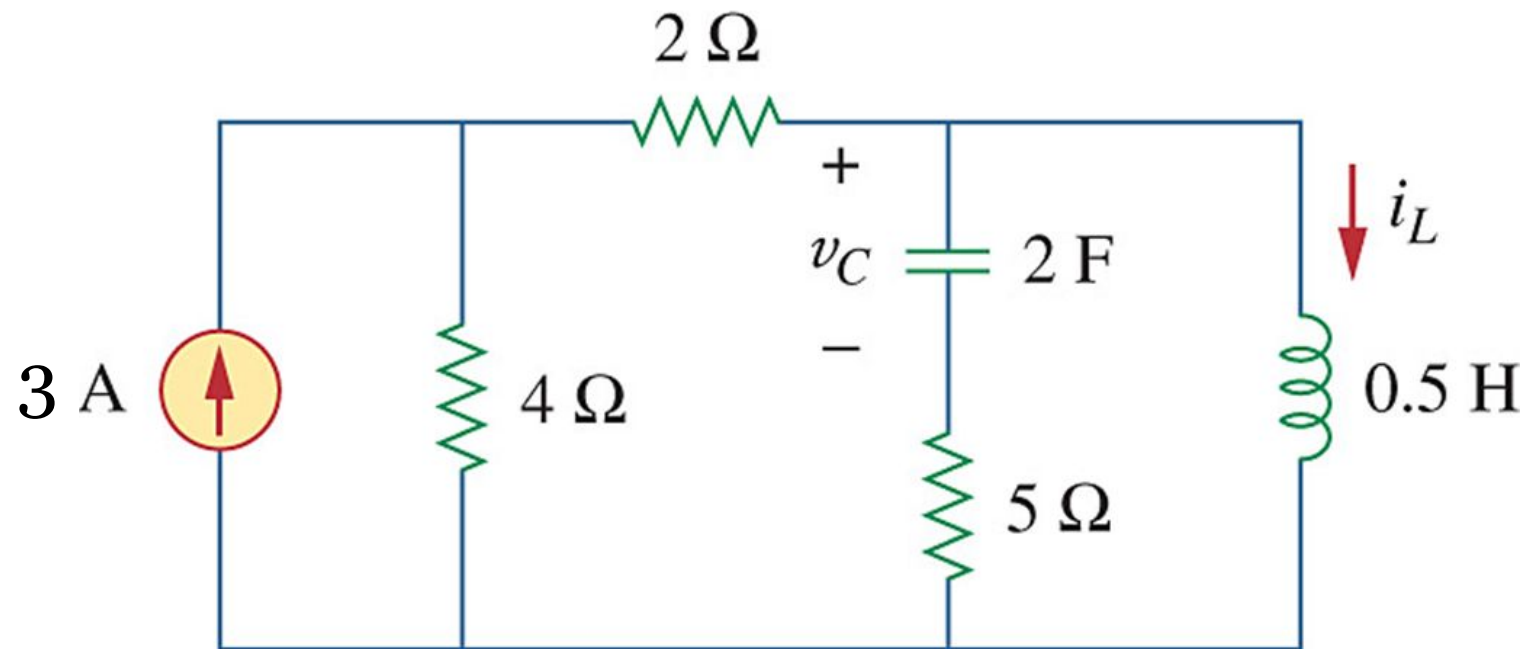


Problem 6.25 & 6.59

○ 전압분배 & 전류분배



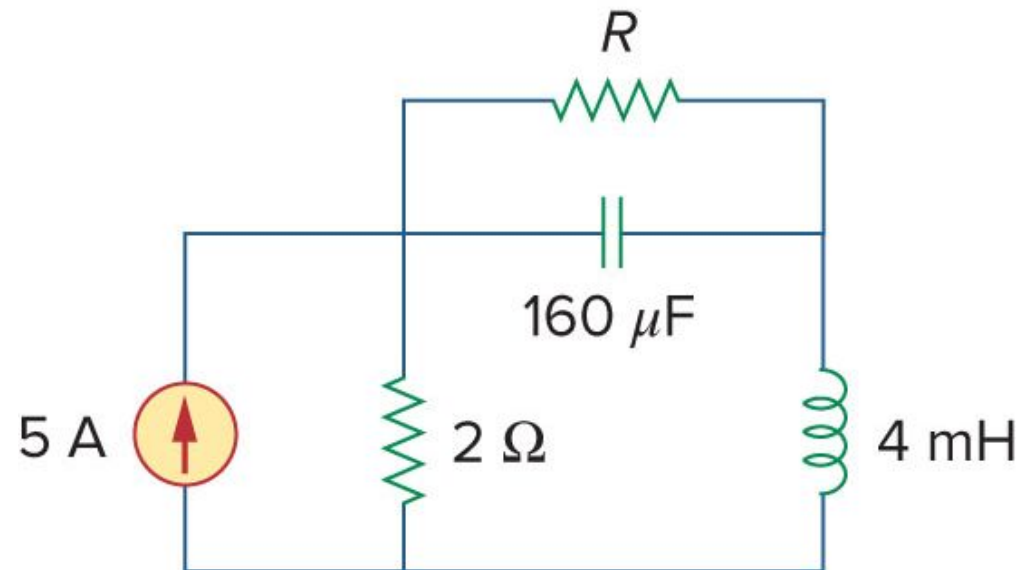
Problem 6.46



Homework #8

#1. Problem 6.47

커패시터에 저장된 에너지와 인덕터에 저장된 에너지가 같도록 R 값을 구하라.

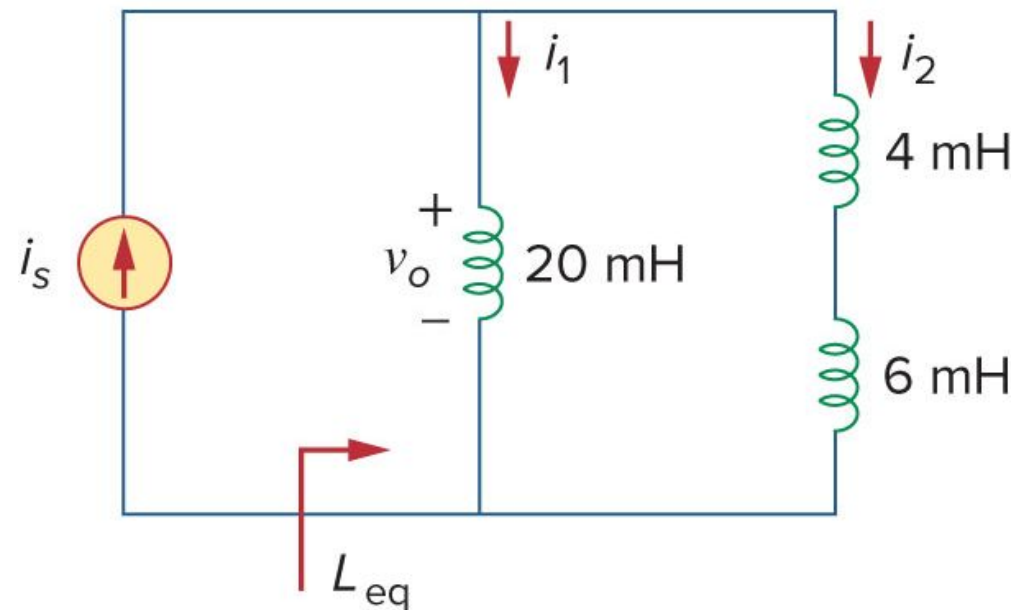


Homework #8

#2. Problem 6.61

(a) $i_s = 3e^{-t} \text{ mA}$ 일 때, L_{eq} , $i_1(t)$, $i_2(t)$, $v_o(t)$

(b) $t = 1$ 일 때, 인덕터에 저장된 에너지를 구하라.

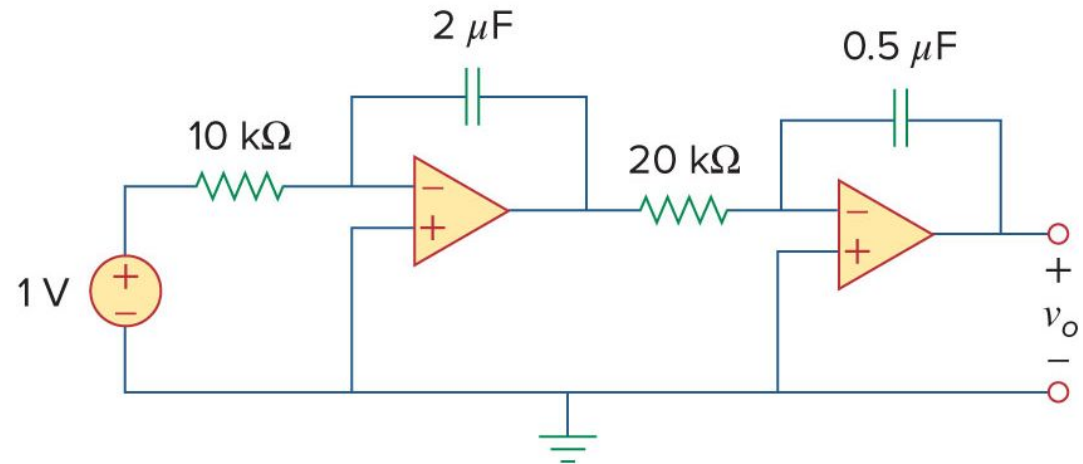


Homework #8

#3. Problem 6.72

아래의 중첩 적분기에 서 $t = 1.5ms$ 일 때 v_o 를 구하라.

($t = 0$ 에서 0 V로 초기화 되었다고 가정한다.)



Homework #8

#4. Problem 6.73

다음 회로가 비반전 적분기라는 것을 보여라.

