10. Calcula los evatro primeros terminos del desarrollo en serve de Taylor en z=0 de la función:

$$f'(z) = -(1+e^{z})^{-2}$$
. e^{z} $f'(0) = -\frac{1}{4}$

$$f''(z) = -e^{\frac{z}{2}(1+e^{z})^{-2}} + e^{\frac{z}{2}} \cdot 2(1+e^{\frac{z}{2}})^{\frac{3}{2}} \cdot e^{\frac{z}{2}} = 2e^{\frac{z}{2}}(1+e^{\frac{z}{2}})^{-3} - e^{\frac{z}{2}}(1+e^{\frac{z}{2}})^{-2}$$

$$=) f(z) \sim \frac{1}{2} - \frac{1}{4}z + \frac{1}{8 \cdot 3!}z^3 = \frac{1}{2} - \frac{z}{4} + \frac{z^3}{48}$$

$$f''(z) = e^z \cos z - e^z \sin z - e^z \sin z - e^z \cos z = -2e^z \sin z$$

=)
$$f(z) \sim 1 + z - \frac{2}{3!} z^3 = 1 + z - \frac{z^3}{3!}$$

c)
$$f(z) = \sqrt{g} z = \frac{senz}{cosz}$$
 $f(0) = 0$

$$f'(z) = \frac{\cos^2 z + \sin^2 z}{(\cos z)^2} = \frac{1}{\cos^2 z} = 1 + 4g^2 z$$
 $f'(0) = 1$

f 1/0) = 0 f 111)(0)=2