

Da semántica a  $\text{for } x:=a_1 \text{ to } a_2 \text{ do } S$  para que sea equivalente  
a  $\text{begin var } z:=a_2; x:=a_1; \text{ while } (x \leq z) \text{ do } (S, x:=x+1) \text{ end}$  con  $z \notin FV(S)$

$$[\text{for}^{++}] \quad \langle x:=a_1, s[z \mapsto \mathcal{N}[a_2]s] \rangle \rightarrow s', \langle S, s' \rangle \rightarrow s'', \langle \text{for } x:=x+1 \text{ to } \mathcal{N}^{-1}(\mathcal{N}[a_2]s) \text{ do } S, s'' \rangle \rightarrow s''$$

$$\langle \text{for } x:=a_1 \text{ to } a_2 \text{ do } S, s \rangle \rightarrow s''' [z \mapsto s z]$$

cundo  $\mathcal{N}[x \leq \mathcal{N}^{-1}(\mathcal{N}[a_2]s)] s' = \text{tt}$

$[\text{for}^{++}]$

$$\langle x:=a_1, s[z \mapsto \mathcal{N}[a_2]s] \rangle \rightarrow s'$$

$$\langle \text{for } x:=a_1 \text{ to } a_2 \text{ do } S, s \rangle \rightarrow s' [z \mapsto s z]$$

cundo  $\mathcal{N}[x > \mathcal{N}^{-1}(\mathcal{N}[a_2]s)] s' = \text{ff}$ .

si  $\mathcal{N}[x \leq z] s'' = \text{tt}$

$[\text{for}^{++}]$

$$\langle z:=a_2, s \rangle \rightarrow s', \langle x:=a_1, s' \rangle \rightarrow s'', \langle S, s'' \rangle \rightarrow s'''$$

$$\langle \text{for } x:=x+1 \text{ to } \mathcal{N}^{-1}(\mathcal{N}[a_2]s) \text{ do } S, s''' \rangle \rightarrow s''''$$

$$\langle \text{for } x:=a_1 \text{ to } a_2 \text{ do } S, s \rangle \rightarrow s'''' [z \mapsto s z]$$

$[\text{for}^{++}]$

$$\langle z:=a_2, s \rangle \rightarrow s', \langle x:=a_1, s' \rangle \rightarrow s''$$

si  $\mathcal{N}[x \leq z] s'' = \text{ff}$

$$\langle \text{for } x:=a_1 \text{ to } a_2 \text{ do } S, s \rangle \rightarrow s'' [z \mapsto s z]$$