Interfacing the geometry software polymake

Version 0.8.6

8 July 2021

Marc Roeder

Marc Roeder

Email: roeder.marc@gmail.com

Abstract

This package provides a very basic interface to the polymake program by Ewgenij Gawrilow, Michael Joswig et al. [GJ]. The polymake program itself is not included.

Copyright

© 2007–2013 Marc Roeder.

This package is distributed under the terms of the GNU General Public License version 2 or later (at your convenience). See the file "LICENSE" or https://www.gnu.org/copyleft/gpl.html

Acknowledgements

This work has been supported by Marie Curie Grant No. MTKD-CT-2006-042685

Contents

1	Installation and Preface				
	1.1	A few words about the installation of polymake	4		
	1.2	Setting variables for external programs	4		
2	Polymake interaction				
	2.1	Creating Polymake Objects	6		
	2.2	Accessing Properties of Polymake Objects	7		
	2.3	Example: Creating and Accessing Polymake Objects	8		
	2.4	Writing to Polymake Objects	9		
	2.5	Calling Polymake and converting its output	10		
	2.6	An Example	11		
3	Global Variables				
	3.1	Getting information about polymake output	13		
	3.2	Variables for system interaction	13		
4	Converting Polymake Output				
	4.1	The General Method	15		
	4.2	Conversion Functions	16		
Re	eferen	ices	19		
Index					

Installation and Preface

To install the package, just unpack it in your packages directory (usually ~/gap/pkg for local installation). To use polymaking, you need a working installation of the program polymake https://polymake.org. The package has been tested on linux and Mac OS X (10.4, 10.5 and 10.6). But it should be as platform independent as GAP and polymake.

The interaction with polymake is restricted to writing files and carrying out simple operations. These looked like

polymake file KEYWORD1 KEYWORD2 KEYWORD3

on the command line for polymake versions before 4. The keywords are polymake methods without arguments. Since polymake no longer supports this interface the polymaking package provides the script lib/pm_script_arg.pl to emulate this.

polymake --script lib/pm_script_arg.pl KEYWORD1 KEYWORD2 KEYWORD3 Using custom scripts is not supported.

Every call to polymake will re-start the program anew. This causes considerable overhead. The number of calls to polymake is reduced by caching the results in the so-called PolymakeObject in GAP. As of polymaking version 0.8.0, old versions of polymake (i.e. versions before 2.7.9) are not supported anymore.

1.1 A few words about the installation of polymake

polymaking will try to guess the location of polymake. If this fails, a warning is issued at load time (InfoWarning level 1). Note that the guessing procedure is suppressed when POLYMAKE_COMMAND (3.2.1) is set manually (see 1.2.3).

setenv PATH \${PATH}:<your polymakepath>

The general rule is: If polymaking finds polymake by itself, there is nothing to worry about.

1.2 Setting variables for external programs

As polymaking uses the program polymake, it needs to know where this program lives. The communication with polymake is done by writing files for polymake and reading its output (as returned to standard output "the prompt"). Note that the interface does not read any polymake file.

1.2.1 SetPolymakeDataDirectory

```
▷ SetPolymakeDataDirectory(dir)
```

(method)

Sets the directory in which all polymake files are created to *dir*. The standard place for these files is a temporary directory generated when the package is loaded. This manipulates POLYMAKE_DATA_DIR (3.2.2).

1.2.2 SetPolymakeCommand

```
    ▷ SetPolymakeCommand(command)
```

(method)

Sets the name for the polymake program to *command*. This manipulates POLYMAKE_COMMAND (3.2.1).

1.2.3 Setting variables permanently

To permanently set the values of POLYMAKE_COMMAND (3.2.1), and POLYMAKE_DATA_DIR (3.2.2), add the lines

```
POLYMAKE_DATA_DIR:=Directory("/home/mypolymakedatadir");
POLYMAKE_COMMAND:=Filename(Directory("/home/mypolymakebindir/"),"polymake");
```

to your .gaprc file (see The .gaprc file???). Note that these have to be *before* the LoadPackage("polymaking"); line. Or you can change the values of the above variables by editing lib/environment.gi

Polymake interaction

2.1 Creating Polymake Objects

The interaction with the polymake program is done via files. A PolymakeObject is mainly a pointer to a file and a list of known properties of the object. These properties need not be stored in the file. Whenever polymake is called, the returned value is read from standard output and stored in the PolymakeObject corresponding to the file for which polymake is called. The files for polymake are written in the old (non-xml) format. The first run of polymake converts them into the new (xml) format. This means that changes to the file by means of the methods outlined below after the first run of polymake will probably lead to corrupted files.

2.1.1 CreateEmptyFile

▷ CreateEmptyFile(filename)

(method)

Returns: nothing

Creates an empty file with name filename. Note that filename has to include the full path and the directory for the file must exist.

2.1.2 CreatePolymakeObject

\triangleright	<pre>CreatePolymakeObject()</pre>	(method)
\triangleright	<pre>CreatePolymakeObject(appvertyp)</pre>	(method)
\triangleright	<pre>CreatePolymakeObject(dir)</pre>	(method)
\triangleright	<pre>CreatePolymakeObject(dir, appvertyp)</pre>	(method)
\triangleright	<pre>CreatePolymakeObject(prefix, dir)</pre>	(method)
\triangleright	<pre>CreatePolymakeObject(prefix, dir, appvertyp)</pre>	(method)

Returns: PolymakeObject

If called without arguments, this method generates an empty file in the directory defined by POLYMAKE_DATA_DIR (3.2.2). If a directory dir is given (this directory must exist), an empty file is generated in this directory. If prefix is not given, the file is called polyN where N is the current runtime. If a file of this name already exists, a number is appended separated by a dot (example: "poly1340" and "poly1340.1"). If prefix is given, the filename starts with this prefix. Optionally, the file can be generated with a header specifying application, version and type of the object. This is done by passing the triple of strings appvertyp to CreatePolymakeObject. A valid triple

is ["polytope", "2.3", "RationalPolytope"]. Validity is checked by CheckAppVerTypList (2.1.3).

2.1.3 CheckAppVerTypList

▷ CheckAppVerTypList(appvertyp)

(method)

Returns: bool

Checks if the triple *arppvertyp* of strings specifies an application and type of polymake version 2.3. More specifically, the first entry has to be an application from ["polytope", "surface", "topaz"] and the third entry has to be a type corresponding to the application given in the first entry. The second entry is not checked.

2.1.4 CreatePolymakeObjectFromFile

▷ CreatePolymakeObjectFromFile(filename)

(method)

▷ CreatePolymakeObjectFromFile(dir, filename)

(method)

Returns: PolymakeObject

This method generates a PolymakeObject corresponding to the file *filename* in the directory *dir*. If *dir* is not given, the POLYMAKE_DATA_DIR is used. If no file with name *filename* exists in *dir* (or POLYMAKE_DATA_DIR, respectively), an empty file is created. Note that the contents of the file do not matter for the generation of the object. In particular, the object does not know any of the properties that might be encoded in the file. The only way to transfer information from files to PolymakeObjects is via Polymake (2.5.1).

2.2 Accessing Properties of Polymake Objects

A PolymakeObject contains information about the directory of its file, the name of its file and about properties calculated by calling Polymake (2.5.1). The properties returned by the polymake program are stored under the name polymake assigns to them (that is, the name of the data block in the corresponding file). The following methods can be used to access the information stored in a PolymakeObject. But be careful! All functions return the actual object. No copies are made. So if you change one of the returned objects, you change the PolymakeObject itself.

2.2.1 DirectoryOfPolymakeObject

DirectoryOfPolymakeObject(poly)

(method)

Returns: Directory

Returns the directory of the file associated with poly.

2.2.2 FilenameOfPolymakeObject

(method)

Returns: String

Returns the name of the file associated with *poly*. This does only mean the name of the *file*, not the full path. For the full path and file name see FullFilenameOfPolymakeObject (2.2.3)

2.2.3 FullFilenameOfPolymakeObject

⊳ FullFilenameOfPolymakeObject(poly)

(method)

Returns: String

Returns the file associated with the PolymakeObject poly with its complete path.

2.2.4 NamesKnownPropertiesOfPolymakeObject

▷ NamesKnownPropertiesOfPolymakeObject(poly)

(method)

Returns: List of Strings

Returns a list of the names of all known properties. This does only include the properties returned by Polymake (2.5.1), "dir" and "filename" are not included. If no properties are known, fail is returned.

2.2.5 KnownPropertiesOfPolymakeObject

▷ KnownPropertiesOfPolymakeObject(poly)

(method)

Returns: Record

Returns the record of all known properties. If no properties are known, fail is returned.

2.2.6 PropertyOfPolymakeObject

```
▷ PropertyOfPolymakeObject(poly, name)
```

(method)

Returns the value of the property name if it is known. If the value is not known, fail is returned. name must be a String.

2.3 Example: Creating and Accessing Polymake Objects

Suppose the file /tmp/threecube.poly contains the three dimensional cube in polymake form. Now generate a PolymakeObject from this file and call Polymake (2.5.1) to make the vertices of the cube known to the object.

```
### suppose we have a polymake file /tmp/threecube.poly
### containing a cube in three dimensions
gap> cube:=CreatePolymakeObjectFromFile(Directory("/tmp"),"threecube.poly");
<polymake object. No properties known>
gap> FilenameOfPolymakeObject(cube);
"threecube.poly"
gap> FullFilenameOfPolymakeObject(cube);
"/tmp/threecube.poly"
    #nothing is known about the cube:
gap> NamesKnownPropertiesOfPolymakeObject(cube);
fail
gap> Polymake(cube, "VERTICES");
[[-1, -1, -1], [1, -1, -1], [-1, 1, -1], [1, 1, -1], [-1, -1, 1],
    [1, -1, 1], [-1, 1, 1], [1, 1, 1]]
# Now <cube> knows its vertices:
```

2.4 Writing to Polymake Objects

To transfer data from GAP to polymake, the following methods can be used. But bear in mind that none of these functions test if the resulting polymake file is still consistent.

2.4.1 AppendToPolymakeObject

This appends the string string to the file associated to the PolymakeObject poly. It is not tested if the string is syntactically correct as a part of a polymake file. It is also not tested if the string is compatible with the data already contained in the file.

INEQUALITIES, POINTS and VERTICES can be appended to a polymake object using the following functions:

2.4.2 AppendPointlistToPolymakeObject

```
▷ AppendPointlistToPolymakeObject(poly, pointlist)
    Returns: nothing
```

Takes a list pointlist of vectors and converts it into a string which represents a polymake block labeled "POINTS". This string is then added to the file associated with poly. The "POINTS" block of the file associated with poly then contains points with leading ones, as polymake uses affine notation.

2.4.3 AppendVertexlistToPolymakeObject

Does the same as AppendPointlistToPolymakeObject, but with "VERTICES" instead of "POINTS".

2.4.4 AppendInequalitiesToPolymakeObject

Just appends the inequalities given in <code>ineqlist</code> to the polymake object <code>poly</code> (with caption "IN-EQUALITIES"). Note that this does not check if an "INEQUALITIES" section does already exist in the file associated with <code>poly</code>.

2.4.5 ConvertMatrixToPolymakeString

▷ ConvertMatrixToPolymakeString(name, matrix)

(method)

Returns: String

This function takes a matrix matrix and converts it to a string. This string can then be appended to a polymake file via AppendToPolymakeObject (2.4.1) to form a block of data labeled name. This may be used to write blocks like INEQUALITIES or FACETS.

2.4.6 ClearPolymakeObject

▷ ClearPolymakeObject(poly)

(method)

▷ ClearPolymakeObject(poly, appvertyp)

(method)

Returns: nothing

Deletes all known properties of the PolymakeObject *poly* and replaces its file with an empty one.

If the triple of strings appvertyp specifying application, version and type (see CheckAppVerTypList (2.1.3)) is given, the file is replaced with a file that contains only a header specifying application, version and type of the polymake object.

There are also methods to manipulate the known values without touching the file of the PolymakeObject:

2.4.7 WriteKnownPropertyToPolymakeObject

(method)

Takes the object data and writes it to the known properties section of the PolymakeObject poly. The string name is used as the name of the property. If a property with that name already exists, it is overwritten. Again, there is no check if data is consistent, correct or meaningful.

2.4.8 UnbindKnownPropertyOfPolymakeObject

□ UnbindKnownPropertyOfPolymakeObject(poly, name)

(method)

If the PolymakeObject *poly* has a property with name *name*, that property is unbound. If there is no such property, fail is returned.

2.5 Calling Polymake and converting its output

2.5.1 Polymake

▷ Polymake(poly, option: PolymakeNolookup)

(method)

This method calls the polymake program (see POLYMAKE_COMMAND (3.2.1)) with the option option. You may use several keywords such as "FACETS VERTICES" as an option. The returned value is cut into blocks starting with keywords (which are taken from output and not looked up in option). Each block is then interpreted and translated into GAP readable form. This translation is done using the functions given in ObjectConverters (4.1.4). The first line of each block of polymake output is taken as a keyword and the according entry in ObjectConverters (4.1.4) is called

to convert the block into GAP readable form. If no conversion function is known, an info string is printed and fail is returned. If only one keyword has been given as option, Polymake returns the result of the conversion operation. If more than one keyword has been given or the output consists of more than one block, Polymake returns fail. In any case, the calculated values for each block are stored as known properties of the PolymakeObject poly as long as they are not fail. If Polymake is called with an option that corresponds to a name of a known property of poly, the known property is returned. In this case, there is no call of the external program. (see below for suppression of this feature).

Note that the command Polymake returns fail if nothing is returned by the program polymake or more than one block of data is returned. For example, the returned value of Polymake(poly, "VISUAL") is always fail. Likewise, Polymake(poly, "POINTS VERTICES") will return fail (but may add new known properties to poly). For a description of the conversion functions, see chapter 4.

If the option *PolymakeNolookup* is set to anything else than false, the polymake program is called even if *poly* already has a known property with name *option*.

Note that whenever Polymake (2.5.1) returns fail, a description of the problem is stored in POLYMAKE_LAST_FAIL_REASON (3.1.2). If you call Polymake (2.5.1) with more than one keyword, POLYMAKE_LAST_FAIL_REASON (3.1.2) is changed before polymake is called. So any further reason to return fail will overwrite it.

2.6 An Example

Let's generate a three dimensional permutahedron.

```
_ Example
gap> S:=SymmetricGroup(3);
Sym([1..3])
gap> v := [1,2,3];
[1,2,3]
gap> points:=Orbit(S,v,Permuted);;
gap> permutahedron:=CreatePolymakeObject();
<polymake object. No properties known>
gap> AppendPointlistToPolymakeObject(permutahedron,points);
gap> Polymake(permutahedron, "VOLUME");
gap> Polymake(permutahedron, "N_VERTICES");
      #Now <permutahedron> knows its number of vertices, but not the vertices:
gap> PropertyOfPolymakeObject(permutahedron, "VERTICES");
gap> NamesKnownPropertiesOfPolymakeObject(permutahedron);
[ "VOLUME", "N_VERTICES" ]
    #Let's look at the object!
gap> Polymake(permutahedron, "VISUAL");
#I There was no or wrong polymake output
gap> Polymake(permutahedron, "DIM");
```

Global Variables

3.1 Getting information about polymake output

3.1.1 InfoPolymaking

▷ InfoPolymaking (info class)

If set to at least 2, the output of polymake is shown. At level 1, warnings are shown. This is the default. And at level 0, the polymake package remains silent.

3.1.2 POLYMAKE_LAST_FAIL_REASON

▷ POLYMAKE_LAST_FAIL_REASON

(global variable)

Contains a string that explains the last occurrence of fail as a return value of Polymake (2.5.1).

3.2 Variables for system interaction

The variables for interaction with the system are contained in the file environment.gi. Each of these variables has a function to set it, see 1.2. If POLYMAKE_COMMAND or POLYMAKE_DATA_DIR are set at startup, they are not overwritten. So if you don't want (or don't have the rights) to modify environment.gi, you can set the variables in your .gaprc file.

3.2.1 POLYMAKE_COMMAND

▷ POLYMAKE_COMMAND (global variable)

This variable should contain the name of the polymake program in the form as returned by Filename So a probable value is Filename (Directory("/usr/local/bin"), "polymake").

3.2.2 POLYMAKE_DATA_DIR

▷ POLYMAKE_DATA_DIR

(global variable)

In this directory the files for polymake will be created. By default, this generates a temporary directory using DirectoryTemporary

Converting Polymake Output

4.1 The General Method

When polymake is called, its output is read as a string and then processed as follows:

- 1. the lines containing upper case letters are found. These are treated as lines containing the keywords. Each of those lines marks the beginning of a block of data.
- 2. The string is then cut into a list of blocks (also strings). Each block starts with a line containing the keyword and continues with some lines of data.
- 3. for each of the blocks, the appropriate function of ObjectConverters is called. Here "appropriate" just means, that the keyword of the block coincides with the name of the function.
- 4. The output of the conversion function is then added to the known properties of the PolymakeObject for which Polymake was called.

4.1.1 Converter- Philosopy

The converter functions should take meaningful polymake data into meaningful GAP data. This sometimes means that the (mathematical) representation is changed. Here is an example: polymake writes vectors as augmented affine vectors of the form 1 a1 a2 a3... which does not go very well with the usual GAP conventions of column vectors and multiplying matrices from the right. So polymaking converts such a vector to [a1,a2,a3,...] and the user is left with the problem of augmentation and left or right multiplication.

Another area where the GAP object isn't a literal translation from the polymake world is combinatorics. In Polymake, list elements are enumerated starting from 0. GAP enumerates lists starting at 1. So the conversion process adds 1 to the numbers corresponding to vertices in facet lists, for example.

The conversion process is done by the following methods:

4.1.2 ConvertPolymakeOutputToGapNotation

▷ ConvertPolymakeOutputToGapNotation(string)

(method)

Returns: Record having polymake keywords as entry names and the respective converted polymake output as entries.

Given a the output of the polymake program as a string *string*, this method first calls SplitPolymakeOutputStringIntoBlocks (4.1.3). For each of the returned blocks, the name (=first line) of the block is read and the record ObjectConverters (4.1.4) is looked up for an entry with that name. If such an entry exists, it (being a function!) is called and passed the block. The returned value is then given the name of the block and added to the record returned by ConvertPolymakeOutputToGapNotation.

4.1.3 SplitPolymakeOutputStringIntoBlocks

▷ SplitPolymakeOutputStringIntoBlocks(string)

(method)

Returns: List of strings – "blocks"–

The string string is cut at the lines starting with an upper case character and consisting only of upper case letters, numbers and underscore (_) characters. The parts are returned as a list of strings. The initial string string remains unchanged.

4.1.4 ObjectConverters

▷ ObjectConverters

(global variable)

The entries of this record are labeled by polymake keywords. Each of the entries is a function which converts a string returned by polymake to GAP format. So far, only a few converters are implemented. To see which, try RecNames (ObjectConverters);

You can define new converters using the basic functions described in section 4.2.

4.2 Conversion Functions

The following functions are used for the functions in ObjectConverters (4.1.4).

4.2.1 ConvertPolymakeNumber

▷ ConvertPolymakeNumber(string)

(method)

The string string is converted to a rational number. Unlike Rat, it tests, if the number represented by string is a floating point number an converts it correctly. If this is the case, a waring is issued.

4.2.2 ConvertPolymakeScalarToGAP

▷ ConvertPolymakeScalarToGAP(list)

(method)

If *list* contains a single string, this string is converted into a number using ConvertPolymakeNumber (4.2.1).

4.2.3 ConvertPolymakeMatrixOrListOfSetsToGAP

▷ ConvertPolymakeMatrixOrListOfSetsToGAP(list)

(method)

 ${\tt \triangleright ConvertPolymakeMatrixOrListOfSetsToGAPPlusOne}(list) \\$

(method)

Tries to decide if the list *list* of strings represents a matrix or a list of sets by testing if they start with "{". It then calls either ConvertPolymakeMatrixToGAP (4.2.4) or ConvertPolymakeListOfSetsToGAP (4.2.8). The "PlusOne" version calls ConvertPolymakeListOfSetsToGAPPlusOne (4.2.8) if *list* represents a list of sets.

4.2.4 ConvertPolymakeMatrixToGAP

▷ ConvertPolymakeMatrixToGAP(list) (method)
▷ ConvertPolymakeMatrixToGAPKillOnes(list) (method)

The list *list* of strings is interpreted as a list of row vectors and converted into a matrix. The "KillOnes" version removes the leading ones.

4.2.5 ConvertPolymakeVectorToGAP

▷ ConvertPolymakeVectorToGAP(list) (method)
▷ ConvertPolymakeVectorToGAPKillOne(list) (method)
▷ ConvertPolymakeIntVectorToGAPPlusOne(list) (method)

As the corresponding "Matrix" version. Just for vectors. ConvertPolymakeIntVectorToGAPPlusOne requires the vector to contain integers. It also adds 1 to every entry.

4.2.6 ConvertPolymakeBoolToGAP

▷ ConvertPolymakeBoolToGAP(list)

(method)

If *list* contains a single string, which is either 0,false,1, or true this function returns false or true, respectively.

4.2.7 ConvertPolymakeSetToGAP

▷ ConvertPolymakeSetToGAP(list)

(method)

Let *list* be a list containing a single string, which is a list of numbers separated by whitespaces and enclosed by { and } . The returned value is then a set of rational numbers (in the GAP sense).

4.2.8 ConvertPolymakeListOfSetsToGAP

Let *list* be a list containing several strings representing sets. Then each of these strings is converted to a set of rational numbers and the returned value is the list of all those sets. The "PlusOne" version adds 1 to every entry.

${\bf 4.2.9}\quad Convert Polymake Graph To GAP$

(method)

Let list be a list of strings representing sets (that is, a list of integers enclosed by $\{$ and $\}$). Then a record is returned containing two sets named .vertices and .edges.

References

[GJ] Ewgenij Gawrilow and Michael Joswig. polymake. http://polymake.org/. 2

Index

```
AppendInequalitiesToPolymakeObject, 9
                                          ObjectConverters, 16
AppendPointlistToPolymakeObject, 9
                                          Polymake, 10
AppendToPolymakeObject, 9
                                          POLYMAKE_COMMAND, 13
AppendVertexlistToPolymakeObject, 9
                                          POLYMAKE_DATA_DIR, 13
CheckAppVerTypList, 7
                                          POLYMAKE_LAST_FAIL_REASON, 13
ClearPolymakeObject, 10
                                          PropertyOfPolymakeObject, 8
ConvertMatrixToPolymakeString, 10
                                          SetPolymakeCommand, 5
ConvertPolymakeBoolToGAP, 17
                                          SetPolymakeDataDirectory, 5
ConvertPolymakeGraphToGAP, 18
                                          SplitPolymakeOutputStringIntoBlocks, 16
ConvertPolymakeIntVectorToGAPPlusOne,
       17
                                          UnbindKnownPropertyOfPolymakeObject, 10
ConvertPolymakeListOfSetsToGAP, 17
ConvertPolymakeListOfSetsToGAPPlusOne,
                                          WriteKnownPropertyToPolymakeObject, 10
       17
ConvertPolymakeMatrixOrListOfSets-
       ToGAP, 16
ConvertPolymakeMatrixOrListOfSetsToGA-
       PPlusOne, 16
ConvertPolymakeMatrixToGAP, 17
ConvertPolymakeMatrixToGAPKillOnes, 17
ConvertPolymakeNumber, 16
ConvertPolymakeOutputToGapNotation, 15
ConvertPolymakeScalarToGAP, 16
ConvertPolymakeSetToGAP, 17
ConvertPolymakeVectorToGAP, 17
ConvertPolymakeVectorToGAPKillOne, 17
CreateEmptyFile, 6
CreatePolymakeObject, 6
CreatePolymakeObjectFromFile, 7
DirectoryOfPolymakeObject, 7
FilenameOfPolymakeObject, 7
FullFilenameOfPolymakeObject, 8
InfoPolymaking, 13
KnownPropertiesOfPolymakeObject, 8
NamesKnownPropertiesOfPolymakeObject, 8
```