PS\_MOPSO tests Page 1 of 28

 $Testing \ \underline{mopsocd}(Multi-objective \ Particle \ Swarm \ Optimization \ with \ Crowding \ Distance) \ and \ mopsopsa \ algorithm \ v.1$ 

Here are results of running mopsocd and mopsopsa\_v1 on testing functions.

Load algorithms, test functions and utilities:

```
source('../mopsocd.R')
source('../mopsocds.R')
source('../moea.test.dtlz2.R')
source('../mopsopsa_v1.R')
```

Set number of points to be generated for True Pareto Front:

```
pfpoints <- 10000
```

Visualizations of solutions MOPSOCD vs MOPSOPSA\_V1

Color conventions: Black = True Pareto front, Green = Nondominated solutions, Red = All stored solutions

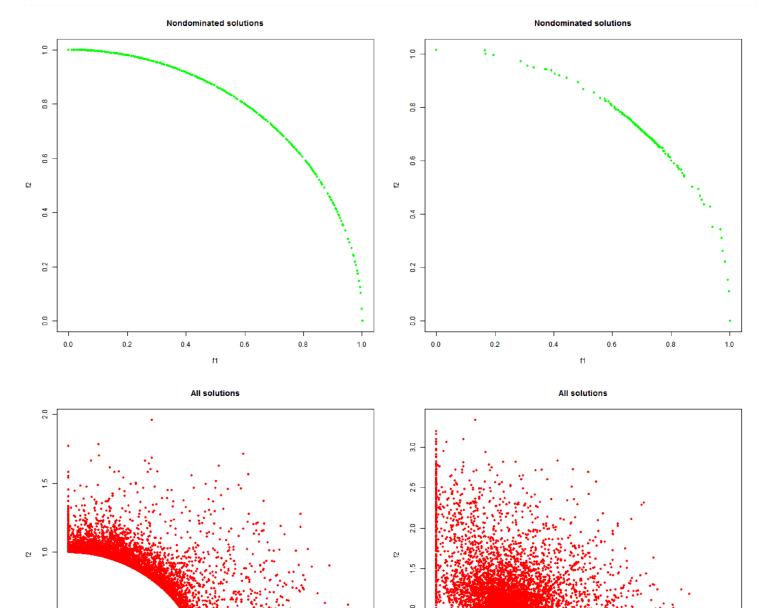
## DTLZ2 Test Functions

0.5

0.0

0.0

```
d <- 11
s1 <- mopsocds(dtlz2_2, varcnt=d, fncnt=2, lowerbound=rep(0, d), upperbound=rep(1,d), opt=0)
s2 <- mopsopsa_v1(dtlz2_2, varcnt=d, fncnt=2, lowerbound=rep(0, d), upperbound=rep(1,d), opt=0)
draw_n(s1, s2, dtlz2_2front, pfpoints)</pre>
```



0.5

0.0

0.0

0.5

1.0

1.5

f1

2.0

2.5

3.0

1.0

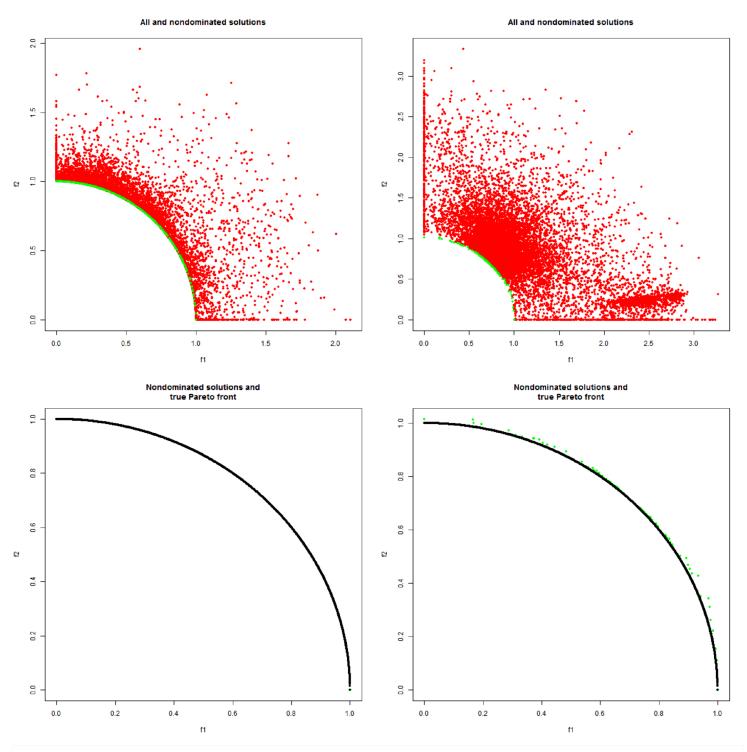
f1

1.5

2.0

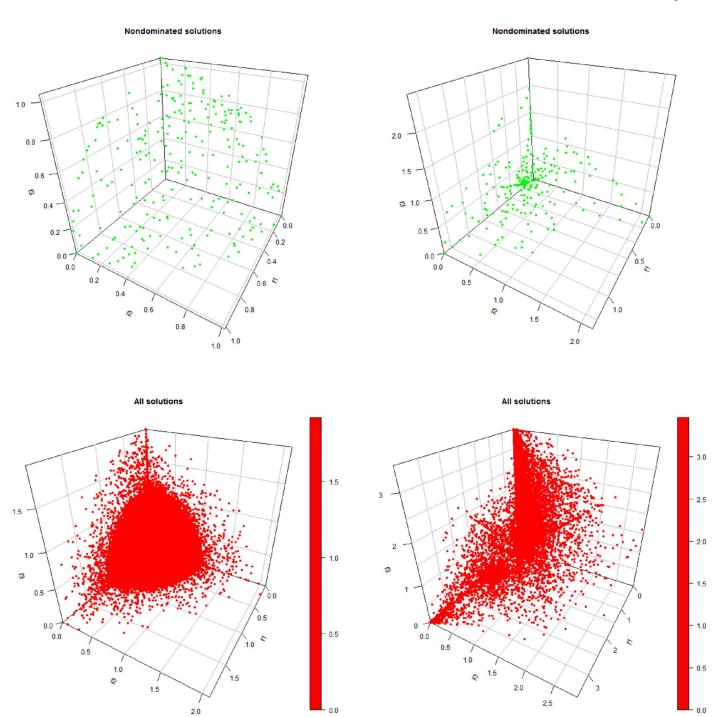
0.5

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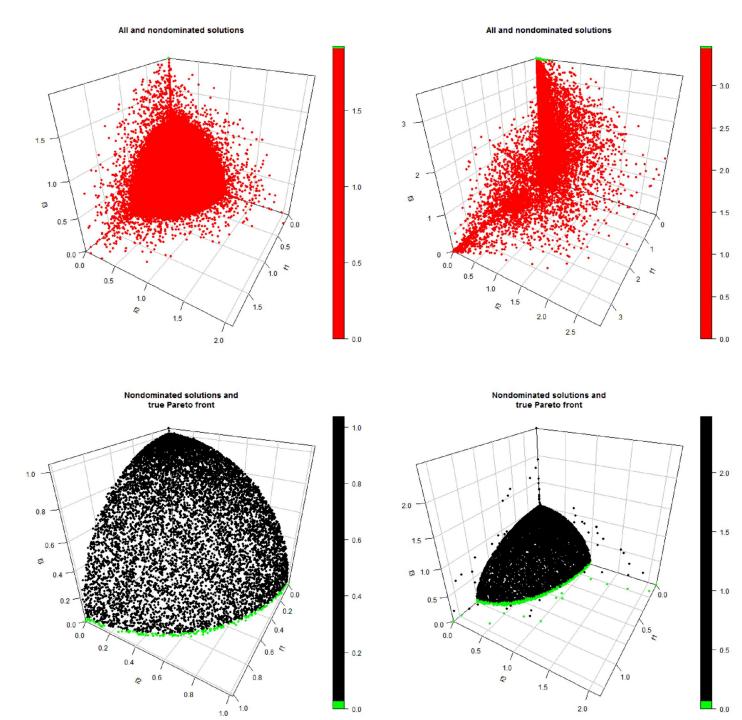


d <- 12 s1 <- mopsocds(dtlz2  $\square$ , varcnt=d, fncnt= $\square$ , lowerbound=rep(0, d), upperbound=rep(1,d), opt=0) s2 <- mopsopsa\_v1(dtlz2  $\square$ , varcnt=d, fncnt= $\square$ , lowerbound=rep(0, d), upperbound=rep(1,d), opt=0) draw\_n(s1, s2, dtlz2  $\square$ front, pfpoints)

PS\_MOPSO tests Page 3 of 28



PS\_MOPSO tests Page 4 of 28

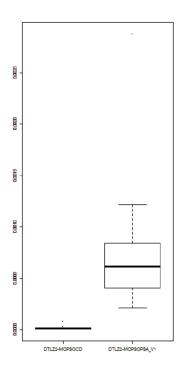


 $Boplots\ of\ results\ from\ 20\ independent\ runs\ of\ MOPSOCD\ and\ MOPSOPSA\_V1\ on\ test\ functions\ for\ 2\ objectives:$ 

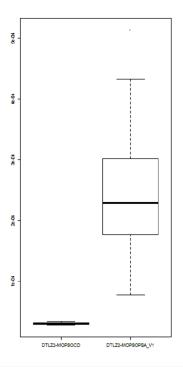
```
n <- 20
ob0 <- 2
mat <- per _ es (n, test_functions20, test_functions_fronts20, ob0=2, d=11, pfpoints, al0_func=c(mopsocds, mopsopsa_v1))
titles = c('00002-M000000', '00002-M000000000', '00002-M00000000')
per _ o p o s(n, mat, titles)

110 "00 performance measures on 20 runs0"
```

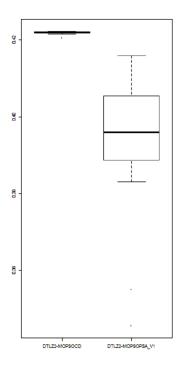
PS\_MOPSO tests Page of 28

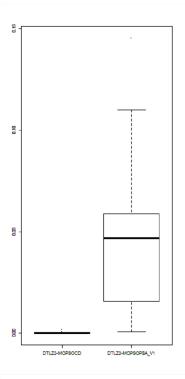


□□ □1□ "□□□ performance measures on 20 runs□"



□□ □1□ "□□ performance measures on 20 runs□"

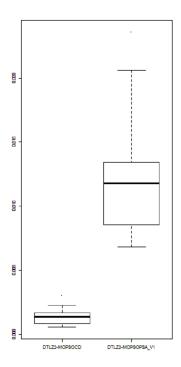




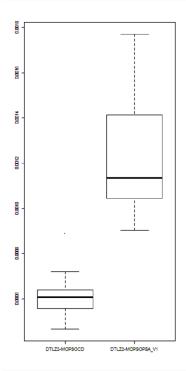
mat\_2ob
 <- as.data.frame(mat)</pre>

```
ob0 <- 0
mat <- perf test(n, test_functions00, test_functions_fronts00, ob0=0, d=12, pfpoints, al0_func=c(mopsocds, mopsopsa_v1))
titles = c(*0002-M000000*, *00002-M000000*0*)
perf_boxplots(n, mat, titles)

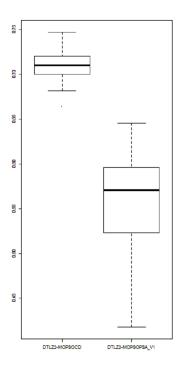
110 "00 performance measures on 20 runs0"
```

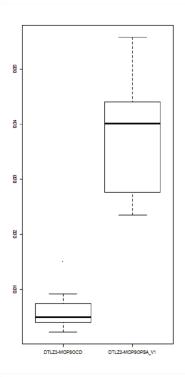


□□ □1□ "□□□ performance measures on 20 runs□"



 $\Box\Box$   $\Box\Box\Box$  " $\Box\Box$  performance measures on 20 runs $\Box$  "

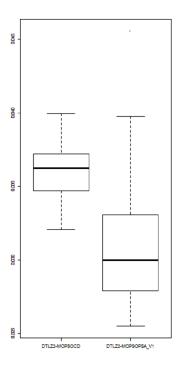




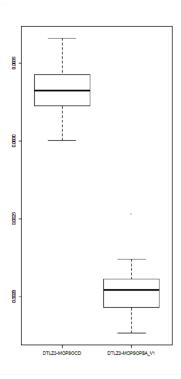
mat\_OobO <- as.data.frame(mat)

```
ob0 <- 0
mat <- perf test(n, test_functions00, test_functions_fronts00, ob0=0, d=10, pfpoints, al0_func=c(mopsocd, mopsopsa_v1))
titles = c('00002-M000000', '00002-M00000000001')
perf_boxplots(n, mat, titles)

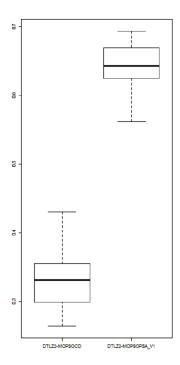
110 "00 performance measures on 20 runs0"
```

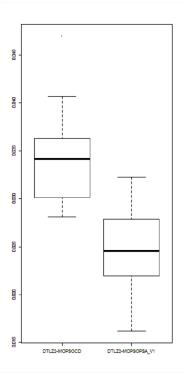


□□ □1□ "□□□ performance measures on 20 runs□"



□□ □1□ "□□ performance measures on 20 runs□"

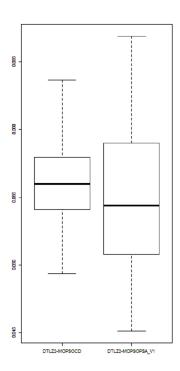




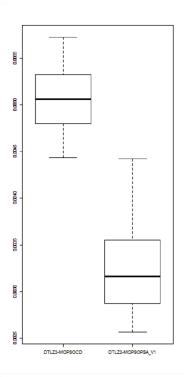
mat\_\_ob0 <- as.data.frame(mat)

```
ob0 <- 0
mat <- perf test(n, test_functions00, test_functions_fronts00, ob0=0, d=10, pfpoints, al0_func=c(mopsocd, mopsopsa_v1))
titles = c(**\text{0}\text{1}\text{0}\text{2}\text{-}\text{M}\text{1}\text{0}\text{1}\text{0}} \text{0}')
perf_boxplots(n, mat, titles)

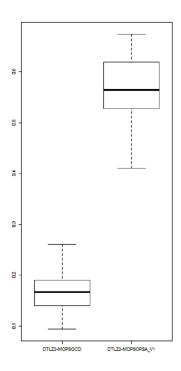
10 010 "00 performance measures on 20 runs0"
```

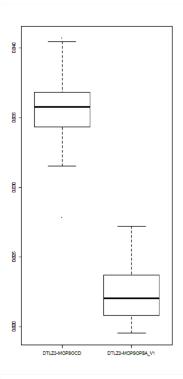


□□ □1□ "□□□ performance measures on 20 runs□"



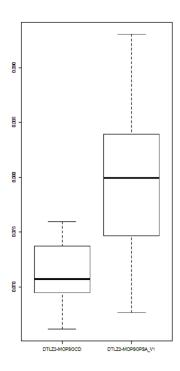
 $\Box\Box$   $\Box\Box$  " $\Box\Box$  performance measures on 20 runs $\Box$ "



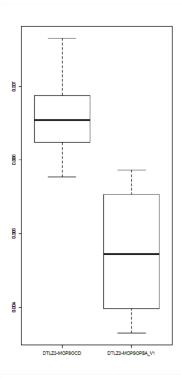


mat\_\_ob\_ <- as.data.frame(mat)

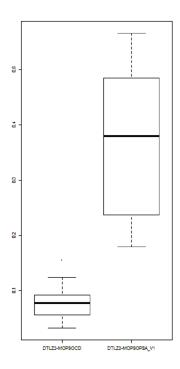
```
ob0 <- 0
mat <- perf_test(n, test_functions00, test_functions_fronts00, ob0=0, d=10, pfpoints, al0_func=c(mopsocd, mopsopsa_v1))
titles = c(**\text{0}\text{1}\text{0}\text{2}\text{-}\text{M}\text{1}\text{0}\text{1}\text{0}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}
```

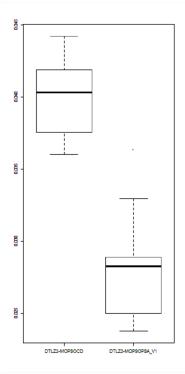


□□ □1□ "□□□ performance measures on 20 runs□"



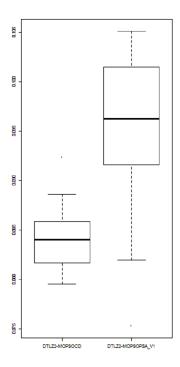
□□ □1□ "□□ performance measures on 20 runs□"



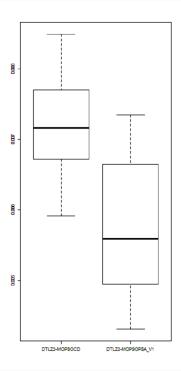


mat\_OobO <- as.data.frame(mat)

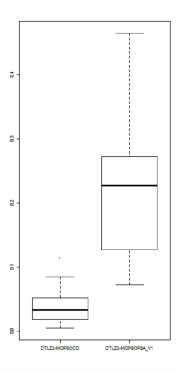
```
ob0 <- 0
mat <- perf_test(n, test_functions0, test_functions_fronts0, ob0=0, d=10, pfpoints, al0_func=c(mopsocd, mopsopsa_v1))
titles = c(**\text{0}\text{1}\text{2}\text{-}\text{M}\text{1}\text{1}\text{0}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\text{1}\t
```

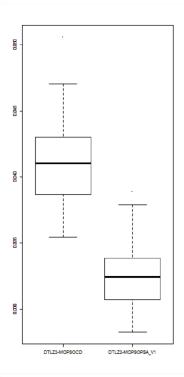


□□ □1□ "□□□ performance measures on 20 runs□"



□□ □1□ "□□ performance measures on 20 runs□"

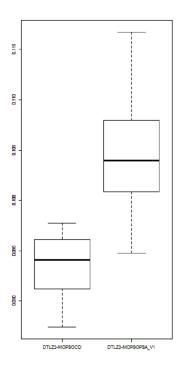




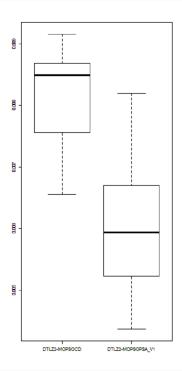
mat\_OobO <- **as.data.frame**(mat)

```
ob0 <- 0
mat <- perf_test(n, test_functions00, test_functions_fronts00, ob0=0, d=10, pfpoints, al0_func=c(mopsocd, mopsopsa_v1))
titles = c('00002-M000000', '00002-M00000000001')
perf_boxplots(n, mat, titles)

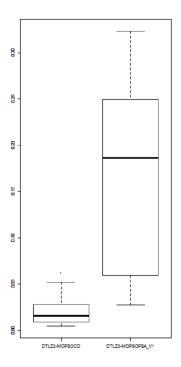
110 "00 performance measures on 20 runs0"
```



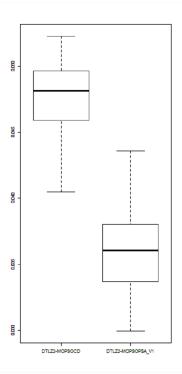
□□ □1□ "□□□ performance measures on 20 runs□"



□□ □1□ "□□ performance measures on 20 runs□"

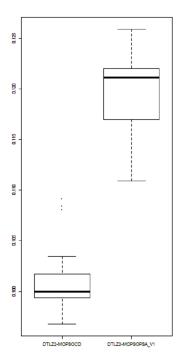


 $\Box\Box$   $\Box\Box$  " $\Box\Box$  performance measures on 20 runs $\Box$ "

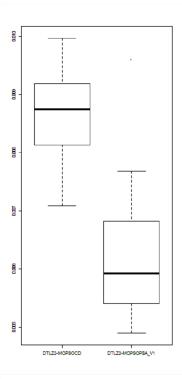


```
mat_OobO <- as.data.frame(mat)
```

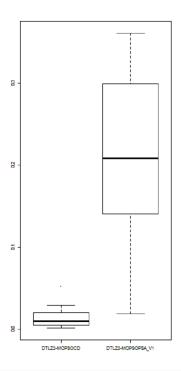
```
ob0 <- 10
mat <- perf_test(n, test_functions100, test_functions_fronts100, ob0=10, d=10, pfpoints, all_func=c(mopsocd, mopsopsa_v1))
titles = c('00002-M00000000, '00002-M000000000001')
perf_boxplots(n, mat, titles)</pre>
```

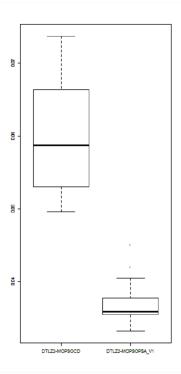


□□ □1□ "□□□ performance measures on 20 runs□"

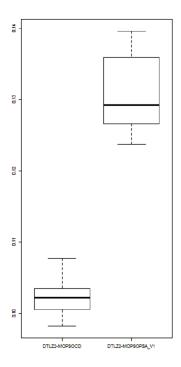


□□ □1□ "□□ performance measures on 20 runs□"

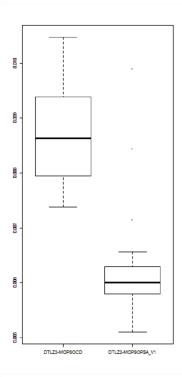




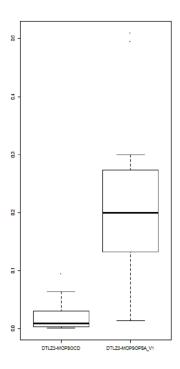
mat\_10ob <- as.data.frame(mat)

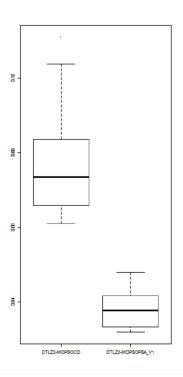


□□ □1□ "□□□ performance measures on 20 runs□"



 $\Box\Box$   $\Box\Box$  " $\Box\Box$  performance measures on 20 runs $\Box$ "

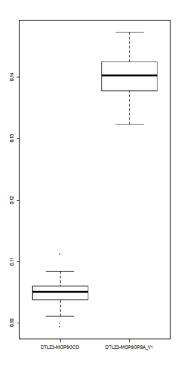




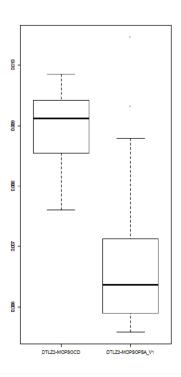
mat\_12ob <- as.data.frame(mat)

```
obd <- 10
mat <- perf test(n, test_functions100, test_functions_fronts100, obd=10, d=20, pfpoints, all_func=c(mopsocd, mopsopsa_v1))
titles = c("0002-M000000", "00002-M000000")
perf_boxplots(n, mat, titles)

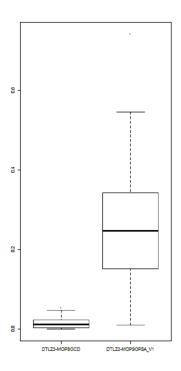
110 "00 performance measures on 20 runs0"
```



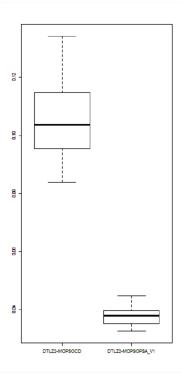
□□ □1□ "□□□ performance measures on 20 runs□"



□□ □1□ "□□ performance measures on 20 runs□"

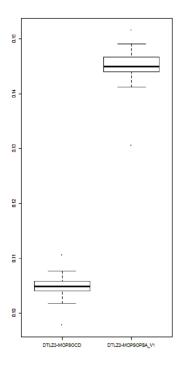


 $\Box\Box$   $\Box\Box$  " $\Box\Box$  performance measures on 20 runs $\Box$ "

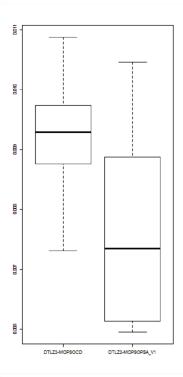


mat\_10ob0 <- as.data.frame(mat)

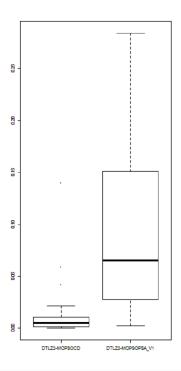
```
ob0 <- 10
mat <- perf test(n, test_functions100, test_functions_fronts100, ob0=10, d=20, pfpoints, al0_func=c(mopsocd, mopsopsa_v1))
titles = c(**00002-**M000000**, **100002-**M0000000**)
perf_boxplots(n, mat, titles)</pre>
```



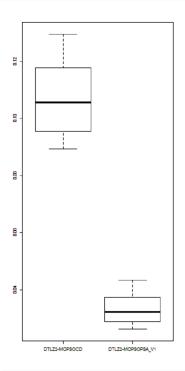
□□ □1□ "□□□ performance measures on 20 runs□"



□□ □1□ "□□ performance measures on 20 runs□"

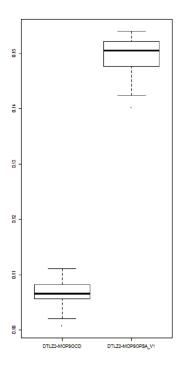


 $\Box\Box$   $\Box\Box$  " $\Box\Box$  performance measures on 20 runs $\Box$ "

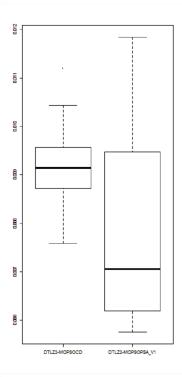


```
mat_1\[ ob\[ <- as.data.frame(mat) \]</pre>
```

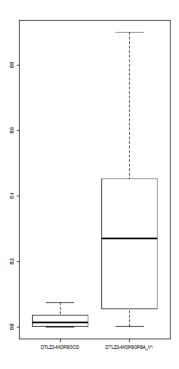
```
ob0 <- 20
mat <- perf test(n, test_functions200, test_functions_fronts200, ob0=20, d=20, pfpoints, all_func=c(mopsocd, mopsopsa_v1))
titles = c("00002-M0000000", "00002-M0000000")
perf_boxplots(n, mat, titles)</pre>
```



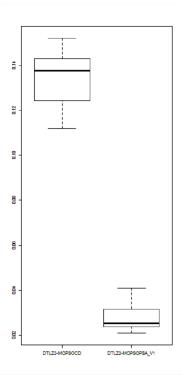
□□ □1□ "□□□ performance measures on 20 runs□"



 $\Box\Box$   $\Box\Box\Box$  " $\Box\Box$  performance measures on 20 runs $\Box$  "



□□ □1□ "□□ performance measures on 20 runs□"



mat\_20ob
 <- as.data.frame(mat)</pre>