

전기회로 (가, 나)

Chapter 2 : Basic Laws

2017. 1학기

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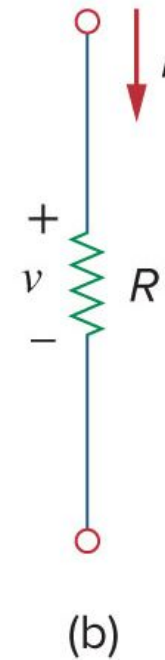
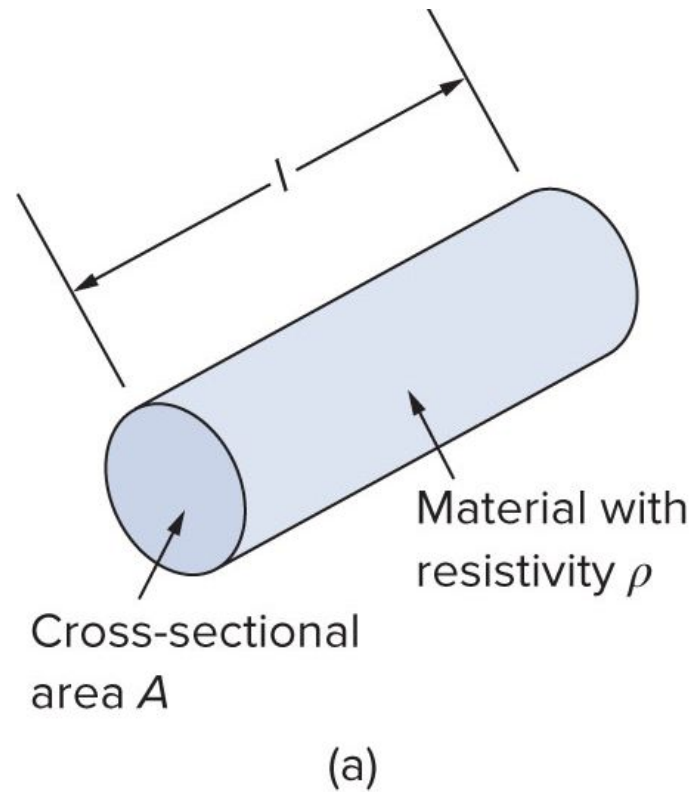
Learning Goals

- Ohm's law
- 회로 구성 요소
- Kirchhoff's law
- 직렬연결 & 병렬연결
- 와이-델타 변환
- 응용

2.2 저항 (Resistance)

전류의 흐름을 방해하는 회로 요소를 저항 (Resistor)이라 하고,
기호 R 로 표시한다.

$$R = \rho \frac{l}{A}$$



2.2 Resistivity (고유저항)

Material	Resistivity ($\Omega \cdot m$)	Usage
Silver	1.64×10^{-8}	Conductor
Copper	1.72×10^{-8}	Conductor
Aluminum	2.80×10^{-8}	Conductor
Gold	2.45×10^{-8}	Conductor
Carbon	4.00×10^{-5}	Semiconductor
Germanium	47.00×10^{-2}	Semiconductor
Silicon	6.40×10^2	Semiconductor
Paper	1.00×10^{10}	Insulator
Mica	5.00×10^{11}	Insulator
Glass	1.00×10^{12}	Insulator
Teflon	3.00×10^{12}	Insulator

반도체

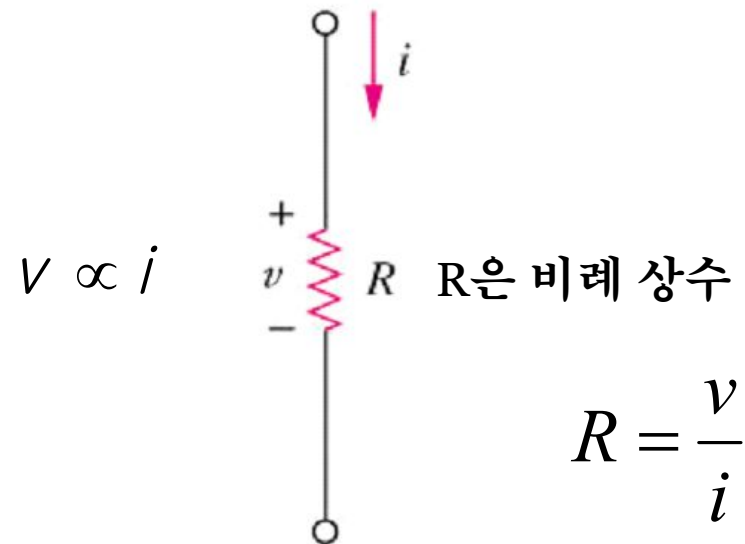
2.2 Ohm's Law

- Ohm's law (옴의 법칙)

$$v = iR$$

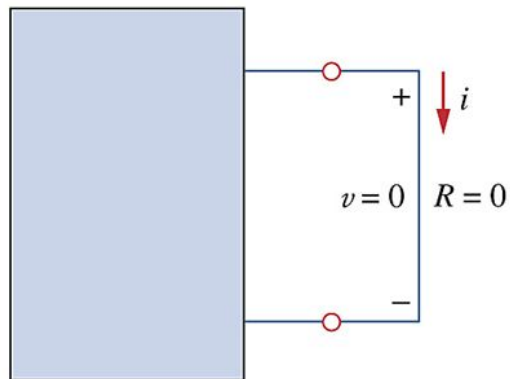
- 저항(resistor, R) : 전류의 흐름을 방해하는 소자

- 단위 : Ω (옴) = V/A



2.2 Extreme Cases

- short circuit (단락(短絡)) : $R = 0$



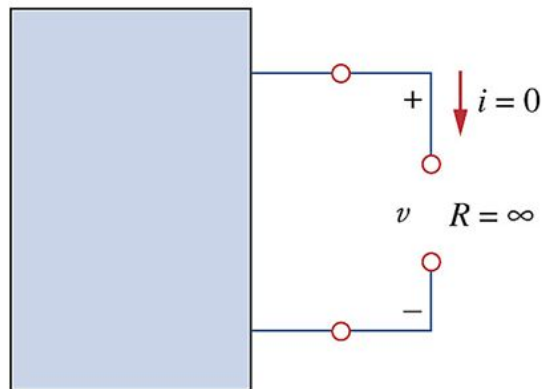
$i (= v/R = 0/0)$ 의 값은?

→ 다른 곳에서 결정

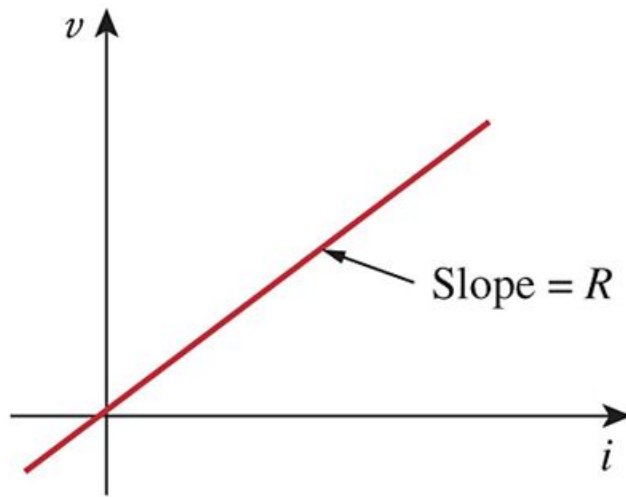
만약 $v \neq 0$ 이고 $R = 0$ 이면???

→ 합선

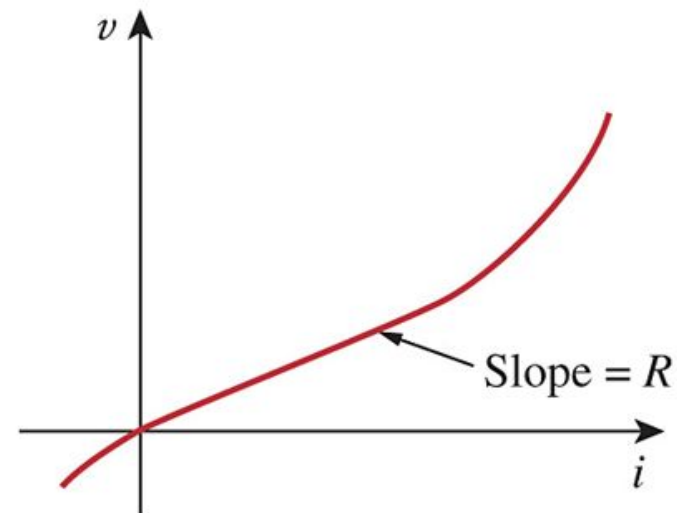
- open circuit (개방(開放)) : $R = \infty$



2.2 Ohm's Law (revisited)



[선형저항 (linear resistor)]



[비선형저항 (nonlinear resistor)]

2.2 Conductance

$$G = \frac{1}{R} = \frac{i}{v} \quad \text{단위 : } \Omega \text{ (mho 모) 또는 S (siemens 지멘스)}$$

$$i = Gv$$

2.2 Power (revisited)

- 저항에 의하여 사용된 전력 (power)

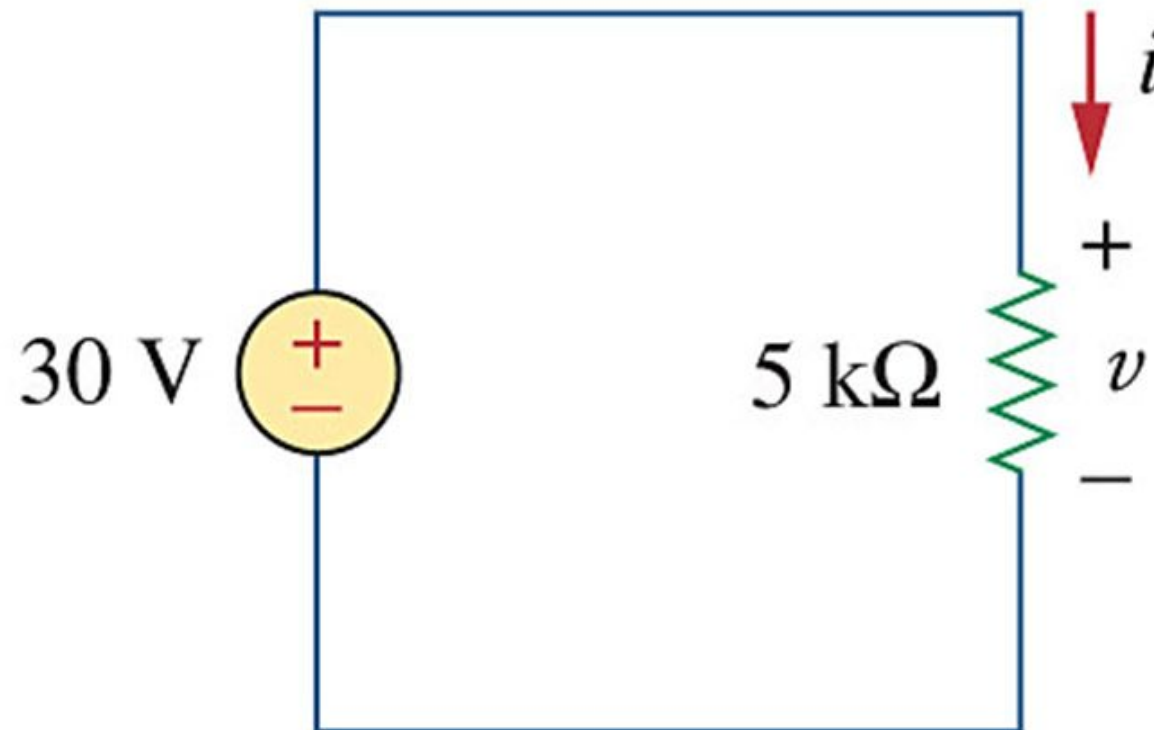
$$p = vi = i^2 R = \frac{v^2}{R}$$

$$p = vi = v^2 G = \frac{i^2}{G}$$

Quiz] power는 전류나 전압에 대하여 선형적인가?

2.2 Example 2.2

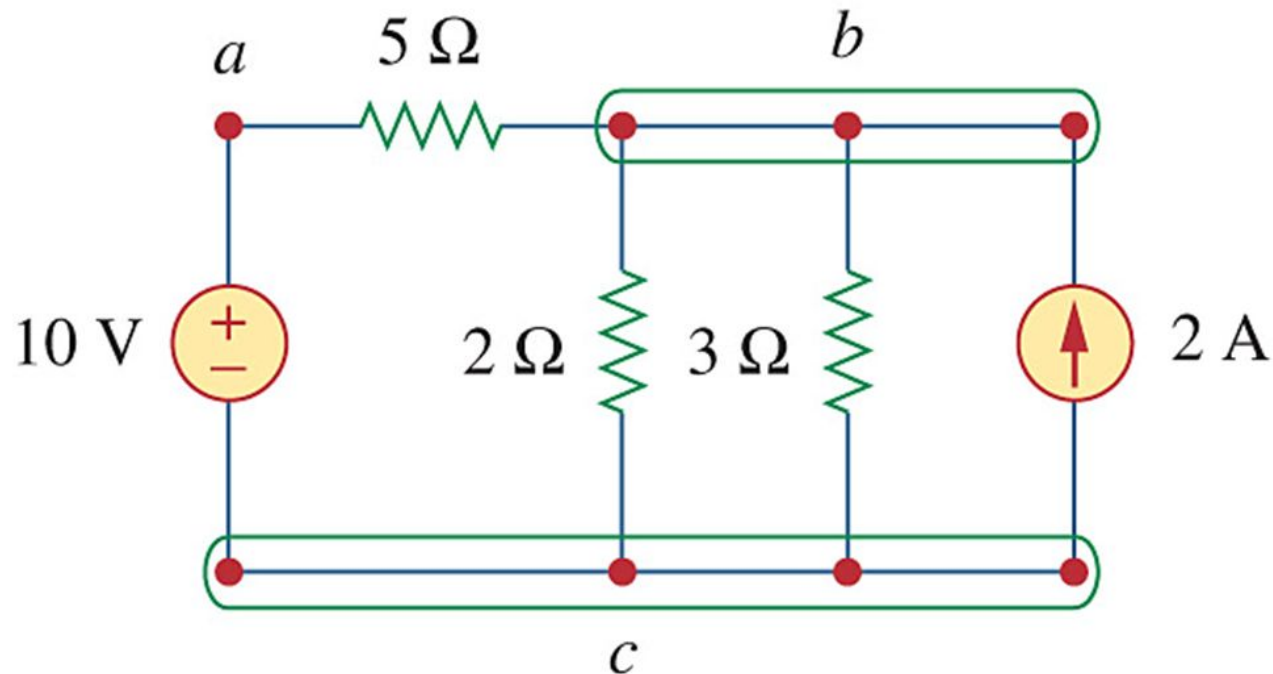
- 다음 회로에서 전류 i , 컨덕턴스 G , 전력 p 를 구하라



2.3 Topology

회로를 구성하는 요소

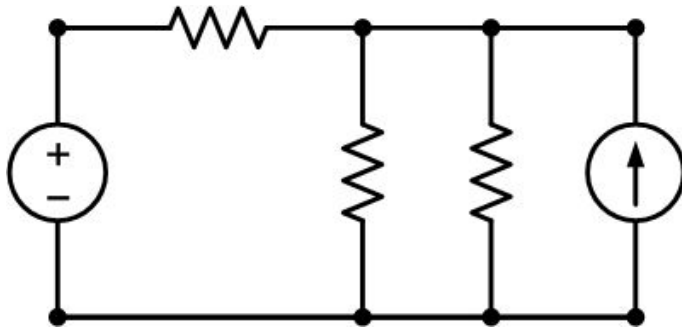
- branch : 회로에 연결된 각각의 소자
- node : branch의 연결점
- loop : 회로내의 폐 경로



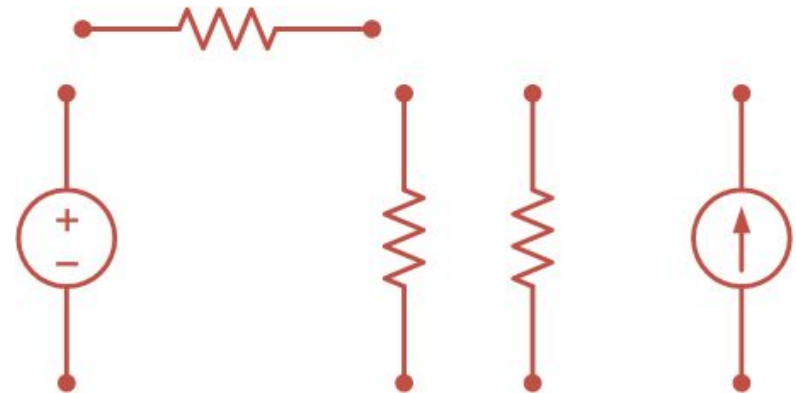
2.3 Branch

- 전압원/전류원, 저항 등의 회로를 구성하는 요소 (element)

Original Circuit



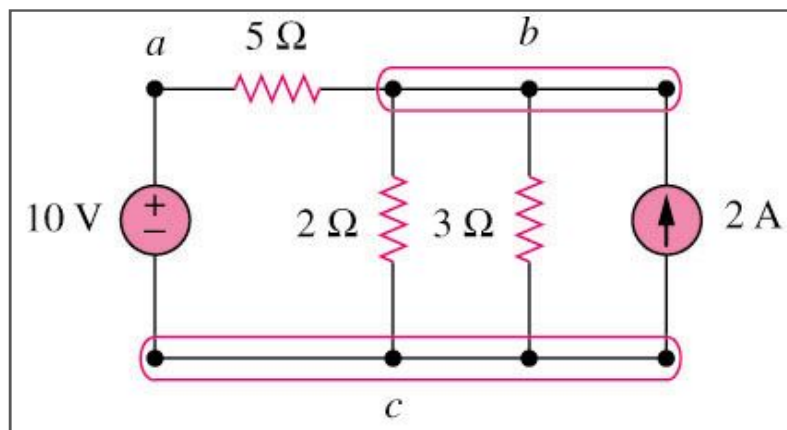
Branches



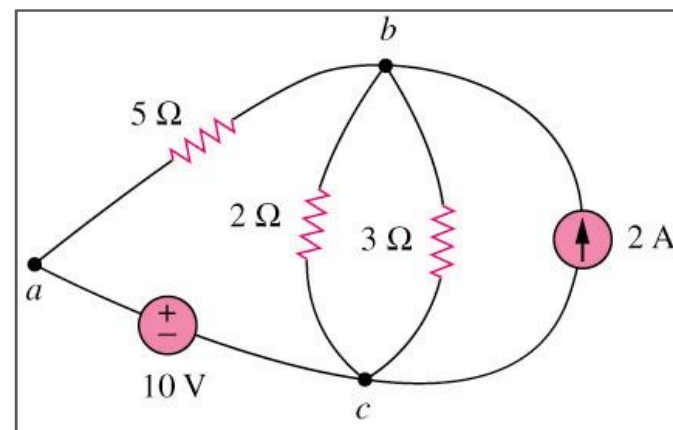
2.3 Node

- 2개 이상의 branch의 연결점

Original Circuit

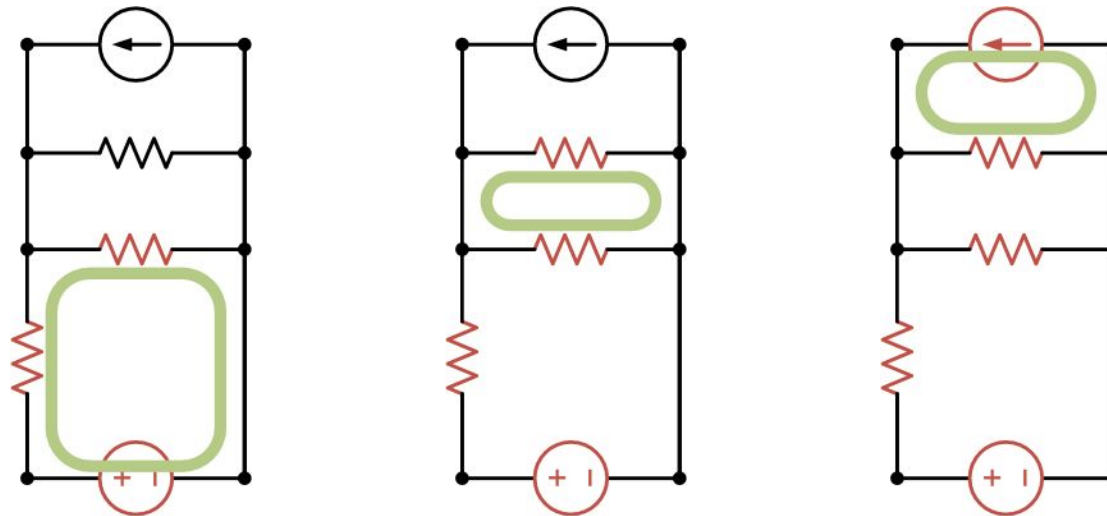


Equivalent Circuit



2.3 Loop

- 회로내의 폐 경로 (closed loop)
- 독립 loop
 - 다른 독립 loop의 일부가 아닌 branch를 가지고 있는 loop



node(n), branch(b), loop(l)의 상관 관계

$$b = l + n - 1$$

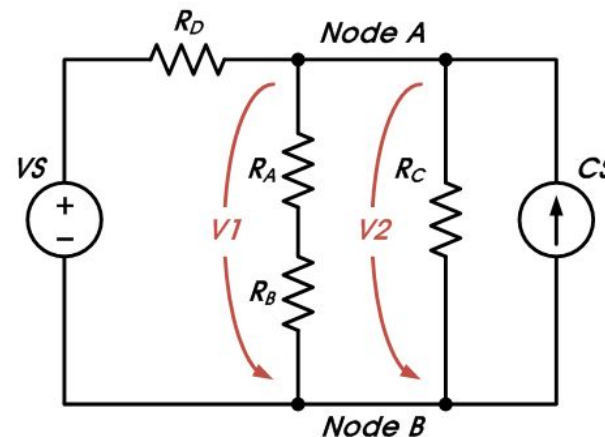
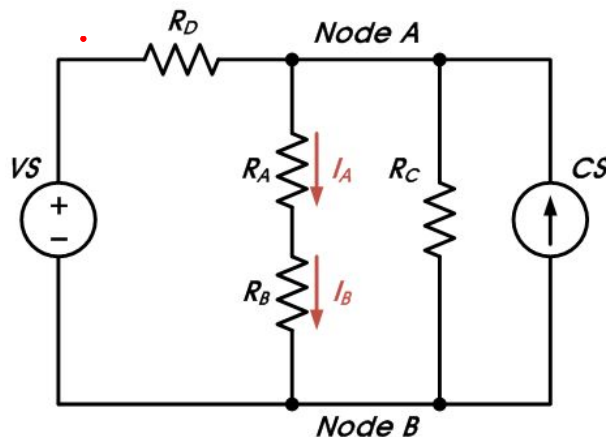
2.3 Series & Parallel

● Series (직렬연결)

- 2개의 요소가 하나의 node를 공유
- 각 요소에 흐르는 전류는 동일

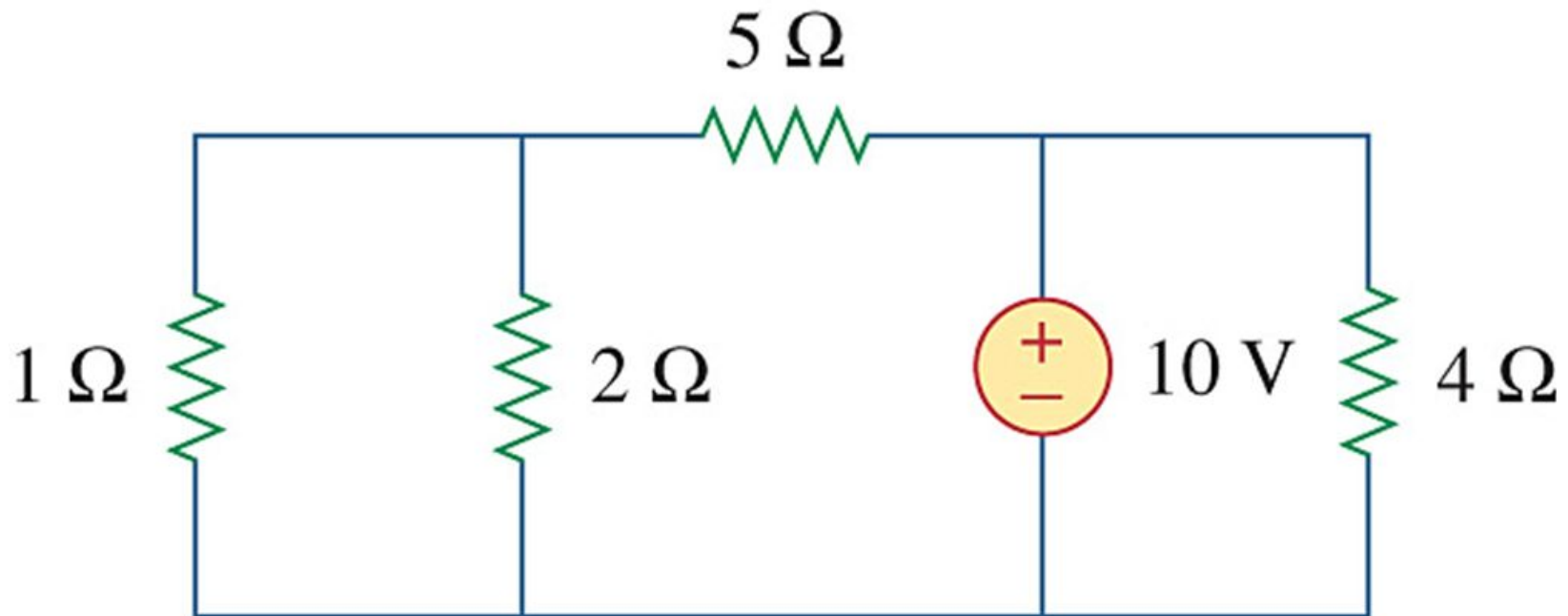
● Parallel (병렬연결)

- 2개 이상의 요소가 같은 2개의 node사이에 연결
- 2개의 node사이의 전압은 동일



Practice (실전문제) 2.4

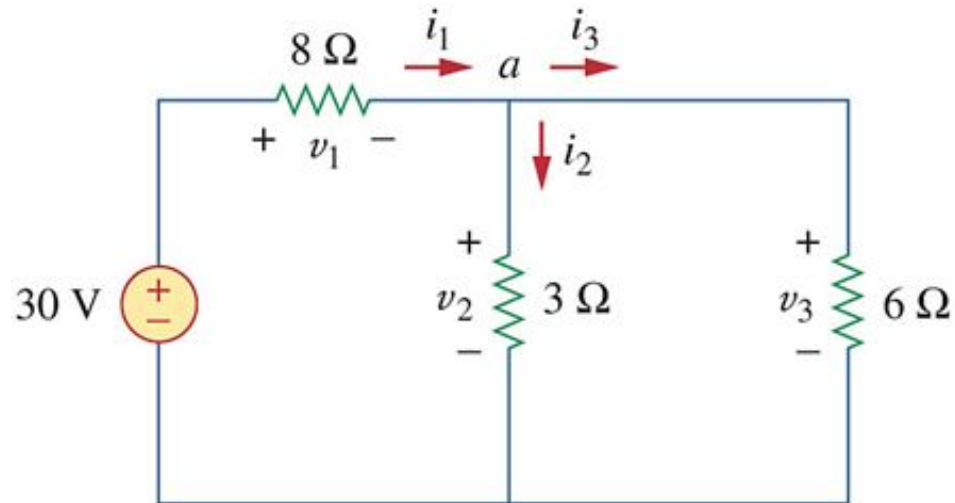
- 다음 회로에선 몇 개의 branch와 node가 있는가?
- 직렬 및 병렬인 회로 요소를 구별하여 나타내라.



2.4 Kirchhoff's Law (키르히호프의 법칙)

회로 해석

- 각 node의 전압 결정
- 각 branch의 전류 결정



회로 해석 방법

- Ohm's law ($v = iR$)
- Kirchhoff's law
 - KCL (Kirchhoff's current law)
 - KVL (Kirchhoff's voltage law)

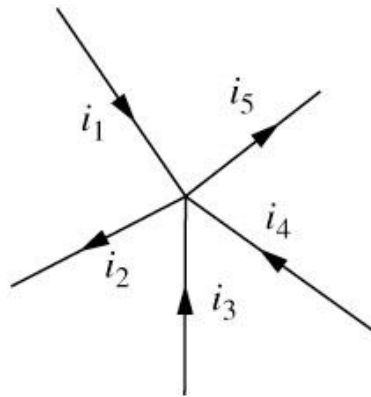
2.4 KCL

● Kirchhoff's current law (KCL)

- 하나의 node를 통과하는 전류의 대수적 합은 “0” ← “전하 보존의 법칙”

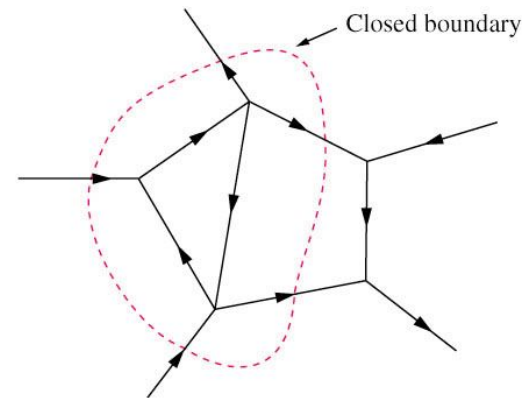
$$\sum_{n=1}^N i_n = 0$$

- 하나의 node 기준 : 들어가는 전류의 합 = 나가는 전류의 합



$$i_1 + (-i_2) + i_3 + i_4 + (-i_5) = 0$$

$$i_1 + i_3 + i_4 = i_2 + i_5$$

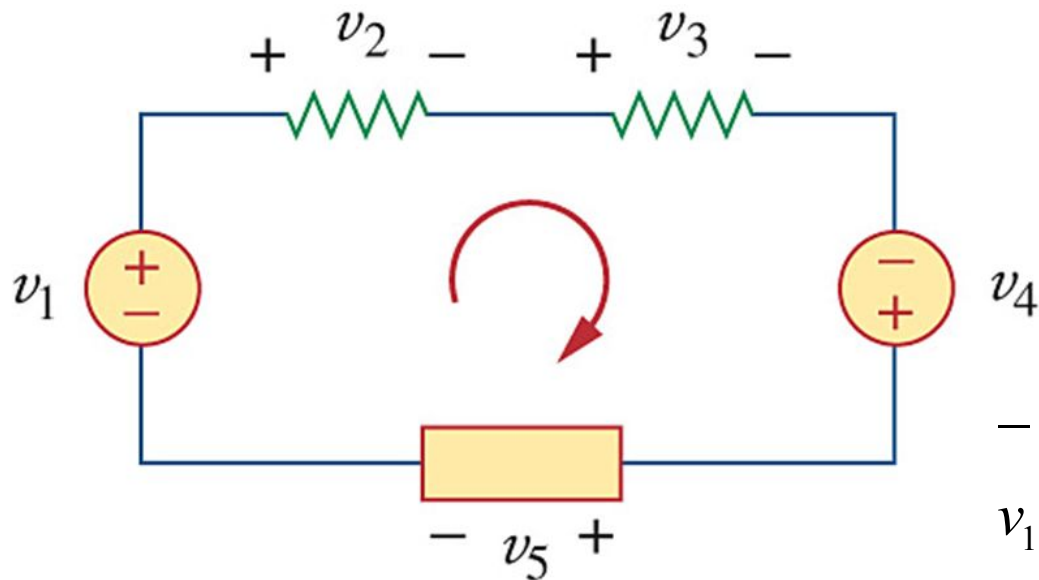


2.4 KVL

- Kirchhoff's voltage law (KVL)

- 폐 경로에서 전압의 대수적 합은 “0”

$$\sum_{m=1}^M v_m = 0 \quad \leftarrow \text{“에너지 보존의 법칙”}$$

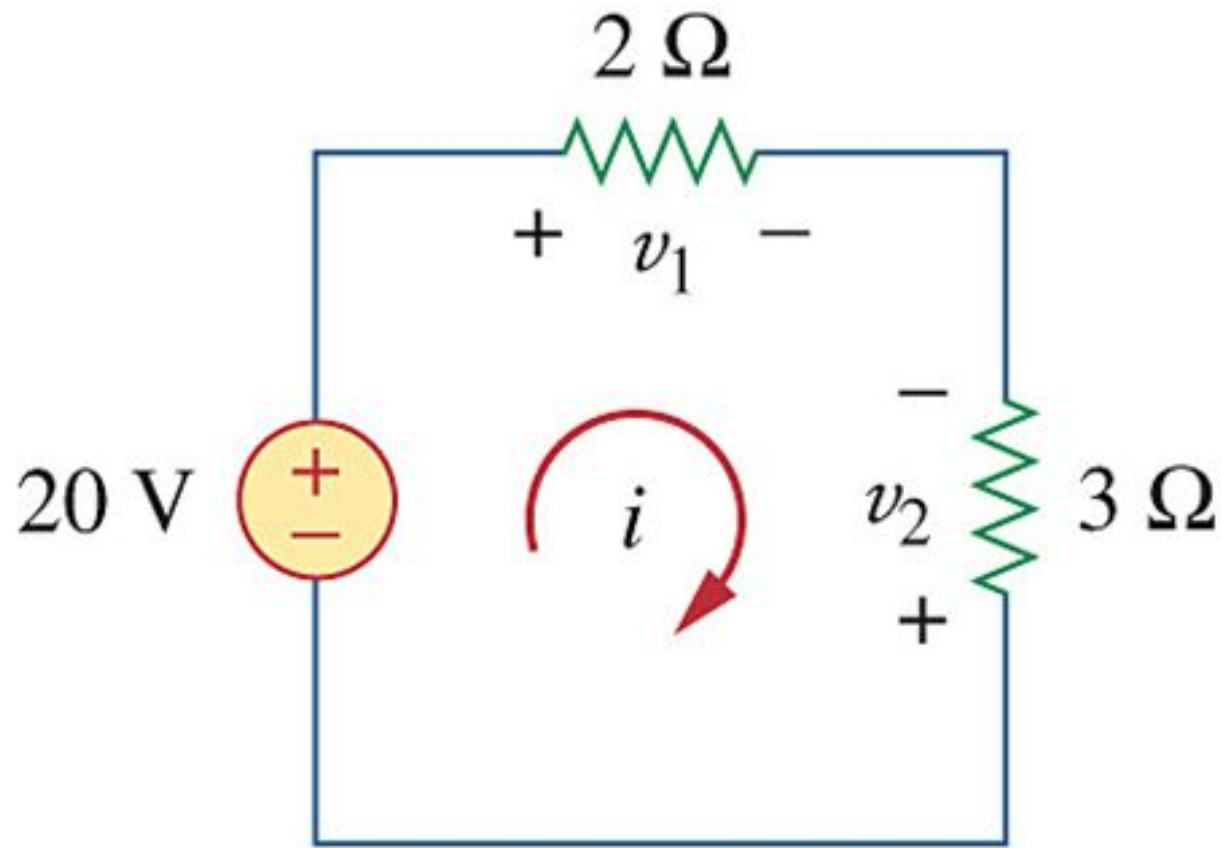


$$-v_1 + v_2 + v_3 - v_4 + v_5 = 0$$

$$v_1 + v_4 = v_2 + v_3 + v_5$$

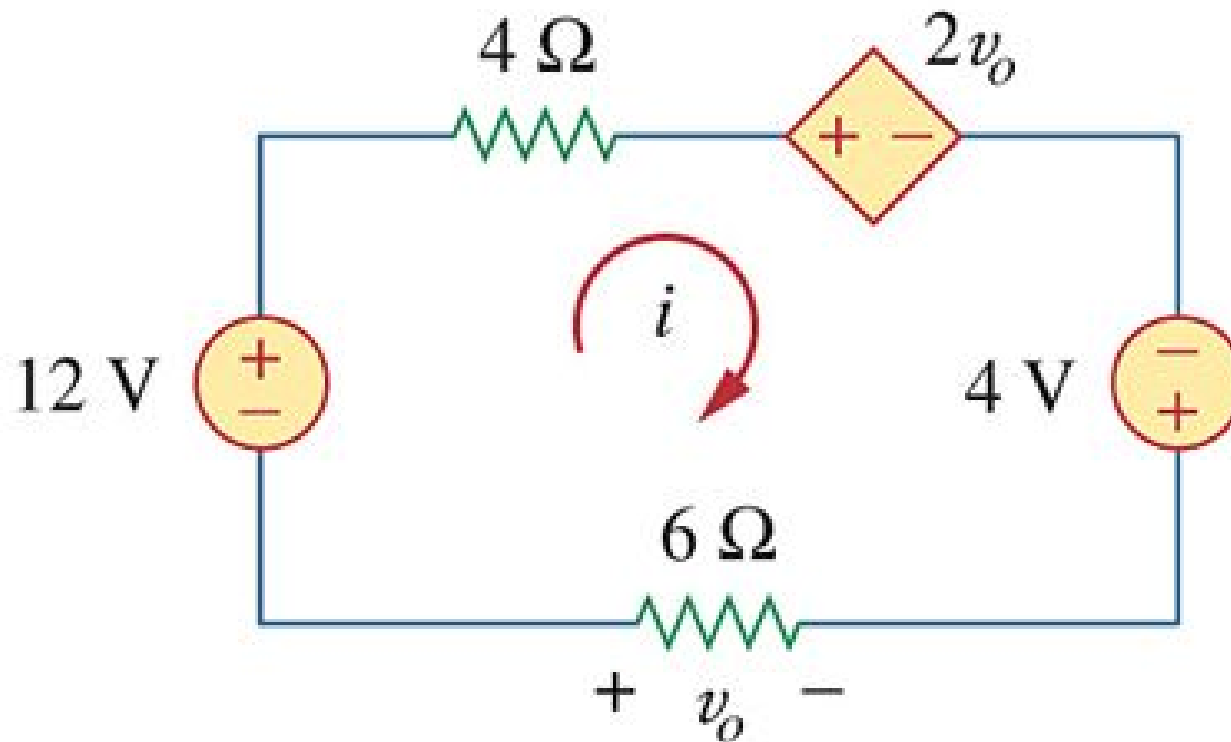
Example 2.5

- 다음 회로에서 전압 v_1 과 v_2 를 구하라.



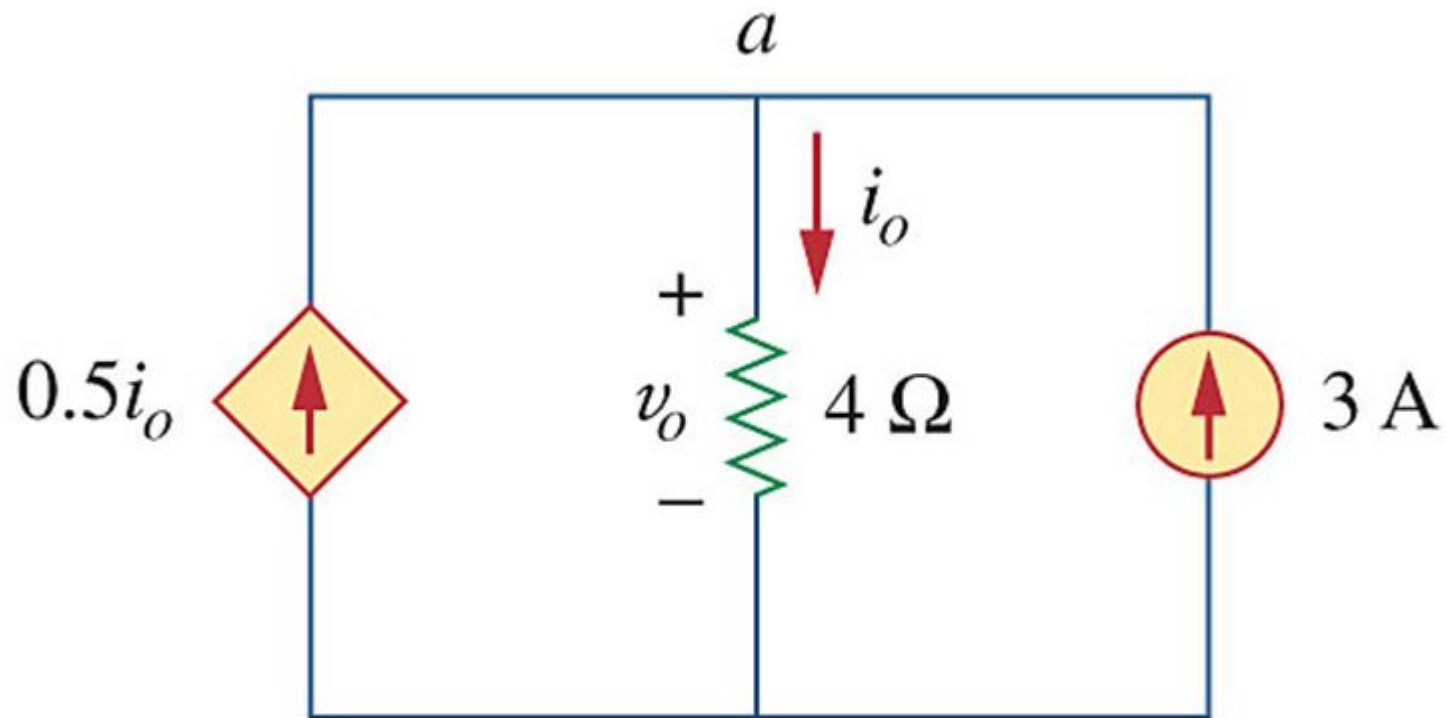
Example 2.6

- 다음 회로에서 v_o 와 i 를 구하라.



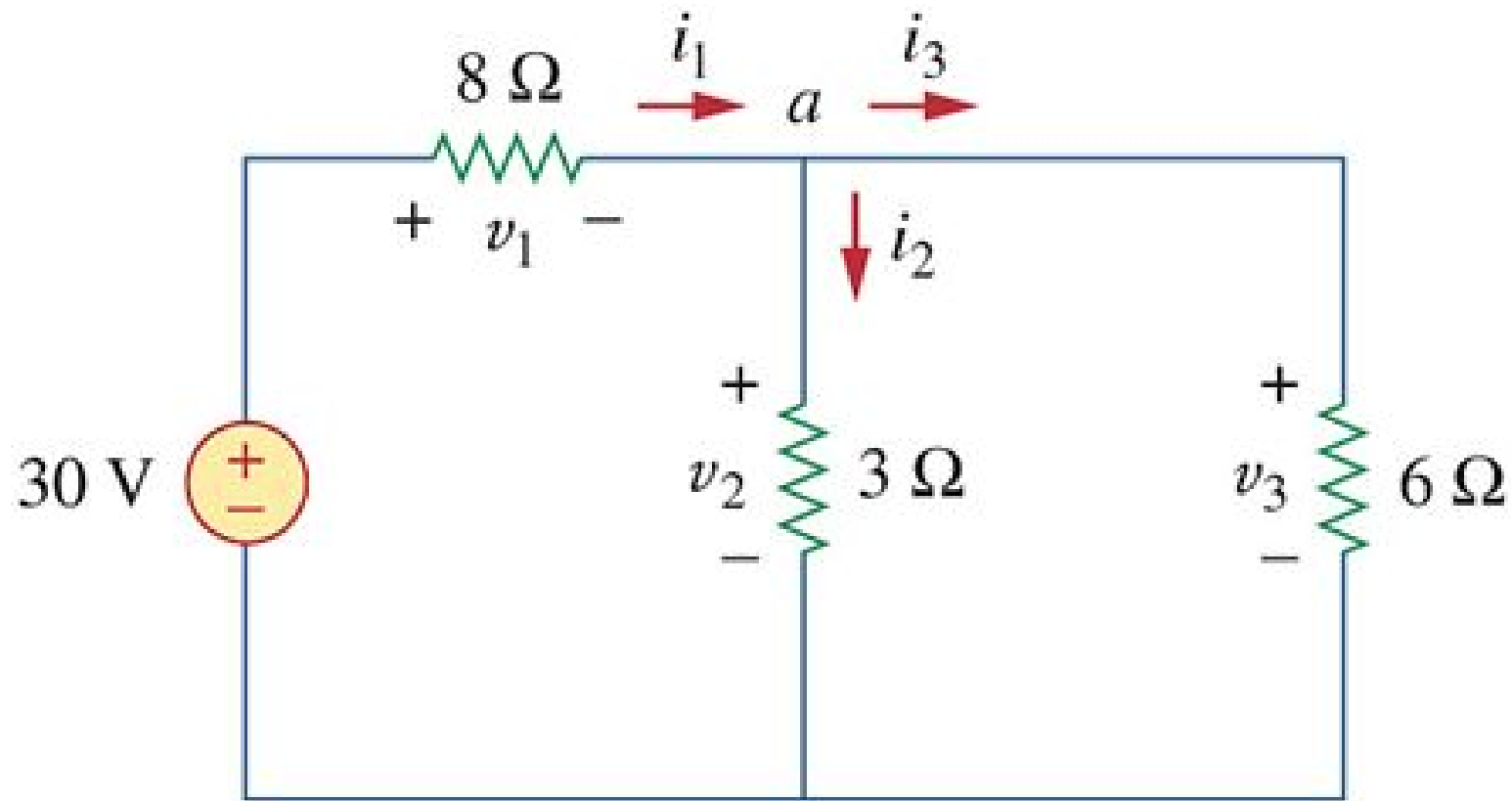
Example 2.7

- 다음 회로에서 전류 i_o 와 전압 v_o 를 구하라.



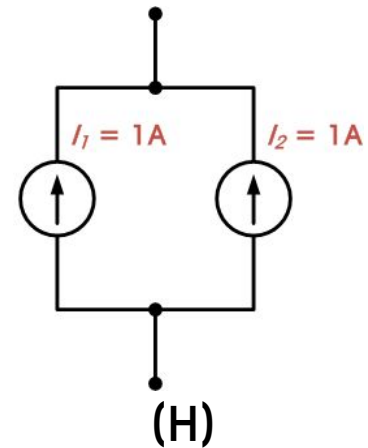
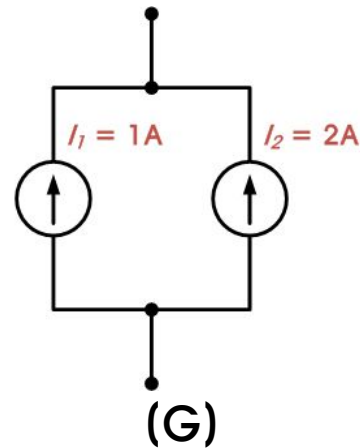
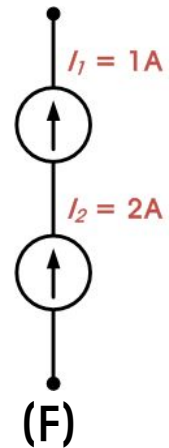
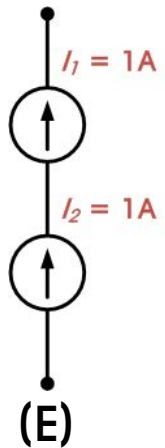
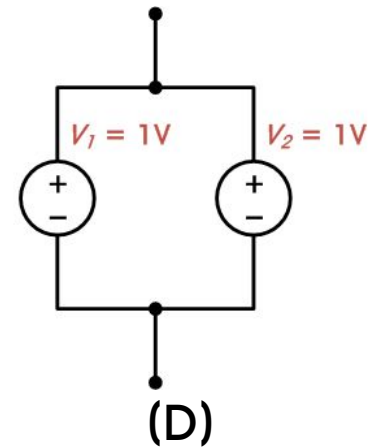
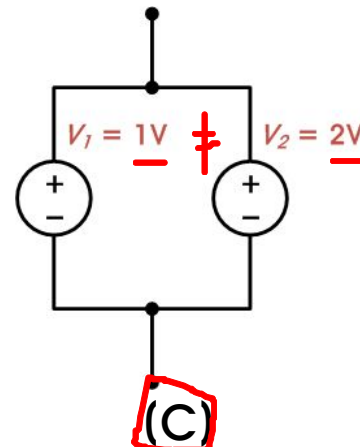
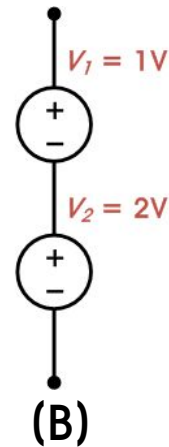
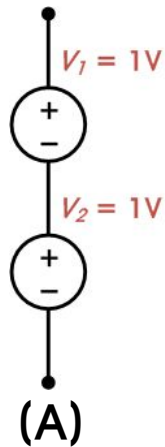
Example 2.8

- 다음 회로에서 전류와 전압을 구하라.



2.4 Kirchhoff's Law

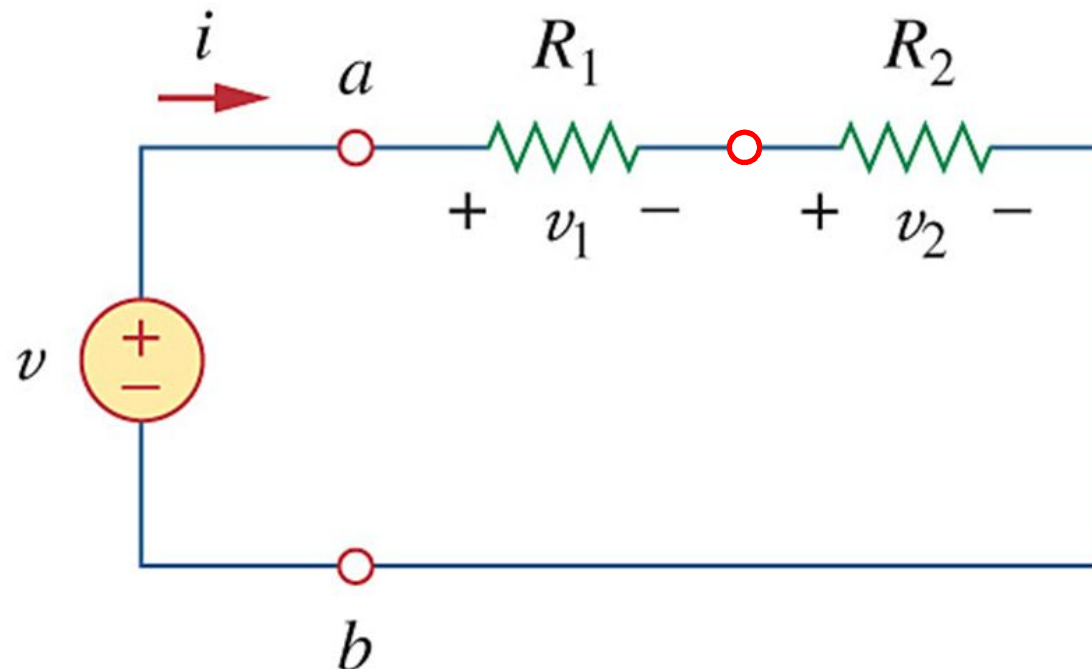
◦ 다음 중 키르히호프 법칙에 위배되는 것은?



2.5 직렬 저항

● Series (직렬)

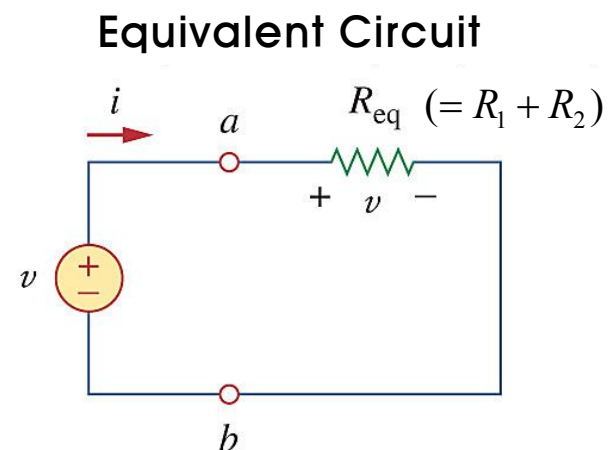
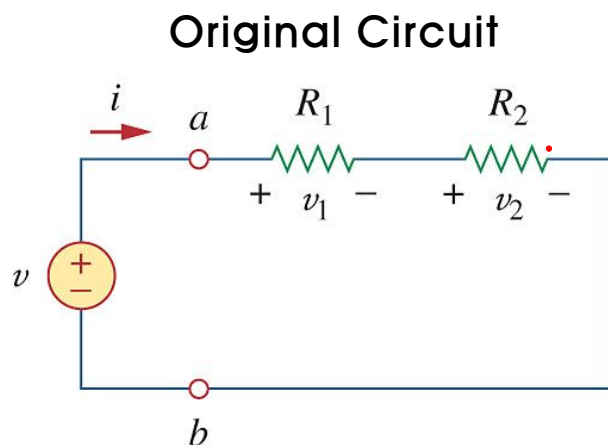
- 2개 이상의 element가 순차적으로 연결
- 2개의 element는 하나의 node를 공유
- 동일한 전류가 흐름.



2.5 직렬에서의 등가 저항

- 직렬 연결된 저항의 등가저항은 **각 저항의 합**

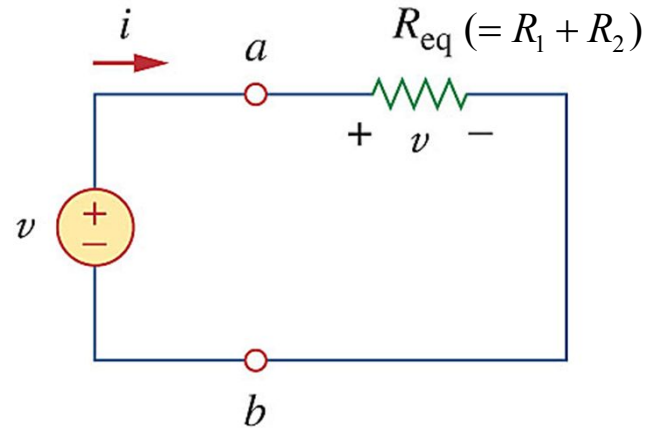
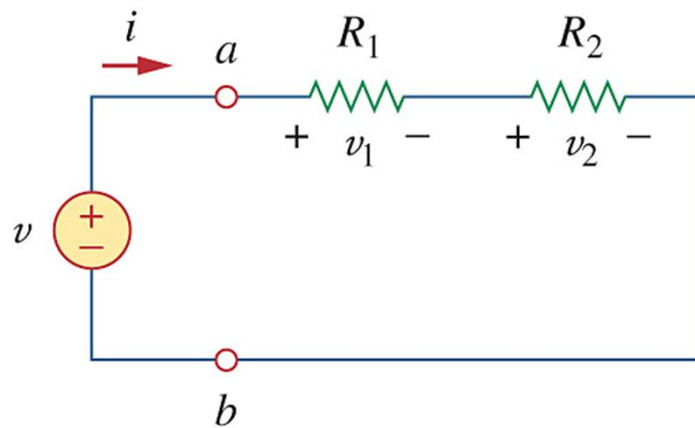
$$R_{eq} = R_1 + R_2 + \cdots + R_N = \sum_{n=1}^N R_n$$



2.5 직렬에서의 전압분배

○ 전압분배기 (Voltage divider)

- 직렬 연결된 저항에서의 voltage drop를 이용하여 원하는 전압을 생성



$$i = \frac{v}{R_1 + R_2}$$

$$v_1 = \frac{R_1}{R_1 + R_2} v, \quad v_2 = \frac{R_2}{R_1 + R_2} v$$

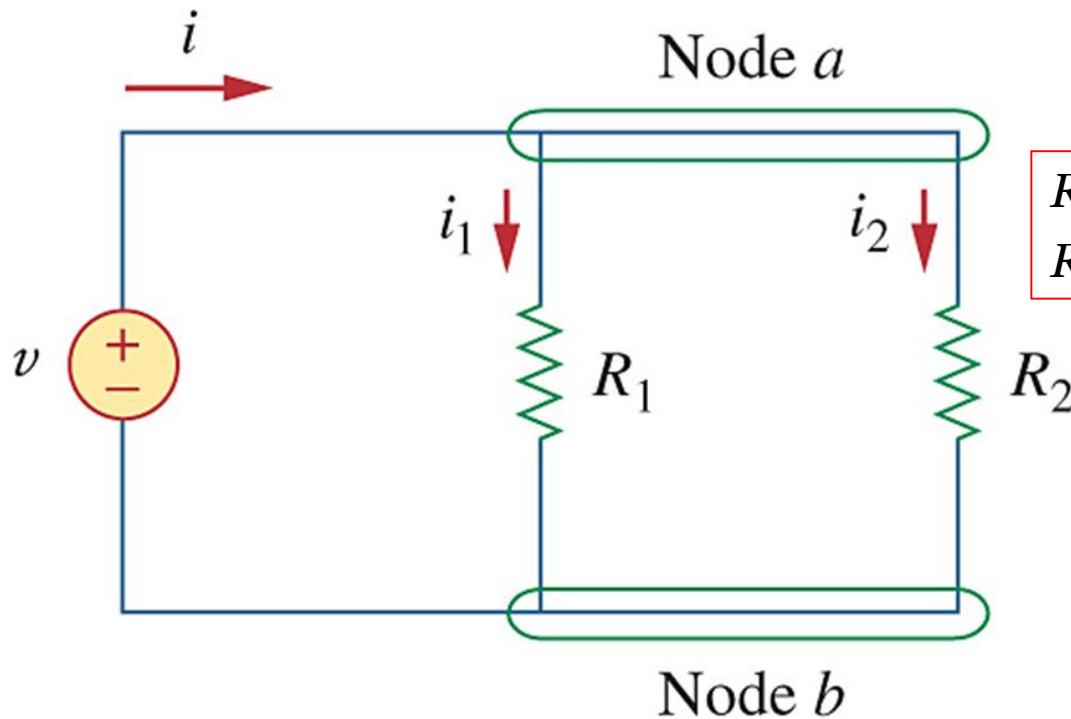
큰 저항에 전압이 더 많이 걸린다.!

$$v_n = \frac{R_n}{R_1 + R_2 + \cdots + R_N} v$$

2.6 병렬 저항

● Parallel (병렬)

- 2개 이상의 element가 같은 2개의 node 사이에 연결
- node사이에는 동일한 전압이 걸림.



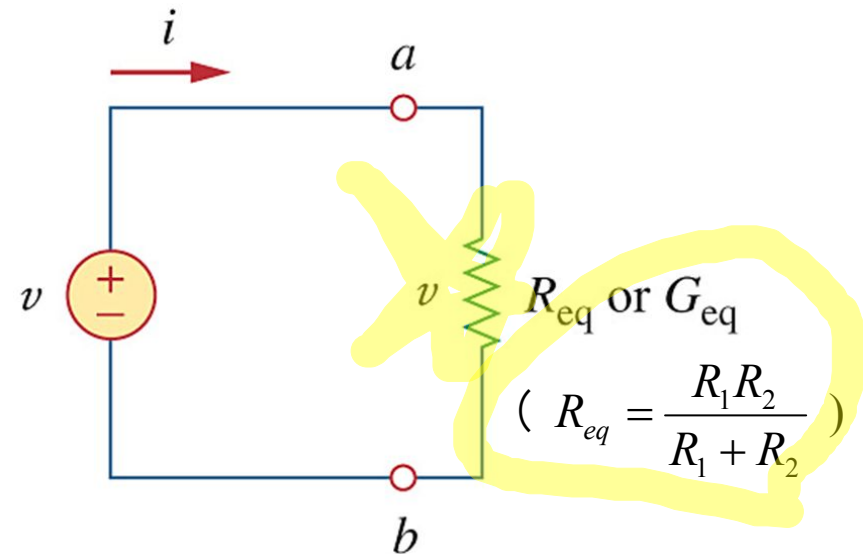
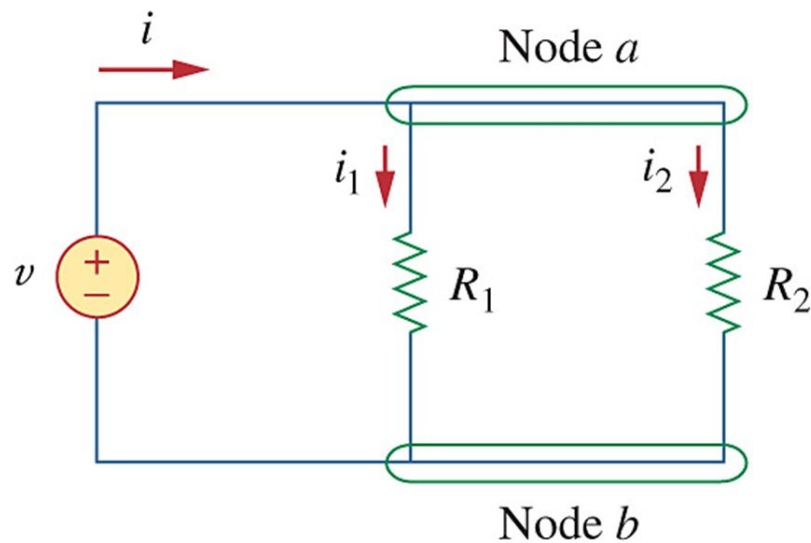
R_1 과 R_2 는 병렬로 연결됨
 R_1 과 R_2 에서는 동일한 전압 강하

2.5 병렬에서의 등가 저항

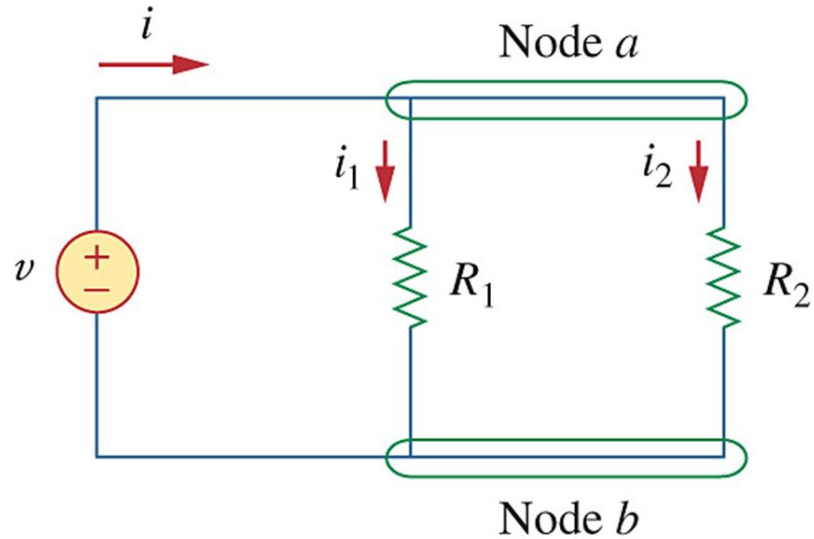
- 병렬 연결된 컨덕턴스의 등가는 **각 컨덕턴스의 합**

$$G_{eq} = G_1 + G_2 + \cdots + G_N = \sum_{n=1}^N G_n$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \cdots + \frac{1}{R_N} = \sum_{n=1}^N \frac{1}{R_n}$$



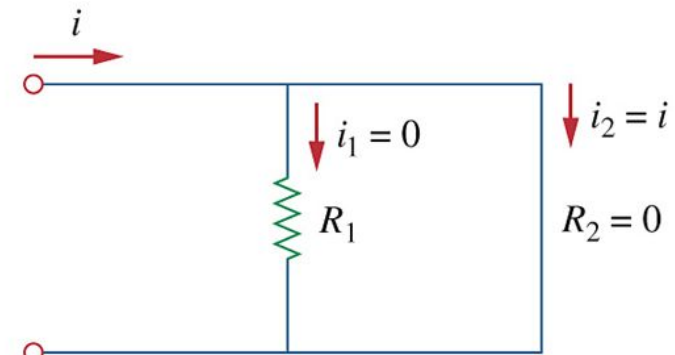
2.5 병렬에서의 전류분배



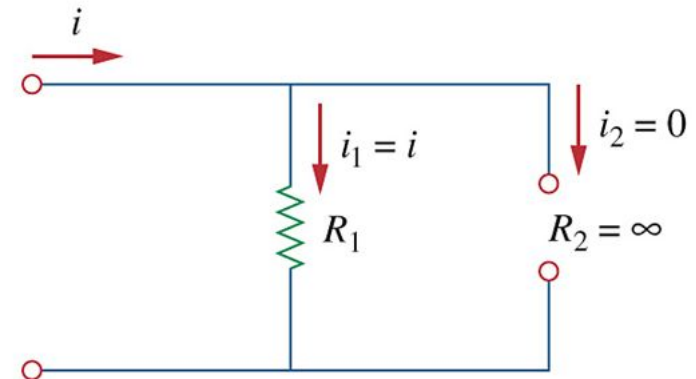
$$i_1 = \frac{R_2}{R_1 + R_2} i$$

$$i_2 = \frac{R_1}{R_1 + R_2} i$$

전류는 저항이 적은 곳으로 더 많이 흐른다.



[단락의 경우]



[개방의 경우]

2.5 직렬저항과 병렬저항

○ 직렬저항

$$R_{eq} = R_1 + R_2 + \cdots + R_N = \sum_{n=1}^N R_n \quad \leftarrow \text{가장 큰 저항보다 항상 크다.}$$

$$\text{if } R_1 = R_2 = \cdots R_N = R, \quad R_{eq} = NR$$

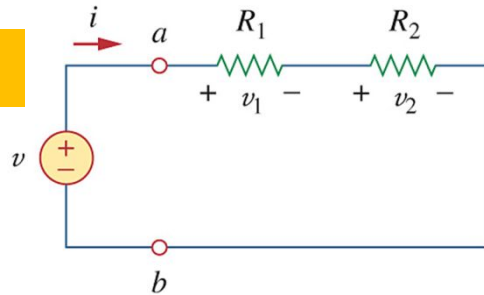
○ 병렬저항

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \cdots + \frac{1}{R_N} = \sum_{n=1}^N \frac{1}{R_n} \quad \leftarrow \text{가장 작은 저항보다 항상 작다.}$$

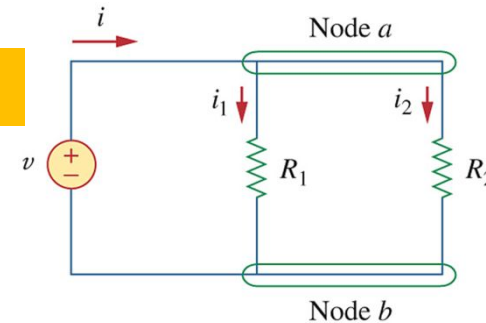
$$\text{if } R_1 = R_2 = \cdots R_N = R, \quad R_{eq} = R / N$$

Resistance vs. Conductance

직렬연결



병렬연결



$$R_{eq} = R_1 + R_2 + \dots + R_N$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_N}$$

$$\frac{1}{G_{eq}} = \frac{1}{G_1} + \frac{1}{G_2} + \dots + \frac{1}{G_N}$$

$$G_{eq} = G_1 + G_2 + \dots + G_N$$

$$v_1 = \frac{R_1 v}{R_1 + R_2}, \quad v_2 = \frac{R_2 v}{R_1 + R_2}$$

$$v = v_1 = v_2 = \frac{i}{G_1 + G_2}$$

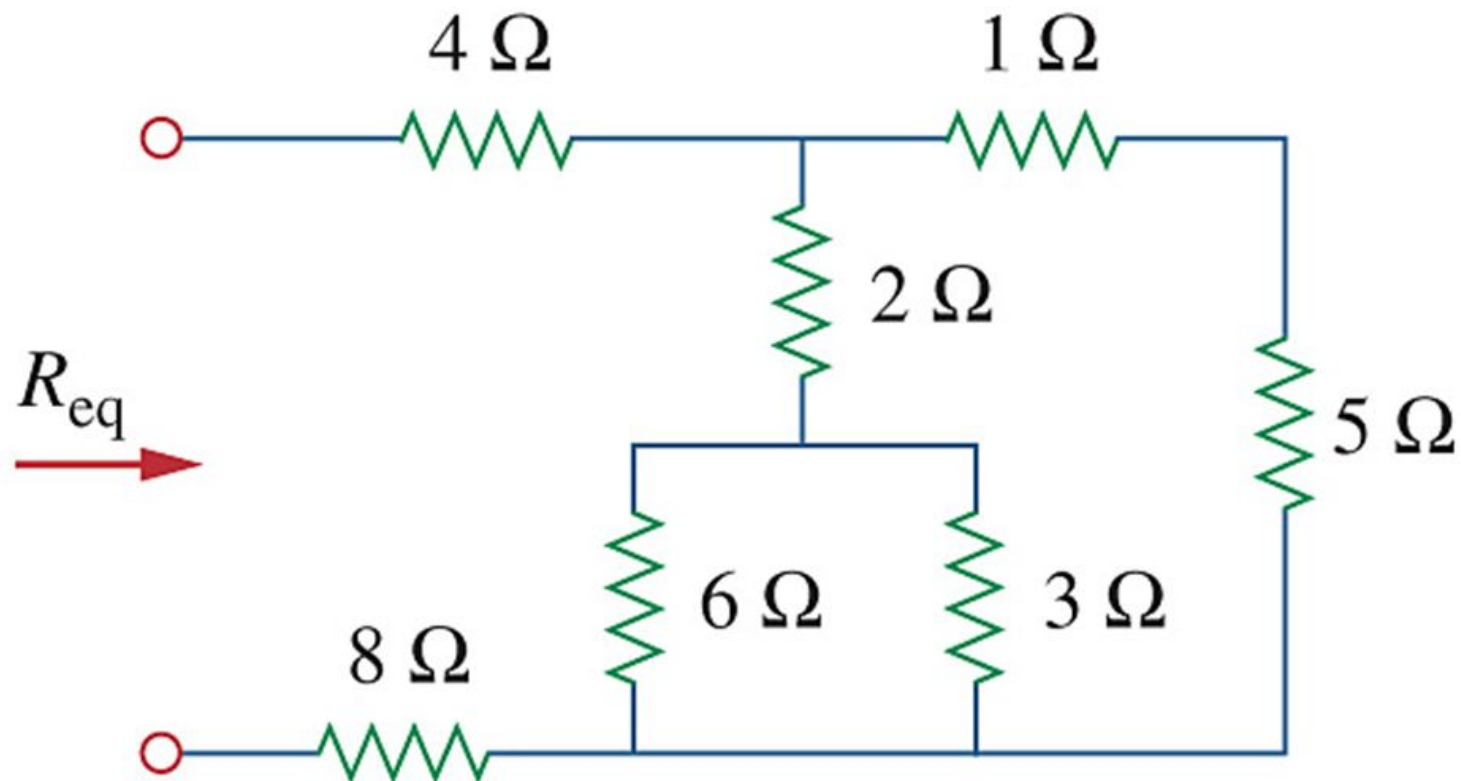
$$i = i_1 = i_2 = \frac{v}{R_1 + R_2}$$

$$i_1 = \frac{G_1 i}{G_1 + G_2}, \quad i_2 = \frac{G_2 i}{G_1 + G_2}$$

Principle of Duality : $v \leftrightarrow i$, $R \leftrightarrow G$

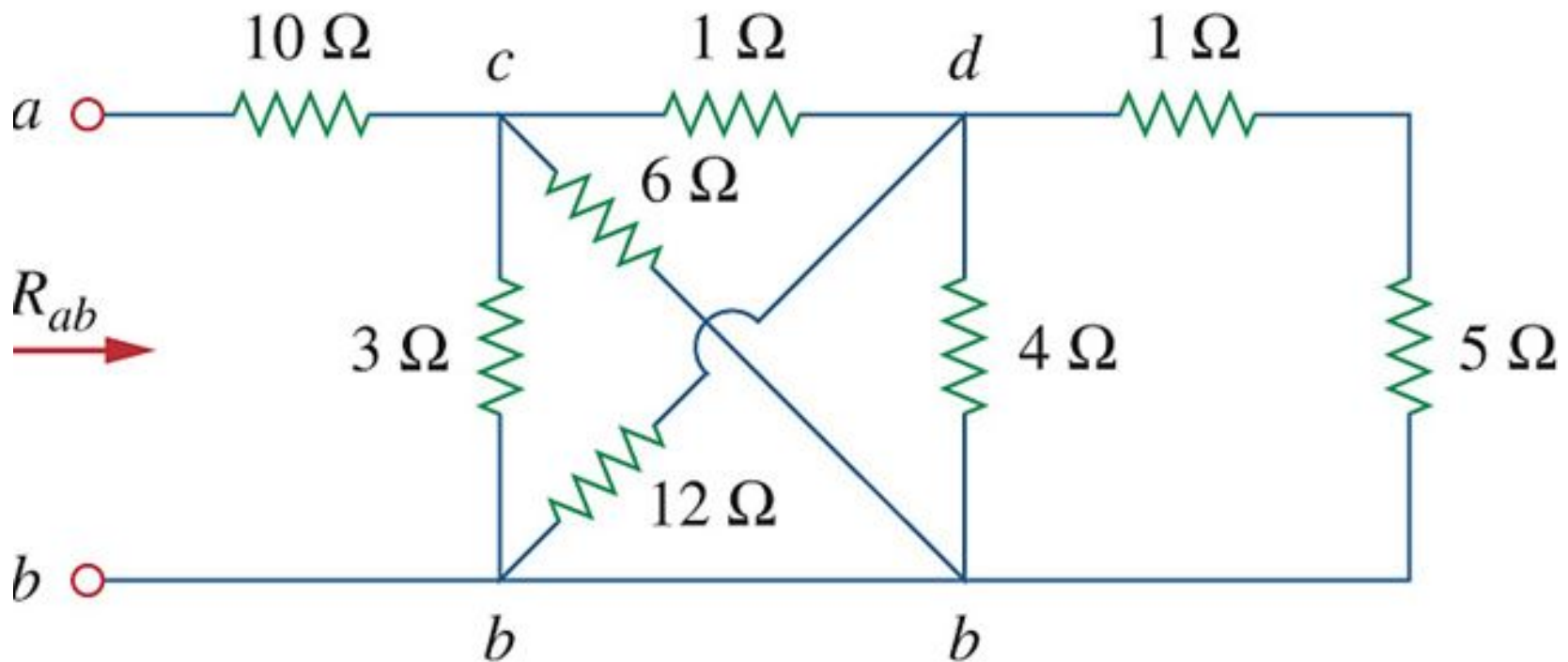
Example 2.9

- 다음 회로에서 R_{eq} 를 구하라.



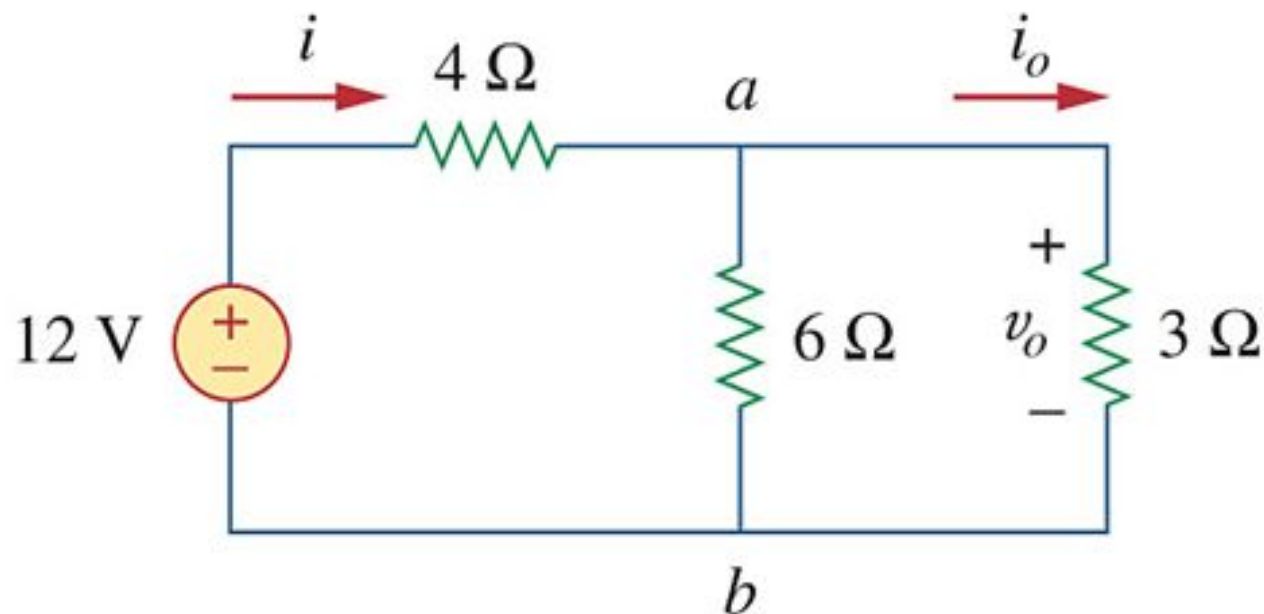
Example 2.10

- 다음 회로에서 등가 저항 R_{ab} 를 구하라.



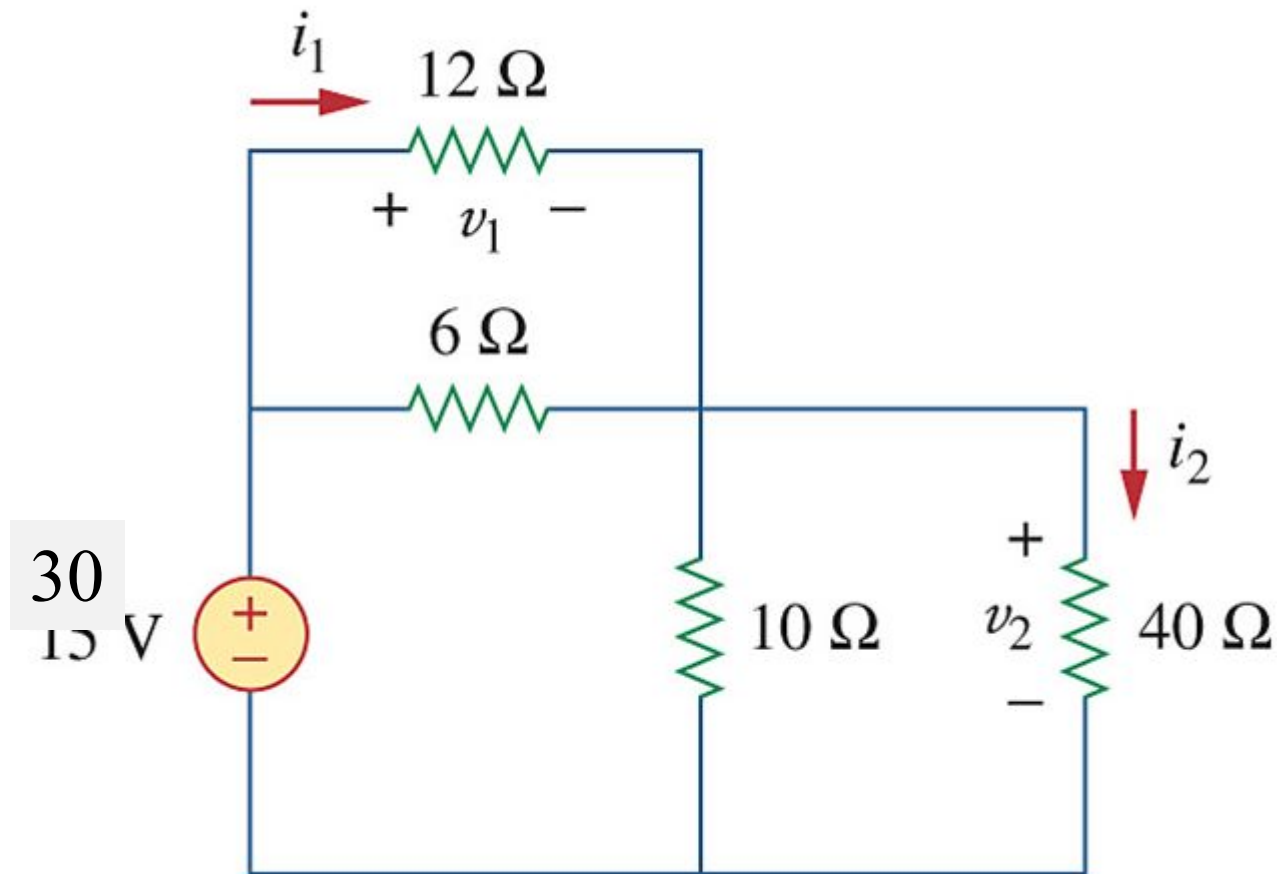
Example 2.12

- 다음 회로에서 i_0 , v_0 와 3Ω 저항에서 소모된 전력을 구하라.



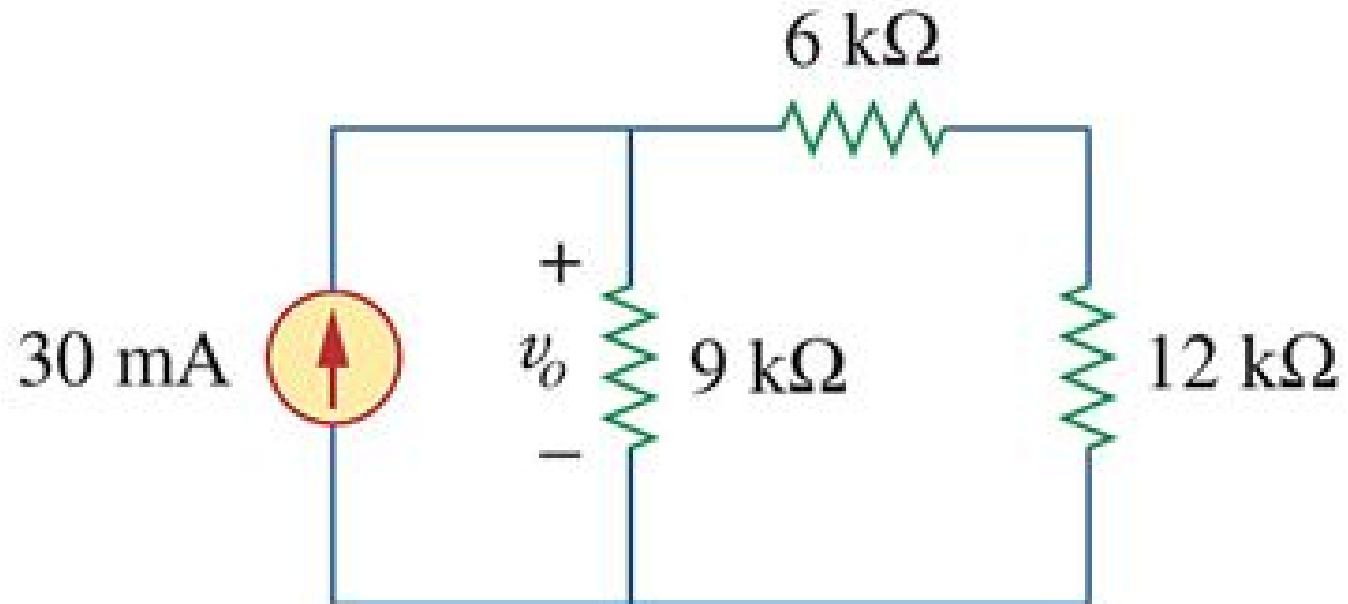
Practice 2.12

- 다음 회로에서 v_1 과 v_2 를 구하라. 전류 i_1 과 i_2 그리고 $12\ \Omega$ 과 $40\ \Omega$ 저항에서 소모된 전력을 구하라.



Example 2.13

- 전압 v_o 를 구하라

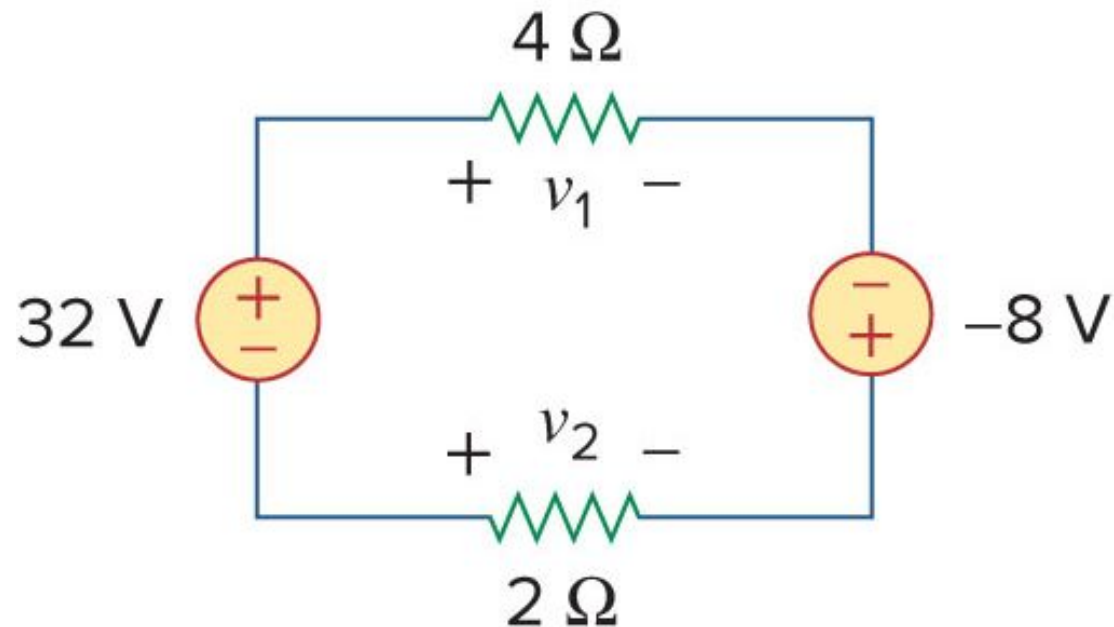


Homework #2

- Due : 다음 수업시간에 제출

#1. Practice(본문 실전문제) 2.5

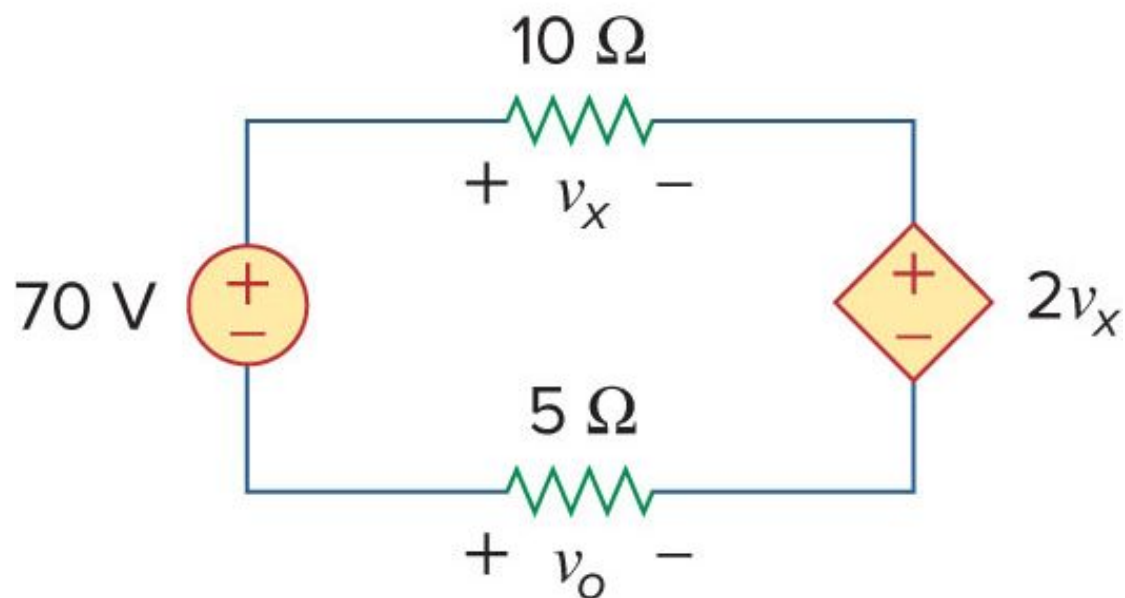
다음 회로에서 전압 v_1 과 v_2 를 구하라.



Homework #2

#2. Practice (본문 실전문제) 2.6

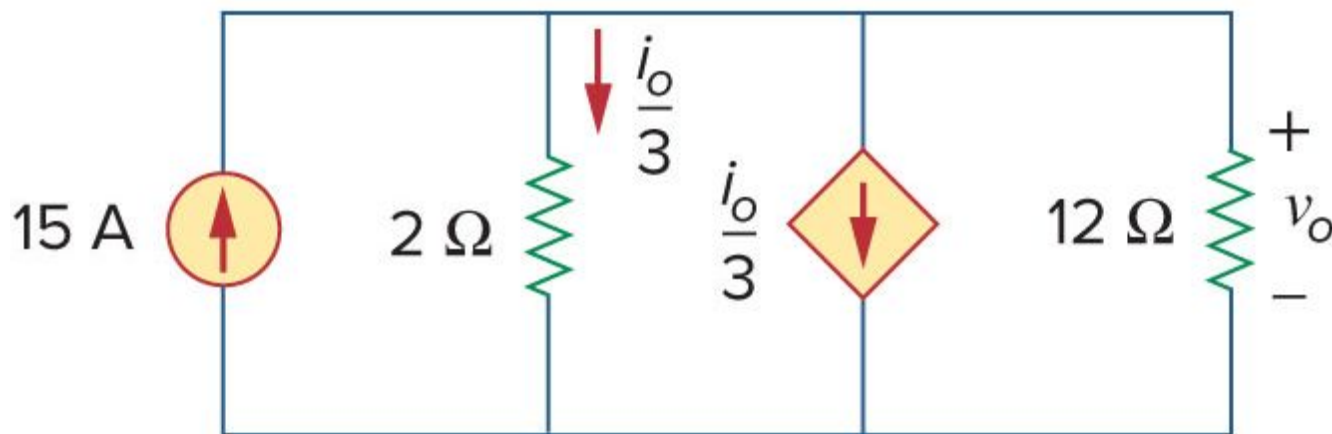
다음 회로에서 전압 v_x 과 v_o 를 구하라.



Homework #2

#3. Practice(본문 실전문제) 2.7

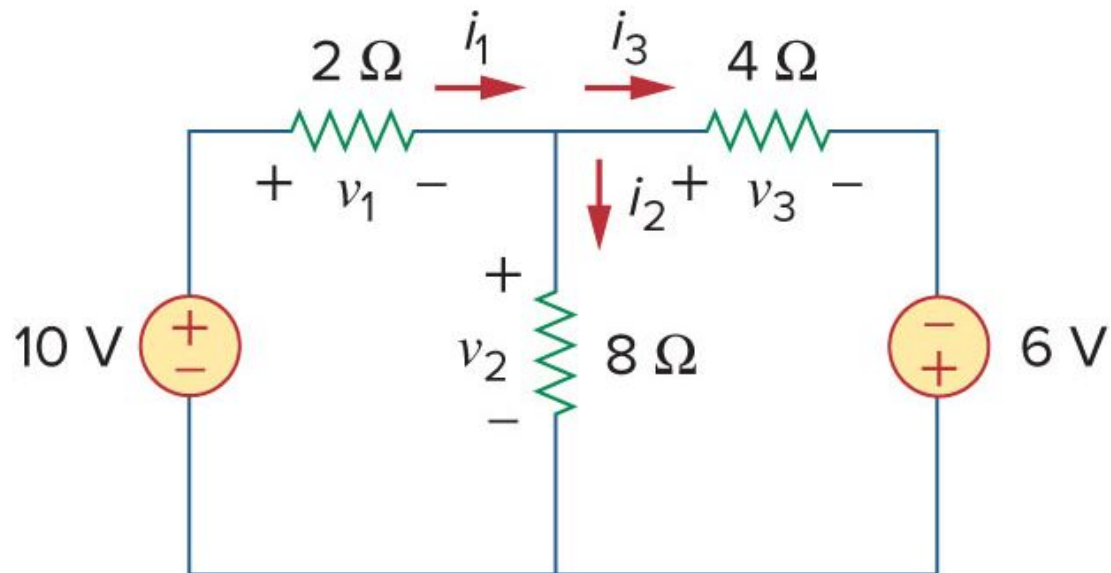
다음 회로에서 전압 v_o 와 전류 i_o 를 구하라.



Homework #2

#4. Practice(본문 실전문제) 2.8

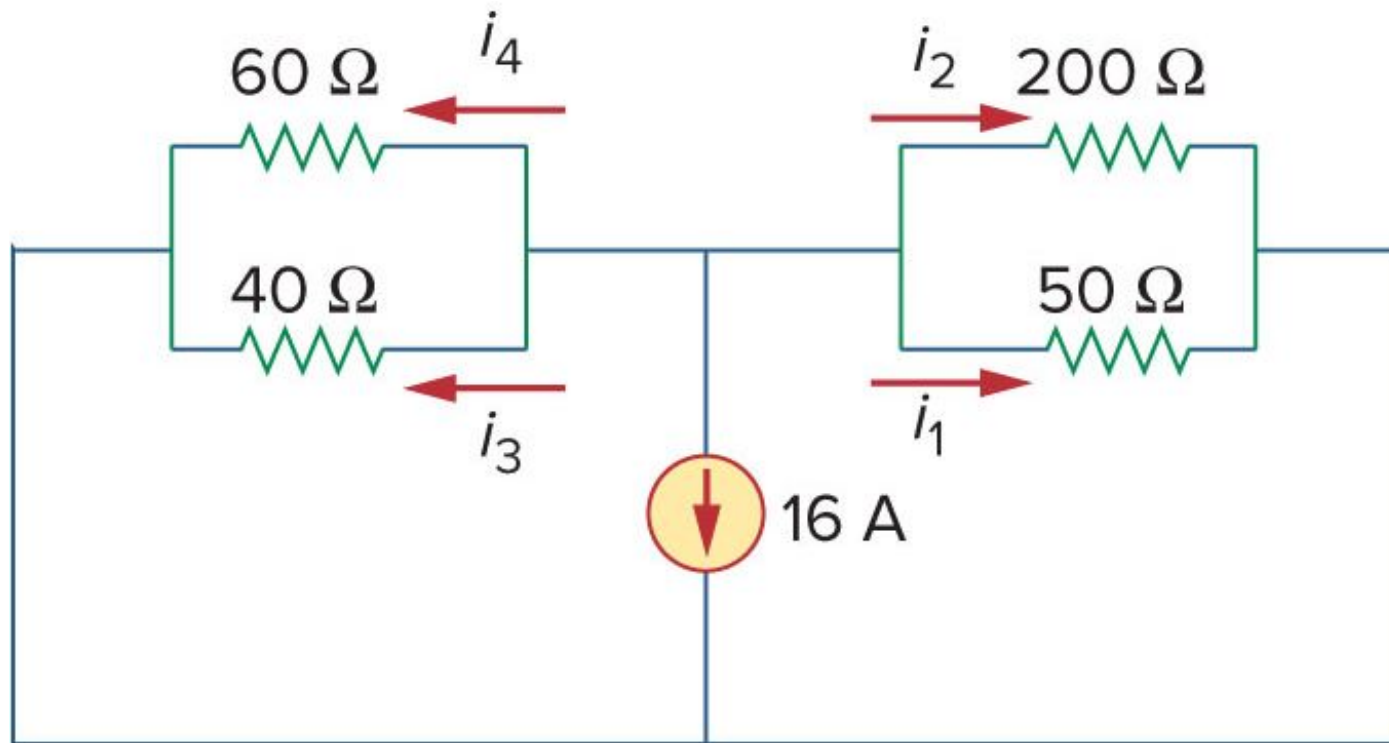
다음 회로에서 전류와 전압을 구하라.



Homework #2

#5. Problem(문제) 2.32

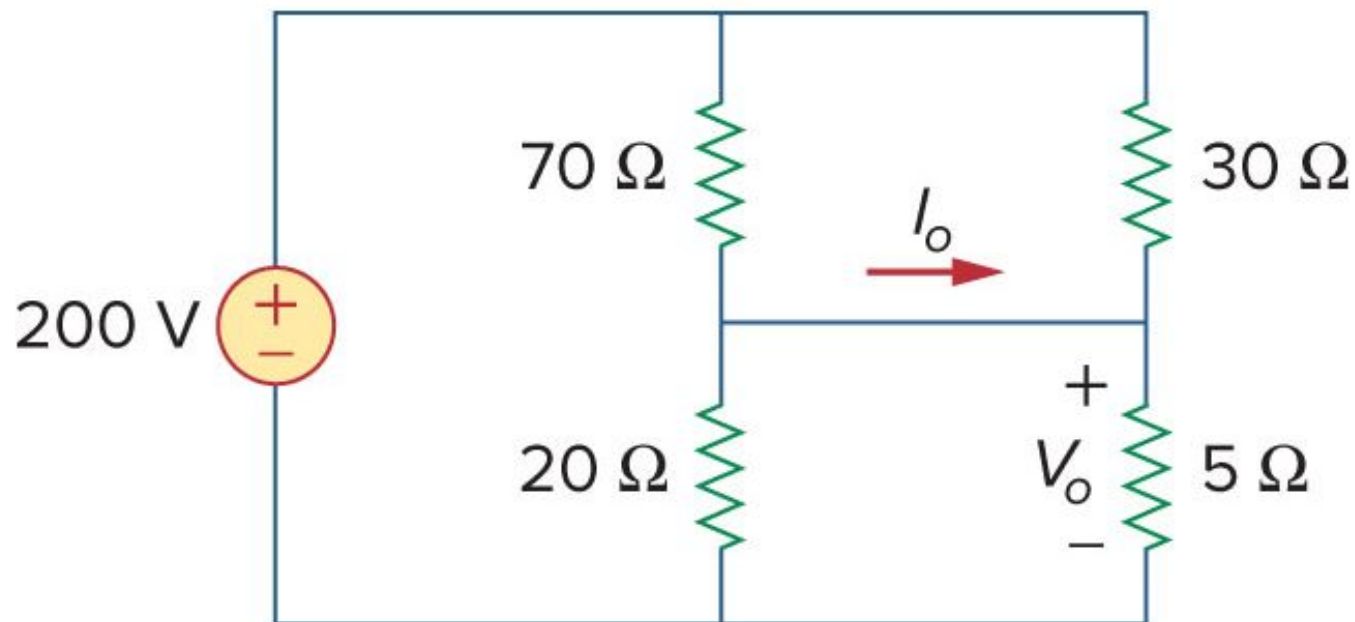
다음 회로에서 전류 $i_1 \sim i_4$ 를 구하라.



Homework #2

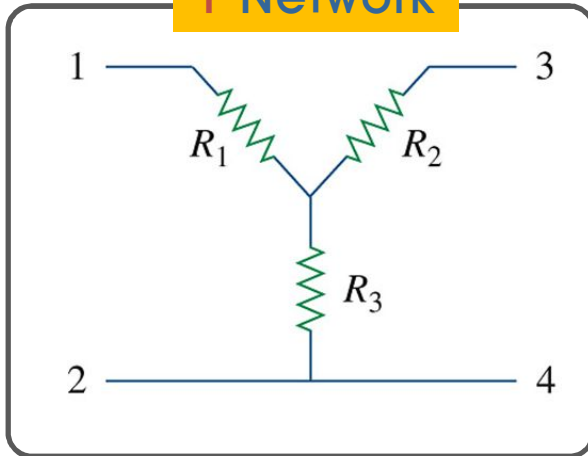
#6. Problem(문제) 2.35

다음 회로에서 V_o 와 I_o 를 구하라.



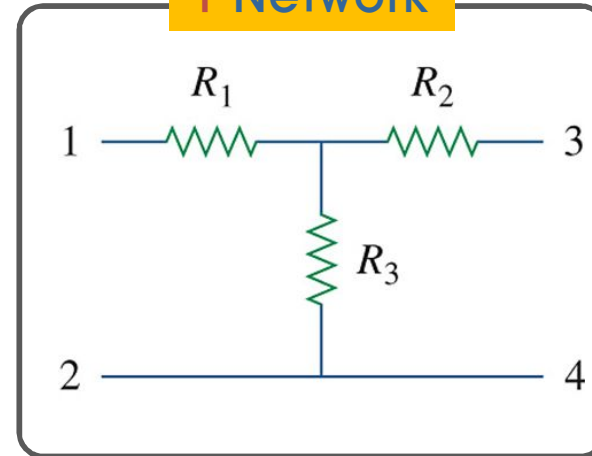
2.7 와이-델타 변환

Y Network

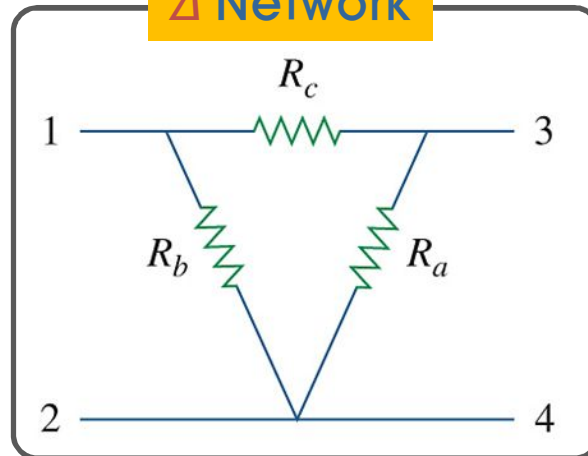


\equiv

T Network

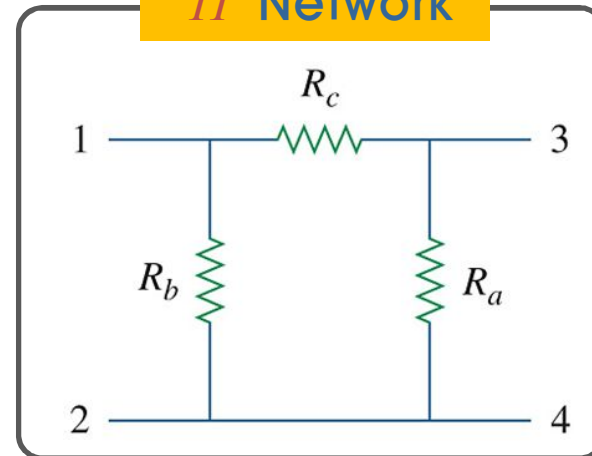


Δ Network

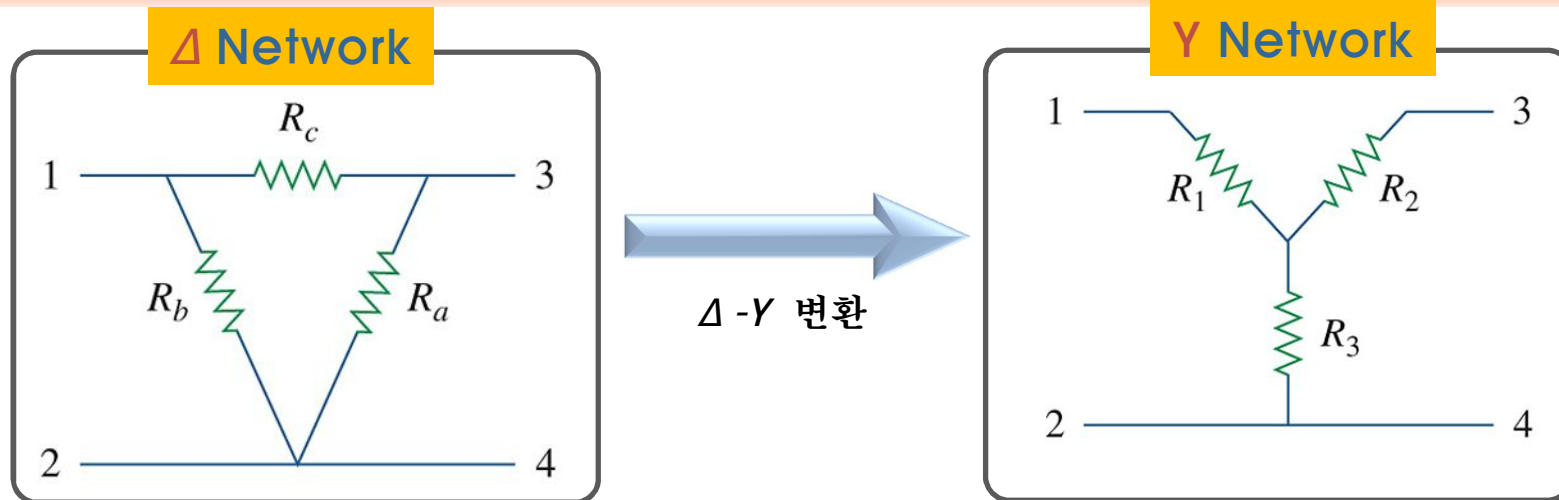


\equiv

Π Network



2.7 델타-와이 변환



$$R_{12}(\Delta) = R_b \parallel (R_a + R_c)$$

$$R_{13}(\Delta) = R_c \parallel (R_a + R_b)$$

$$R_{34}(\Delta) = R_a \parallel (R_b + R_c)$$

$$R_{12}(\Delta) = R_{12}(Y)$$

$$R_{13}(\Delta) = R_{13}(Y)$$

$$R_{34}(\Delta) = R_{34}(Y)$$

$$R_{12}(Y) = R_1 + R_3$$

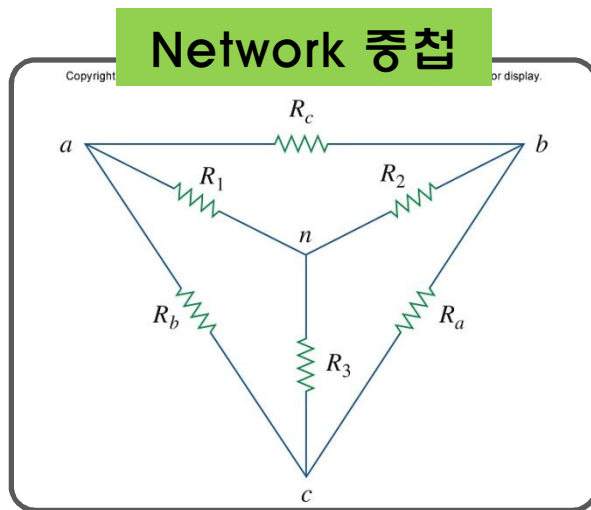
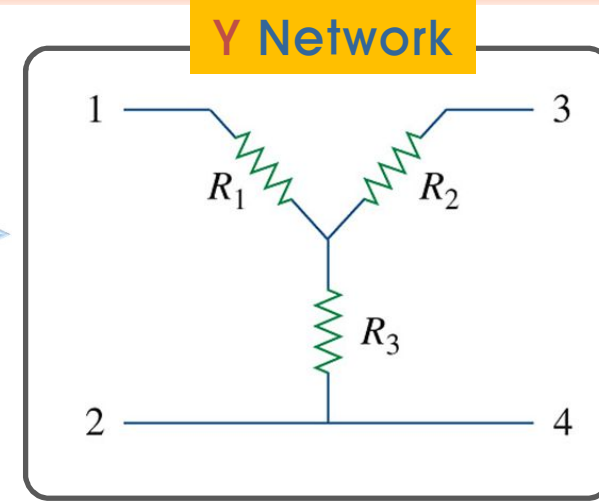
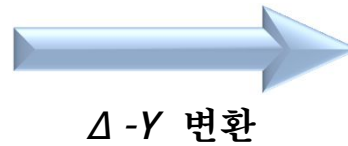
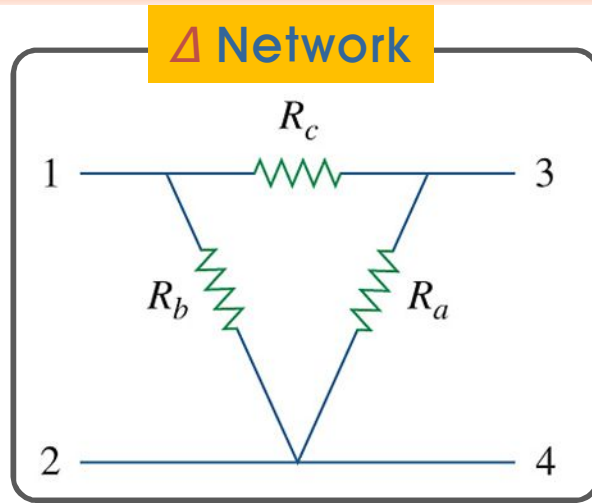
$$R_{13}(Y) = R_1 + R_2$$

$$R_{34}(Y) = R_2 + R_3$$



$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}, \quad R_2 = \frac{R_c R_a}{R_a + R_b + R_c}, \quad R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

2.7 델타-와이 변환

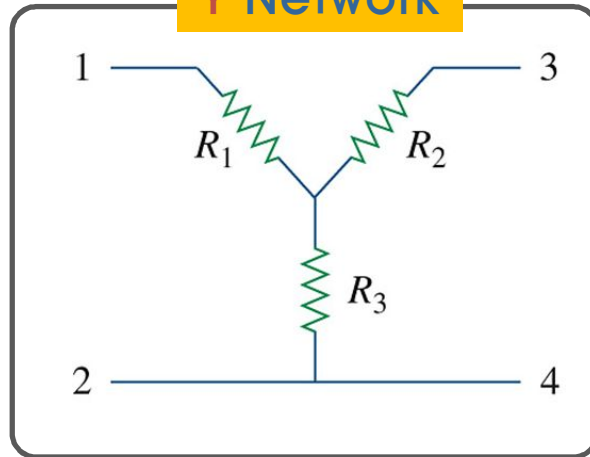


Y의 저항 = $\frac{\text{인접하는 } \Delta \text{의 두 저항의 곱}}{\Delta \text{ 저항의 합}}$

$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}, \quad R_2 = \frac{R_c R_a}{R_a + R_b + R_c}, \quad R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

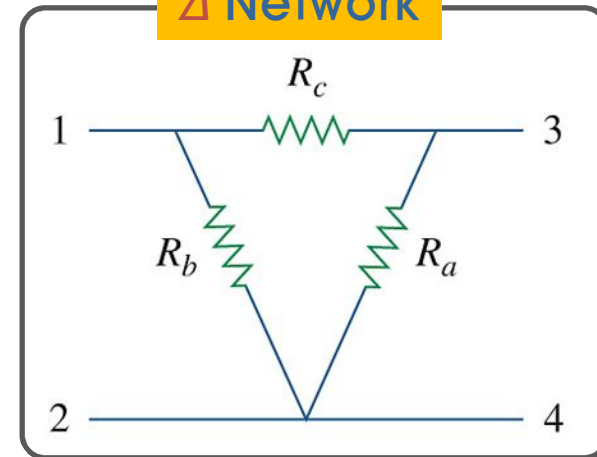
2.7 와이-델타 변환

Y Network

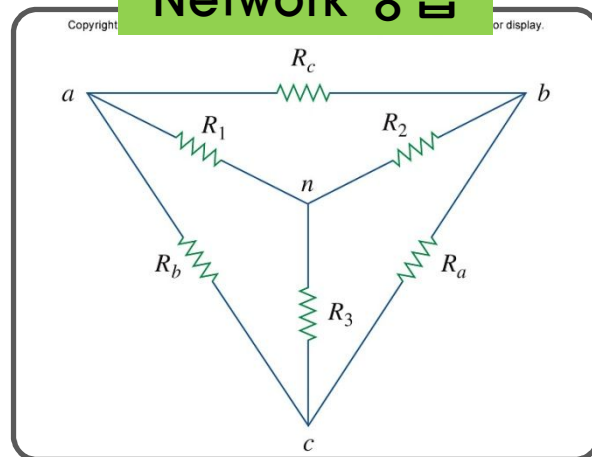


Y-Δ 변환

Δ Network



Network 중첩



$$\Delta \text{의 저항} = \frac{\text{모든 조합으로 두 저항 곱의 합}}{\text{반대편의 Y 저항}}$$

$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

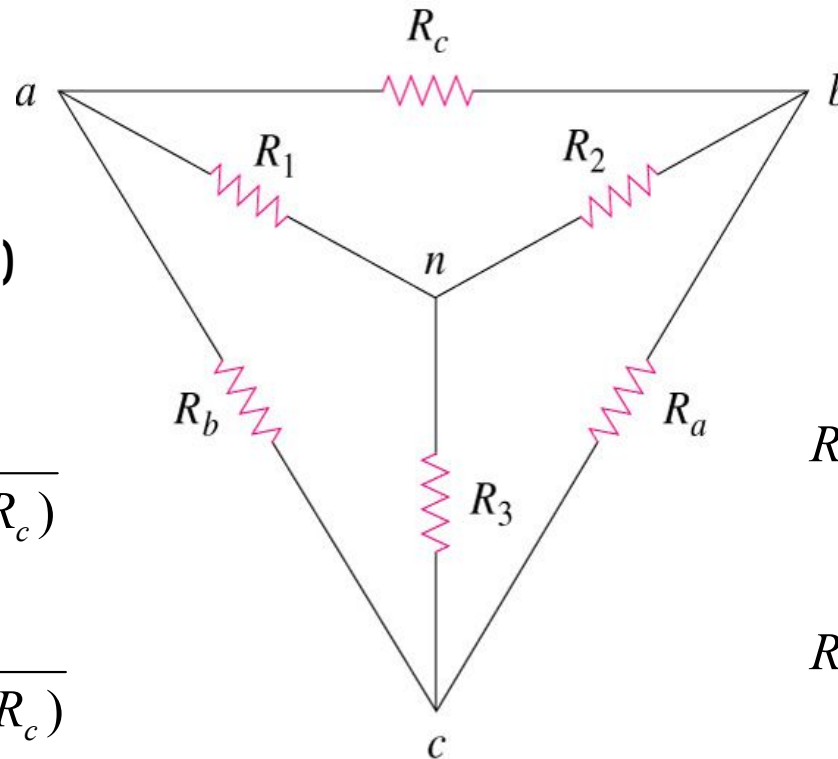
2.7 와이-델타 변환 (Summary)

Delta → Y (Star)

$$R_1 = \frac{R_b R_c}{(R_a + R_b + R_c)}$$

$$R_2 = \frac{R_c R_a}{(R_a + R_b + R_c)}$$

$$R_3 = \frac{R_a R_b}{(R_a + R_b + R_c)}$$



Y (Star) → Delta

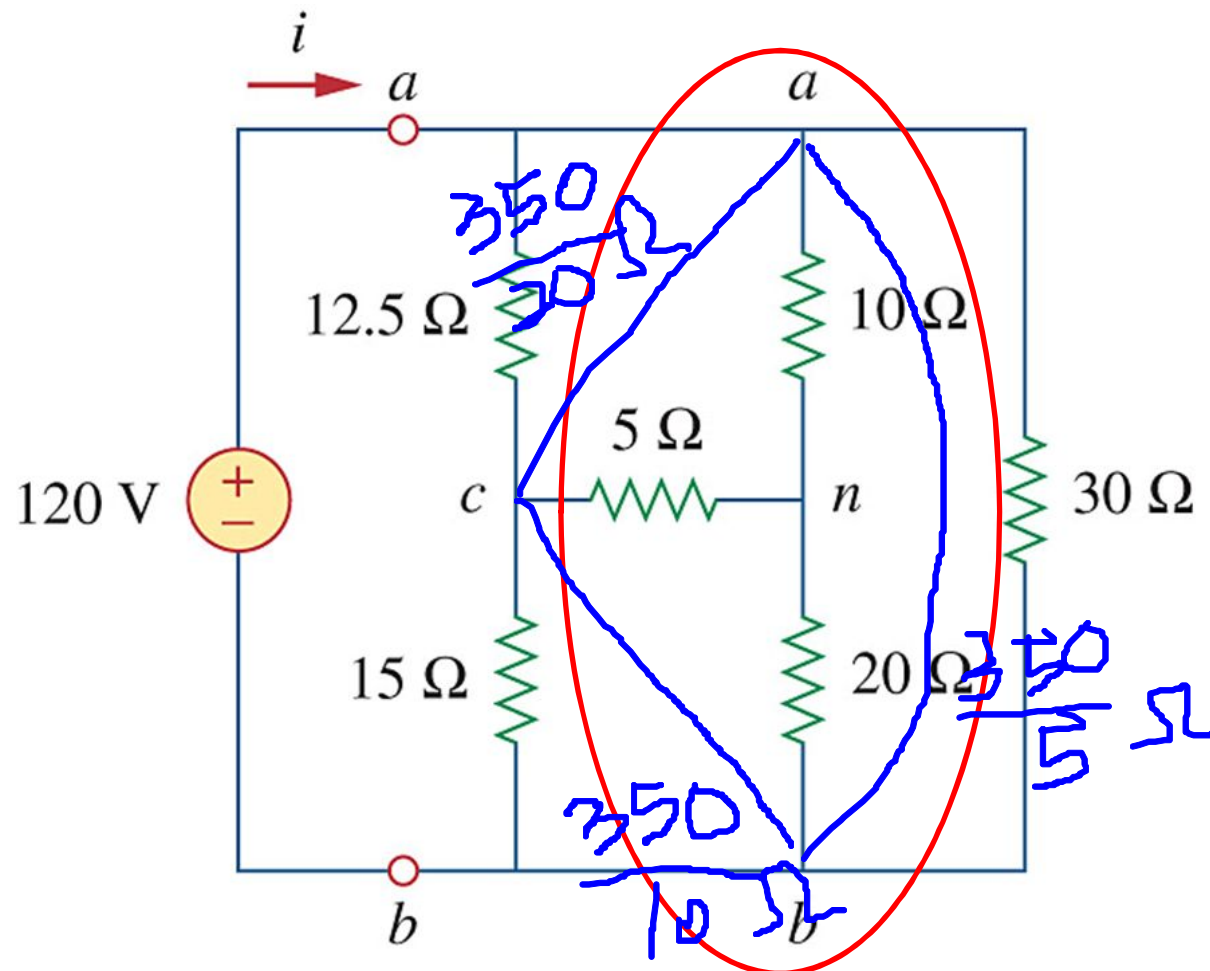
$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

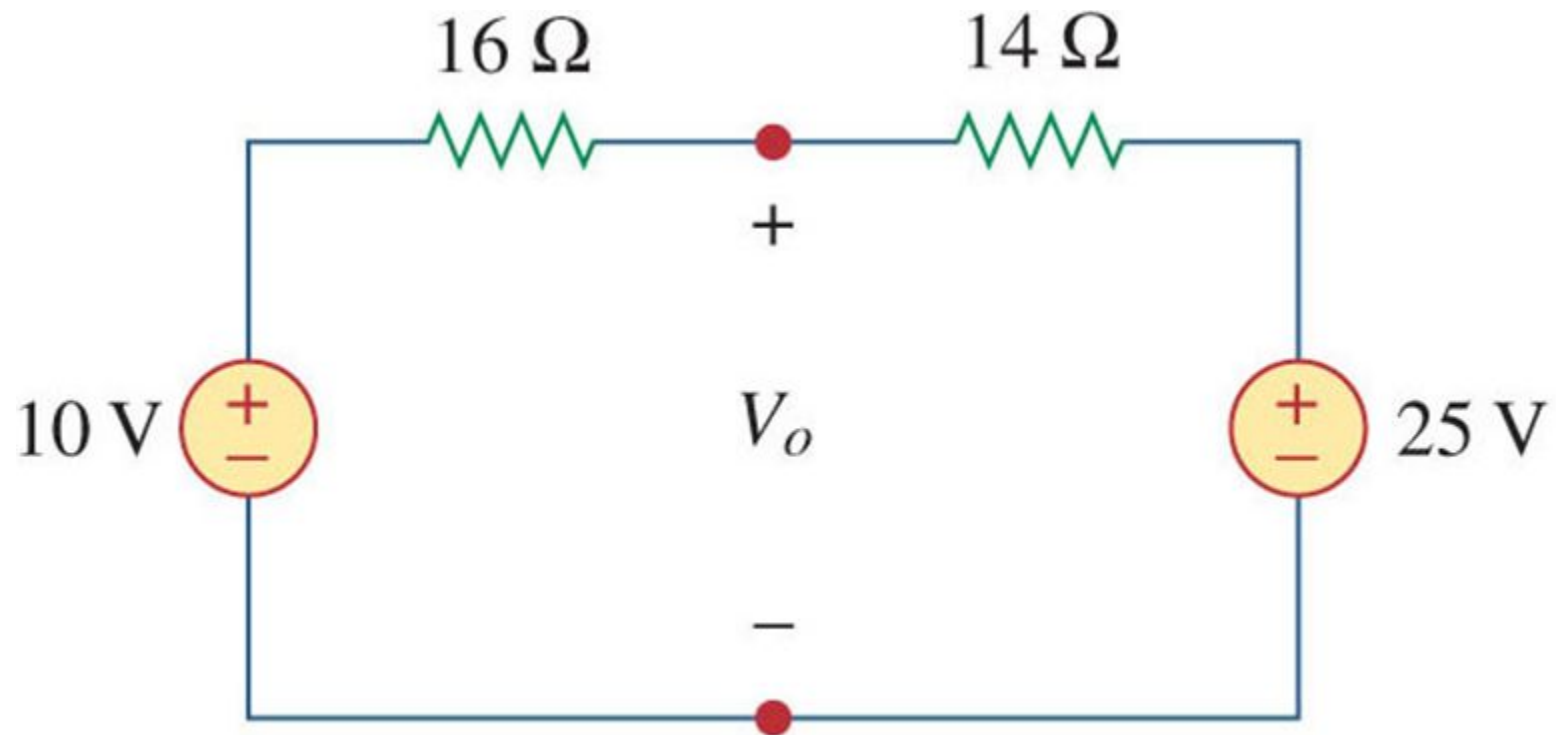
Example 2.15

○ 와이-델타 변환 이용



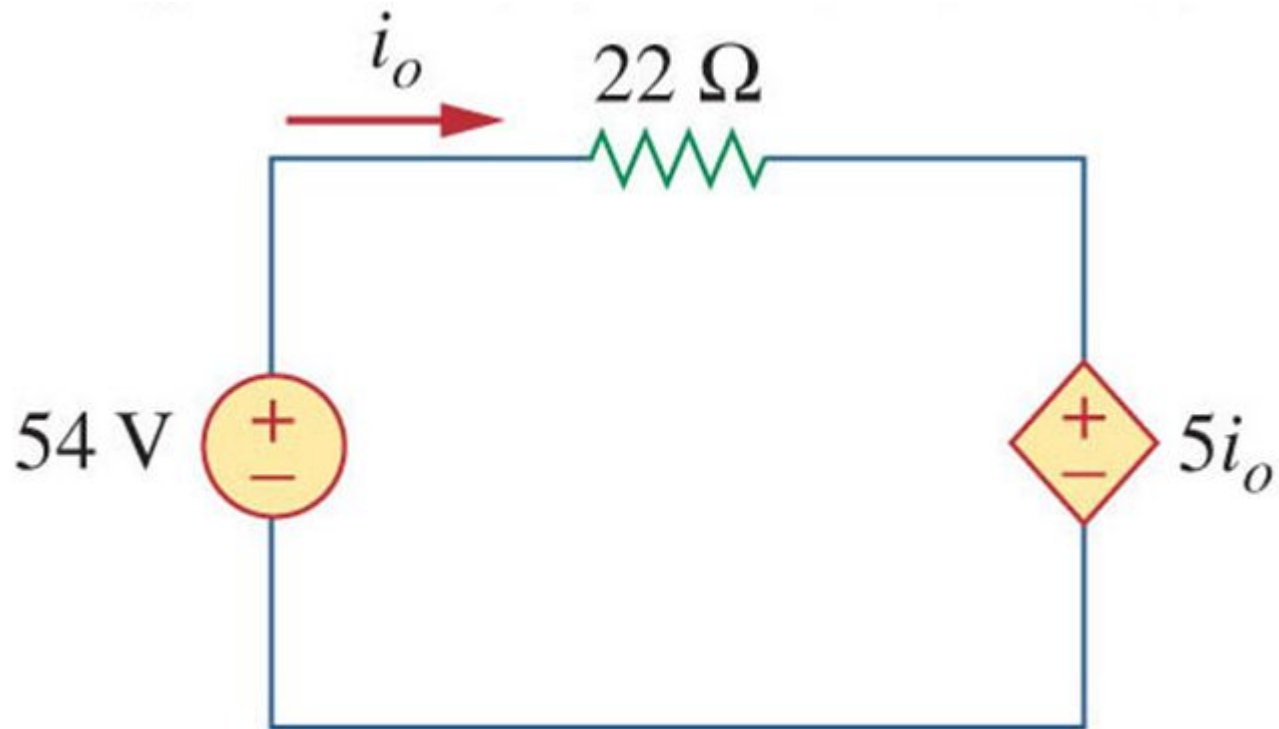
Problem 2.16

- 다음 회로에서 전압 V_o 를 구하라.



Problem 2.20

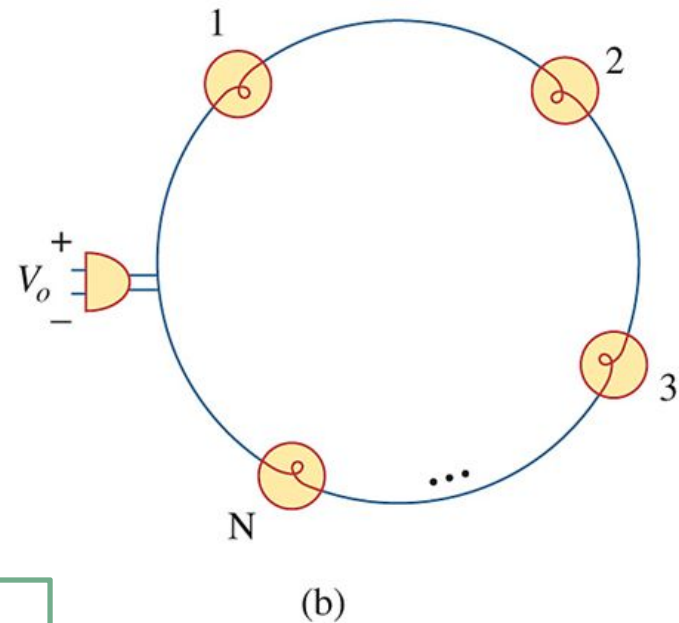
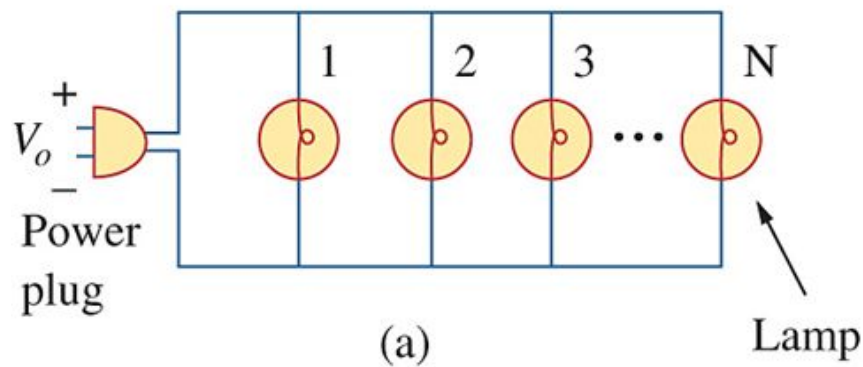
- 다음 회로에서 전류 i_o 를 구하라.



2.8 응용 : 조명 시스템

Quiz

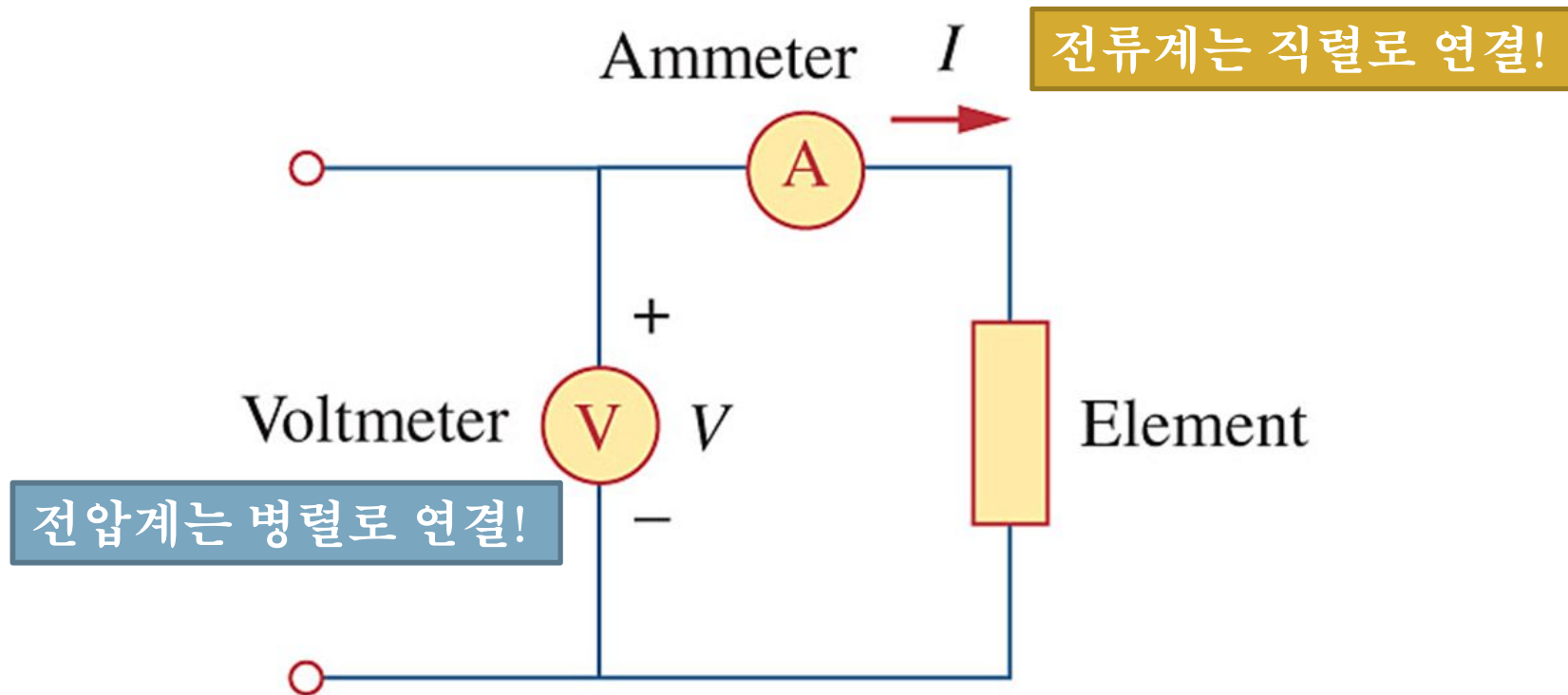
- 직렬연결이 좋은가? 아니면 병렬연결이 좋은가?



Why?

- 고장 나도 하나만 문제!
- 고장 원인 확인 쉬워!
- 물건 만들기도 쉬워!

2.8 응용 : 전압계와 전류계



- Quiz : 전압계와 전류계의 내부저항의 이상적인 값은?

전압계 : ∞
전류계 : 0

Homework #3

- Problem(문제) 2.15, 2.17, 2.21, 2,22
- Due : 다음 수업시간까지



◦ Quiz #1

- Homework #2, #3 중에서 출제
- 다음 수업시간 (10분)

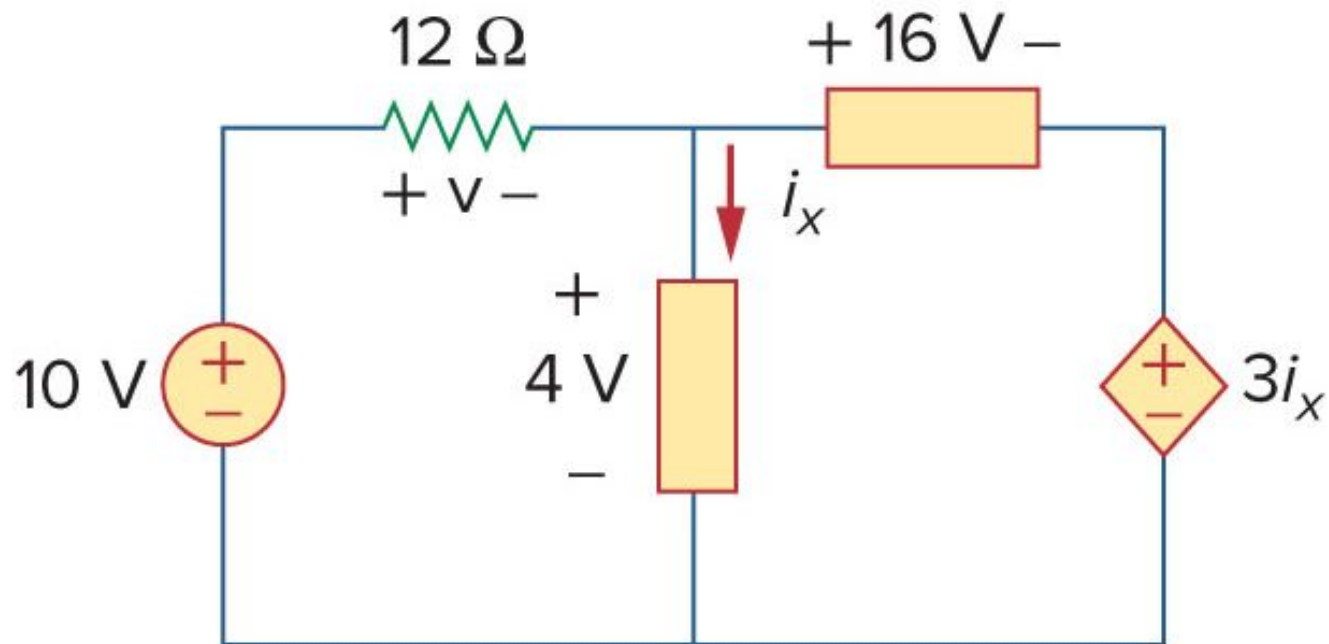
Homework #3

- Problem(문제) 2.15, 2.17, 2.21, 2,22
- Due : 다음 수업시간까지
- Quiz #1
 - Homework #2, #3 중에서 출제
 - 다음 수업시간 (10분)

Homework #3

#1. Problem(문제) 2.15

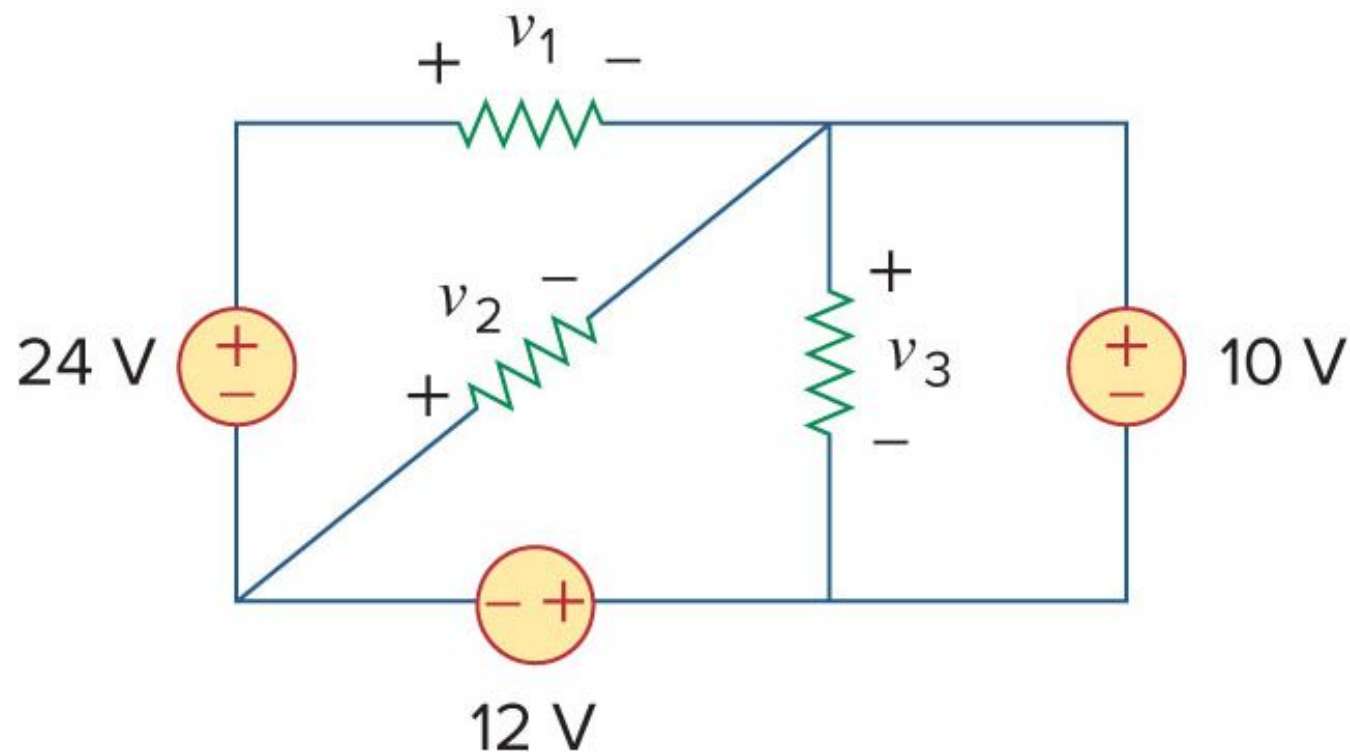
다음 회로에서 전압 v 와 전류 i_x 를 구하라.



Homework #3

#1. Problem(문제) 2.17

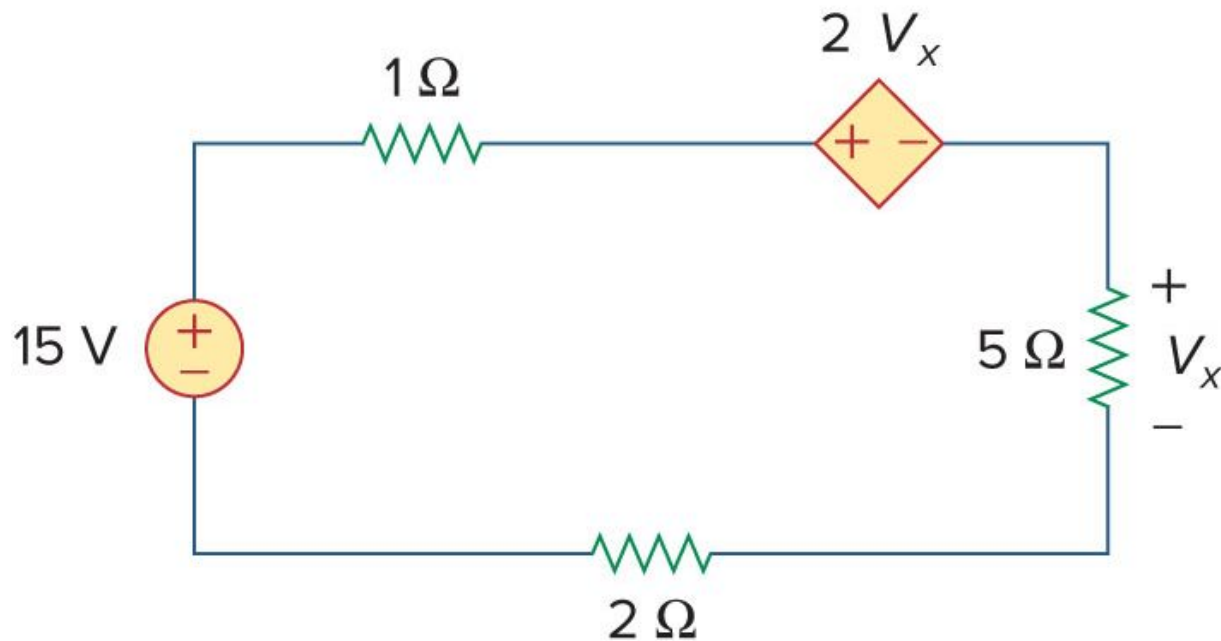
다음 회로에서 전압 v_1, v_2, v_3 를 구하라.



Homework #3

#3. Problem(문제) 2.21

다음 회로에서 전압 V_x 를 구하라.



Homework #3

#4. Problem(문제) 2.22

다음 회로에서 전압 V_o 와 종속 전원에 의해 소모되는 전력을 구하라.

