

①

$$\int \mathcal{L}(f, y, x) \underbrace{p(x, y)}_{\text{data dist.}} dx dy$$

$$(x_1, y_1), \dots, (x_n, y_n) \sim p(x, y).$$

$$\approx \frac{1}{n} \sum_{i=1}^n \mathcal{L}(f, y_i, x_i)$$

standard way

$$\mathcal{L}(f, \tilde{y}_i, x_i)$$

y_i \tilde{y}_i
 true y. counts

$$\frac{1}{n} \sum_{i=1}^n \int \mathcal{L}(f, y_i, x_i) \underbrace{p(y_i | \tilde{y}_i)}_{\substack{\text{Dirichlet posterior} \\ \text{w/ samples}}} dy_i$$

$$\text{sgd.} \approx$$

②

\min_{θ}

$$\int \mathcal{L}(f_{\theta}, y, x) \underbrace{p(y|x)}_{0/1} \underbrace{p(x)}_{\text{or } \square} dx dy$$

0/1

$p(y|x)$ is continuous.

\square or \square



Dirichlet for estimating $p(y|x)$
 Sampling from posterior to capture uncertainty.