

Diffie-Hellman key exchange

Diffie-Hellman algorithm is used to establish a shared secret between two parties which can be used for secret communication for exchanging data over a public network.

The algorithm in itself is very simple. Let's assume that Alice wants to establish a shared secret with Bob. Here is an example of the protocol with secret values (6 and 15).

- 1) Alice and Bob agree to use a prime number $p = 23$ and base $g = 5$. (These two values are chosen in this way to ensure that the resulting shared secret can take on any value from 1 to $p-1$).
- 2) Alice chooses a secret integer $a = 6$, then sends Bob $A = g^a \bmod p$ ($A = 5^6 \bmod 23 = 8$)
- 3) Bob chooses a secret integer $b = 15$, then sends Alice $B = g^b \bmod p$ ($B = 5^{15} \bmod 23 = 19$)
- 4) Alice computes $s = B^a \bmod p$ ($s = 19^6 \bmod 23 = 2$)
- 5) Bob computes $s = A^b \bmod p$ ($s = 8^{15} \bmod 23 = 2$)
- 6) Alice and Bob now share a secret (the number 2).

The number Alice get at step 4 is same as Bob got at step 5.

Bob computes:

$$A^b \bmod p = (g^a \bmod p)^b \bmod p = g^{ab} \bmod p$$

Alice computes:

$$B^a \bmod p = (g^b \bmod p)^a \bmod p = g^{ba} \bmod p$$

Diffie-Hellman algorithm is primarily used as a method of exchanging cryptography keys for use in symmetric encryption algorithms like AES. Please note that information is not shared during the key exchange. Here the two parties are creating a key together.

Fill in the missing gaps in order for this algorithm to work!

Sample output

Alice's Secret Key is 2 Bob's Secret Key is 2
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