Due Date: 5/3/2019 Problem F.2: Fractals

Problem F.2

Fractals

Due Date: 5/3/2019 Folder: FinalProject

File Name: F2_Fractal_Name.py

Points: 20 points

Problem Background

Start with a shape, say a triangle. Consider each point on the triangle to be defined by a set of vectors

$$S_0 = {\begin{bmatrix} x \\ y \end{bmatrix}}$$
: the point (x, y) is a point on the triangle}.

Different values for t correspond to different places on the triangle. To generate a fractal, we will perform 3 transformations on all of these vectors to generate a new set of points S_1 . Here is one example of these transformations. For each vector $v \in S_0$, we generate 3 new vectors w_1, w_2, w_3

$$w_{1} = \begin{bmatrix} \frac{1}{4} & 0\\ 0 & \frac{1}{4} \end{bmatrix} v + \begin{bmatrix} 0\\ 0 \end{bmatrix}$$

$$w_{2} = \begin{bmatrix} \frac{1}{4} & 0\\ 0 & \frac{1}{4} \end{bmatrix} v + \begin{bmatrix} 0.5\\ 0 \end{bmatrix}$$

$$w_{3} = \begin{bmatrix} \frac{1}{4} & 0\\ 0 & \frac{1}{4} \end{bmatrix} v + \begin{bmatrix} 0.5\\ 0.5 \end{bmatrix}$$

All three of these new vectors are then added to a new set S_1 . If this process is performed for all vectors $v \in S_0$, we generate a new set S_1 . When all the points in S_1 are plotted we see three new triangles. We then perform this transformation yet again on all vectors in S_1 to generate a set S_2 . By continuing this process repeatedly, we obtain a fractal image.

Your project will be to generate all the S_i sets up to some maximum value for i. The plot each one to see how the image changes. In general, the transformations shown above can be written as

$$w_1 = A_1 v + b_1$$
$$w_2 = A_2 v + b_2$$
$$w_3 = A_3 v + b_3$$

where A_i are matrices and b_i are vectors. You will also be changing the matrices and vectors to see how it affects the fractal image. In addition, you will change the initial image to see how it affects the resulting fractal.

Program Criteria

Write a program that does the following:

- Create an initial image. This could be a geometric object, your name, a face. Really anything that can be plotted in Python and described using vectors, that is points (x, y).
- Apply the above transformations, or something similar, to your image, thus obtaining a new set of points that looks like 3 new transformed copies of your image.

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 \bullet Continue applying the transformations to the previous points for N iterations. Be sure to make N a variable so that the number of iterations can be changed easily.

 \bullet Plot the final image that is created after N iterations.

Deliverables

Place the following in a folder named FinalProject in your repository:

- A Python file F2_Fractal_Name.py that satisfies the program criteria.
- A PDF file F2_Fractal_Name.pdf that describes how your program works. This should be a description of how you went about solving this problem. You should go into some detail about your solution method, but I don't want to see something about every if statement and for loop. As an example of the type of description I'm looking for, see the file Goldbach_explanation.doc in the Final Problem folder of my repo.
- Include in your PDF file the original image you used.
- Include also at least one of the following:
 - \star Use a different starting image. Discuss how the final image after N iterations compares to what you got with your first image.
 - * Change the transformation done to the image. This could involve changing the matrix A_i , changing the vectors b_i , or adding another transformation entirely. Discuss how the final image compares to the final image using your original transformations.