10.- Calcula los evatro primeros terminos del desarrollo en serve de Taylor en 2:0 de la función:

$$f'(z) = -(1+e^{z})^{-2}$$
. e^{z} $f'(0) = -\frac{1}{4}$

$$f''(z) = -e^{\frac{z}{2}(1+e^{z})^{-2}} + e^{\frac{z}{2}} \cdot 2(1+e^{\frac{z}{2}})^{\frac{3}{2}} \cdot e^{\frac{z}{2}} = 2e^{\frac{z}{2}}(1+e^{\frac{z}{2}})^{-3} - e^{\frac{z}{2}}(1+e^{\frac{z}{2}})^{-2}$$

$$=) f(z) \sim \frac{1}{2} - \frac{1}{4}z + \frac{1}{8 \cdot 3!}z^3 = \frac{1}{2} - \frac{z}{4} + \frac{z^3}{48}$$

=)
$$f(z) \sim 1 + z - \frac{2}{31}z^3 = 1 + z - \frac{z^3}{3}$$

c)
$$f(z) = \sqrt{g} z = \frac{senz}{cosz}$$

$$f'(z) = \frac{\cos^2 z + \sin^2 z}{(\cos z)^2} = \frac{1}{\cos^2 z} = 1 + 4g^2 z$$

f(0)=0

f'(0)=1

f 1/0) = 0 f 111)(0)=2