### Assignment 3

https://github.com/jchryssanthacopoulos/quantum\_information/tree/main/assignment\_3

# Quantum Information and Computing AA 2022–23

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#### Exercise 1: Matrix Multiplication Scaling



- Matrix multiplication program extended to parse command-line arguments using get\_command\_argument
- Python script written in Jupyter notebook to make subprocess calls to Fortran program to get runtimes

```
$ compiled/exercise 1 00 \
--mat mul method matmul --num rows 3 \
--num_cols 3 --num_inner_dim 4 --debug
mat mul method = matmul
num_rows = 3
num cols = 3
num inner dim = 4
Running in debug mode ...
Matrix A =
  0.43 0.39
               0.04
  0.42 0.95 0.88
                     0.55
  0.01 0.19 0.47
                     0.62
Matrix B =
  0.10 0.37 0.73
  0.96 0.39 0.38
  0.03 0.53 0.23
  0.21 0.36 0.69
Product =
        0.39 0.59
  1.10 1.19 1.25
         0.55 0.62
Elapsed time = 7.0000000000E-06
```

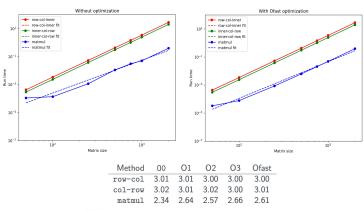
```
def get_run_time(mat_mul_method, flag, mat_dim):
    ""Get the run time for the given matrix multiplication method,
    optimization flag, and matrix dimension.
    """ matrix dimension.
    """ mat_mul_method", mat_mul_method,
    """ num_rows", str(mat_dim),
    """ num_cols", str(mat_dim),
    """ num_inner_dim", str(mat_dim)
}

output = subprocess.run(
    run_params, stdout=subprocess.PIPE, encoding='ascii'
)
lines = output.stdout.split('\n')
return float(lines[4].split('=')[1])
```

#### Exercise 1: Matrix Multiplication Scaling



## Linear fit of log run time to log matrix size performed with numpy's polyfit



**Table:** Polynomial time complexity, given by coefficient a in fit  $\log T = a \log N + b$ 

#### Exercise 2: Eigenproblem



- Hermitian matrix created with random number generator
- Eigenvalues computed using zheev

```
function rand hermitian matrix(n) result(H)
   integer n
   integer ii, ii
   complex*16, dimension(n, n) :: H
                                                                  ! compute eigenvalues in ascending order
   do ii = 1, n
       do ii = 1, ii
                                                                  call zheev('N', 'U', ndim, H, ndim, eigvals, work, lwork, rwork, info)
           if (ii /= ii) then
               ! sample random complex numbers off the diagonal
                                                                  ! compute eigenvalue spacings and average
              H(11, 11) = cmplx(RAND(8)+2 - 1, RAND(8)+2 - 1)
                                                                  ave delta eigvals = (eigvals(ndim) - eigvals(1)) / (ndim - 1)
              H(ii, ii) = conig(h(ii, ii))
                                                                  do ii = 1. ndin - 1
                                                                       norm eigval spacings(ii) = (eigvals(ii + 1) - eigvals(ii)) / ave delta eigvals
               ! sample real numbers on the diagonal
                                                                  end do
              H(ii, ii) = BMND(8)*2 - 1
           end if
   end do
end function
```

#### Exercise 3: Random Matrix Theory



- Distribution of normalized spacings P(s) produced for Hermitian and diagonal matrix
- Fit to  $P(s) = as^{\alpha} \exp(bs^{\beta})$  performed using scipy's curve\_fit function

```
def func(x, a, b, alpha, beta):
    return a * x ** alpha * np.exp(b * x ** beta)
    popt, pcov = curve_fit(func, bin_centers, norm_count)
    popt
array([13.79272512, -2.82466922, 2.59653888, 1.32155578])
```

Matrix	а	Ь	$\alpha$	$\beta$
hermitian	$13.792 \pm 2.266$	$-2.825 \pm 0.166$	$2.597 \pm 0.091$	$1.322 \pm 0.043$
diagonal	$1.017 \pm 0.007$	$-1.018 \pm 0.008$	$0.005 \pm 0.002$	$0.987 \pm 0.005$