

# Predicting CO<sub>2</sub> Emissions

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STATS/DATASCI 112

Question

How well can we predict a country's  
CO<sub>2</sub> emissions?

What about if we don't use any factors relating to what type of energy it uses?

# Data Collection

# Our World in Data

# Population Division World Urbanization Prospects 2018



THE WORLD BANK  
IBRD • IDA

# FOR TUNE

# kaggle

1 Walmart

2 Amazon

3 State Grid

4 China National Petroleum

5 Sinopec Group

6 Saudi Aramco

7 Apple

8 Volkswagen

9 China State Construction Engineering

10 CVS Health

| Annual Total Population at Mid-Year (thousands) |   |      |           |           |           |           |           |         |      |
|---|---|------|-----------|-----------|-----------|-----------|-----------|---------|------|
| ISO 3166-1 numeric                              | Location                                | Note | 1950      | 1951      | 1952      | 1953      | 1954      | Entity  | Code |
| 900   | World                                   |      | 2 536 275 | 2 583 817 | 2 630 584 | 2 677 230 | 2 724 262 | Algeria | AFG  |
| 901   | Less developed mgl.a                    |      | 814 865   | 824 219   | 834 071   | 844 264   | 854 832   | Algeria | AFG  |
| 902   | Less developed mgl.b                    |      | 1 721 410 | 1 759 604 | 1 796 513 | 1 832 967 | 1 869 431 | Algeria | AFG  |
| 941   | Less developed cou.c                    |      | 185 289   | 189 052   | 202 905   | 206 885   | 211 045   | Algeria | AFG  |
| 934   | Less developed r.d                      |      | 1 526 151 | 1 560 552 | 1 593 608 | 1 626 082 | 1 658 326 | Algeria | AFG  |
| 948   | Less developed regions, excluding China |      | 1 187 187 | 1 178 538 | 1 203 695 | 1 228 485 | 1 258 404 | Algeria | AFG  |
| 1003  | High-income countr.e                    |      | 672 896   | 680 530   | 685 859   | 687 445   | 706 262   | Algeria | AFG  |
| 1517  | Middle-income countr.e                  |      | 1 734 481 | 1 772 384 | 1 808 889 | 1 844 730 | 1 880 558 | Algeria | AFG  |
| 1501  | Lower-middle-income e                   |      | 778 277   | 792 189   | 807 013   | 822 677   | 839 186   | Algeria | AFG  |
| 1502  | Upper-middle-income e                   |      | 956 204   | 980 195   | 1 001 876 | 1 022 054 | 1 041 402 | Algeria | AFG  |
| 1008  | Low-income countr.e                     |      | 129 287   | 129 689   | 131 162   | 134 184   | 136 584   | Algeria | AFG  |
| 947   | Sub-Saharan Africa, f                   |      | 179 621   | 183 039   | 186 628   | 190 378   | 194 285   | Algeria | AFG  |
| 903   | Africa                                  |      | 228 670   | 233 277   | 238 113   | 243 178   | 248 471   | Algeria | AFG  |
| 910   | Eastern Africa                          |      | 86 758    | 88 206    | 89 712    | 91 272    | 92 896    | Algeria | AFG  |
| 108   | Burundi                                 |      | 2 309     | 2 359     | 2 404     | 2 445     | 2 487     | Algeria | AFG  |
| 171   | Comoros                                 |      | 159       | 163       | 167       | 170       | 173       | Algeria | AFG  |
| 202   | Djibouti                                |      | 62        | 63        | 65        | 66        | 68        | Algeria | AFG  |
| 232   | Eritrea                                 |      | 1 142     | 1 160     | 1 180     | 1 201     | 1 224     | Algeria | AFG  |
| 231   | Ethiopia                                |      | 18 128    | 18 467    | 18 820    | 19 184    | 19 560    | Algeria | AFG  |
| 404   | Kenya                                   |      | 6 077     | 6 240     | 6 412     | 6 593     | 6 782     | Algeria | AFG  |
| 420   | Madagascar                              |      | 4 084     | 4 188     | 4 297     | 4 349     | 4 444     | Algeria | AFG  |
| 454   | Malawi                                  |      | 2 954     | 3 008     | 3 065     | 3 125     | 3 187     | Algeria | AFG  |
| 480   | Mauritius                               | 1    | 493       | 506       | 521       | 537       | 554       | Algeria | AFG  |
| 178   | Mayotte                                 |      | 15        | 16        | 16        | 17        | 18        | Algeria | AFG  |
| 908   | Mozambique                              |      | 6 152     | 6 249     | 6 353     | 6 463     | 6 580     | Algeria | AFG  |
| 628   | Niger                                   |      | 248       | 259       | 269       | 277       | 284       | Algeria | AFG  |
| 646   | Rwanda                                  |      | 2 180     | 2 251     | 2 313     | 2 378     | 2 449     | Algeria | AFG  |
| 690   | Seychelles                              |      | 36        | 37        | 37        | 38        | 38        | Algeria | AFG  |
| 708   | Somalia                                 |      | 2 264     | 2 308     | 2 352     | 2 397     | 2 444     | Algeria | AFG  |
| 728   | South Sudan                             |      | 2 883     | 2 902     | 2 928     | 2 953     | 2 978     | Algeria | AFG  |
| 800   | Uganda                                  |      | 5 108     | 5 309     | 5 456     | 5 611     | 5 748     | Algeria | AFG  |
| 834   | United Republic of T                    |      | 2 7 650   | 7 847     | 8 056     | 8 275     | 8 503     | Algeria | AFG  |
| 884   | Zambia                                  |      | 2 310     | 2 367     | 2 428     | 2 494     | 2 562     | Algeria | AFG  |
| 716   | Zimbabwe                                |      | 2 747     | 2 830     | 2 917     | 3 009     | 3 104     | Algeria | AFG  |
| 911   | Malawi Africa                           |      | 26 444    | 26 965    | 27 490    | 28 032    | 28 583    | Algeria | AFG  |
| 24  | Angola                                  |      | 4 448     | 4 629     | 4 775     | 4 880     | 5 005     | Algeria | AFG  |
| 120   | Cameroon                                |      | 4 307     | 4 383     | 4 460     | 4 539     | 4 621     | Algeria | AFG  |
| 140   | Central African Republi                 |      | 1 327     | 1 340     | 1 353     | 1 368     | 1 383     | Algeria | AFG  |

| Annual CO2 emissions |      |      |                      |         |      |      |                      |         |      |
|----------------------|------|------|----------------------|---------|------|------|----------------------|---------|------|
| Entity               | Code | Year | Annual CO2 emissions | Entity  | Code | Year | Annual CO2 emissions | Entity  | Code |
| Algeria              | AFG  | 1969 | 14658                | Algeria | AFG  | 1990 | 84523                | Algeria | AFG  |
| Algeria              | AFG  | 1991 | 84523                | Algeria | AFG  | 1992 | 81600                | Algeria | AFG  |
| Algeria              | AFG  | 1993 | 81600                | Algeria | AFG  | 1994 | 100236               | Algeria | AFG  |
| Algeria              | AFG  | 1995 | 100236               | Algeria | AFG  | 1996 | 183200               | Algeria | AFG  |
| Algeria              | AFG  | 1997 | 292120               | Algeria | AFG  | 1998 | 329700               | Algeria | AFG  |
| Algeria              | AFG  | 1999 | 384931               | Algeria | AFG  | 2000 | 413885               | Algeria | AFG  |
| Algeria              | AFG  | 2001 | 480736               | Algeria | AFG  | 2002 | 688564               | Algeria | AFG  |
| Algeria              | AFG  | 2003 | 700736               | Algeria | AFG  | 2004 | 838551               | Algeria | AFG  |
| Algeria              | AFG  | 2005 | 1008917              | Algeria | AFG  | 2006 | 1081188              | Algeria | AFG  |
| Algeria              | AFG  | 2007 | 1281865              | Algeria | AFG  | 2008 | 1223391              | Algeria | AFG  |
| Algeria              | AFG  | 2009 | 947252               | Algeria | AFG  | 2010 | 975037               | Algeria | AFG  |
| Algeria              | AFG  | 2011 | 1880554              | Algeria | AFG  | 2012 | 1530347              | Algeria | AFG  |
| Algeria              | AFG  | 2013 | 1026566              | Algeria | AFG  | 2014 | 1915132              | Algeria | AFG  |
| Algeria              | AFG  | 2015 | 2121383              | Algeria | AFG  | 2016 | 1980859              | Algeria | AFG  |
| Algeria              | AFG  | 2017 | 2384175              | Algeria | AFG  | 2018 | 2153300              | Algeria | AFG  |
| Algeria              | AFG  | 2019 | 2232754              | Algeria | AFG  | 2020 | 1790302              | Algeria | AFG  |
| Algeria              | AFG  | 2021 | 1978483              | Algeria | AFG  | 2022 | 2094810              | Algeria | AFG  |
| Algeria              | AFG  | 2023 | 2518954              | Algeria | AFG  | 2024 | 2821540              | Algeria | AFG  |
| Algeria              | AFG  | 2025 | 3001422              | Algeria | AFG  | 2026 | 3113628              | Algeria | AFG  |
| Algeria              | AFG  | 2027 | 3113628              | Algeria | AFG  | 2028 | 2746555              | Algeria | AFG  |
| Algeria              | AFG  | 2029 | 2746555              | Algeria | AFG  | 2030 | 2024226              | Algeria | AFG  |

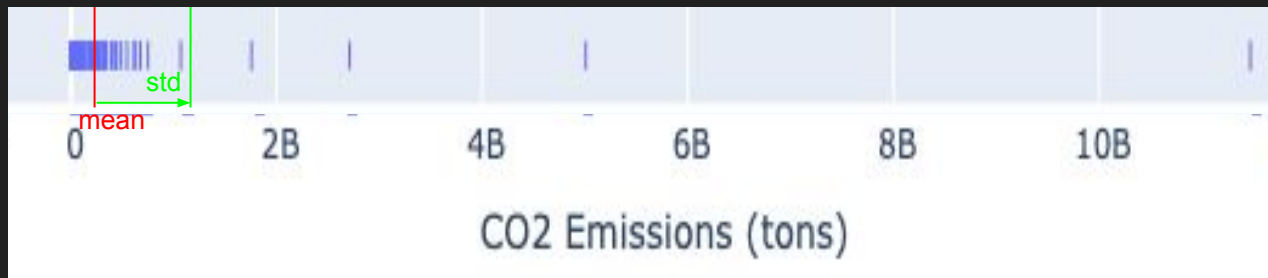
# Data Analysis

|     | Country   | Code | Year | Population | Urban Percentage | GDP Per Capita (US\$) | Electricity Generation (TWh) | FDI Inflow (US\$) | Biofuel Share (%) | Coal Share (%) | Fossil Fuel Share (%) | Gas Share (%) | Low Carbon Share (% Oil Share %) |        |
|-----|-----------|------|------|------------|------------------|-----------------------|------------------------------|-------------------|-------------------|----------------|-----------------------|---------------|----------------------------------|--------|
| 0   | Australia | AUS  | 1990 | 17041000   | 85.4             | 18249                 | 100                          | 6457776855        | 0                 | 42.032         | 95.922                | 15.869        | 4.078                            | 38.021 |
| 1   | Australia | AUS  | 1991 | 17272000   | 85.4             | 18860                 | 100                          | 2612066526        | 0                 | 43.151         | 95.609                | 15.31         | 4.331                            | 37.207 |
| 2   | Australia | AUS  | 1992 | 17486000   | 85.3             | 18824                 | 100                          | 4941906671        | 0                 | 42.972         | 95.648                | 15.68         | 4.352                            | 36.996 |
| 3   | Australia | AUS  | 1993 | 17687000   | 85.2             | 17700                 | 100                          | 5312435141        | 0                 | 42.05          | 95.654                | 15.806        | 4.346                            | 37.758 |
| 4   | Australia | AUS  | 1994 | 17883000   | 85               | 18129                 | 100                          | 4458484243        | 0                 | 41.263         | 95.871                | 16.881        | 4.129                            | 37.727 |
| 5   | Australia | AUS  | 1995 | 18077000   | 84.9             | 20446                 | 100                          | 13268875155       | 0                 | 41.562         | 96.069                | 16.603        | 3.931                            | 37.904 |
| 6   | Australia | AUS  | 1996 | 18272000   | 84.8             | 22020                 | 100                          | 4563952446        | 0                 | 42.196         | 96.058                | 16.313        | 3.942                            | 37.549 |
| 7   | Australia | AUS  | 1997 | 18468000   | 84.6             | 23645                 | 100                          | 8088068962        | 0                 | 43.239         | 96.146                | 15.623        | 3.854                            | 37.284 |
| 8   | Australia | AUS  | 1998 | 18665000   | 84.5             | 21478                 | 100                          | 7597610928        | 0                 | 44.139         | 96.246                | 15.718        | 3.754                            | 36.389 |
| 9   | Australia | AUS  | 1999 | 18864000   | 84.4             | 20698                 | 100                          | 2210917991        | 0                 | 44.911         | 96.283                | 15.425        | 3.717                            | 35.848 |
| 10  | Australia | AUS  | 2000 | 19066000   | 84.2             | 21853                 | 100                          | 14892978180       | 0                 | 45.039         | 96.291                | 15.649        | 3.709                            | 35.604 |
| 11  | Australia | AUS  | 2001 | 19269000   | 84.1             | 19681                 | 100                          | 10717133150       | 0                 | 44.177         | 96.406                | 16.724        | 3.594                            | 35.505 |
| 12  | Australia | AUS  | 2002 | 19475000   | 84.2             | 20291                 | 100                          | 14656321800       | 0                 | 44.511         | 96.341                | 16.959        | 3.659                            | 34.87  |
| 13  | Australia | AUS  | 2003 | 19697000   | 84.3             | 23705                 | 100                          | 8985246029        | 0                 | 45.106         | 96.275                | 16.839        | 3.725                            | 34.33  |
| 14  | Australia | AUS  | 2004 | 19948000   | 84.5             | 30819                 | 100                          | 42907672820       | 0                 | 45.491         | 96.284                | 16.623        | 3.716                            | 34.169 |
| 15  | Australia | AUS  | 2006 | 20574000   | 84.7             | 36570                 | 100                          | 30551100656       | 0.063             | 43.976         | 96.146                | 17.407        | 3.854                            | 34.763 |
| 16  | Australia | AUS  | 2007 | 20947000   | 84.8             | 41023                 | 100                          | 44440090037       | 0.239             | 43.046         | 96.19                 | 19.226        | 3.81                             | 33.918 |
| 17  | Australia | AUS  | 2008 | 21342000   | 84.9             | 49679                 | 100                          | 45100024270       | 0.564             | 44.14          | 96.148                | 18.598        | 3.852                            | 33.41  |
| 18  | Australia | AUS  | 2009 | 21739000   | 85.1             | 42810                 | 100                          | 28683266147       | 0.835             | 43.041         | 95.689                | 19.152        | 4.311                            | 33.496 |
| 19  | Australia | AUS  | 2010 | 22120000   | 85.2             | 52134                 | 100                          | 35210733743       | 1.255             | 39.77          | 94.963                | 22.123        | 5.037                            | 33.071 |
| 20  | Australia | AUS  | 2011 | 22480000   | 85.3             | 62596                 | 100                          | 6554890649        | 1.278             | 37.415         | 93.707                | 22.299        | 6.293                            | 33.992 |
| 21  | Australia | AUS  | 2012 | 22822000   | 85.4             | 68044                 | 100                          | 57500426822       | 1.192             | 35.471         | 93.859                | 22.643        | 6.141                            | 35.745 |
| 22  | Australia | AUS  | 2013 | 231501000  | 85.5             | 68158                 | 100                          | 54465480254       | 1.084             | 33.414         | 93.14                 | 23.806        | 6.86                             | 36.119 |
| 23  | Australia | AUS  | 2014 | 23475000   | 85.6             | 62513                 | 100                          | 6320729079        | 1.025             | 32.667         | 93.756                | 25.103        | 6.244                            | 35.886 |
| 24  | Australia | AUS  | 2015 | 23800000   | 85.7             | 56710                 | 100                          | 46992809567       | 0.917             | 33.326         | 93.496                | 25.97         | 6.504                            | 34.2   |
| 25  | Australia | AUS  | 2016 | 24126000   | 85.8             | 49875                 | 100                          | 42965050135       | 0.776             | 33.045         | 92.793                | 25.535        | 7.207                            | 34.213 |
| 26  | Australia | AUS  | 2017 | 24451000   | 85.9             | 53936                 | 100                          | 48198614234       | 0.878             | 31.977         | 93.115                | 25.289        | 6.885                            | 35.849 |
| 27  | Australia | AUS  | 2018 | 24772000   | 86               | 57207                 | 100                          | 60688590478       | 0.952             | 30.764         | 91.647                | 24.873        | 6.353                            | 36.01  |
| 28  | Australia | AUS  | 2019 | 25089000   | 86.1             | 54541                 | 100                          | 3895497515        | 0.87              | 27.819         | 91.433                | 30.184        | 5.567                            | 33.43  |
| 42  | Iceland   | ISL  | 1992 | 260000     | 91.1             | 27124                 | 100                          | 8648079           | 0                 | 2.904          | 40.448                | 0             | 59.552                           | 37.545 |
| 43  | Iceland   | ISL  | 1994 | 265000     | 91.5             | 24018                 | 100                          | 2394198           | 0                 | 2.821          | 40.389                | 0             | 59.611                           | 37.568 |
| 44  | Iceland   | ISL  | 1996 | 270000     | 91.8             | 27614                 | 100                          | 83381484          | 0                 | 3.006          | 41.624                | 0             | 55.376                           | 38.619 |
| 45  | Iceland   | ISL  | 1997 | 273000     | 92               | 27919                 | 100                          | 148012830         | 0                 | 2.976          | 39.155                | 0             | 60.845                           | 36.179 |
| 46  | Iceland   | ISL  | 1998 | 275000     | 92.1             | 31030                 | 100                          | 154082591         | 0                 | 2.47           | 36.741                | 0             | 63.259                           | 34.271 |
| 47  | Iceland   | ISL  | 1999 | 278000     | 92.3             | 32381                 | 100                          | 66639312          | 0                 | 2.637          | 33.872                | 0             | 66.128                           | 31.234 |
| 48  | Iceland   | ISL  | 2000 | 280000     | 92.4             | 32096                 | 100                          | 155160734         | 0                 | 3.435          | 33.419                | 0             | 66.581                           | 29.084 |
| 49  | Iceland   | ISL  | 2001 | 283000     | 92.5             | 28897                 | 100                          | 163445772         | 0                 | 3.688          | 31.539                | 0             | 66.461                           | 27.851 |
| 50  | Iceland   | ISL  | 2002 | 285000     | 92.7             | 32409                 | 100                          | 91905493          | 0                 | 3.537          | 31.43                 | 0             | 66.57                            | 27.893 |
| 51  | Iceland   | ISL  | 2003 | 288000     | 92.8             | 39476                 | 100                          | 335355205         | 0                 | 3.456          | 31.51                 | 0             | 66.49                            | 28.054 |
| 52  | Iceland   | ISL  | 2004 | 291000     | 92.9             | 47334                 | 100                          | 755317000         | 0                 | 3.548          | 32.307                | 0             | 67.693                           | 28.759 |
| 53  | Iceland   | ISL  | 2005 | 295000     | 93               | 56794                 | 100                          | 3093680067        | 0                 | 3.373          | 32.543                | 0             | 67.457                           | 29.17  |
| 54  | Iceland   | ISL  | 2006 | 300000     | 93.2             | 57492                 | 100                          | 3876554983        | 0                 | 3.146          | 30.161                | 0             | 69.839                           | 27.015 |
| 55  | Iceland   | ISL  | 2007 | 305000     | 93.3             | 69495                 | 100                          | 6872169567        | 0                 | 2.946          | 26.672                | 0             | 73.328                           | 23.727 |
| 56  | Iceland   | ISL  | 2008 | 311000     | 93.4             | 56843                 | 100                          | 1203686964        | 0                 | 2.054          | 19.666                | 0             | 80.334                           | 17.612 |
| 57  | Iceland   | ISL  | 2009 | 316000     | 93.5             | 41301                 | 100                          | 63588140          | 0                 | 1.903          | 18.254                | 0             | 81.746                           | 16.351 |
| 58  | Iceland   | ISL  | 2010 | 320000     | 93.6             | 43237                 | 100                          | 256982201         | 0                 | 2.006          | 17.666                | 0             | 82.334                           | 15.66  |
| 59  | Iceland   | ISL  | 2011 | 323000     | 93.6             | 47714                 | 100                          | 1106958185        | 0                 | 2.005          | 17.452                | 0             | 82.545                           | 15.447 |
| 60  | Iceland   | ISL  | 2012 | 326000     | 93.6             | 45995                 | 100                          | 1024164328        | 0                 | 2.031          | 17.162                | 0             | 82.835                           | 15.13  |
| 61  | Iceland   | ISL  | 2013 | 327000     | 93.6             | 49804                 | 100                          | 472607545         | 0                 | 2.265          | 17.588                | 0             | 82.367                           | 15.324 |
| 62  | Iceland   | ISL  | 2014 | 328000     | 93.7             | 54576                 | 100                          | 760775539         | 0                 | 1.858          | 17.905                | 0             | 82.011                           | 16.047 |
| 63  | Iceland   | ISL  | 2015 | 330000     | 93.7             | 52551                 | 100                          | 1145767444        | 0                 | 1.969          | 18.744                | 0             | 81.019                           | 16.775 |
| 127 | Singapore | SGP  | 1990 | 3013000    | 100              | 11861                 | 100                          | 5574738855        | 0                 | 0.091          | 99.914                | 0             | 0.086                            | 99.822 |
| 128 | Singapore | SGP  | 1991 | 3097000    | 100              | 14502                 | 100                          | 4887094440        | 0                 | 0.053          | 99.755                | 0             | 0.245                            | 99.702 |
| 129 | Singapore | SGP  | 1992 | 3189000    | 100              | 16135                 | 100                          | 2204342221        | 0                 | 0.072          | 99.772                | 3.501         | 0.228                            | 96.169 |
| 130 | Singapore | SGP  | 1993 | 3288000    | 100              | 18290                 | 100                          | 4686312017        | 0                 | 0.073          | 99.791                | 4.37          | 0.209                            | 95.349 |
| 131 | Singapore | SGP  | 1994 | 3385000    | 100              | 21553                 | 100                          | 8550165226        | 0                 | 0.076          | 99.818                | 3.821         | 0.182                            | 95.92  |
| 132 | Singapore | SGP  | 1995 | 3479000    | 100              | 24914                 | 100                          | 11942852103       | 0                 | 0.034          | 99.825                | 3.665         | 0.175                            | 96.126 |
| 133 | Singapore | SGP  | 1996 | 3566000    | 100              | 26233                 | 100                          | 11432363956       | 0                 | 0.001          | 99.827                | 3.632         | 0.173                            | 96.194 |

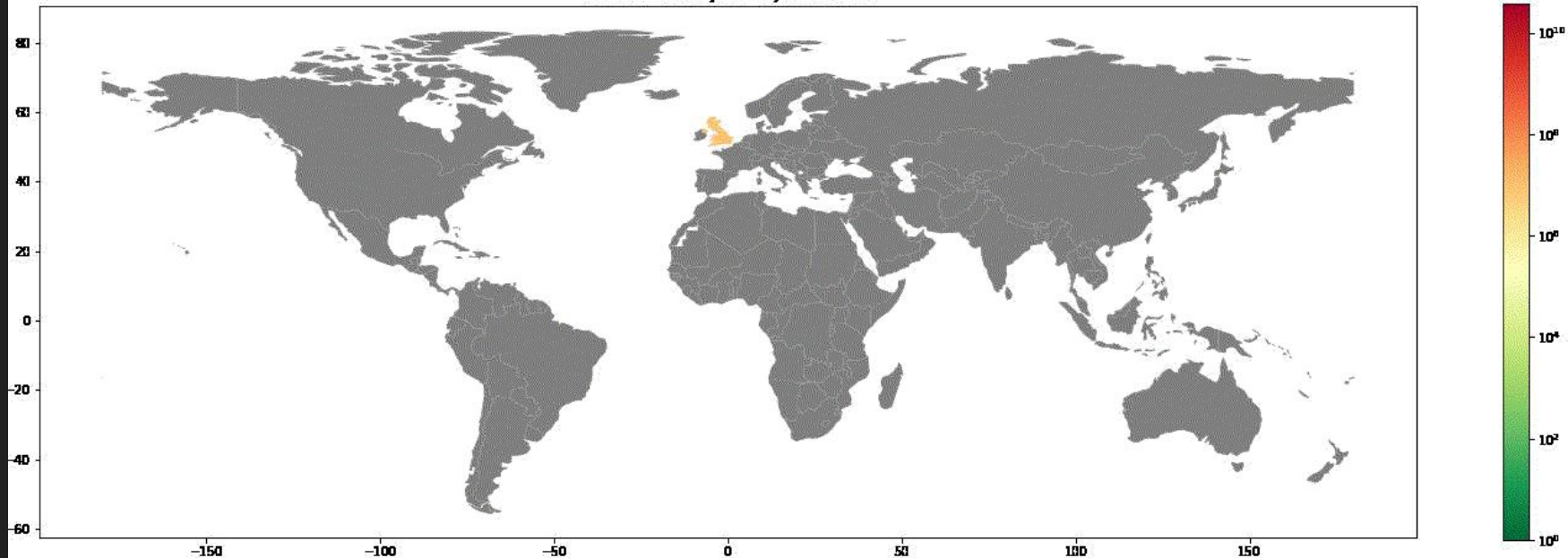


CO<sub>2</sub> Emissions

|       |              |
|-------|--------------|
| count | 1.710000e+02 |
| mean  | 2.102999e+08 |
| std   | 9.869335e+08 |
| min   | 0.000000e+00 |
| 25%   | 5.548892e+06 |
| 50%   | 2.032710e+07 |
| 75%   | 8.857515e+07 |
| max   | 1.147237e+10 |



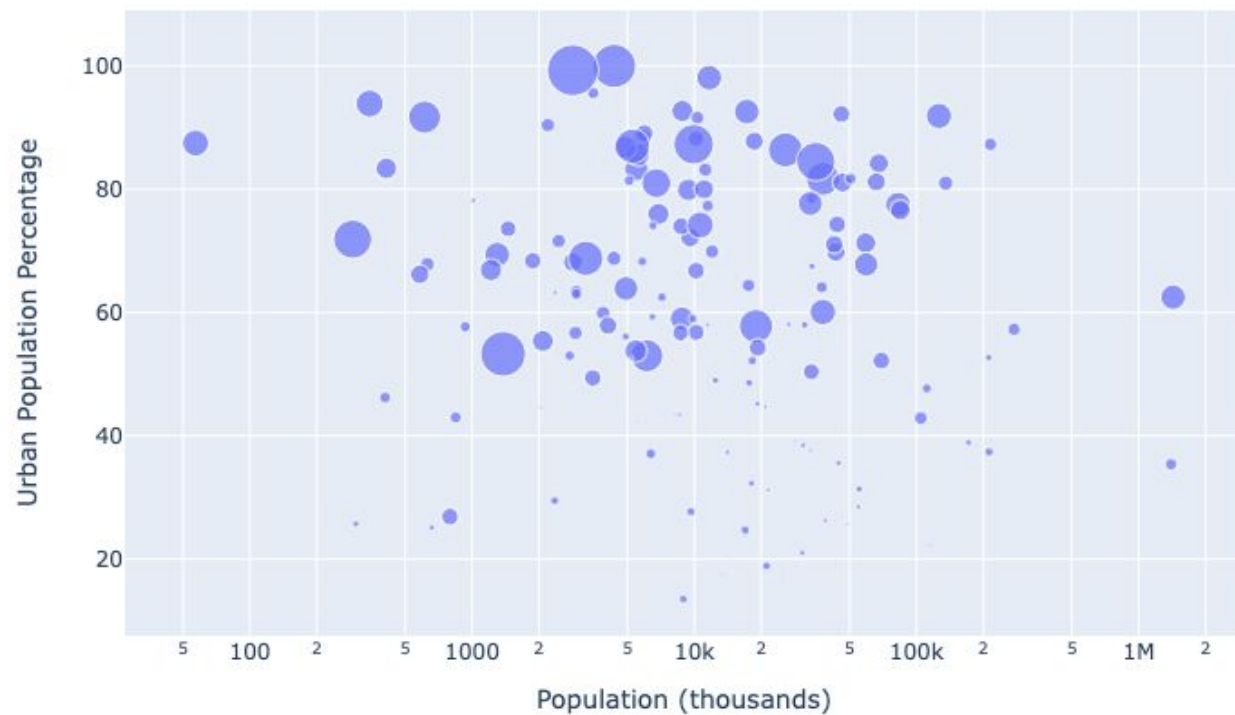
CO2 Emissions by Country 1750 (tons)



# Predicting Variables

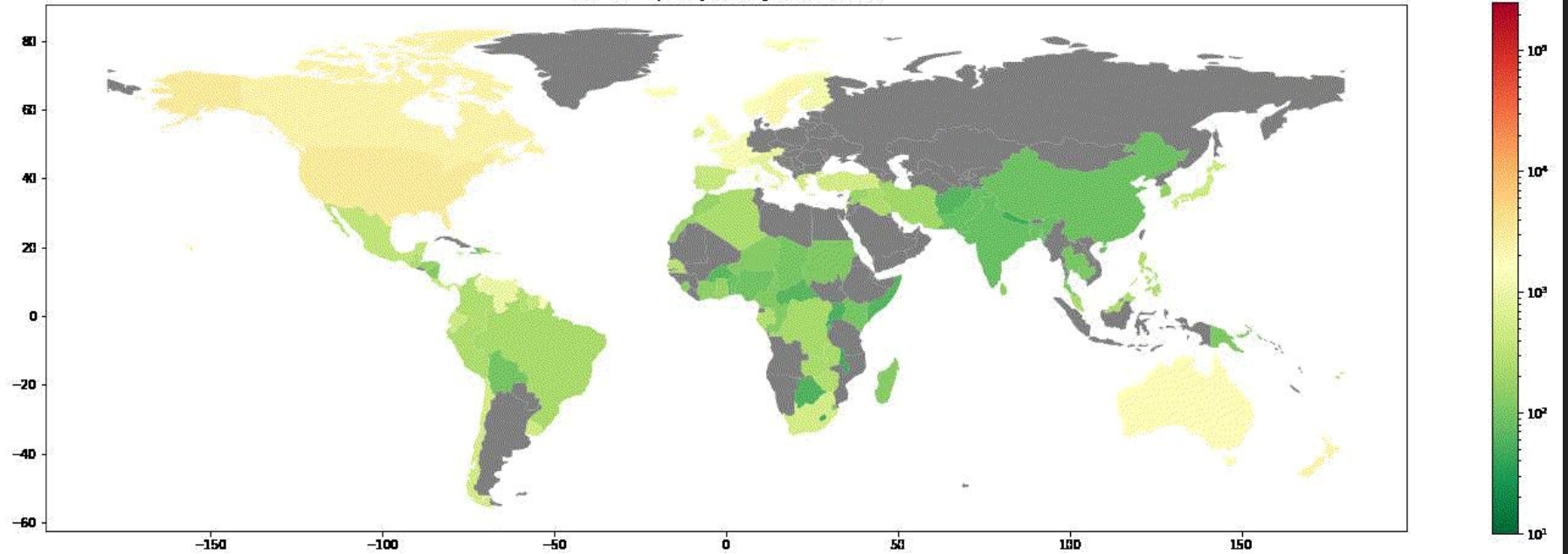
# 1. Population

Per Capita Emissions vs Population and Urban Population Percentage



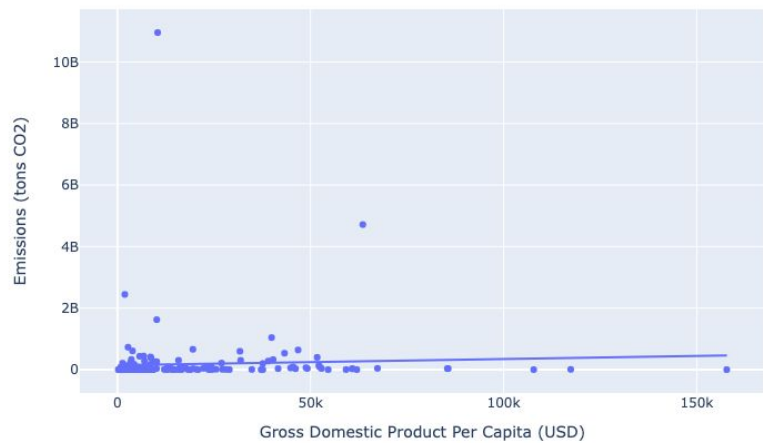
## 2. GDP Per Capita

GDP Per Capita by Country in 1960 (USD)

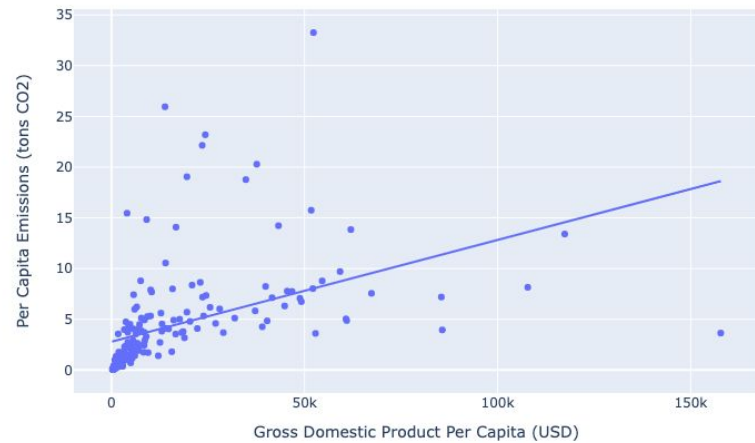




Emissions vs GDP Per Capita

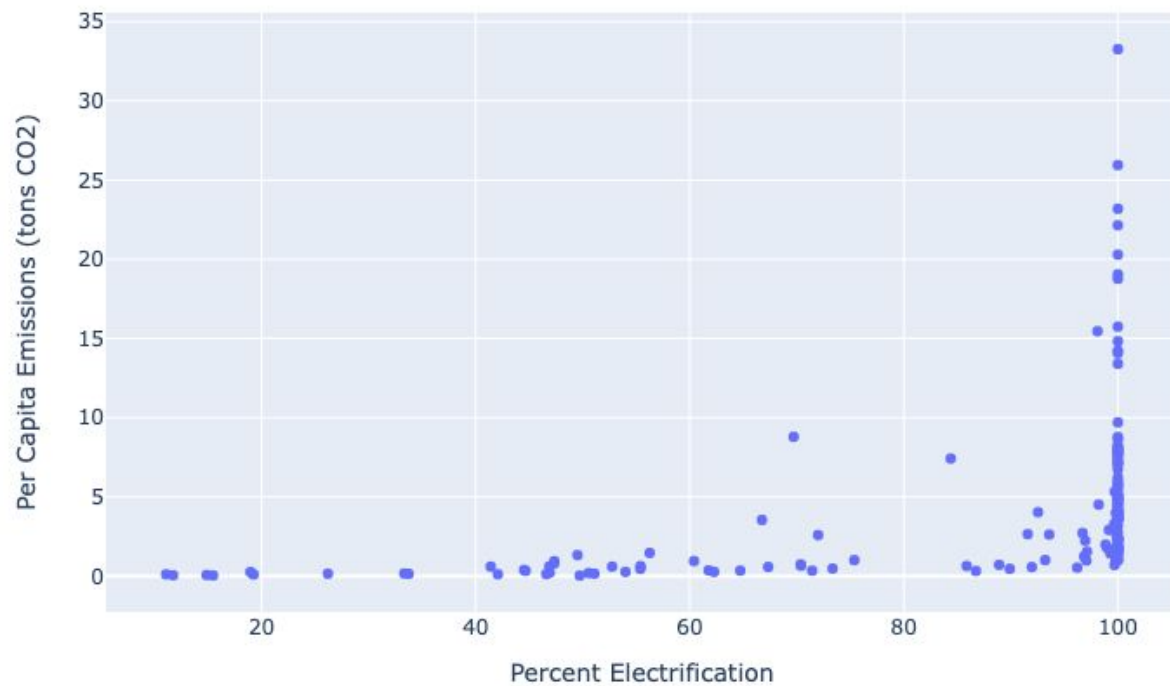


Per Capita Emissions vs GDP Per Capita



### 3. Electrification

## Electrification vs Per Capita Emissions



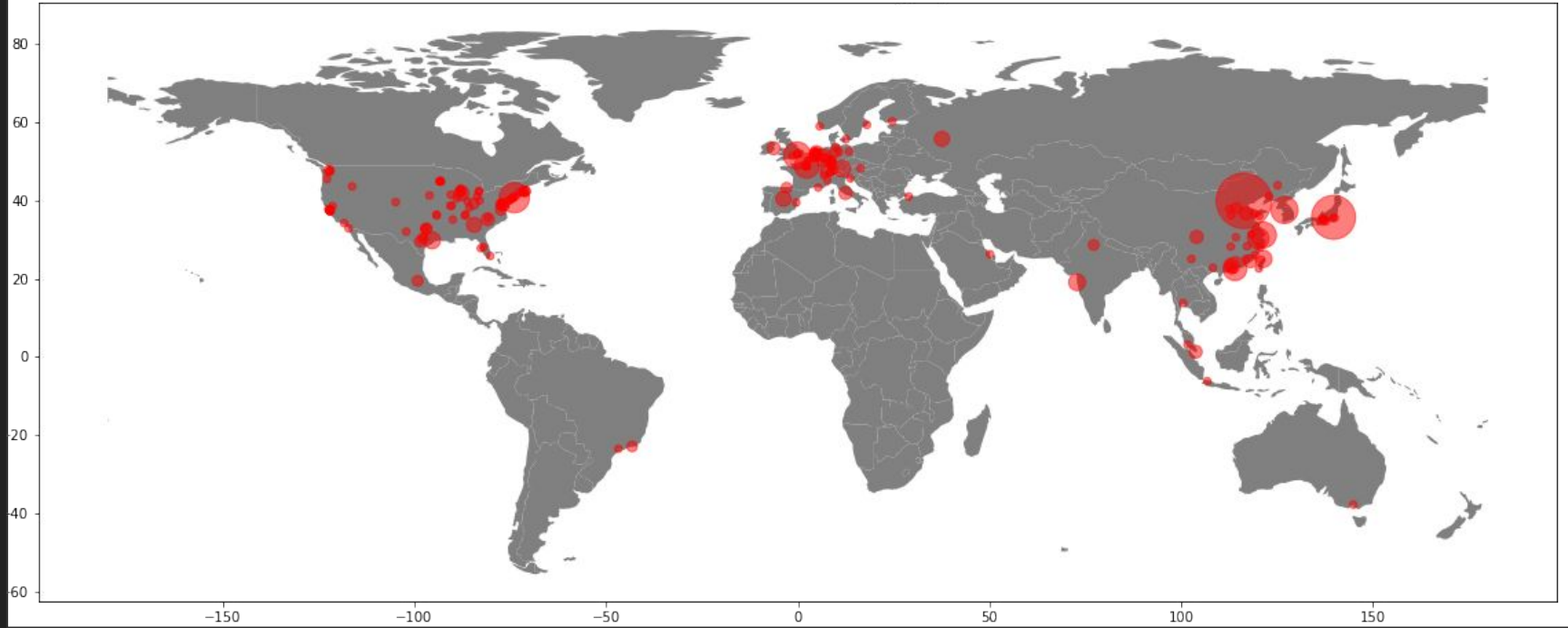
## 4. Foreign Direct Investment

## FDI vs Emissions

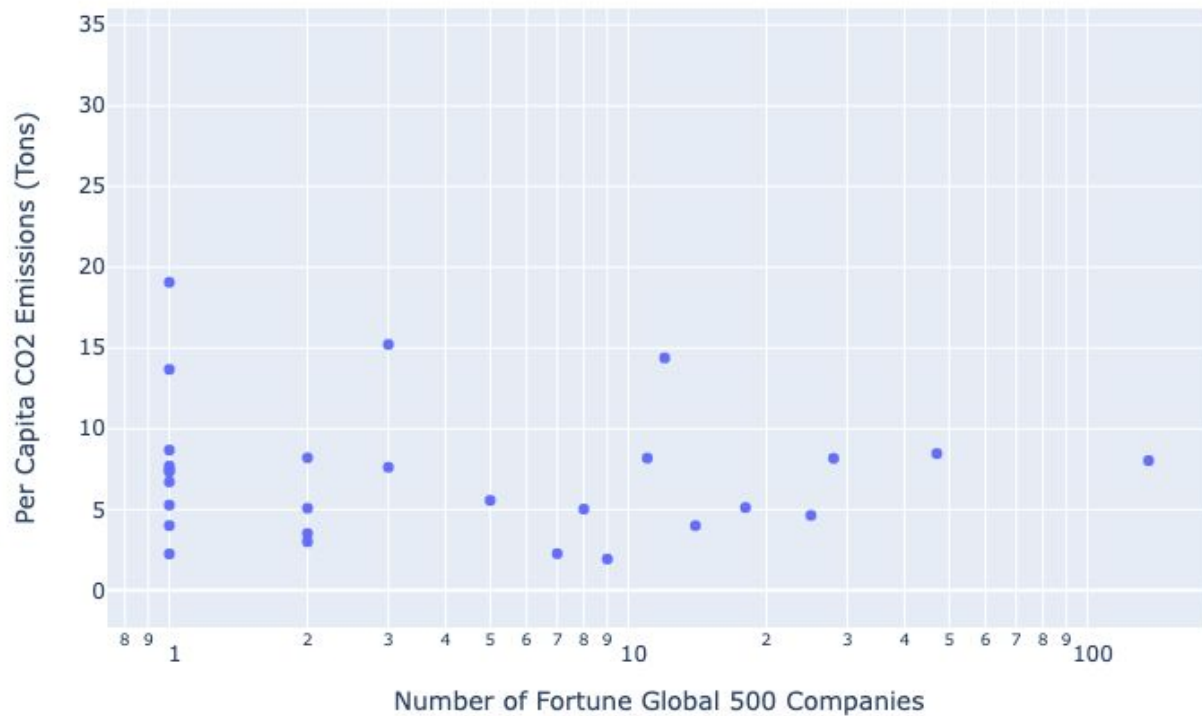


## 5. Fortune 500 Companies

Fortune Global 500 Countries by City



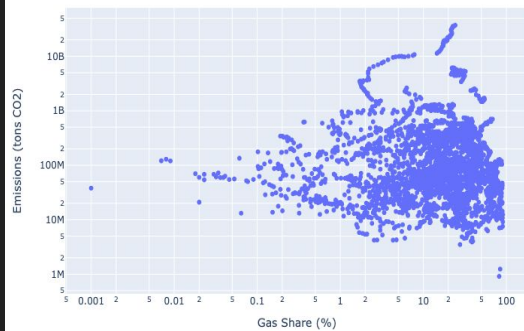
## Fortune 500 Companies vs Per Capita Emissions



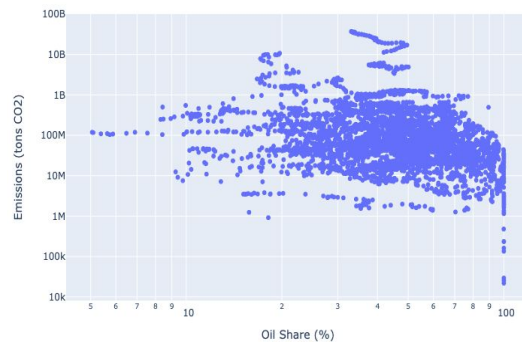


## 6. Energy Sectors

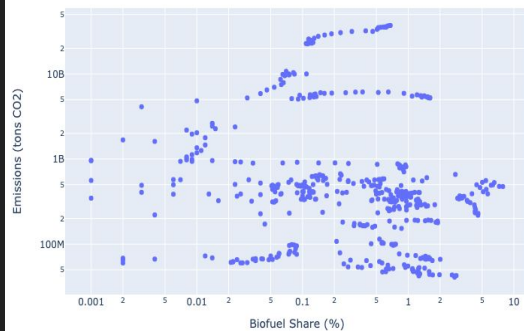
Gas Share (%) vs Emissions



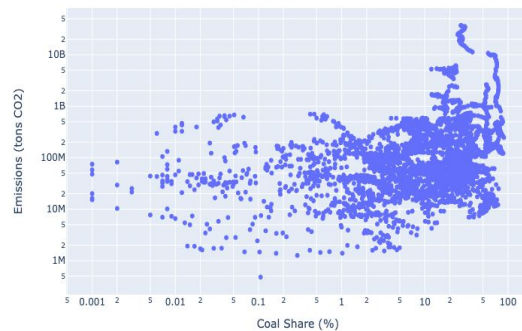
Oil Share (%) vs Emissions



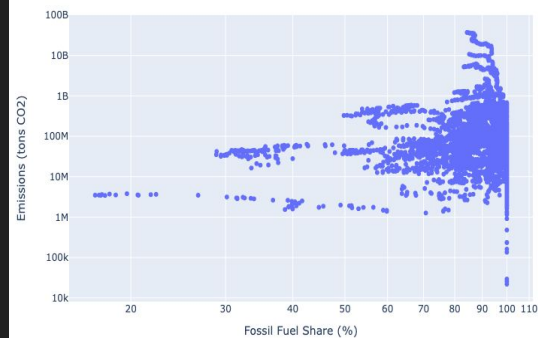
Biofuel Share (%) vs Emissions



Coal Share (%) vs Emissions

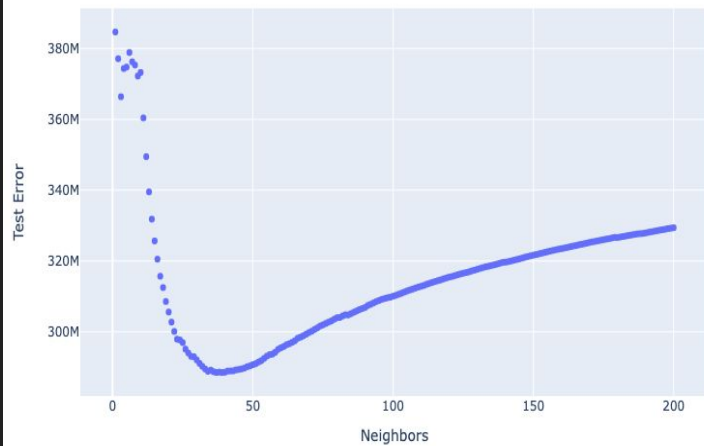


Fossil Fuel Share (%) vs Emissions

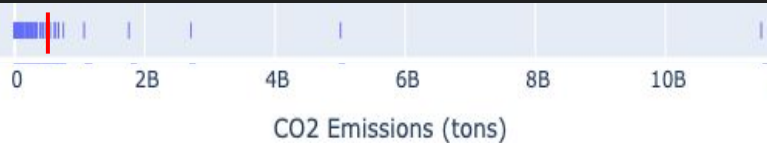
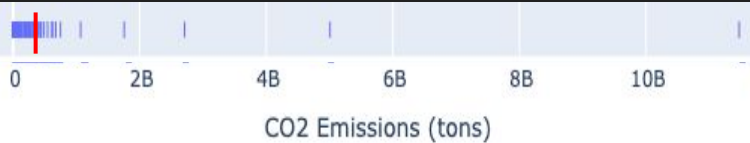
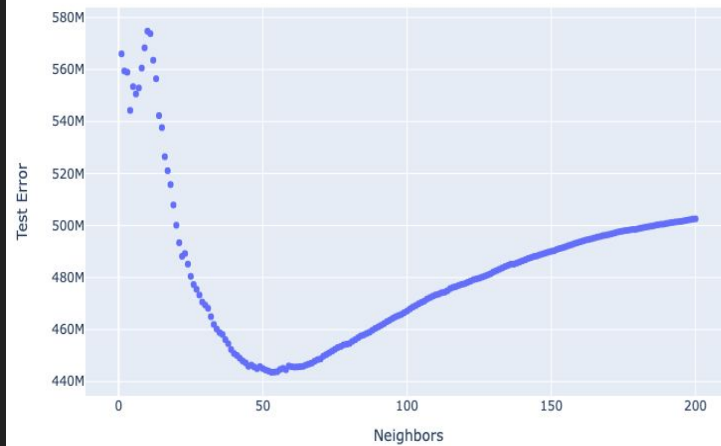


# Machine Learning

Test Error for K-Nearest Neighbors Regressor without Energy

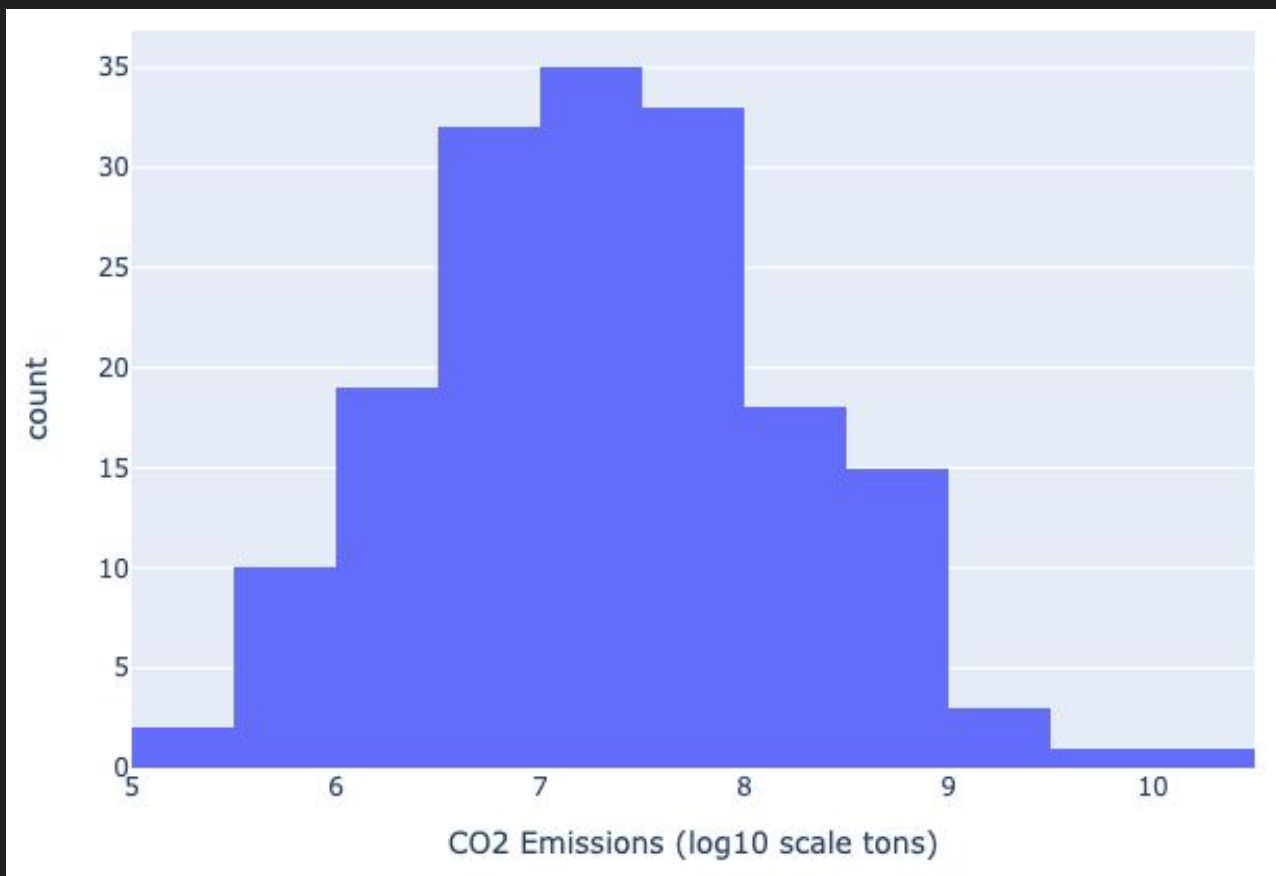


Test Error for K-Nearest Neighbors Regressor with Energy



|                                       | Without Energy Data                    | With Energy Data                       |
|---------------------------------------|--|--|
| K-Nearest Neighbors                   | $2.9 \times 10^8$ tons CO <sub>2</sub> | $4.4 \times 10^8$ tons CO <sub>2</sub> |
| Linear Regression                     | $4.4 \times 10^8$ tons CO <sub>2</sub> | $7.9 \times 10^8$ tons CO <sub>2</sub> |
| Voting Ensemble                       | $3.3 \times 10^8$ tons CO <sub>2</sub> | $5.6 \times 10^8$ tons CO <sub>2</sub> |
| XGBoost                               | $3.2 \times 10^8$ tons CO <sub>2</sub> | $6.4 \times 10^8$ tons CO <sub>2</sub> |
| XGBoost with<br>Hyperparameter Tuning | $2.7 \times 10^8$ tons CO <sub>2</sub> | $5.1 \times 10^8$ tons CO <sub>2</sub> |

# Log Normal Distribution



# Normal RMSE

$$y_{\text{pred}} + \text{RMSE} = y_{\text{true}}$$

Off by Sum

# Log Scale RMSE

$$\log_{10}(y_{\text{pred}}) + \text{RMSE} = \log_{10}(y_{\text{true}})$$

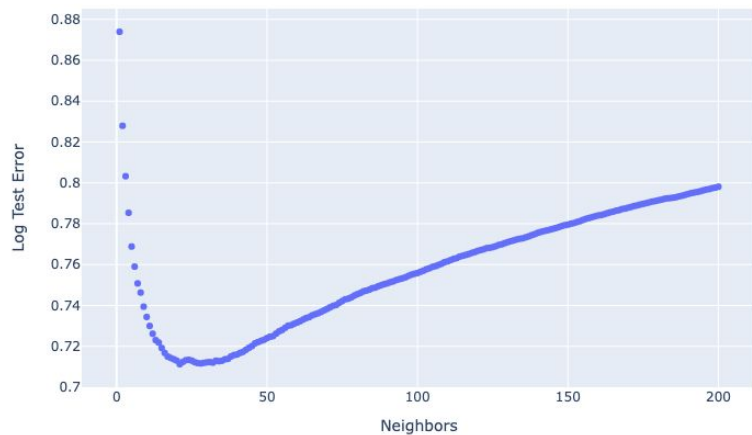
$$10^{\log_{10}(y_{\text{pred}}) + \text{RMSE}} = 10^{\log_{10}(y_{\text{true}})}$$

$$y_{\text{pred}} * 10^{\text{RMSE}} = y_{\text{true}}$$

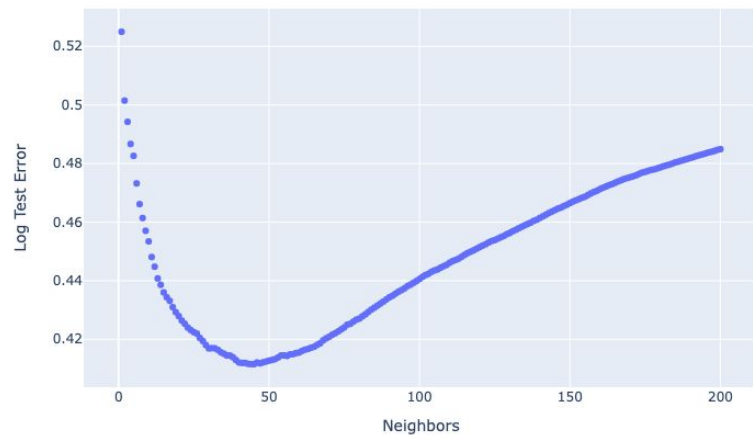
Off by Factor



Test Error for K-Nearest Neighbors Regressor without Energy



Test Error for K-Nearest Neighbors Regressor with Energy



|                                       | Without Energy Data | With Energy Data |
|---------------------------------------|---------------------|------------------|
| K-Nearest Neighbors                   | 0.711               | 0.411            |
| Linear Regression                     | 0.846               | 0.423            |
| Voting Ensemble                       | 0.739               | 0.374            |
| Stacking Ensemble                     | 0.707               | 0.385            |
| XGBoost                               | 0.325               | 0.268            |
| XGBoost with<br>Hyperparameter Tuning | 0.301               | 0.258            |

Accuracy

# Normal RMSE

RMSE > Mean

RMSE  $\approx$  30% std

ML is about 3x as accurate as  
guessing the average value

# Log Scale RMSE

RMSE = 0.258

$$y_{\text{pred}} * 10^{0.258} = y_{\text{true}}$$
$$y_{\text{pred}} * 1.8 = y_{\text{true}}$$

ML is within a factor of 2  
on average