

I. E. S. " SAN ISIDRO

Calificación

$$\Rightarrow 2\cos^2\theta = 1 + \cos 2\theta \Leftrightarrow \cos^2\theta = \frac{1}{2} + \cos 2\theta$$

$$\Rightarrow f(z) = \cos^2\left(\frac{cz}{2}\right) = \frac{1}{2} + \cos\left(\frac{cz}{2}\right) = \frac{1}{2} + \frac{\cos(iz)}{2} = \frac{1}{2} + \frac{\cosh(z)}{2}$$

$$f'(z) = \frac{\text{senhz}}{2}$$

$$f^{(2)}(z) = \frac{\cosh z}{2}$$

$$f^{(3)}(z) = \frac{\sinh z}{2}$$

$$\Rightarrow f^{(n)}(z) = \begin{cases} \frac{\sinh z}{2} & \text{sin impar} \\ \frac{\cosh z}{2} & \text{sin par} \end{cases} f^{(n)}(0) = \begin{cases} \frac{\sinh(0)}{2} = 0 & \text{sin impar} \\ \frac{\cosh(0)}{2} = \frac{1}{2} & \text{sin par} \end{cases}$$

$$= \int f(z) = \cos^{2}(\frac{dz}{2}) = \sum_{n=0}^{\infty} \frac{f^{(n)}(0)}{n!} (z-0)^{n} = 1 + \sum_{n=1}^{\infty} \frac{f^{(n)}(0)}{n!} z^{n} + \sum_{n=1}^{\infty} \frac{f^{(n)}(0)}{n!} z^{n}$$

$$= 1 + \frac{1}{2} \sum_{n=1}^{\infty} \frac{z^{2n}}{2n!}$$

7.- Desarrolla en serie de poteneias las siguientes funciones y halla el radro de convergencia

D(1, 12-12)

f(Z) = Z es holomorte en el disco D(0,1) y en D(1, 11-e'-1)

 $\frac{z}{|c|z^2} = \frac{z}{(z-e^{i\frac{\pi}{4}})(z-e^{i\frac{\pi}{4}})} = \frac{A}{z-e^{i\frac{\pi}{4}}} + \frac{B}{z-e^{i\frac{\pi}{4}}}$