PHYS 2321
Week4: Gauss's Law/Potential

Day 3 Outline

1) Hwk: Ch. 23 P. 2,3,5,9,12,15,17,21,25,28,29,35,36,43, 48,51. MCQ 1-13 odd (Due next Fri)

   Next: Read Ch. 23.1-**8**

2) Ch. 22 Gauss's Law for E near conductors
   a. Example: nested metal spherical shells.
3) Ch. 23 Electric Potential
   a. Potential, V, of a point charge
   b. Electric Potential energy, U, and work
   c. Compare to gravitational PE, U_g

Notes: Next quiz is on Mon on Flux and Gauss's Law.
Return Ch. 21B hwk. Mean=9.54/10.
Ch. 22 PDF is my2321wk4.pdf under "NEW STUFF"

Electric Potential of a Point Charge

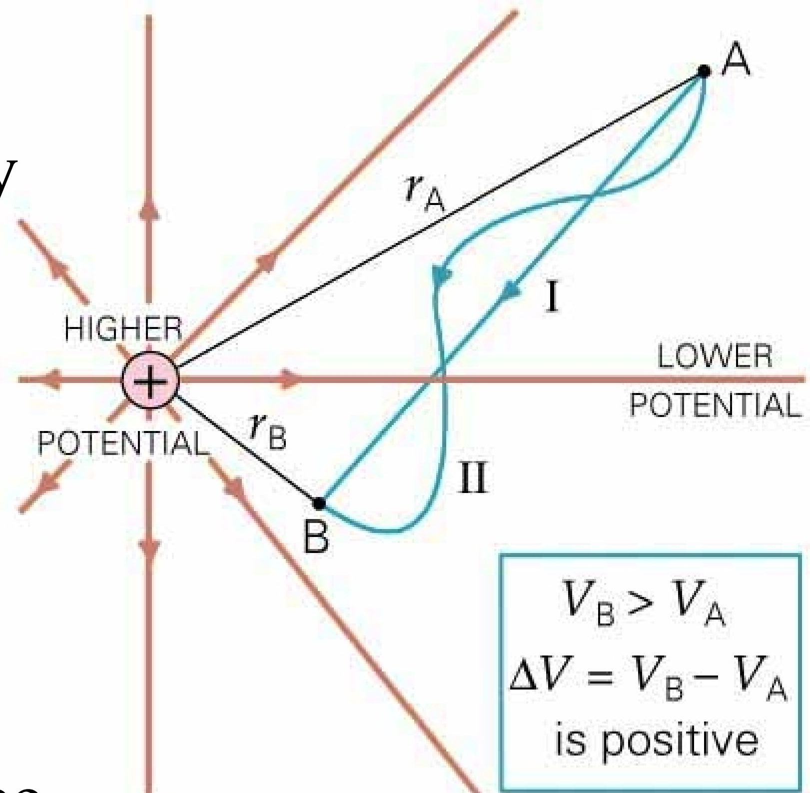
- Recall E field of point charge:

$$\vec{E} = \frac{kq}{r^2}\hat{r}$$

- Electric Potential at r away from a point charge

$$V = \frac{kq}{r}$$

$$V = 0 \quad \text{when} \quad r \rightarrow \infty$$



- Electric potential difference

$$\Delta V_{ab} = \frac{kq}{r_b} - \frac{kq}{r_a}$$

PHYS 2321
Week5: Electric Potential

Day 1 Outline

1) Hwk: Ch. 23 P. 2,3,5,9,12,15,17,21,25,28,29,35,36,43, 48,51. MCQ 1-13 odd (Due this Fri)

   Next: Read Ch. 23.1-**8**

2) Quiz 3 on Flux and Gauss's Law

3) Ch. 23 Electric Potential

   a. Relate V to U, W_{field}, F_E and E

   b. Compare to gravitational PE, U_g

   c. Examples with uniform E-fields.

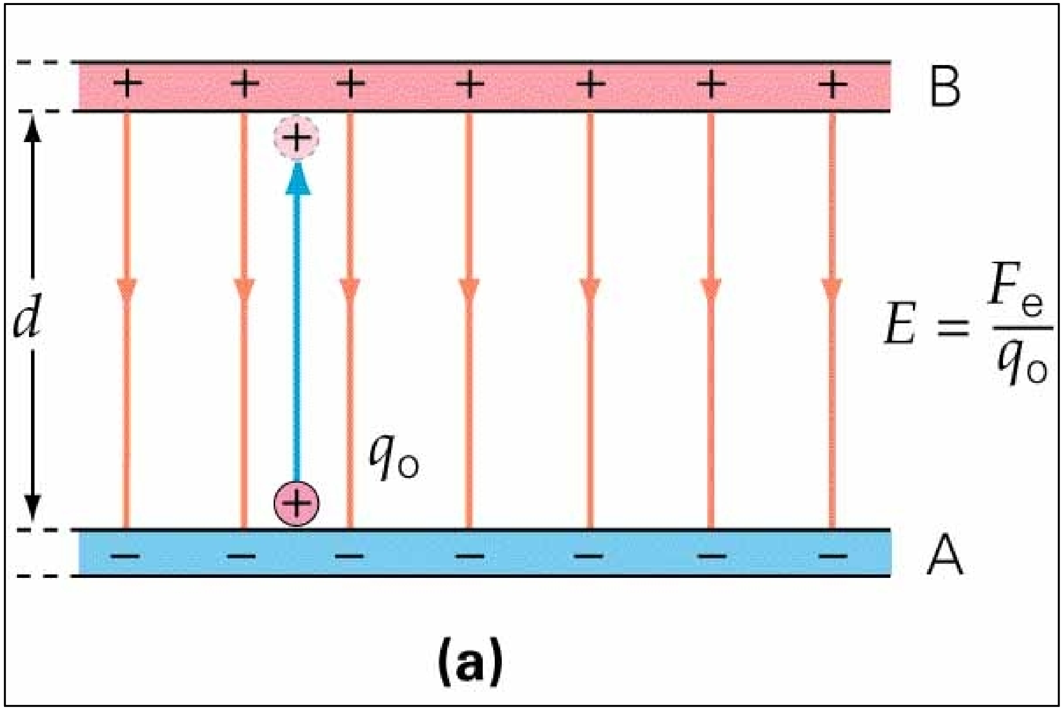
Notes:

Electric Potential

- Electric Potential of a point charge (previous slide)
- Electric potential closely related to *potential energy*
  - $\Delta U = q\Delta V$
  - And to *work*: $W_{byfield} = -q\Delta V = -\Delta U$
  - Convention: both U and V = 0 at r=infinity
- Electric potential closely related to electric force
  - $\mathbf{F}_E \cdot \Delta\mathbf{r} = W_{byfield} = -q\Delta V$
- Electric potential closely related to electric field
  - $\delta V = -E\delta r$ so that potential difference is:

$$\Delta V = -\int \vec{E} \cdot d\,\vec{l}$$

- Electric potential is easier to work with than the E-field because it is not a vector.



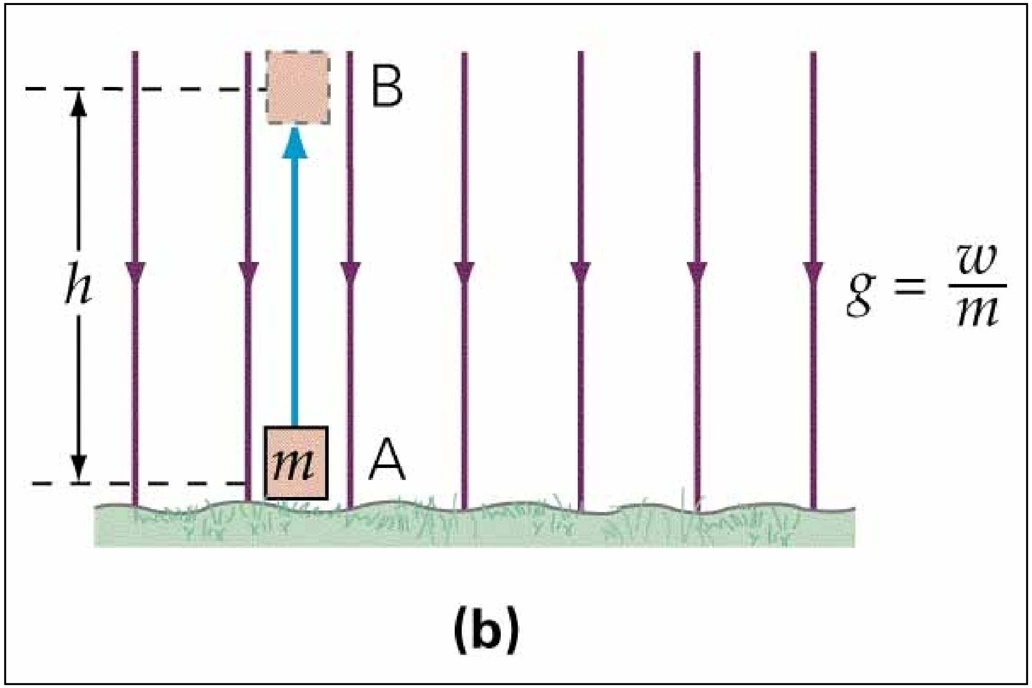
Analogy with gravity

F_E on q_0 is down

$W_{Efield} = -|F_E|d \quad (F_E = q_0 E)$

$\Delta U = -W_{Efield} = |F_E|d$

$\Delta V = \Delta U / q_0$



F_g on m is down

$W_{Gfield} = -|F_g|h \quad (F_g = mg)$

$\Delta U_G = -W_{Gfield} = |F_g|h$

$\Delta V_G = \Delta U_G / m$

PHYS 2321

Week5: Electric Potential

Day 2 Outline

1) Hwk: Ch. 23 P. 2,3,5,9,12,15,17,21,25,28,29,35,36,43,
48,51. MCQ 1-13 odd (Due this Fri)

Next: Read Ch. 23.1-**8**

2) Return Quiz 3. Mean=3.3/8

3) Ch. 23 Electric Potential

a. Examples involving charges in uniform E-fields.

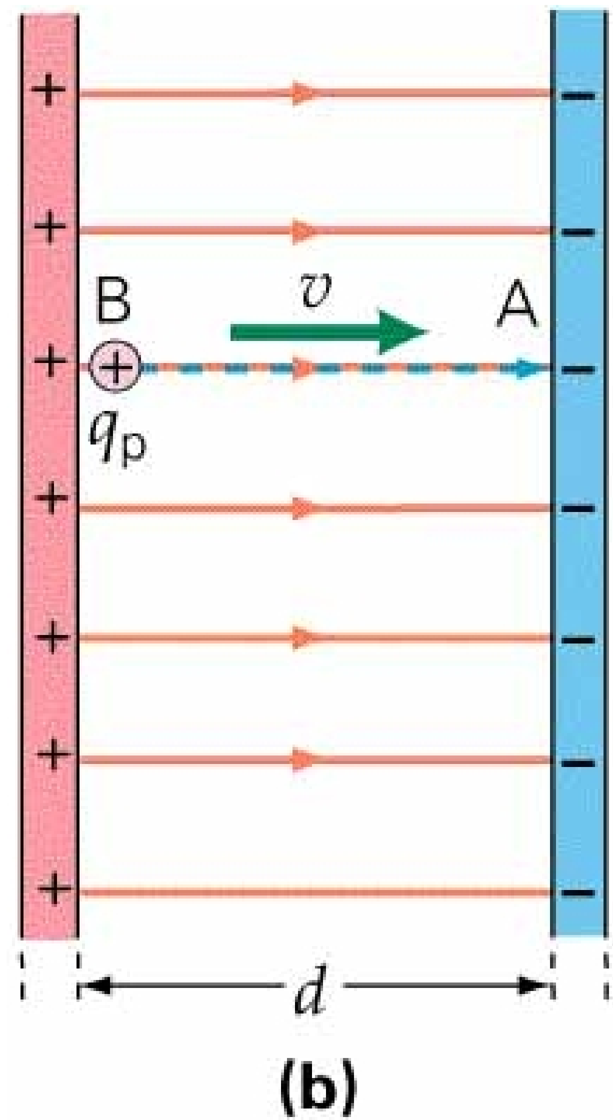
b. Potential and Potential Energy of point charge systems

Notes:

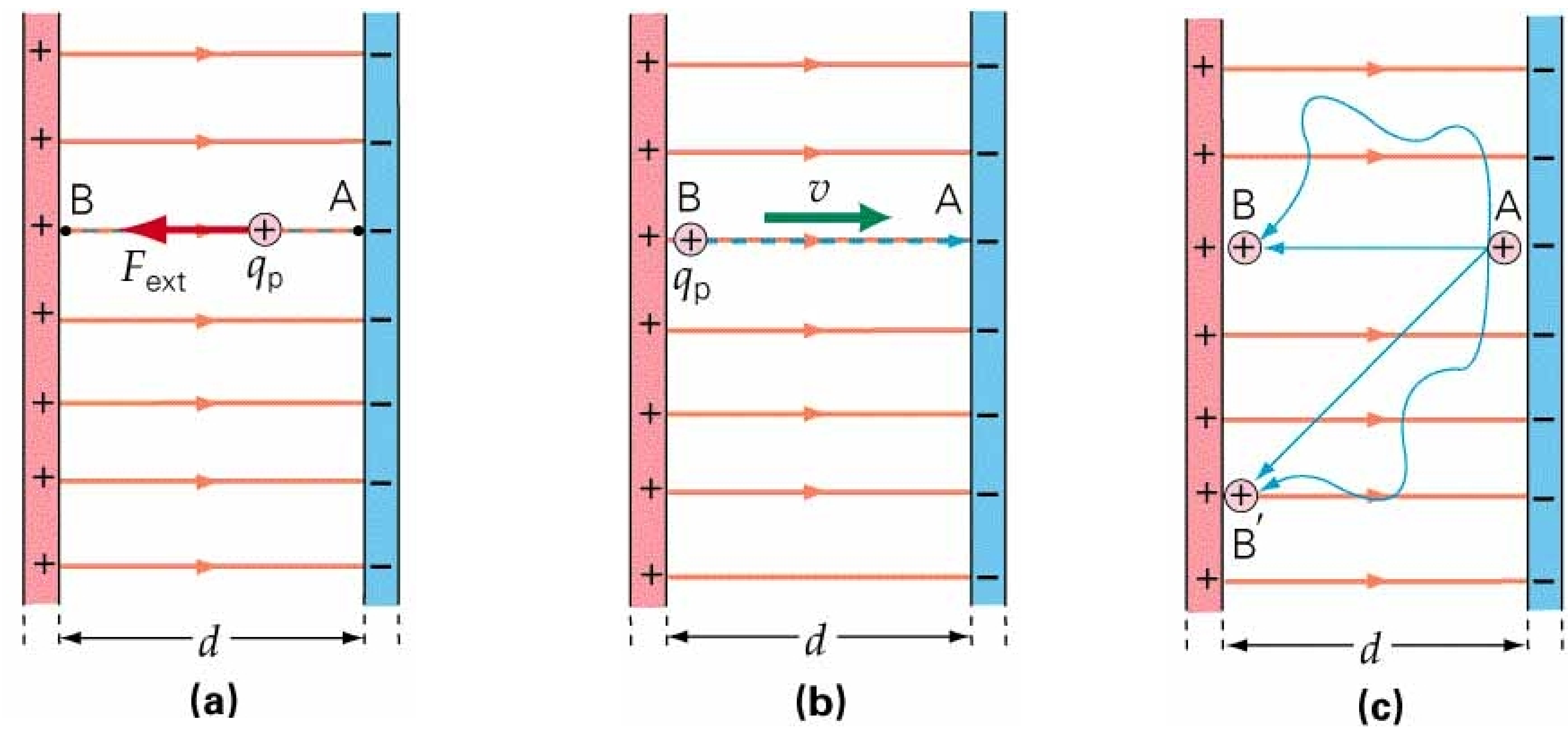
Parallel Plates

- Releasing a positive test charge from rest at point B...

Find expression for v at A given uniform **E** and plate separation d.



Electric Potential Energy
(conservation of energy ideas)



Work is done by "the hand", so we store potential energy, U_E

Charge is released and energy is converted from U_E to KE

Only the displacement in the direction of the E field matters
(ΔU_E independent of path)

PHYS 2321
Week5: Electric Potential

Day 3 Outline

1) Hwk: Ch. 23 P. 2,3,5,9,12,15,17,21,25,28,29,35,36,43, 48,51. MCQ 1-13 odd (Due this ~~Fri~~->Mon)

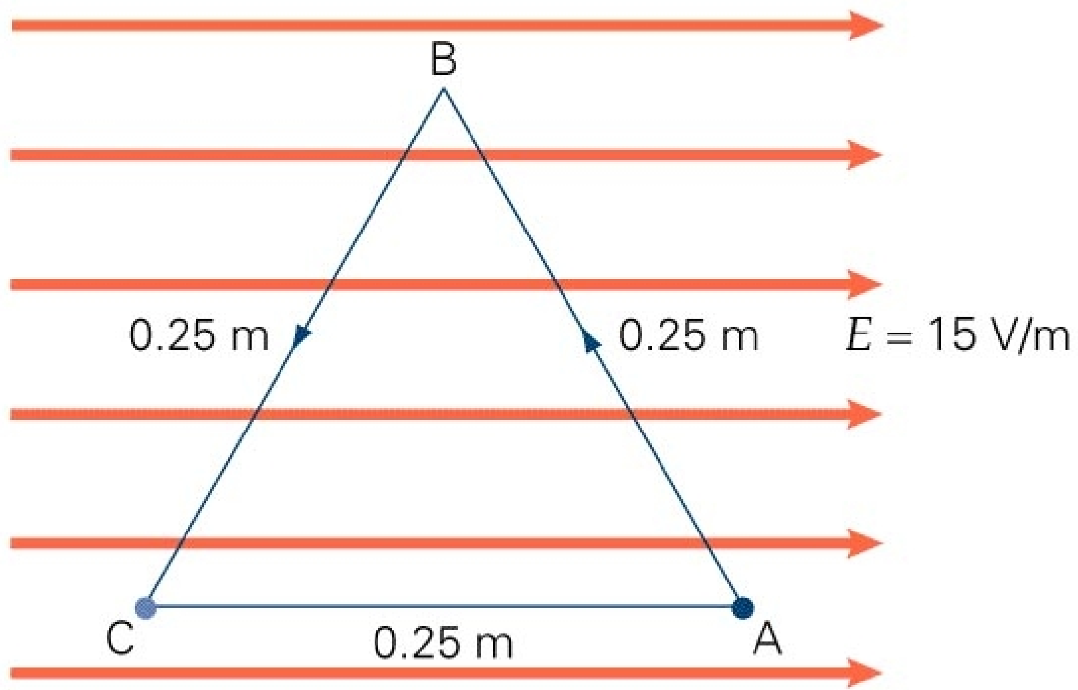
   Next: Read Ch. 23.1-**8**

2) Ch. 23 Electric Potential
   a. Potential and Potential Energy of point charge systems
   b. Potential due to extended charge distributions
   c. How to find E_x,E_y,E_z from V(x,y,z)

Notes: Exam I on Wednesday, Ch. 21-23.
See online “Review for Exam I” (equations)
Review on Monday
Observatory event 8:30-10:30

Problem: closed loop path, ABCA

- Work done is path independent ($\mathbf{F}_E$ is conservative!)
  - Only the initial and final position matter (for ΔU,ΔV, Wfield)
  - Look for an easy solution!
  - True even if E is non-uniform!

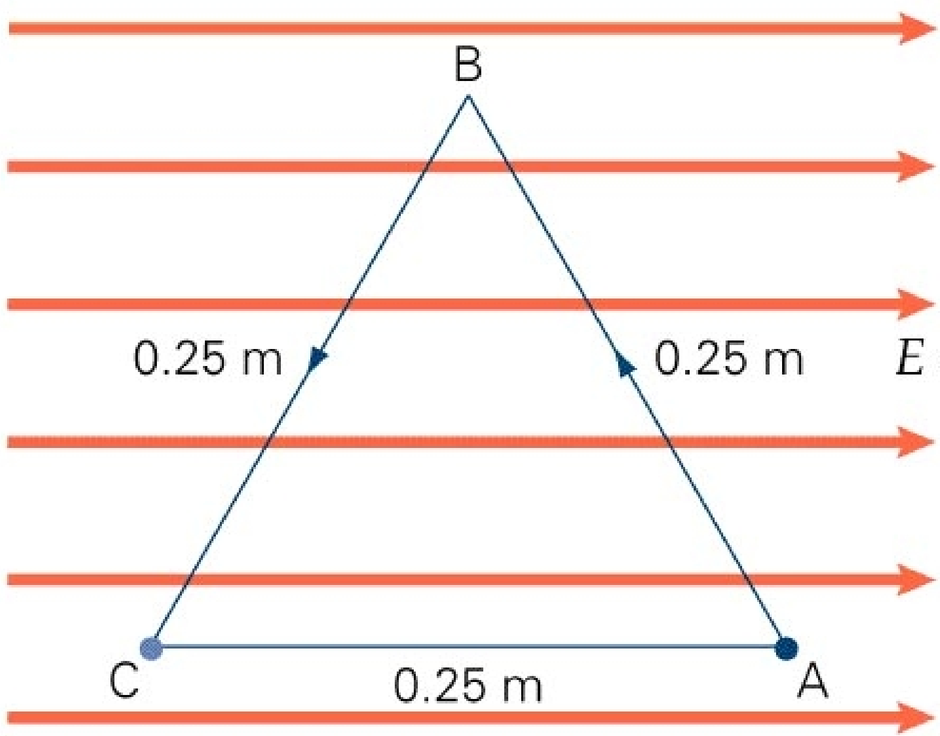


Problem: find ΔV and ΔU along path ABC

Higher V

Most general:

$$\Delta V = -\int \vec{E}\cdot d\vec{R}$$



lower V

$$\Delta V_{ABC} = \Delta V_{AC} = -Ed\cos 180 = \left(15\frac{V}{m}\right)(0.25\,m) = 3.75\,V$$

If q = -*e*:

$$\Delta U = q\Delta V = \left(-1.6\times 10^{-19}C\right)\left(3.75\,V\right) = -6\times 10^{-19}J$$

Problem: find V's on equipotentials if V_A=0.

$V_1 - V_5 = 3.75$ V

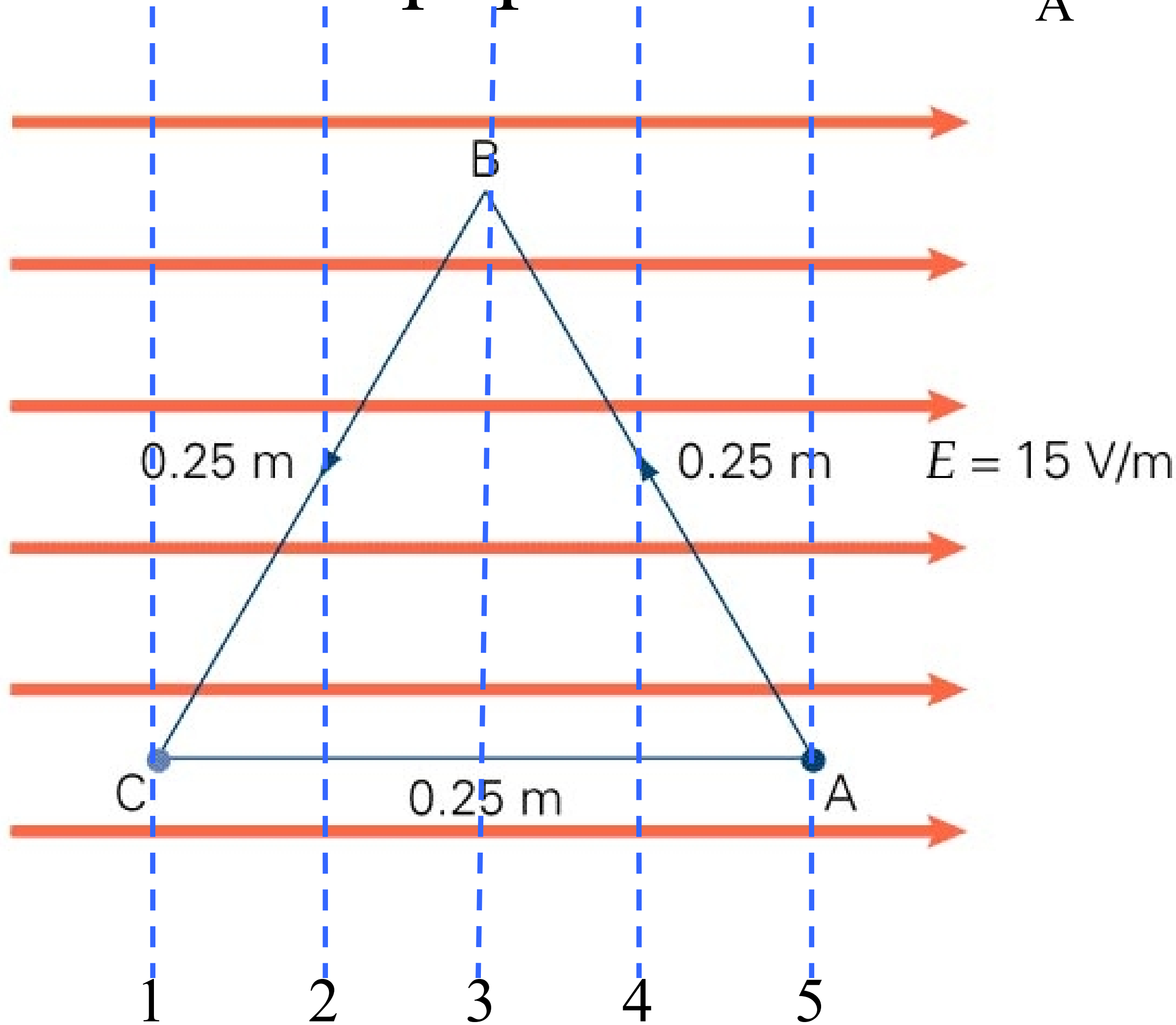
$V_1 = 3.75$ V

$V_2 = 2.8125$ V

$V_3 = 1.875$ V

$V_4 = 0.9375$ V

$V_5 = 0$ V



Electric Potential Energy U_E

- Building up arrangements of charge
  - Energy required to "build" = ΔU
- Bring a point charge in from infinity
  - like charges requires energy
    - repulsive forces
  - unlike charges give up energy
    - attractive forces

$$W = Fd = qEd$$

and $E = \dfrac{kq}{r^2}$

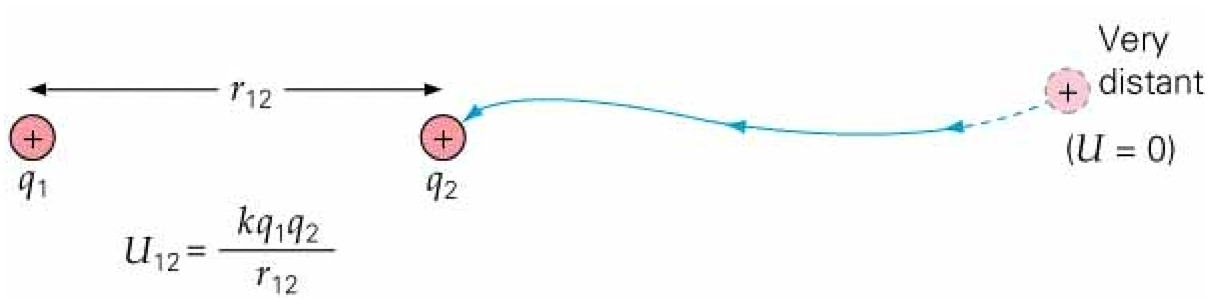
...are difficult to use since E is not a constant.

Can use:

$$U_{12} = \Delta U_{12} = q_2 \Delta V_{\infty 1}$$

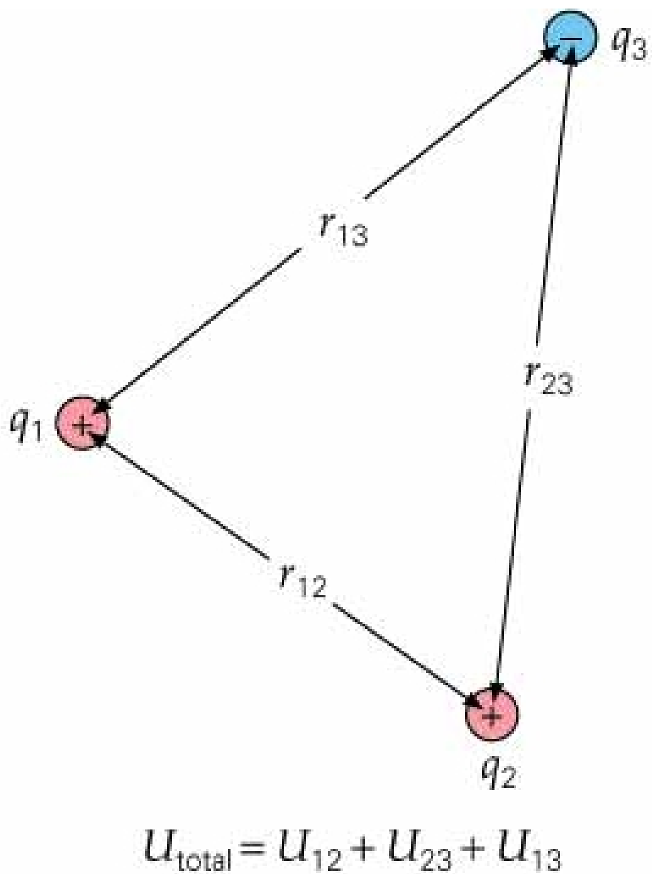
$$V_\infty = 0$$

$$V_1 = k\frac{q_1}{r_{12}}$$



U_E for more than two charges

- Don't double count
- Bring each one in from "infinity"



(b)

- Bringing together like charges requires energy (force them together)

- Bringing together un-like charges gives up energy (fall together naturally)

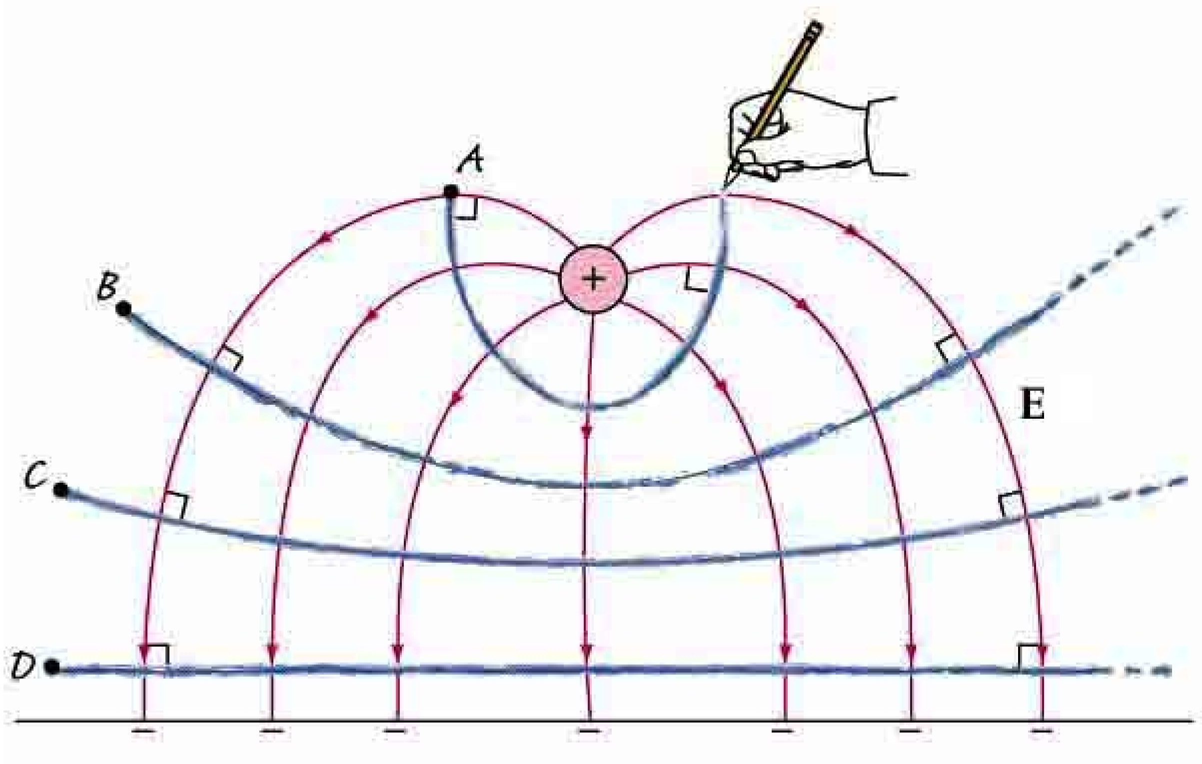
$$U_{12} = k\frac{q_1 q_2}{r_{12}}$$

$$U_{23} = k\frac{q_2 q_3}{r_{23}}$$

$$U_{13} = k\frac{q_1 q_3}{r_{13}}$$

Equipotential Surfaces

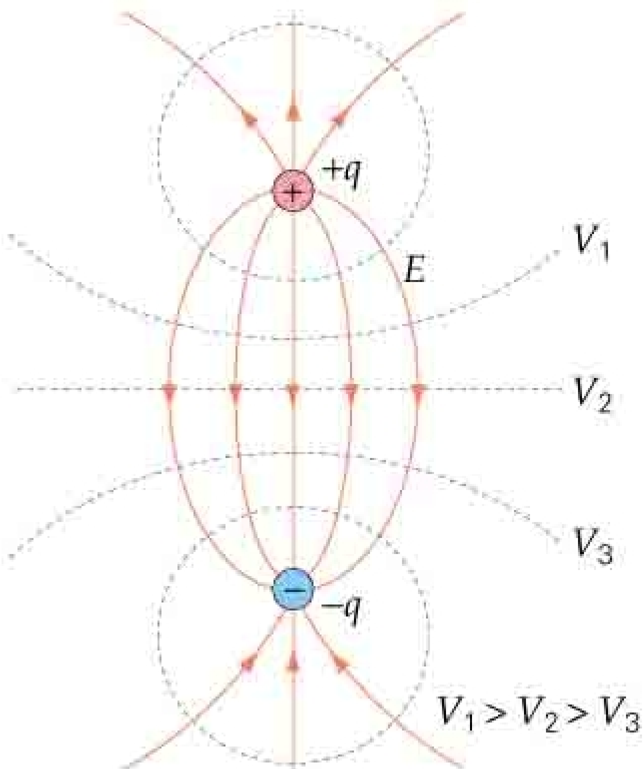
- E field is perpendicular to the equipotential surfaces
- The surface of a conductor is an equipotential surface
  - no E field parallel to the surface in *Electrostatics*
  - gradually "match" the boundaries

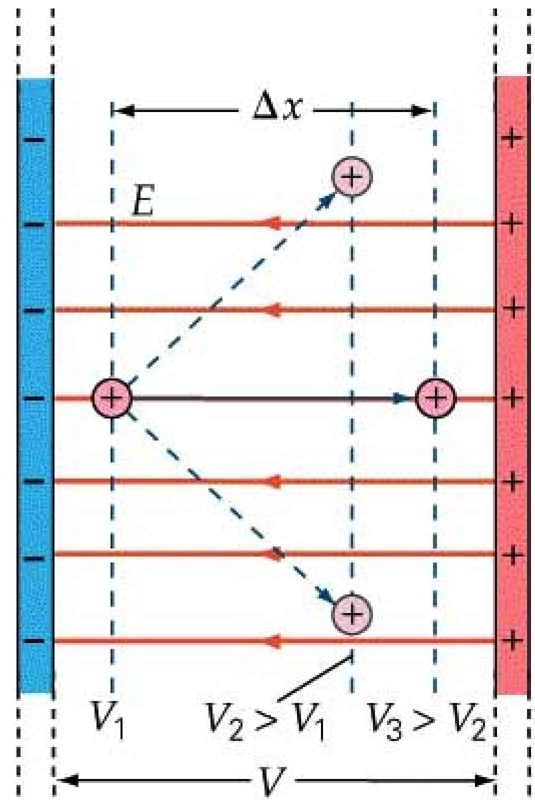


Equipotential Surfaces

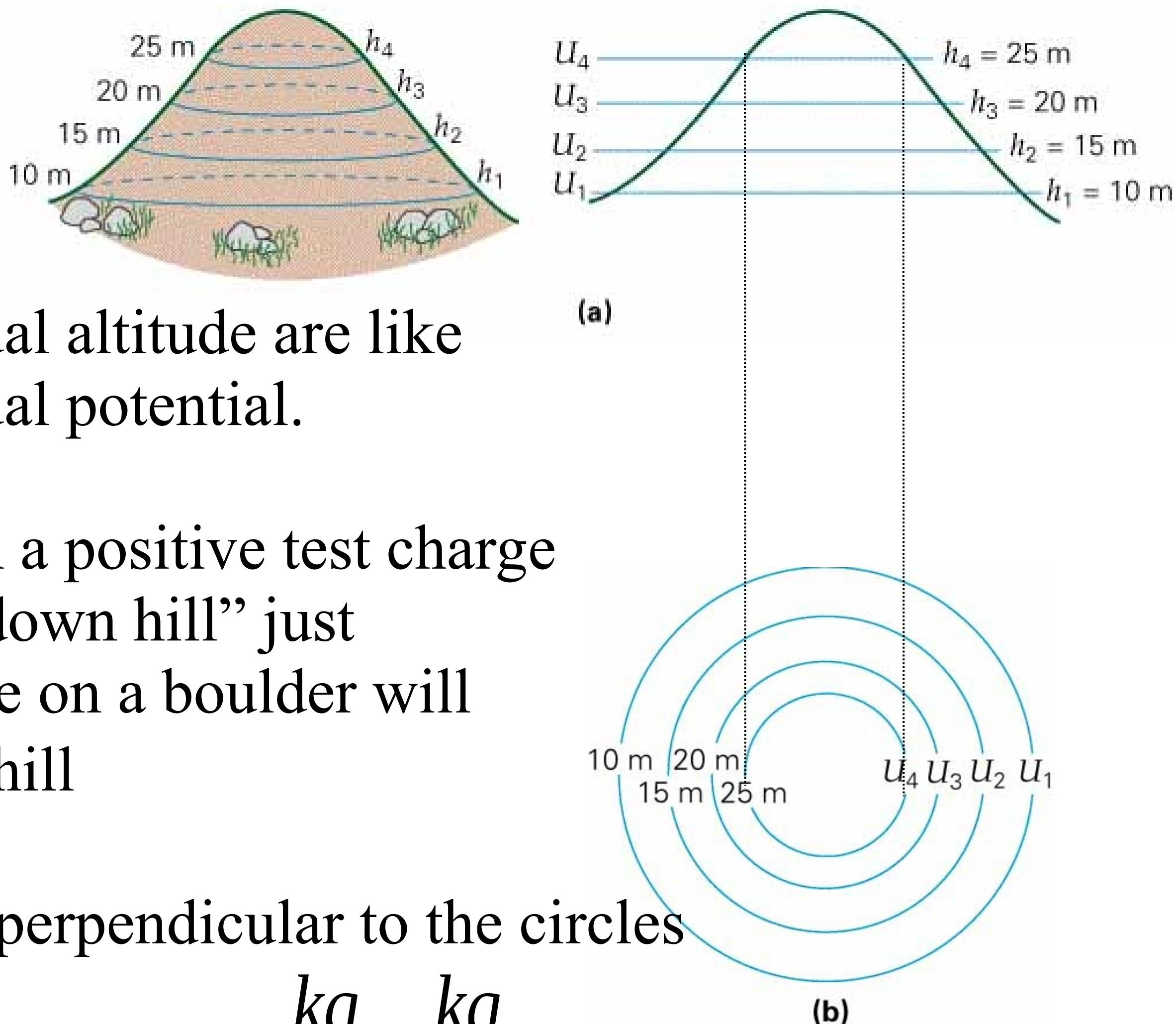
Equipotentials are perpendicular to the E-field lines.

E field points “down hill”





Contours of a map analogy



Lines of equal altitude are like
Lines of equal potential.

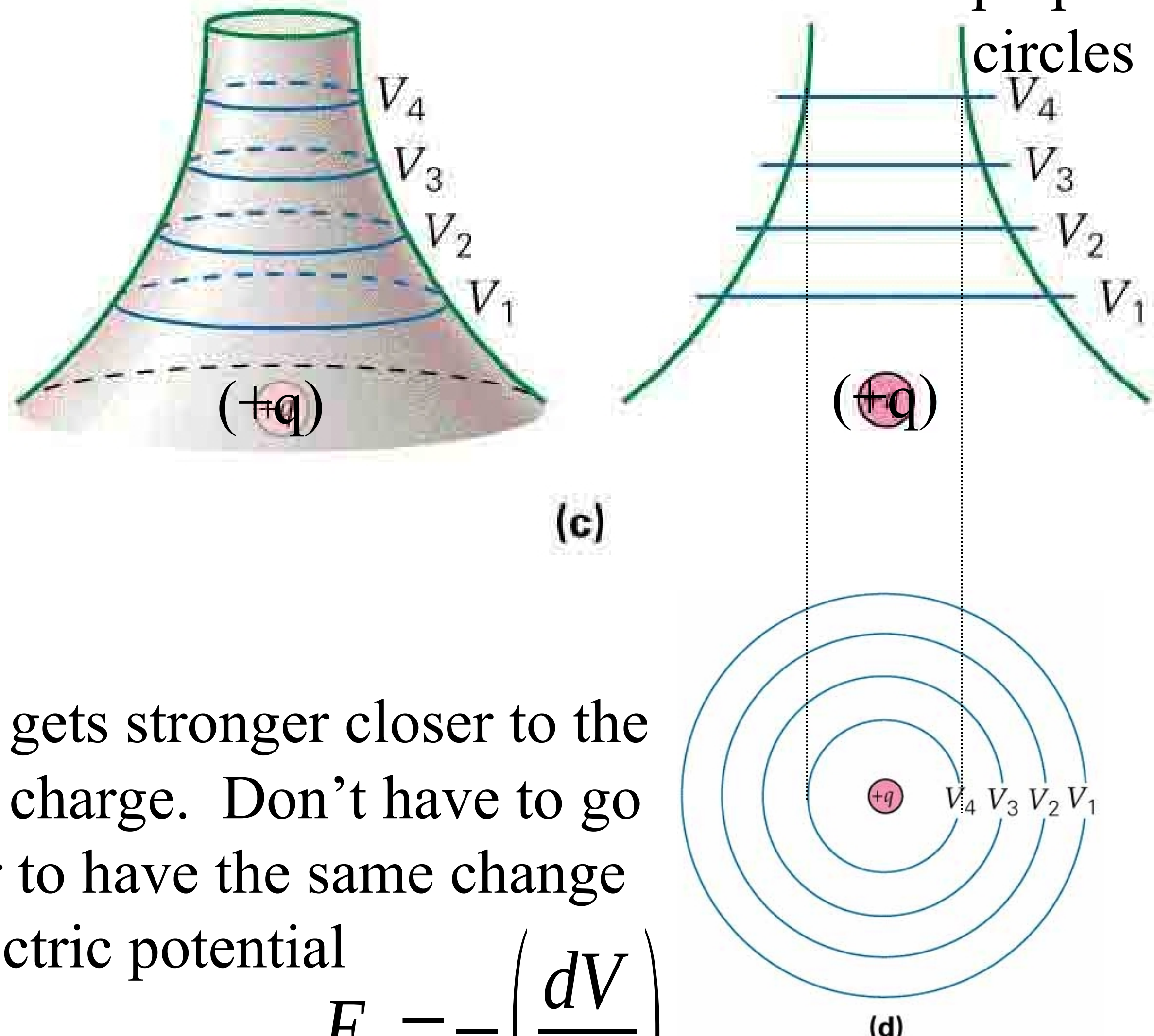
Net force on a positive test charge will point "down hill" just like net force on a boulder will point down hill

F and E are perpendicular to the circles

$$\Delta V_{ab} = \frac{kq}{r_b} - \frac{kq}{r_a}$$

Analogy with Gravity and hills

E field points "down hill" perpendicular to the circles



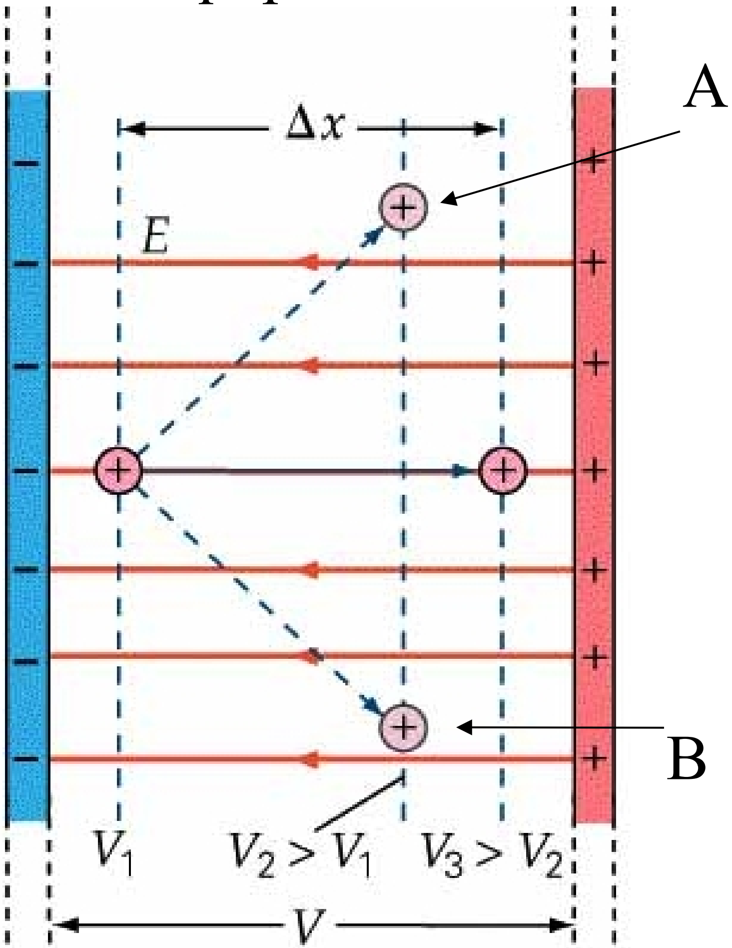
Field gets stronger closer to the point charge. Don't have to go as far to have the same change in electric potential

$$E_r = -\left(\frac{dV}{dr}\right)$$

Slightly misleading (circles would not be evenly spaced for V~1/r)

Equipotential Surfaces

- Imaginary or real surfaces of constant voltage
  - The surfaces of a conductor are equipotential surfaces
- E field and equipotential surfaces are perpendicular to each other



If a charge moves from A to B along an equipotential surface, then

$$\Delta V_{AB} = 0$$

$$\Delta U_{AB} = q\Delta V_{AB} = 0$$