

The ensemble nature of allostery

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Allostery is the process by which biological macromolecules (mostly proteins) transmit the effect of binding at one site to another, often distal, functional site, allowing for regulation of activity. Recent experimental observations demonstrating that allostery can be facilitated by dynamic and intrinsically disordered proteins have resulted in a new paradigm for understanding allosteric mechanisms, which focuses on the conformational ensemble and the statistical nature of the interactions responsible for the transmission of information. Analysis of allosteric ensembles reveals a rich spectrum of regulatory strategies, as well as a framework to unify the description of allosteric mechanisms from different systems.

llostery, first articulated more than 50 years ago¹⁻³, has remained a central focus in biology, owing to the fact that a quantitative description of allostery is fundamental to an understanding of most processes beyond the molecular level, such as cellular signalling⁴ and disease⁵. Allostery has even been referred to as the 'second secret of life'6.7. In spite of its importance, allosteric mechanisms in most instances remain a biophysical enigma, eluding a general, quantifiable and predictive atomic description^{7,8}.

Through the lens of history, it is clear that allosteric concepts and models have evolved over decades as the experimental technologies have improved. The first allosteric proteins studied, such as haemoglobin9, were extensively structured and thus amenable to high-resolution X-ray crystallography. Models of allosteric mechanisms based on such studies were understandably greatly influenced by the static structural images^{10,11}. However, as more experimental structural, dynamic and thermodynamic approaches have been developed, descriptions for allostery have necessarily become more complex. The largely qualitative, static images of end point protein structures have been replaced by more quantitative, dynamic views of allostery, which, unlike static structural models, are more difficult to visualize. Here the historically dominant paradigm of structure-based allostery^{11–14} is briefly reviewed and placed in the context of new discoveries, revealing that allostery can also be associated with changes in dynamics and largescale conformational disorder^{15–18}. Indeed, more recent discoveries emphasize how nature uses the full spectrum of conformational heterogeneity¹⁹ (for example, rigid body movement^{20–22}, folded yet dynamic structure^{4,23–27}, and intrinsic disorder^{28–30}) to facilitate allostery. These recent discoveries challenge traditional understanding of allostery and provide the foundations for developing a framework that unifies descriptions of allostery in structured, dynamic and disordered systems.

From structures to ensembles

The first statement of allostery³¹, arising from the classic experiments of Changeux², is that two distinct sites within one protein, each binding different ligands, could nonetheless interact despite being 'non-overlapping' (that is, presumably distant from each other) in the molecular structure. This 'action at a distance' phenomenon was difficult to interpret in the absence of structural information or site-specific biochemical data.

For decades, the two dominant models for allostery were the 'sequential', or KNF (Koshland–Nemethy–Filmer), model³² and the 'symmetric', or MWC (Monod–Wyman–Changeux), model³. Both proposals were influential and agreed on the importance of conformational change between two well-defined structural end states³³. Whereas the MWC model posited the existence of two pre-existing quaternary states (tensed (T) and relaxed (R)), whose equilibrium was shifted upon binding ligand³, the KNF

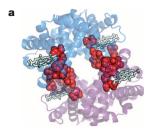
model was based on the appealing, general notion of the inherent flexibility of proteins³² and 'induced-fit' of a binding site in response to ligand^{34,35}. Importantly, both models were successful in describing allostery^{31–36}.

However, it is well known that both the MWC and KNF models are phenomenological³³, and consequently, do not provide insight into how the structure facilitates allosteric communication between sites. It was the birth of structural biology and the development of the influential stereochemical model by Perutz^{10,13} that first addressed this issue and set the course for future allosteric studies. According to this model, which was built upon by many others^{33,37,38}, allostery could be understood in terms of structural changes that could be gleaned through inspection of the high-resolution structure. This structural view of allosteric mechanism has been the reigning paradigm ever since^{39–43}, with some approaches even positing the existence of conserved allosteric pathways that presumably mediate the transmission of information between sites. In fact, such pathways are even evident in haemoglobin⁴⁴ (Fig. 1a).

Nonetheless, the notion that something was amiss (or at least incomplete) with a purely structure-centric understanding of allostery had been recognized for decades. In a classic thermodynamic study of haemoglobin, Parsegian and colleagues⁴⁵ found that the T-to-R transition in haemoglobin involved the binding of approximately 60 additional water molecules (Fig. 1b), and noted "... it is doubtful that the R state would even exist without the stabilization promoted by hydration of the extra surface." In effect, the entire molecule must have a role in mediating allostery. Contrasting the different 'images' of allostery conveyed by Fig. 1 reveals the challenge in quantitatively describing mechanism. Clearly, an understanding of allostery requires not only knowledge of the concerted structural changes between two binding sites, but also the factors that render an allosteric protein 'poised to undergo' the structural change.

The Parsegian quote itself hints at the realization (well-appreciated by the authors of the early models) that allosteric transitions involve multiple states, whose relative populations must be tunable over a range of physiological conditions. Nonetheless, the fact that initial structures were found for the T and R forms of haemoglobin supported the notion that allostery as a general phenomenon might be understood, perhaps in all systems, if only the structures of the allosteric states could be determined. To that end, extensive molecular dynamics^{33,46,47} and coarse-grained network simulation^{20,48} (for those proteins in which rigid body motions could be proposed for the allosteric transition) further suggested that 'allosteric mechanisms reliant primarily upon observable changes in the ensemble-average structure are common and may be dominant'²⁰. Although the discovery of an alternate 'relaxed' structure of haemoglobin by Arnone and co-workers⁴⁹ laid to rest the simple two-state view of allostery, at least for haemoglobin, not fully appreciated was the range of possible regulatory

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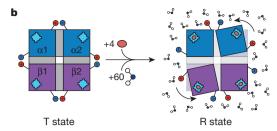


Figure 1 | Structure-based views of allostery. a, Ribbon diagram representation of tetrameric haemoglobin (PDB accession 1GZX) rendered in PyMol (Schrödinger). The proposed pathway responsible for the cooperative transition from tensed (T) to relaxed (R) is highlighted with red spheres and the haem groups are represented as light blue sticks⁴⁴. b, Allosteric transition of tetrameric haemoglobin, as proposed by Perutz^{10,13}. Tetrameric haemoglobin in the T state is depicted on the left with the two α-subunits (blue) and the two

 β -subunits (purple) each with their own haem group (light blue). Salt bridges, depicted as the red positive and blue negative charges, hold the molecule in the T conformation, and these salt bridges are released upon binding of oxygen (orange oval) in the transition to the R conformation (on the right) accompanied by a 15° turn of the subunits relative to each another. Also contributing to the equilibrium are 60 additional water molecules preferentially binding the R state 45 .

strategies that could be used if the full spectrum of binding and conformational states of proteins were to be harnessed.

In 1984 Cooper and Dryden touched on one such possibility when proposing that allostery could be manifested from changes in the width of a conformational distribution, raising the spectre of significant entropic contributions to allostery⁵⁰. These authors rigorously demonstrated, using a statistical thermodynamic formalism, that changes in the frequency and amplitude of thermal fluctuations in a protein upon ligand binding could result in cooperative energies on the order of a few kcal per mol without perturbing the average structure. Importantly, such a situation would be difficult to reconcile by simple inspection of the end-state structures, explaining why experimental examples had escaped detection until recently. The work of Cooper and Dryden has proven prescient³³. The term 'dynamic allostery' has even found its way into the modern lexicon, ostensibly to describe the role of entropy in the thermodynamics of allostery, although unfortunately it is often conflated with motions between relevant ensembles. However, with the development of NMR techniques to study allosteric protein systems at a site-resolved level, both aspects of the role of motion in transitions between functional states are becoming illuminated^{51–55}.

One of the most surprising observations over the past half-decade has been the appearance of allostery in intrinsically disordered proteins (IDPs), systems that are defined by a lack of fixed structure, exhibiting instead extreme conformational fluctuations^{56–60}. Clearly both conformational dynamics of folded structures and large-scale disorder are important for allostery⁶¹, but quantitatively understanding this phenomenon remains a challenge. It is not obvious how the phenomenon of allostery can be understood and described in terms that can do equal justice to both highly structured and highly disordered systems.

Below, we use several recently studied allosteric systems, spanning the continuum of structure/dynamics classification space (Fig. 2), to show how changes in dynamics and disorder are phenomenologically associated with allostery. Initially highlighted are the challenges associated with reconciling allostery in terms of classic structural or deterministic models. However, when allosteric proteins are viewed as ensembles of states, an entirely new palette of expected behaviour is revealed. Importantly, it becomes clear that taxonomic schemes segregating allosteric proteins by amount and/or type of dynamics that change during an allosteric transition may actually obscure similarities between mechanisms that are only phenomenologically different (Box 1). The ensemble nature of allostery revealed through analysis of the full dynamic spectrum of allosteric systems permits a rich repertoire of regulatory strategies and illuminates key organizing principles for describing allostery.

The dynamic continuum of allostery

Arguably the most significant experimental advance in the analysis of allostery has been the development of NMR spectroscopy, which provides information about protein structure, dynamics and thermodynamics ^{16,53,54}. Although the high-resolution structure of a protein provides exquisite insight into the enthalpic contributions of structure and solvent to protein

thermodynamics⁶², the role of entropy remains obscure. The idea of using fast internal motion detected by solution NMR as a proxy for conformational entropy was introduced some time ago^{63,64}, where motion evaluated assuming a specific motional model provided an indirect measure of the number of states visited. The detection of motion in proteins over a wide range of timescales is now well established, but it is the fast picosecond-tonanosecond timescale that seems to be most important for the detection of conformational entropy⁶⁵⁻⁶⁷. The initial model-dependent interpretation of protein dynamics in terms of entropy was problematic⁶⁵ but its use did reveal the probable presence of a large contribution from conformational entropy to the free energy of protein-ligand interactions^{68,69}. To overcome many of the technical difficulties associated with using a dynamic proxy for conformational entropy, Wand and co-workers developed an empirical 'entropy meter' that appears able to quantitatively relate changes in fast internal protein motion measured by NMR relaxation to changes in conformational entropy^{54,70}. This approach has been used to demonstrate the integral role of conformational entropy in molecular recognition by calmodulin⁷⁰ and the catabolite activator protein (CAP)²⁴. The calmodulin

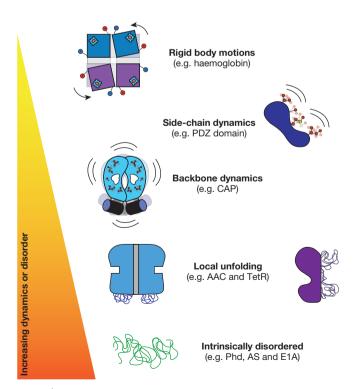
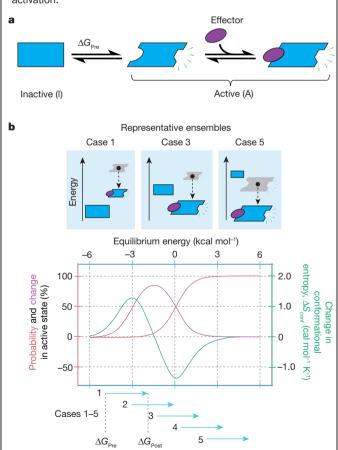


Figure 2 | The dynamic continuum of allosteric phenomena. Schematic representation of allosteric systems with increasing dynamics, disorder or fluctuations on the vertical axis.

BOX 1

Tunable sensitivity in allosteric ensembles

Tuning the sensitivity of the ensemble to an allosteric effector. a, Twostate allosteric protein wherein the effector ligand binds to and stabilizes the active state. This equilibrium (ΔG_{Pre}) can be shifted (ΔG_{Post}) by adding effector. **b.** Shown is the response of the system to an allosteric effector that increases the stability of the active state by 3 kcal mol⁻¹. The observed response is dependent on where the equilibrium is poised before activation. When the inactive state is too dominant (b, top, case 1), activation (that is, adding effector) produces a modest change in activity and an increase in the conformational entropy, S_{conf} (= $-R\Sigma P_i ln P_i$, where P_i is the probability of the *i*th state and the summation is over all states in the ensemble). When the active state is already dominant (case 5), activation again produces a modest effect, but in this case the conformational entropy decreases. Under conditions in which both states are populated (case 3), the change in activity is maximal, but the change in conformational entropy is near zero. This is depicted quantitatively in the graph in the bottom of b: the probability of being active (red), the change in activity (purple) and the change in conformational entropy (green) as a function of ΔG_{Pre} . Importantly, the free energy before (ΔG_{Pre}) and after (ΔG_{Post}) addition of effector ligand determines how the ensemble is poised, which in turn determines both the degree of activity change and whether conformational entropy (as determined from a positions-specific probe of dynamics) will increase, decrease or remain constant upon activation.



system provided illustrations of the various types of dynamical perturbation that can occur: purely local, long-range or directed dynamical transmission, which is perhaps the key to dynamically mediated allostery⁷¹.

The CAP system has been particularly important in exploring the role of conformational entropy in allostery, as discussed below.

NMR analyses of allosteric proteins have revealed a cornucopia of ways that changes in dynamics are associated with allosteric transitions. Indeed, a continuum of dynamic allosteric phenomena has been observed, ranging from rigid body structural changes to intrinsically disordered proteins mediating the response (Fig. 2). The existence of this dynamic continuum suggests that although the two extremes of the spectrum represent radically different structural 'pictures' of allostery, they should nonetheless be amenable to a unified description.

Structured yet dynamic allosteric systems

The classic view of an allosteric protein is one of structure. The protein may have one or more domains or subunits whose structure can be determined, but which may show conformational dynamics when observed in NMR experiments. Many examples of structured allosteric proteins that show dynamic changes have been documented^{4,18,23–26,72}. For reasons described below, these are ideal systems to probe ensemble properties. For now we simply note that the analyses of these types of systems have revealed a number of interesting paradoxes.

Since the initial prediction of dynamic allostery without conformational change by Cooper and Dryden⁵⁰, two important experimental studies have gone on to show that allostery can indeed be manifested essentially without structural change. The first study focused on CAP, a homodimeric transcription factor consisting of a cyclic AMP (cAMP) binding domain coupled to a DNA binding domain (DBD) (Fig. 3a). The biological role of CAP is to bind cAMP, allowing CAP to activate transcription (Fig. 3a, right). Extensive studies have revealed that conformational entropy via backbone and side-chain dynamics is associated with the allosteric response of the system upon cAMP binding^{24–26}. Whether the entire entropic penalty arises from quenching of dynamics upon ligand binding is an open question³³, but certainly a significant contribution of the allosteric response is associated with the quenching of dynamics. Interestingly, highresolution NMR spectroscopy has revealed that the population of bindingcompetent states for wild-type and mutants of CAP in solution is not proportional to the overall binding affinity. Instead, the entropic effects for a number of mutants were shown to correlate with the conformational entropy determined from NMR order-parameters²⁴. In this case, the entropic penalty seems to be the basis of the negative cooperativity binding cAMP increases dynamics in the adjacent domain that must be quenched to bind the second ligand. Interestingly, a recent study of CAP using elastic network models demonstrated that modulation of the normal modes can reproduce these results and can be used to rationally modulate the cooperativity of ligand binding⁷³.

In a second important study, removal of an α -helix ($\Delta \alpha 3$) from a canonical PDZ domain resulted in an increase in side-chain dynamics of the distal binding site 23 (Fig. 3b). The helix in question was presumed to be a molecular scaffold and not expected to affect binding, because it was not present in most other PDZ domains and was physically distal from the binding site²³. Unexpectedly, deletion of α3 (depicted blue in Fig. 3b, right) resulted in a 25-fold reduction in binding affinity that was almost entirely entropic in nature, as determined by isothermal titration calorimetry. NMR studies revealed no global structural perturbations, and relaxation experiments showed no significant changes in the backbone dynamics. The only detectable differences were observed in the side-chain dynamics (Fig. 3b, top right) and the calorimetrically determined entropy change (in other words, the dynamics in the unliganded state). Both the CAP and the PDZ examples were pioneering studies that not only revealed the predicted importance of dynamics and the role of conformational entropy in allosteric mechanism, but also highlighted the limitations of deducing mechanism from static structure alone.

Local unfolding and intrinsic disorder

Moving down the dynamic continuum (bottom of Fig. 2), one of the more recent developments is the realization that local unfolding and intrinsic disorder ⁶¹ can have a significant role in allosterically coupling domains to

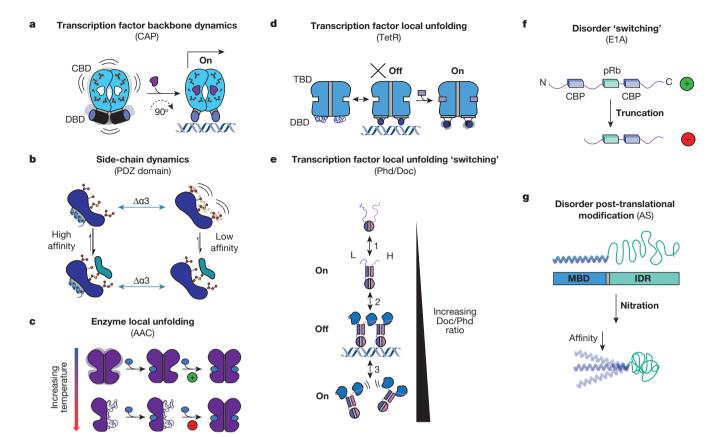


Figure 3 | Allosteric systems from the dynamic continuum. a, CAP homodimer with a cyclic nucleotide binding domain (CBD, blue domains with side chains) and a DNA binding domain (DBD, blue cylinders). Binding energetics of cAMP (purple ligand) quench dynamics in the bound-state ensemble and induce a 90° change in the conformation of the DBD, allowing it to bind DNA and turn on transcription^{24–26}. b, Side-chain dynamics modulate the binding affinity of a canonical PDZ domain to its native ligand with and without α -helix 3 ($\Delta\alpha$ 3, green arrows)²³. c, AAC homodimer with each monomer represented as one purple domain. Binding of the allosteric effector acetyl-CoA (blue oval) is positively cooperative at low temperatures (green '+'), and negatively cooperative at high temperatures (red '-')⁴. d, TetR

homodimer²⁷ depicted as a two-domain protein with a tetracycline binding domain (TBD, blue region, top) and a DBD (blue region, bottom). **e**, Doc/Phd toxin–antitoxin system equilibrium. Phd is depicted as a homodimer (top, blue and purple monomers) and Doc is depicted as the blue ligand²⁸. **f**, Representation of variants of E1A³⁰ shown from N to C terminus with binding sites for ligands in the two variants represented by blue rectangles (CBP) and green rectangles (pRb). **g**, Schematic representation of α -synuclein (AS) with its N-terminal membrane-binding domain (MBD) coupled to its C-terminal IDR. Upon oxidative stress (nitration) the affinity of the MBD decreases (bottom)²⁹.

one another. As shown below, the hallmark feature of these systems is the apparently complex 'tunable' coupling between sites. An example in which local unfolding has a role in allostery is in the enzyme aminoglycoside N-(6')-acetyltransferase II (AAC)—a homodimeric enzyme from Entero-coccus faecium responsible for conferring bacterial resistance to aminoglycoside antibiotics⁴. An allosteric effector of AAC, acetyl-CoA, binds with positive cooperativity at low temperatures and switches to negative cooperativity at higher temperatures as determined by isothermal titration calorimetry (Fig. 3c). NMR reveals that certain backbone amides undergo dynamic broadening as a function of temperature, suggesting that local unfolding is responsible for this switching behaviour. This observation agrees with the change in enthalpy of binding as temperature is increased; the nonlinear temperature dependence at higher temperatures being a signature of local unfolding²⁴.

Another example in which local unfolding has a role in allosteric coupling is the tetracycline repressor (TetR), a homodimeric transcription factor consisting of a Tet binding domain (TBD) and a DBD (Fig. 3d). TetR binds DNA in the absence of the antibiotic (Tet) and is released when Tet binds the TBD, inducing a reduction in binding affinity of the DBD for DNA. A paradoxical observation from structural data was that the inactive Tet-bound (holo) form shows the DBD α -helices, which are involved in binding DNA, to be in a more binding-competent conformation than when they are in the active apo-form. Chaotropic denaturation and *in vitro* operator binding assays performed on TetR, as well as biologically

relevant TetR mutants, revealed that local unfolding of the DBD in the native state ensemble was responsible for this paradox 27 . The protein functions because the DBD is locally unfolded in the absence of Tet, allowing enough conformational flexibility to bind DNA, and hence an increased binding affinity in the absence of Tet (Fig. 3d, left equilibrium). Upon binding Tet, the α -helices responsible for DNA binding are redistributed into an ensemble of conformations that are not completely binding competent. Interestingly, naturally occurring mutants exist that are Tet insensitive and/or have inverted responses, manifesting complexity and tunability like that seen in allostery of locally unfolded or intrinsically disordered sequences 27 .

Perhaps one of the fastest evolving fields in biophysics is protein intrinsic disorder^{59,60}. IDPs stand as a challenge to the structure–function paradigm, as IDPs have no stable tertiary structure under physiological conditions yet are able to function^{58–60}. Seminal bioinformatics and experimental work has revealed that intrinsically disordered regions (IDRs) and IDPs are hyper-abundant in transcription factors and cell signalling pathways. Aside from the fact that they lack a stable structure, IDPs none-theless possess features that would otherwise make them suitable allosteric proteins. These include (1) high specificity for multiple targets resulting from their structural plasticity³⁰; (2) high specificity and low-affinity binding¹⁸; (3) fast association and dissociation rates for proper turnover⁵⁸; and (4) enrichment of post-translational modification sites⁷⁵ and splicing isoforms⁷⁶. To no surprise, several IDPs have been shown to exhibit allostery as part of

their role in signalling. Interestingly, just as with proteins that exhibit local unfolding, allosteric IDPs exhibit complex coupling behaviour. Three examples highlight this complexity.

The first case involves the Phd/Doc toxin–antitoxin system (Fig. 3e) that inhibits the ribosome A site. As part of its regulatory cycle, Phd controls its own transcription by binding DNA at its own operon. Notably, increasing the ratio of Doc/Phd initially inhibits transcription, and as the ratio exceeds a certain biological threshold, transcription is activated again, exhibiting 'conditional cooperativity'²⁸. Conditional cooperativity results from the delicate balance of the ensemble of states present in solution. Phd has a locally unfolded carboxy terminus, which undergoes a disorder-to-order transition that exposes high-affinity (H) and low-affinity (L) binding sites (equilibrium 1, Fig. 3e). Increasing the ratio of Doc/Phd leads to partial saturation of the H and L sites by Doc, which in turn stabilizes the DBD of Phd, allowing DNA binding and transcription repression (equilibrium 2, Fig. 3e). Finally, increasing the Doc/Phd ratio further leads to saturation of the H and L binding sites, which leads to dissociation from DNA and activates transcription again (equilibrium 3, Fig. 3e).

Another recently reported example³⁰ involves the IDP adenovirus early region 1A protein (E1A) (Fig. 3f). E1A can bind two different host proteins, CREB binding protein (CBP) and retinoblastoma protein (pRB), in its capacity to disrupt host cellular signalling. Single-molecule fluorescence resonance energy transfer (smFRET) was used to dissect the cooperative nature of the coupled folding and binding involving CBP and pRB. By measuring the cooperativity of binding using different truncated E1A constructs, these authors elegantly demonstrated cooperativity switching between the CBP and pRB sites, wherein positive coupling (green '+' in Fig. 3f) becomes negative (red '-' in Fig. 3f).

Importantly, IDPs are enriched in post-translational modifications 75 , telling of separate mechanisms that nature may use to regulate the allosteric response of the ensemble. An example of this occurs in α -synuclein, implicated in Parkinson's disease 29 . α -Synuclein is composed of an aminoterminal membrane-binding domain and a C-terminal IDR (Fig. 3g) and exhibits reduced membrane-binding affinity under oxidative stress 29 . Using smFRET and NMR, it was shown that nitration of the C terminus shifts its conformational ensemble to a more globally extended conformation, which is accompanied by a reduction in binding affinity (Fig. 3g, bottom). Because the C-terminal IDR is known to interact with a variety of ligands, these results suggest that α -synuclein may use this allosteric coupling to regulate the biological response. Modulation of the conformational ensemble in IDPs and IDRs via these post-translational modifications may be a general mechanism for rapid, reversible control of biological response. How this may occur is discussed in more detail in the following section.

As the examples in Fig. 3 reveal, the hallmark feature of allostery in locally unfolded and intrinsically disordered proteins is a general mechanism whereby cooperativity between two sites can not only be tuned (high or low) by environmental conditions, but the actual sign of the coupling can change, transforming an activator into a repressor, or vice versa. A single static picture of the protein does not reveal how the same ligand, binding to the same site on the same protein, can transmit structural information from one site to another, causing a more favourable conformation to bind ligand under one circumstance and a less-favourable conformation under another. Restated more bluntly, it is not clear how the same ligand binding to the same site can cause either one biological effect or its 'opposite'.

Here we show that by formulating the phenomenon of allostery in terms of thermodynamic ensembles, many of the seemingly complex and confounding properties of allosteric proteins, including the results of adding different allosteric ligands, emerge as a straightforward consequence of the heterogeneity in the system. From these allosteric ensembles, ground rules emerge that can be used to guide future experimental inquiry.

Allosteric ligands remodel the energy landscape

Much in same way that the ability of a protein to fold can be understood in terms of the conformational 'energy landscape' of the protein^{77–79}, so too can allosteric coupling. According to this framework, all possible conformations of a protein are sampled (or populated) according to their

energies; lower energy conformations are sampled more often than those of higher energy. Because the binding of any ligand to a state increases how often the state is sampled^{15,80}, allosteric ligands effectively remodel the energy landscape of allosteric proteins¹⁸. This key point has been discussed, at least in qualitative terms, in a number of recent reviews^{5,15,18}. The take-home message is that the energy landscape can be smooth with many accessible states in its conformational ensemble, discrete with few states, or something in between, and each of these scenarios can provide its own biological advantage.

However, stabilities and coupling energies in proteins are generally very modest, suggesting that no single state, or sets of allosteric states, will necessarily dominate the ensemble. In other words, allosteric mechanisms may be more statistical, and less deterministic, than classical models suggest. Indeed, a more quantitative look at the landscape, using ensemble models that divide the protein into interacting component parts^{61,81,82}, illuminates the statistical nature of the signalling process, and reveals a wealth of regulatory opportunities directly resulting from the heterogeneity in the ensemble (Box 2).

Of course, treating allosteric proteins as ensembles is not a new idea. Early work on the lambda phage repressor, for example, demonstrated that consideration of all the accessible ligated states was necessary to understand its biological function⁸³. However, when conformational heterogeneity at each binding site is explicitly considered in addition to the degeneracy of ligated species, important ground rules for allostery emerge⁸.

First, all ensembles have tunable sensitivity, wherein the same perturbation can produce a range of results, simply based on where a given equilibrium is poised before perturbation. This reality not only affects function but also the interpretation of conformational entropy changes in allosteric transitions, which, in principle, can change from positive to negative, even for the same transition (Box 1).

Second, ensembles contain a plurality of potential allosteric mechanisms, a point that can be demonstrated by noting that allosteric proteins often segregate different functions (for example, effector-binding and activity) into different domains. This allows for a straightforward enumeration of the ensemble that accounts for each functional domain to be in the active or inactive conformation^{8,61,84}, both with and without other domains in their functional states. Binding of the effector molecule stabilizes the active form of the effector-binding domain, which in turn can stabilize (or destabilize) the functional domain (Box 2)61. This is so because, according to landscape theory^{77–79}, all of the possible states in the ensemble have some finite probability based on their energies. Thus, if landscape theory holds, within any ensemble, there exist sub-ensembles in which two different binding sites are either positively coupled (both domains active) or negatively coupled (one domain active and the other inactive) (Box 2). In other words, the potential for different allosteric mechanisms is already preencoded in the ensemble, a property that is uniquely provided by an ensemble allosteric model8.

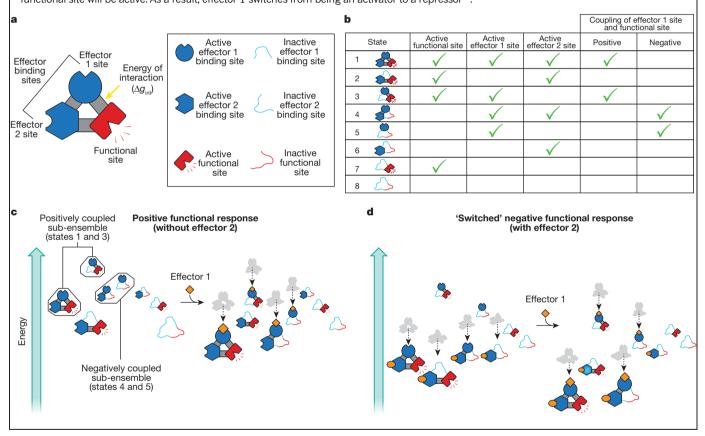
The question remains as to what determines positive or negative coupling between two binding sites. In the context of the ensemble, the answer is the relative stability of the different states, which is determined by the equilibrium between the active and inactive state of each domain and the interaction energy between domains. In fact, the signs of the interaction energies are the key parameters in determining whether allosteric proteins can switch between activation and repression^{61,84}. The critical insight is that the overall allosteric behaviour is an ensemble-weighted contribution of all the states and thus cannot be reconciled in the context of a single structure⁸⁵. Instead the effect is statistical. Under one set of conditions, the ensemble could be poised such that two domains would be positively coupled, because the properties of the positively coupled sub-ensemble dominate the average. However, any perturbation of the ensemble that remodels the energy landscape may change which sub-ensemble dominates, and thus, transform activation into repression, or vice versa (Box 2).

Importantly, perturbations can arise from any number of sources, including post-translational modification (for example, phosphorylation, methylation, sumoylation, nitration²⁹), alternative splicing or translation start sites⁷⁶, truncation³⁰, temperature⁴ and the binding of a second allosteric

BOX 2

The ensemble view as a framework to explain allostery

a-c, Allosteric proteins can be viewed, to a first approximation, as a functional domain coupled to one or a number of effector-binding domains that interact with each other. To illustrate how an ensemble can switch the outcome of binding a particular effector molecule, we consider a protein with two effector-binding domains, which can interact with each other, as well as the functional site (a). Each domain can be inactive or active, together with (or separately from) the other domain, producing an ensemble of eight possible states (b, first column). In each state, the effector 1 binding site is in the active conformation (b, third column) either with or without the functional site in the active conformation (b, second column). Thus, the ensemble consists of states in which effector 1 site is positively coupled to the functional site (states 1 and 3; b, fifth column) and negatively coupled (states 4 and 5; b. sixth column)—that is, the effector 1 and functional sites are both active, or the effector 1 site is active while the functional site is inactive, respectively. Which set of states will govern the overall observed allosteric transition is determined primarily by the magnitude and sign of the interaction energies, Δg_{int} , between each domain (a)⁶¹. To see how this affects function, we consider the energy of all the states in the ensemble under a particular set of conditions (c)8. In the absence of effector 1, protein conformations in which the functional site is active have high energy, and so the probability of the functional site being active is low. Effector 1 binding lowers the energies (dotted lines in c) of all states in which the effector 1 binding site is active, including conformations that contain the active form of the functional site. This increases the probability that the functional site will be active. The sizes of the depicted structures indicate the probability of their formation; larger structures are more likely to form. Addition of effector 2, in the absence of effector 1, redistributes the ensemble to a new starting position (d, left) so that the two lowest energy conformations now have active functional sites. Addition of effector 1 binds to and lowers the energy of the same states as described above (dotted lines in d). In this instance, however, only one of the two lowest energy states has the functional site in the active conformation, lowering the probability that the functional site will be active. As a result, effector 1 switches from being an activator to a repressor84.



effector to a different effector-binding domain (Box 2). In short, redistributing the ensemble can modulate the mechanism. As shown in Box 2, remodelling of the ensemble with effector 2 corresponds to dialing-in (in a rheostat-like fashion) the negative coupling contribution to the overall allosteric coupling.

Discussion

The importance of an ensemble representation of allostery is that it highlights the statistical nature of the allosteric coupling process. The classic notion of an allosteric pathway, through a static picture of the protein, often conveys a deterministic (or at least homogeneous) picture of the signal propagation process, wherein each molecule at any instant is in the same conformation or at least can be equally well represented by the same average conformation. The ensemble model states that, in the most general

case, activity is an ensemble-weighted contribution of all species present in solution, regardless of how structurally dissimilar they may be. As such, the important questions shift from identification of the single active conformation, or the allosteric pathway through the protein, to questions that focus on identifying the fraction of molecules that have each domain in the active conformation, and/or the fraction of time a particular set of interactions exist when the functional site (and/or the effector-binding domains) is in its active conformation. An important point critical to characterizing an allosteric ensemble is that, although a given effector molecule may bind to only a small fraction of the states in an ensemble, thus directly stabilizing only those states, stabilization will redistribute the entire ensemble, changing the probability of every state (Box 2). Consequently, every state in the ensemble can be regarded as a potential allosteric state, regardless of whether it binds one or a number of effectors or is functionally

silent. Such silent states, simply as a consequence of being populated, attenuate the impact of effector binding on the activity (Box 2). Indeed, the numerous examples that show complex, stability-dependent and tunable coupling^{28,30,86} suggest that the principles outlined here are at play in real allosteric systems.

An important question is how to practically leverage the ensemble view of allostery. The most immediate impact could be refocusing inquiry into allosteric mechanism, particularly as it pertains to IDPs, in which structural methods have limited applicability. The ensemble allosteric model described here and elsewhere ^{8,61,84} suggests that experimental determination of stabilities and coupling energies represents a viable strategy for determining the relevant states in both disordered and structured ensembles and the relative stabilities of each. Of course, this should not be misconstrued as minimizing the importance of structural characterization of IDPs. Significant progress has been made in modelling disordered ensembles at atomic resolution using various experimental constraints ^{87–91}. The future challenge will be for these computed ensembles to reproduce the observed highly variable and complex switching behaviour seen in many IDPs.

With regard to structured proteins, the ensemble model of allostery provides insight into important lines of inquiry. Specifically, because the sensitivity of an allosteric protein is maximal at the threshold of a transition (Box 1), many important states are likely to be minutely, albeit measurably, populated under functional conditions (that is, between 1 and 5%). As such, experimental and computational strategies to identify lowprobability states are critical. In addition to NMR^{55,92-95}, fundamental progress has been made in detecting such low-populated states combining other structural biology techniques^{51,96}, with at least one X-ray crystallography study corroborating the states detected by NMR⁵¹. The ability to observe alternative conformations masked by the cryogenic temperatures typically used in structural analysis^{51,97}, and to resolve, using ensemble refinement, multiple states from crystal data collected at room temperature98, reveal a much richer dynamic picture. Similarly, new data analysis methods applied to electron microscopy images quite expectedly reveal multiple conformational states of macromolecules99.

Interestingly, the ensemble model also provides a potential framework for interpreting long-time scale molecular dynamics simulations of allosteric proteins 100. If such simulations can provide the amount of time that specific interactions are made (and the co-occurrence with other interactions), molecular dynamics could be used to map the energy landscape of the allosteric process, possibly even illuminating the multitude of mechanisms pre-encoded in the ensemble. Indeed, a recent long-time molecular dynamics simulation 101 reveals the statistical nature of the interactions associated with allosteric drugs of the muscarinic acetylcholine receptor (M2 receptor), indicating that interactions are not obligatorily associated with ligand-bound or -unbound states. Other computational approaches, such as coarse-grained modelling of the normal modes of proteins, yield predictive cooperative energies even in the absence of structural change⁷³. Ongoing and future efforts to integrate computation, structure and even different models of allostery and function 102 are likely to be critical to understanding signalling within large macromolecular complexes¹⁰³.

Finally, the ensemble representation of allostery is particularly appealing when considering protein design and evolution. The genetic record clearly shows that nature has evolved and adopted a finite number of functional and binding domains, and has combined them in different ways to make new proteins with different functions and regulatory properties^{104,105}. The ensemble representation suggests that by simply manipulating either or both the active/inactive equilibrium for different domains and the coupling between domains, evolution or design of allosteric proteins may be much more straightforward than a detailed inspection of the atomic structure of the protein suggests. Future research directions should include whether allosteric proteins can be designed or evolved without detailed consideration of the structure, and whether positively coupled domains can be transformed to negatively coupled ones, simply by identifying the thermodynamic ground rules for switching⁸⁴ and rationally changing the relevant parameters^{106–108}. Although the answers to such questions are

uncertain, what is certain is that as more dynamic and disordered systems have become amenable to experimental inquiry, the ensemble nature of allostery has become clear.

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