Assignment 5 - 70 points possible

Apple, Bird, Cookie:

Data from Google's Quick, Draw! Game

We will perform 2 tasks in this homework. The first is to build a classifier that can tell whether a drawing is of an apple, a bird, or a cookie. The data is taken from a game you can play online, developed by Google, called Quick, Draw! The drawings are all Pictionary-style quick sketches of things. Google has already done the work of turning the drawings into grayscale 28 x 28 images that are good for machine learning. Since the images don't have that many pixels, the drawings are simplified, and there is a lot of data, this is an example of a relatively easy task for machine learning generally and neural networks in particular. (There are many similar datasets here:

 $\frac{https://console.cloud.google.com/storage/browser/quickdraw_dataset/full/numpy_bitmap;tab=objects?}{pli=1&prefix=&forceOnObjectsSortingFiltering=false})$

Before you do anything else in this assignment, it's *strongly recommended* that you do two things with your Google Colab setup. First, go to the upper right and select "Connect to a hosted runtime." Second, go to the menu at the top and select Runtime->Change runtime type->Pick GPU. Selecting "GPU" will dramatically speed up the training times for the neural networks in this assignment. But, picking GPU also resets the runtime, which is why you should do this before anything else.

Download the two zip files associated with this homework at https://drive.google.com/file/d/14UmGyFC_WSywNcm2yrCfe0x04luA4208/view?usp=sharing and https://drive.google.com/file/d/14UmGyFC_WSywNcm2yrCfe0x04luA4208/view?usp=sharing and place them in your own Google Drive. Then run the code boxes below (possibly modifying the path) to mount the drive and unzip the files.

```
from google.colab import drive
drive.mount('/content/gdrive')
    Mounted at /content/gdrive
# You may need to change "NNAssign" to your own directory name
!unzip gdrive/MyDrive/'Junior Year'/'DS 340'/'HW 5'/apple bird cookie.zip
    Archive: gdrive/MyDrive/Junior Year/DS 340/HW 5/apple bird cookie.zip
       inflating: full_numpy_bitmap_apple.npy
       inflating: __MACOSX/._full_numpy_bitmap_apple.npy
       inflating: full_numpy_bitmap_bird.npy
       inflating: MACOSX/. full numpy bitmap bird.npy
       inflating: full numpy bitmap cookie.npy
       inflating: __MACOSX/._full_numpy_bitmap_cookie.npy
import numpy as np
apples = np.load('full numpy bitmap apple.npy')
birds = np.load('full_numpy_bitmap_bird.npy')
cookies = np.load('full_numpy_bitmap_cookie.npy')
```

(1, 2pts) Call np.concatenate to join the three datasets together into a single array called "all_kinds". Notice that the three datasets should be passed to np.concatenate as a tuple.

```
# TODO concatenate the data
all_kinds = np.concatenate((apples, birds, cookies))
```

(2, 3 pts) Now we need a list of labels that is as long as all_kinds. Create a list named "labels" that is as long as all_kinds, where each element identifies which kind of drawing can be found at that place in all_kinds. Label apples as 0, birds as 1, and cookies as 2. (You may find it useful to call len() on the apples, birds, and cookies arrays.)

```
# TODO make labels
labels = [0] * len(apples) + [1] * len(birds) + [2] * len(cookies)
```

Now we'll call train_test_split to separate the data into training and testing data.

```
from sklearn.model_selection import train_test_split
x_train, x_test, y_train, y_test = train_test_split(all_kinds, labels)
```

(3, 2pts) This data ranges from 0 to 255, but neural networks tend to work best when the data is between 0 and 1. Scale the train and test data by dividing it by 255.

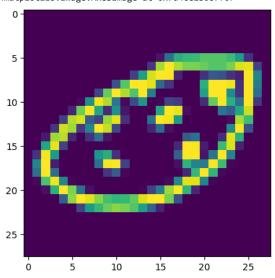
```
# TODO scale the data
print(x_train.shape)
x_train = x_train/255
x_test = x_test/255
(307235, 784)
```

(4, 5pts) If we examine the shape of x, it isn't quite what we want yet - it is an array of arrays that are of size length-of-data x 784. 784 is 28x28, and we want our convolutional neural networks to perceive the data as a 28x28 square instead of one long array of 784 elements. Call x_train.reshape() and x_test.reshape() so that their dimensions are length-of-data x 28 x 28. (Note that reshape expects a tuple that is the size as its argument. You can pass -1 as one of the dimensions if you don't want to figure out how long the array is.)

If your reshape worked correctly, the following code should show a apple, bird, or cookie sketch. If it didn't work, it will look like random noise. If you're not sure, you can always try more images.

```
import matplotlib.pyplot as plt plt.imshow(x_train[0]) # Should be a recognizable image if we reshaped correctly
```

<matplotlib.image.AxesImage at 0x7d4ce2b087f0>



As the last step before creating the neural network, we will turn the labels into one-hot encodings, like [0,0,1] instead of 2. There's a handy keras function that does this, and we're just going to call it for you.

```
from tensorflow import keras
num_classes = 3
y_train = keras.utils.to_categorical(y_train, num_classes)
y_test = keras.utils.to_categorical(y_test, num_classes)
```

(5, 9pts) Rather than create a network completely from scratch, it makes sense to start with a network that you know does something similar. One of the keras tutorials shows how to do digit recognition with a relatively small deep neural network. The dataset, the MNIST digit dataset, is very similar to ours because it consists of 28 x 28 black and white line drawings. Consult the "Build a Model" and "Train the model" sections of https://keras.io/examples/vision/mnist_convnet/ and get that neural network running on our apple, bird, and cookie data. (Be sure to leave a comment indicating that you borrowed the structure from there.)

```
from tensorflow.keras import layers
input_shape = (28,28,1)
batch_size = 128
epochs = 15
```

- # TODO borrow the MNIST model with attribution
- # model architecture from fchollet

```
model = keras.Sequential(
   keras.Input(shape=input_shape),
   layers.Conv2D(32, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(64, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Flatten(),
   layers.Dropout(0.5),
   layers.Dense(num classes, activation="softmax"),
model.summary()
  Model: "sequential"
  Layer (type)
                Output Shape
                            Param #
  ______
  conv2d (Conv2D)
                (None, 26, 26, 32)
                            320
  max_pooling2d (MaxPooling2 (None, 13, 13, 32)
  conv2d 1 (Conv2D)
                            18496
                (None, 11, 11, 64)
  max_pooling2d_1 (MaxPoolin (None, 5, 5, 64)
  g2D)
  flatten (Flatten)
                (None, 1600)
  dropout (Dropout)
                (None, 1600)
  dense (Dense)
                (None, 3)
                            4803
  _____
  Total params: 23619 (92.26 KB)
  Trainable params: 23619 (92.26 KB)
  Non-trainable params: 0 (0.00 Byte)
# TODO compile and fit the model
model.compile(loss="categorical_crossentropy", optimizer="adam", metrics=["accuracy"])
model.fit(x_train, y_train, batch_size = batch_size, epochs=epochs, validation_split=0.1)
  Epoch 1/15
  Epoch 2/15
  Epoch 3/15
  Epoch 4/15
  Epoch 5/15
  Epoch 6/15
  Epoch 7/15
  Epoch 8/15
```

(6, 2pts) Evaluate the model on the test set with the code below. You should have a test accuracy well above 90%.

```
score = model.evaluate(x_test, y_test, verbose=0)
print("Test loss:", score[0])
print("Test accuracy:", score[1])

Test loss: 0.047915734350681305
   Test accuracy: 0.9842401146888733
```

→ Cats and Dogs

It was relatively easy to get good performance on that task, because the size of each input is small and the features needed for success weren't too complicated. We'll now try a classification task with real images. This is a moderately well-known "cats and dogs" dataset. Unzip the dogs-vs-cats dataset in the current directory. You can examine the files to see pictures of cats and dogs with varying dimensions and varying poses.

```
from google.colab import drive
drive.mount('/content/gdrive')
    Mounted at /content/gdrive
!unzip gdrive/MyDrive/"Junior Year"/"DS 340"/"HW 5"/dogs-vs-cats.zip
```

115

```
intlating: dogs-vs-cats/train/cats/cat./8/.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.787.jpg
       inflating: dogs-vs-cats/train/cats/cat.4402.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.4402.jpg
       inflating: dogs-vs-cats/train/cats/cat.11524.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.11524.jpg
       inflating: dogs-vs-cats/train/cats/cat.793.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.793.jpg
       inflating: dogs-vs-cats/train/cats/cat.2067.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.2067.jpg
       inflating: dogs-vs-cats/train/cats/cat.5708.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.5708.jpg
       inflating: dogs-vs-cats/train/cats/cat.4416.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.4416.jpg
       inflating: dogs-vs-cats/train/cats/cat.3379.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.3379.jpg
       inflating: dogs-vs-cats/train/cats/cat.11530.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.11530.jpg
       inflating: dogs-vs-cats/train/cats/cat.12039.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.12039.jpg
       inflating: dogs-vs-cats/train/cats/cat.6201.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.6201.jpg
       inflating: dogs-vs-cats/train/cats/cat.9132.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.9132.jpg
       inflating: dogs-vs-cats/train/cats/cat.1208.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.1208.jpg
       inflating: dogs-vs-cats/train/cats/cat.6567.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.6567.jpg
       inflating: dogs-vs-cats/train/cats/cat.9654.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.9654.jpg
       inflating: dogs-vs-cats/train/cats/cat.7679.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/. cat.7679.jpg
       inflating: dogs-vs-cats/train/cats/cat.11256.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.11256.jpg
       inflating: dogs-vs-cats/train/cats/cat.4370.jpg
       inflating: MACOSX/dogs-vs-cats/train/cats/._cat.4370.jpg
       inflating: dogs-vs-cats/train/cats/cat.2701.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.2701.jpg
       inflating: dogs-vs-cats/train/cats/cat.10148.jpg
       inflating: __MACOSX/dogs-vs-cats/train/cats/._cat.10148.jpg
    dogs-vs-cats gdrive MACOSX sample data
import tensorflow as tf
from tensorflow import keras
from tensorflow.keras import layers
import tensorflow as tf
image_size = (180, 180)
batch size = 32
# Data from https://www.kaggle.com/competitions/dogs-vs-cats/
# Code from https://keras.io/examples/vision/image_classification_from_scratch/
train ds = tf.keras.preprocessing.image dataset from directory(
    "dogs-vs-cats/train",
    validation split=0.2,
    subset="training",
    seed=1337,
    image_size=image_size,
```

```
batch_size=batch_size,
)
val_ds = tf.keras.preprocessing.image_dataset_from_directory(
    "dogs-vs-cats/train",
    validation_split=0.2,
    subset="validation",
    seed=1337,
    image_size=image_size,
    batch_size=batch_size,
)

Found 25000 files belonging to 2 classes.
    Using 20000 files for training.
    Found 25000 files belonging to 2 classes.
    Using 5000 files for validation.
```

(7, 9pts) We'll suppose that the closest starting point network we have on hand for this is the MNIST network again. Adapt it to this dataset with the following changes:

- The input shape is 180 x 180 x 3.
- Put the rescaling of dividing values by 255 in the network itself with a layers. Rescaling() layer after the Input layer.
 https://www.tensorflow.org/api_docs/python/tf/keras/layers/Rescaling
- The final "softmax" activation function is only appropriate for multiclass classification. Change this to a more appropriate activation function for binary classification.
- Name the model model2 to work with the training code below.

```
# TODO create model2
# model architecture from fchollet
input_shape2 = (180, 180, 3)
model2 = keras.Sequential(
       keras.Input(shape=input shape2),
       layers.Rescaling(scale=1./255),
       layers.Conv2D(32, kernel_size=(3, 3), activation="relu"),
       layers.MaxPooling2D(pool size=(2, 2)),
       layers.Conv2D(64, kernel_size=(3, 3), activation="relu"),
       layers.MaxPooling2D(pool_size=(2, 2)),
       layers.Flatten(),
       layers.Dropout(0.5),
       layers.Dense(1, activation="sigmoid"),
model2.summary()
    Model: "sequential"
     Layer (type)
                                  Output Shape
                                                            Param #
     rescaling (Rescaling)
                                  (None, 180, 180, 3)
     conv2d (Conv2D)
                                  (None, 178, 178, 32)
                                                            896
     max_pooling2d (MaxPooling2 (None, 89, 89, 32)
                                                            0
```

```
D)
conv2d 1 (Conv2D)
                        (None, 87, 87, 64)
                                               18496
max_pooling2d_1 (MaxPoolin (None, 43, 43, 64)
 g2D)
 flatten (Flatten)
                         (None, 118336)
                                               0
dropout (Dropout)
                         (None, 118336)
dense (Dense)
                                               118337
                         (None, 1)
______
Total params: 137729 (538.00 KB)
Trainable params: 137729 (538.00 KB)
Non-trainable params: 0 (0.00 Byte)
```

You can train the network using the following code.

<keras.src.callbacks.History at 0x7d4b60620b80>

```
epochs = 15
model2.compile(loss="binary_crossentropy", optimizer="adam", metrics=["accuracy"])
model2.fit(train_ds, epochs=epochs, validation_data=val_ds) # Validation data instead of fraction
    Epoch 1/15
    625/625 [==========] - 47s 70ms/step - loss: 0.6269 - accuracy: 0.6472 - val loss: 0.5511 - val accuracy: 0.7282
    Epoch 2/15
    625/625 [=========== ] - 38s 61ms/step - loss: 0.5203 - accuracy: 0.7459 - val loss: 0.4979 - val accuracy: 0.7586
    Epoch 3/15
    625/625 [============] - 35s 55ms/step - loss: 0.4476 - accuracy: 0.7932 - val_loss: 0.5094 - val_accuracy: 0.7610
    625/625 [==========] - 37s 58ms/step - loss: 0.3924 - accuracy: 0.8227 - val loss: 0.4799 - val accuracy: 0.7784
    Epoch 5/15
    625/625 [============] - 37s 59ms/step - loss: 0.3447 - accuracy: 0.8493 - val_loss: 0.4924 - val_accuracy: 0.7880
    Epoch 6/15
    625/625 [==========] - 37s 58ms/step - loss: 0.3050 - accuracy: 0.8666 - val loss: 0.5178 - val accuracy: 0.7898
    Epoch 7/15
    625/625 [============ ] - 35s 55ms/step - loss: 0.2687 - accuracy: 0.8846 - val loss: 0.5424 - val accuracy: 0.7892
    Epoch 8/15
    625/625 [==========] - 40s 64ms/step - loss: 0.2372 - accuracy: 0.9022 - val loss: 0.5554 - val accuracy: 0.7914
    Epoch 9/15
    625/625 [===========] - 35s 56ms/step - loss: 0.2162 - accuracy: 0.9093 - val_loss: 0.5865 - val_accuracy: 0.7728
    Epoch 10/15
    625/625 [===========] - 36s 57ms/step - loss: 0.2010 - accuracy: 0.9175 - val_loss: 0.6280 - val_accuracy: 0.7902
    Epoch 11/15
    Epoch 12/15
    625/625 [============] - 53s 84ms/step - loss: 0.1656 - accuracy: 0.9323 - val_loss: 0.6271 - val_accuracy: 0.7862
    Epoch 13/15
    625/625 [==========] - 36s 57ms/step - loss: 0.1597 - accuracy: 0.9373 - val loss: 0.6455 - val accuracy: 0.7870
    Epoch 14/15
    625/625 [==========] - 36s 57ms/step - loss: 0.1527 - accuracy: 0.9394 - val loss: 0.6930 - val accuracy: 0.7874
    Epoch 15/15
```

(8, 6pts) The validation loss went down and then up, indicating overfitting, so we possibly could proceed to regularization steps at this point; nevertheless, for photos, we probably want to try some deeper architectures than for the hand drawings. Probably, the features extracted for the MNIST and apple/bird/cookie datasets are simpler than what's necessary for photos. This implies needing more layers. One strategy used by some well-known networks is to add blocks each consisting of a Conv2D layer followed by MaxPooling2D layer, where each Conv2D layer has twice as many filters as the last one (so 32, 64, 128 ...). You can see our current architecture already follows this pattern. Try training networks with one, two, and three more of these blocks between the last MaxPooling2D layer and the Flatten() call.

```
# TODO define model3 with one more block of Conv2D and pooling
model3 = keras.Sequential([
    keras.Input(shape=input_shape2),
    layers.Rescaling(scale=1./255),
    layers.Conv2D(32, kernel_size=(3, 3), activation="relu"),
    layers.MaxPooling2D(pool_size=(2, 2)),
    layers.Conv2D(64, kernel_size=(3, 3), activation="relu"),
    layers.MaxPooling2D(pool_size=(2, 2)),
    layers.Conv2D(128, kernel_size=(3, 3), activation="relu"),
    layers.MaxPooling2D(pool_size=(2, 2)),
    layers.Flatten(),
    layers.Dropout(0.5),
    layers.Dense(1, activation="sigmoid"),
])
model3.summary()
```

Model: "sequential 10"

Layer (type)	Output Shape	Param #
rescaling_13 (Rescaling)		0
conv2d_31 (Conv2D)	(None, 178, 178, 32)	896
<pre>max_pooling2d_31 (MaxPooli ng2D)</pre>	(None, 89, 89, 32)	0
conv2d_32 (Conv2D)	(None, 87, 87, 64)	18496
<pre>max_pooling2d_32 (MaxPooli ng2D)</pre>	(None, 43, 43, 64)	0
conv2d_33 (Conv2D)	(None, 41, 41, 128)	73856
<pre>max_pooling2d_33 (MaxPooli ng2D)</pre>	(None, 20, 20, 128)	0
flatten_14 (Flatten)	(None, 51200)	0
dropout_14 (Dropout)	(None, 51200)	0
dense_14 (Dense)	(None, 1)	51201
Total params: 144449 (564.25 Trainable params: 144449 (56 Non-trainable params: 0 (0.0	KB) 4.25 KB)	

```
epochs = 15
model3.compile(loss="binary crossentropy", optimizer="adam", metrics=["accuracy"])
model3.fit(train_ds, epochs=epochs, validation_data=val ds)
    Epoch 1/15
    625/625 [===========] - 45s 69ms/step - loss: 0.5871 - accuracy: 0.6757 - val loss: 0.5049 - val accuracy: 0.7576
    Epoch 2/15
    625/625 [==========] - 42s 66ms/step - loss: 0.4651 - accuracy: 0.7811 - val loss: 0.4364 - val accuracy: 0.8012
    Epoch 3/15
    625/625 [============= ] - 39s 61ms/step - loss: 0.4081 - accuracy: 0.8139 - val_loss: 0.3969 - val_accuracy: 0.8266
    Epoch 4/15
    625/625 [============ - 36s 56ms/step - loss: 0.3613 - accuracy: 0.8396 - val loss: 0.3836 - val accuracy: 0.8338
    Epoch 5/15
    625/625 [===========] - 38s 60ms/step - loss: 0.3173 - accuracy: 0.8625 - val_loss: 0.3911 - val_accuracy: 0.8322
    Epoch 6/15
    625/625 [===========] - 35s 56ms/step - loss: 0.2888 - accuracy: 0.8788 - val_loss: 0.3798 - val_accuracy: 0.8376
    Epoch 7/15
    Epoch 8/15
    Epoch 9/15
    625/625 [==========] - 37s 59ms/step - loss: 0.2132 - accuracy: 0.9114 - val loss: 0.4057 - val accuracy: 0.8520
    Epoch 10/15
    625/625 [===========] - 36s 58ms/step - loss: 0.1930 - accuracy: 0.9197 - val_loss: 0.3995 - val_accuracy: 0.8508
    Epoch 11/15
    625/625 [============== ] - 39s 61ms/step - loss: 0.1715 - accuracy: 0.9308 - val_loss: 0.4020 - val_accuracy: 0.8516
    Epoch 12/15
    625/625 [===========] - 35s 56ms/step - loss: 0.1651 - accuracy: 0.9333 - val loss: 0.3935 - val accuracy: 0.8562
    Epoch 13/15
    625/625 [============] - 35s 56ms/step - loss: 0.1483 - accuracy: 0.9413 - val_loss: 0.3894 - val_accuracy: 0.8568
    Epoch 14/15
    625/625 [==========] - 38s 60ms/step - loss: 0.1383 - accuracy: 0.9430 - val loss: 0.3896 - val accuracy: 0.8620
    Epoch 15/15
    625/625 [============] - 38s 61ms/step - loss: 0.1288 - accuracy: 0.9496 - val_loss: 0.4198 - val_accuracy: 0.8546
    <keras.src.callbacks.History at 0x7d4b6011e470>
# TODO define model4 with two more blocks of Conv2D and pooling
model4 = keras.Sequential([
   keras.Input(shape=input_shape2),
   layers.Rescaling(scale=1./255),
   layers.Conv2D(32, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(64, kernel size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(128, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool size=(2, 2)),
   layers.Conv2D(256, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Flatten(),
   layers.Dropout(0.5),
   layers.Dense(1, activation="sigmoid"),
1)
model4.summary()
→ Model: "sequential_2"
    Layer (type)
                            Output Shape
                                                  Param #
```

```
rescaling 2 (Rescaling)
                           (None, 180, 180, 3)
    conv2d_7 (Conv2D)
                           (None, 178, 178, 32)
                                               896
    max_pooling2d_7 (MaxPoolin (None, 89, 89, 32)
    g2D)
    conv2d_8 (Conv2D)
                           (None, 87, 87, 64)
                                               18496
    max_pooling2d_8 (MaxPoolin (None, 43, 43, 64)
                                               0
    g2D)
    conv2d_9 (Conv2D)
                           (None, 41, 41, 128)
                                               73856
    max pooling2d 9 (MaxPoolin (None, 20, 20, 128)
    conv2d_10 (Conv2D)
                           (None, 18, 18, 256)
                                               295168
    max pooling2d 10 (MaxPooli (None, 9, 9, 256)
    ng2D)
    flatten_2 (Flatten)
                           (None, 20736)
    dropout 2 (Dropout)
                           (None, 20736)
    dense_2 (Dense)
                                               20737
                           (None, 1)
    ______
   Total params: 409153 (1.56 MB)
   Trainable params: 409153 (1.56 MB)
   Non-trainable params: 0 (0.00 Byte)
epochs = 15
model4.compile(loss="binary_crossentropy", optimizer="adam", metrics=["accuracy"])
model4.fit(train_ds, epochs=epochs, validation_data=val_ds)
   Epoch 1/15
   625/625 [===========] - 43s 65ms/step - loss: 0.6648 - accuracy: 0.5889 - val loss: 0.5687 - val accuracy: 0.7162
   Epoch 2/15
   625/625 [===========] - 36s 58ms/step - loss: 0.5398 - accuracy: 0.7276 - val_loss: 0.4831 - val_accuracy: 0.7684
   Epoch 3/15
   625/625 [============= ] - 38s 60ms/step - loss: 0.4553 - accuracy: 0.7865 - val_loss: 0.4151 - val_accuracy: 0.8086
   Epoch 4/15
   625/625 [==========] - 38s 61ms/step - loss: 0.3883 - accuracy: 0.8253 - val loss: 0.3695 - val accuracy: 0.8388
   Epoch 5/15
   625/625 [===========] - 36s 58ms/step - loss: 0.3386 - accuracy: 0.8533 - val_loss: 0.3596 - val_accuracy: 0.8472
   Epoch 6/15
   Epoch 7/15
   625/625 [============] - 35s 55ms/step - loss: 0.2592 - accuracy: 0.8906 - val_loss: 0.3100 - val_accuracy: 0.8686
   Epoch 8/15
   625/625 [===========] - 36s 58ms/step - loss: 0.2259 - accuracy: 0.9055 - val_loss: 0.2785 - val_accuracy: 0.8848
   Epoch 9/15
   Epoch 10/15
   625/625 [===========] - 35s 56ms/step - loss: 0.1720 - accuracy: 0.9301 - val_loss: 0.2717 - val_accuracy: 0.8896
   Epoch 11/15
```

```
Epoch 12/15
   625/625 [==========] - 37s 59ms/step - loss: 0.1326 - accuracy: 0.9473 - val loss: 0.2774 - val accuracy: 0.8990
   Epoch 13/15
   Epoch 14/15
   625/625 [==========] - 37s 59ms/step - loss: 0.1083 - accuracy: 0.9559 - val loss: 0.2779 - val accuracy: 0.9014
   Epoch 15/15
   625/625 [===========] - 41s 66ms/step - loss: 0.1040 - accuracy: 0.9593 - val_loss: 0.2914 - val_accuracy: 0.8996
   <keras.src.callbacks.History at 0x7c85283057e0>
# TODO model5 with three more blocks of Conv2D and pooling
model5 = keras.Sequential([
   keras.Input(shape=input_shape2),
   layers.Rescaling(scale=1./255),
   layers.Conv2D(32, kernel size=(3, 3), activation="relu"),
  layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(64, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool size=(2, 2)),
   layers.Conv2D(128, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(256, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(512, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Flatten(),
   layers.Dropout(0.5),
   layers.Dense(1, activation="sigmoid"),
])
model5.summary()
```

Model: "sequential 3"

Layer (type)	Output Shape	Param #
rescaling_3 (Rescaling)	(None, 180, 180, 3)	0
conv2d_11 (Conv2D)	(None, 178, 178, 32)	896
<pre>max_pooling2d_11 (MaxPooli ng2D)</pre>	(None, 89, 89, 32)	0
conv2d_12 (Conv2D)	(None, 87, 87, 64)	18496
<pre>max_pooling2d_12 (MaxPooli ng2D)</pre>	(None, 43, 43, 64)	0
conv2d_13 (Conv2D)	(None, 41, 41, 128)	73856
<pre>max_pooling2d_13 (MaxPooli ng2D)</pre>	(None, 20, 20, 128)	0
conv2d_14 (Conv2D)	(None, 18, 18, 256)	295168
<pre>max_pooling2d_14 (MaxPooli ng2D)</pre>	(None, 9, 9, 256)	0
conv2d_15 (Conv2D)	(None, 7, 7, 512)	1180160

```
max pooling2d 15 (MaxPooli (None, 3, 3, 512)
                                                 0
     ng2D)
    flatten_3 (Flatten)
                                                 0
                            (None, 4608)
    dropout 3 (Dropout)
                            (None, 4608)
    dense_3 (Dense)
                            (None, 1)
                                                  4609
    ______
    Total params: 1573185 (6.00 MB)
    Trainable params: 1573185 (6.00 MB)
    Non-trainable params: 0 (0.00 Byte)
epochs = 15
model5.compile(loss="binary crossentropy", optimizer="adam", metrics=["accuracy"])
model5.fit(train_ds, epochs=epochs, validation_data=val_ds)
    Epoch 1/15
    625/625 [============= ] - 43s 65ms/step - loss: 0.6811 - accuracy: 0.5480 - val_loss: 0.6413 - val_accuracy: 0.6058
    Epoch 2/15
    625/625 [===========] - 35s 56ms/step - loss: 0.5850 - accuracy: 0.6811 - val_loss: 0.4866 - val_accuracy: 0.7604
    Epoch 3/15
    625/625 [=========== ] - 37s 59ms/step - loss: 0.4619 - accuracy: 0.7806 - val loss: 0.3909 - val accuracy: 0.8202
    Epoch 4/15
    625/625 [==========] - 36s 57ms/step - loss: 0.3631 - accuracy: 0.8402 - val loss: 0.3100 - val accuracy: 0.8596
    Epoch 5/15
    625/625 [===========] - 37s 59ms/step - loss: 0.2875 - accuracy: 0.8769 - val_loss: 0.2897 - val_accuracy: 0.8744
    Epoch 6/15
    625/625 [==========] - 35s 56ms/step - loss: 0.2344 - accuracy: 0.9015 - val loss: 0.2633 - val accuracy: 0.8866
    Epoch 7/15
    625/625 [=========== - 37s 59ms/step - loss: 0.1945 - accuracy: 0.9190 - val loss: 0.2589 - val accuracy: 0.8924
    Epoch 8/15
    625/625 [============ - 36s 57ms/step - loss: 0.1608 - accuracy: 0.9345 - val loss: 0.2492 - val accuracy: 0.8930
    Epoch 9/15
    625/625 [==========] - 37s 59ms/step - loss: 0.1252 - accuracy: 0.9487 - val loss: 0.2771 - val accuracy: 0.8984
    Epoch 10/15
    625/625 [===========] - 35s 56ms/step - loss: 0.1104 - accuracy: 0.9566 - val_loss: 0.2435 - val_accuracy: 0.9096
    Epoch 11/15
    625/625 [==========] - 38s 60ms/step - loss: 0.0896 - accuracy: 0.9646 - val loss: 0.2529 - val accuracy: 0.9076
    Epoch 12/15
    625/625 [============] - 36s 57ms/step - loss: 0.0831 - accuracy: 0.9677 - val_loss: 0.3111 - val_accuracy: 0.9036
    Epoch 13/15
    625/625 [==========] - 35s 56ms/step - loss: 0.0762 - accuracy: 0.9707 - val loss: 0.3363 - val accuracy: 0.9026
    Epoch 14/15
    625/625 [=========== - 36s 57ms/step - loss: 0.0612 - accuracy: 0.9761 - val loss: 0.3022 - val accuracy: 0.9000
    Epoch 15/15
    <keras.src.callbacks.History at 0x7c8510705ba0>
```

(9, 6pts) Architecture search could continue all day, but let's take a different approach to improving the network further. When the accuracy on the training data is higher than the validation accuracy, this is evidence of overfitting. Two approaches to handling overfitting are:

- More dropout. We have one big layer of dropout, but we could have one or more additional layers of Dropout(0.2).
- Data augmentation. If the dataset is randomly rotated and flipped, this encourages features that are robust against these transformations, and it makes it harder to overfit the data. We can work this into the pipeline itself with layers.RandomFlip("horizontal") and

layers.RandomRotation(0.1).

Train a new network with these two ideas worked into your best architecture so far. (Your best architecture is the one that you achieved the highest validation accuracy on.) The dropout locations are up to you. Use 20 epochs instead of 15, since these methods slow down the learning somewhat.

```
# TODO model6 with data augmentation and some extra dropout
model6 = keras.Sequential([
   keras.Input(shape=input_shape2),
   layers.Rescaling(scale=1./255),
   layers.RandomFlip("horizontal"),
   layers.RandomRotation(0.1),
   layers.Conv2D(32, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(64, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Dropout(0.2),
   layers.Conv2D(128, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Conv2D(256, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Dropout(0.2),
   layers.Conv2D(512, kernel_size=(3, 3), activation="relu"),
   layers.MaxPooling2D(pool_size=(2, 2)),
   layers.Flatten(),
   layers.Dropout(0.5),
   layers.Dense(1, activation="sigmoid"),
])
```

model6.summary()

Model: "sequential 6"

Layer (type)	Output Shape	Param #
rescaling_6 (Rescaling)	(None, 180, 180, 3)	0
<pre>random_flip_2 (RandomFlip)</pre>	(None, 180, 180, 3)	0
random_rotation (RandomRot ation)	(None, 180, 180, 3)	0
conv2d_26 (Conv2D)	(None, 178, 178, 32)	896
<pre>max_pooling2d_26 (MaxPooli ng2D)</pre>	(None, 89, 89, 32)	0
conv2d_27 (Conv2D)	(None, 87, 87, 64)	18496
<pre>max_pooling2d_27 (MaxPooli ng2D)</pre>	(None, 43, 43, 64)	0
dropout_10 (Dropout)	(None, 43, 43, 64)	0
conv2d_28 (Conv2D)	(None, 41, 41, 128)	73856
<pre>max_pooling2d_28 (MaxPooli ng2D)</pre>	(None, 20, 20, 128)	0

```
conv2d 29 (Conv2D)
                            (None, 18, 18, 256)
                                                  295168
    max_pooling2d_29 (MaxPooli (None, 9, 9, 256)
                                                  0
     ng2D)
    dropout 11 (Dropout)
                            (None, 9, 9, 256)
     conv2d_30 (Conv2D)
                            (None, 7, 7, 512)
                                                  1180160
     max pooling2d_30 (MaxPooli (None, 3, 3, 512)
                                                  0
     ng2D)
    flatten_6 (Flatten)
                            (None, 4608)
                            (None, 4608)
    dropout_12 (Dropout)
    dense_6 (Dense)
                            (None, 1)
                                                  4609
    ______
    Total params: 1573185 (6.00 MB)
    Trainable params: 1573185 (6.00 MB)
    Non-trainable params: 0 (0.00 Byte)
epochs = 20
model6.compile(loss="binary crossentropy", optimizer="adam", metrics=["accuracy"])
model6.fit(train_ds, epochs=epochs, validation_data=val_ds)
    Epoch 1/20
    625/625 [===========] - 46s 71ms/step - loss: 0.6810 - accuracy: 0.5599 - val_loss: 0.6502 - val_accuracy: 0.6412
    625/625 [==========] - 43s 68ms/step - loss: 0.6146 - accuracy: 0.6636 - val loss: 0.5630 - val accuracy: 0.7160
    Epoch 3/20
    625/625 [============] - 43s 69ms/step - loss: 0.5453 - accuracy: 0.7264 - val_loss: 0.4969 - val_accuracy: 0.7638
    625/625 [==========] - 44s 69ms/step - loss: 0.4815 - accuracy: 0.7710 - val loss: 0.4104 - val accuracy: 0.8118
    Epoch 5/20
    625/625 [============= ] - 44s 69ms/step - loss: 0.4391 - accuracy: 0.7957 - val_loss: 0.3652 - val_accuracy: 0.8330
    Epoch 6/20
    625/625 [=========== - 44s 70ms/step - loss: 0.4003 - accuracy: 0.8210 - val loss: 0.4222 - val accuracy: 0.7900
    Epoch 7/20
    625/625 [============] - 44s 69ms/step - loss: 0.3570 - accuracy: 0.8413 - val_loss: 0.3143 - val_accuracy: 0.8616
    Epoch 8/20
    625/625 [===========] - 43s 69ms/step - loss: 0.3399 - accuracy: 0.8511 - val_loss: 0.2713 - val_accuracy: 0.8866
    Epoch 9/20
    625/625 [==========] - 44s 69ms/step - loss: 0.3103 - accuracy: 0.8634 - val loss: 0.3141 - val accuracy: 0.8588
    Epoch 10/20
    625/625 [===========] - 44s 70ms/step - loss: 0.2995 - accuracy: 0.8698 - val_loss: 0.2428 - val_accuracy: 0.9004
    Epoch 11/20
    Epoch 12/20
    625/625 [===========] - 44s 69ms/step - loss: 0.2733 - accuracy: 0.8828 - val_loss: 0.2381 - val_accuracy: 0.8998
    Epoch 13/20
    625/625 [===========] - 44s 70ms/step - loss: 0.2689 - accuracy: 0.8852 - val_loss: 0.2204 - val_accuracy: 0.9088
    Epoch 14/20
    625/625 [===========] - 43s 69ms/step - loss: 0.2581 - accuracy: 0.8880 - val_loss: 0.2098 - val_accuracy: 0.9136
    Epoch 15/20
    625/625 [===========] - 43s 69ms/step - loss: 0.2533 - accuracy: 0.8921 - val_loss: 0.2048 - val_accuracy: 0.9114
    Epoch 16/20
```

(10, 7pts) Rather than building a model from nearly scratch, a different approach ("transfer learning") is to take an existing model that did something similar, including its trained weights, and retrain only a few layers at the very end of the model, keeping the rest of the model "frozen." This allows complex features learned from a lot of data to be used on smaller problems with less data, and it saves on training time as well.

You can base your code on the transfer learning example provided in lecture. (Note that since this is a binary classification problem instead of multiclass, you will need to change the final layer's activation function and the loss function.) You should keep the "adam" optimizer we've been using all along. You should only need to train to 7 epochs.

```
from keras.applications.vgg16 import VGG16
# TODO: define model7 using transfer learning
# Architecture based on https://machinelearningmastery.com/how-to-develop-a-convolutional-neural-network-to-classify-photos-of-dogs-and-cats/
model = VGG16(include top=False, input shape=(180,180,3)) # we'll replace the "top" with our own layers
for layer in model.layers:
  layer.trainable = False # these won't learn
# add new classifier layers
flat = layers.Flatten()(model.layers[-1].output) # connect to last layer of VGG
drop1 = layers.Dropout(0.5)(flat)
cls = layers.Dense(128, activation='relu')(drop1)
drop2 = layers.Dropout(0.5)(cls)
output = layers.Dense(1, activation='sigmoid')(drop2)
# define new model
model7 = keras.models.Model(inputs=model.inputs, outputs=output)
model7.compile(loss="binary crossentropy", optimizer="adam", metrics=["accuracy"])
model7.fit(train_ds, epochs=7,validation_data=val_ds)
   Epoch 1/7
   625/625 [==============] - 87s 118ms/step - loss: 0.6535 - accuracy: 0.9193 - val_loss: 0.1082 - val_accuracy: 0.9608
   Epoch 2/7
   Epoch 3/7
   Epoch 4/7
   Epoch 5/7
   625/625 [=============== - 74s 118ms/step - loss: 0.1069 - accuracy: 0.9639 - val_loss: 0.1066 - val_accuracy: 0.9628
   Epoch 6/7
   Epoch 7/7
   625/625 [============== - 74s 117ms/step - loss: 0.0909 - accuracy: 0.9661 - val_loss: 0.1038 - val_accuracy: 0.9642
   <keras.src.callbacks.History at 0x7e5e4c1ad510>
```

(11, 19pts) Last, answer these questions.

(a, 6 pts) Suppose we have a small perceptron with 3 inputs, no hidden units, and one output unit. The 2 inputs represent car attributes: cost (normalized to [0,1]), and mileage on the car (normalized to [0,1]). Assume the input neurons have no activation functions. Can this tiny network learn the rule, "fire if cost < 0.5, or mileage < 0.5"? If so, specify the weights in the network. If not, describe the smallest network you can that can effectively represent this rule (assuming the inputs still don't have activation functions and the output neuron's activation function is a step function) - give specific weights that would work.

TODO The tiny network cannot learn the rule "fire if cost < 0.5, or mileage < 0.5" if the input neurons have no activation functions.

The smallest network that can effectively represent this rule would be a two layer neural network with 2 neurons in the first layer, and 1 neuron in the second layer. The 2 neurons in the first layer would be able to learn the rule "fire if \cos < 0.5" and "fire if mileage < 0.5" (one rule for each neuron). The weights that could be specified could be $w_0=0.5$ and $w_1=-1$ where the neuron decides to fire if $w_0+\sum w_ix_i>0$. If the first input x_1 (representing \cos) is less than 0.5, then the inequality would be true, leading to the neuron to fire. These weights would also apply to the second neuron in the first layer to fire when the mileage is less than 0.5.

The single neuron in the second layer would utilize the OR boolean operation, taking in the outputs from the 2 neurons in the first layer. The weights for the neuron in the second layer would be $w_0=-0.5$, and $w_1,w_2=0.5$ where the neuron uses the inequality $w_0+\sum w_ix_i\geq 0$ to determine if it fires.

This tiny network would be able to learn the rule "fire if cost < 0.5, or mileage < 0.5."

(b, 3pts) Give values for a 3x3 convolutional filter that would plausibly detect small X's in the image - the meeting of two diagonal lines. Assume the lines are both white or both black (your choice).

TODO A convolutional filter that would plausibly detect small X's in the image - the meeting of two diagonal lines would be:

[[1, -1, 1],

[-1, 1, -1],

[1, -1, 1]]

This convolutional filter would detect small X's in the image because this filter would be the most active when the diagonal pixels in the filter are the similar while the non-diagonal pixels are very different from the diagonal pixels. This convolutional filter will highlight the intersection of these diagonal lines, and detect the small X's in the image.

(c, 3pts) Transfer learning is effective, and it's more effective the more similar the original task was to the present one. Skim the Wikipedia page on ImageNet, the dataset used to train VGG-16 (and maybe follow up by searching this subset of ImageNet's classes: https://gist.github.com/yrevar/942d3a0ac09ec9e5eb3a). Is there reason to think transfer learning with VGG-16 might be particularly effective for classifying cats and dogs?

TODO One reason why transfer learning with VGG-16 might be particularly effective for classifying cats and dogs is because the ImageNet dataset contains 120 categories of dog breeds to showcase fine-grained classification. Since VGG-16 was trained on the ImageNet dataset, VGG-16 would be able to precicely identify dogs, and is able to classify 120 different dog breeds. Due to the this training dataset, transfer learning with VGG-16 would be particularly effective for classifying cats and dogs.

(d, 3pts) Suppose we introduce a new activation function in all the neurons in our neural network, $g(x) = \sin(x)$. We then notice vanishing gradient problems. What are some values of x that would be particularly problematic for this function in backpropagation?

TODO Some values of x that would be particularly problematic for this function in backpropagation would be $\frac{\pi}{2}, \frac{3\pi}{2}, \dots$ This is because the gradient at these x values would be 0, causing the vanishing gradient problem to quickly occur during backpropagation.

(e, 4pts) A museum wants to train a neural network to identify plants, using museum plant specimens. In some cases they only have one example of a species, though, making a train/test split difficult. They decide to use data augmentation in these cases, putting most of the augmented images in the training set with the original image, but also putting a few augmented images in the test set in each case. Will this classifier have good performance "in the wild" on these species? Why or why not? Would we get better performance if we just trained on the unaugmented, single image?

TODO I believe that the classifier trained on data with additional data augmentation will have good performance "in the wild" on these species. Data augmentation would enable the model to learn more generic features about the species of plant, learning to correctly classify the plant even when the image is rotated and flipped, better simulating the differing camera angles and images gained from the real world.

The model would have much worse performance if it was just trained on the unaugmented, single image. If the model was only trained on the single image of the species of plant, the model would easily overfit to the singular image, and wouldn't be able to easily recognize other photos of the same species.

When you're done, use "File->Download .ipynb" and upload your .ipynb file to Blackboard, along with a PDF version (File->Print->Save as PDF) of your assignment.